Lab Class 08

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```
fna.data <- read.csv("C:\\Users\\jorda\\Downloads\\WisconsinCancer.csv")
wisc.df <- data.frame(fna.data, row.names=1)
head(wisc.df)</pre>
```

| | diagnosis | radius_mean | texture_mean p | perimeter_mean | area_mean | 1 |
|----------|-----------|--------------|-----------------|-----------------|-----------|-------------|
| 842302 | M | 17.99 | 10.38 | 122.80 | 1001.0 |) |
| 842517 | М | 20.57 | 17.77 | 132.90 | 1326.0 |) |
| 84300903 | M | 19.69 | 21.25 | 130.00 | 1203.0 |) |
| 84348301 | M | 11.42 | 20.38 | 77.58 | 386.3 | L |
| 84358402 | M | 20.29 | 14.34 | 135.10 | 1297.0 |) |
| 843786 | M | 12.45 | 15.70 | 82.57 | 477.1 | L |
| | smoothnes | s_mean compa | ctness_mean con | ncavity_mean co | oncave.po | ints_mean |
| 842302 | 0 | .11840 | 0.27760 | 0.3001 | | 0.14710 |
| 842517 | 0 | .08474 | 0.07864 | 0.0869 | | 0.07017 |
| 84300903 | 0 | .10960 | 0.15990 | 0.1974 | | 0.12790 |
| 84348301 | 0 | .14250 | 0.28390 | 0.2414 | | 0.10520 |
| 84358402 | 0 | .10030 | 0.13280 | 0.1980 | | 0.10430 |
| 843786 | 0 | .12780 | 0.17000 | 0.1578 | | 0.08089 |
| | symmetry_ | mean fractal | _dimension_mean | n radius_se tex | ture_se p | erimeter_se |
| 842302 | 0. | 2419 | 0.0787 | 1 1.0950 | 0.9053 | 8.589 |
| 842517 | 0. | 1812 | 0.05667 | 7 0.5435 | 0.7339 | 3.398 |
| 84300903 | 0. | 2069 | 0.05999 | 9 0.7456 | 0.7869 | 4.585 |
| 84348301 | 0. | 2597 | 0.09744 | 4 0.4956 | 1.1560 | 3.445 |
| 84358402 | 0. | 1809 | 0.05883 | 3 0.7572 | 0.7813 | 5.438 |
| 843786 | 0. | 2087 | 0.07613 | 3 0.3345 | 0.8902 | 2.217 |
| | area_se s | moothness_se | compactness_se | e concavity_se | concave. | ooints_se |
| 842302 | 153.40 | 0.006399 | 0.04904 | 4 0.05373 | | 0.01587 |
| 842517 | 74.08 | 0.005225 | 0.01308 | 0.01860 | | 0.01340 |
| 84300903 | 94.03 | 0.006150 | 0.04006 | 0.03832 | | 0.02058 |
| 84348301 | 27.23 | 0.009110 | 0.07458 | 0.05661 | | 0.01867 |
| 84358402 | 94.44 | 0.011490 | 0.02463 | 0.05688 | | 0.01885 |

| 843786 | 27.19 | 0.00751 | LO | 0.03345 | 0.03 | 3672 | 0.01137 |
|----------|-------------------------|----------|-----------|-----------|------------|---------------|---------|
| | symmetry_se | fractal_ | dimensi | on_se rad | ius_worst | texture_wors | t |
| 842302 | 0.03003 | | 0.00 | 06193 | 25.38 | 17.3 | 3 |
| 842517 | 0.01389 | | 0.00 | 03532 | 24.99 | 23.4 | 1 |
| 84300903 | 0.02250 | | 0.00 | 04571 | 23.57 | 25.5 | 3 |
| 84348301 | 0.05963 | | 0.00 | 09208 | 14.91 | 26.5 | O |
| 84358402 | 0.01756 | | 0.00 | 05115 | 22.54 | 16.6 | 7 |
| 843786 | 0.02165 | | 0.00 | 05082 | 15.47 | 23.7 | 5 |
| | perimeter_wo | rst area | a_worst a | smoothnes | s_worst co | ompactness_wo | rst |
| 842302 | 184 | .60 | 2019.0 | | 0.1622 | 0.6 | 656 |
| 842517 | 158 | .80 | 1956.0 | | 0.1238 | 0.18 | 366 |
| 84300903 | 152 | .50 | 1709.0 | | 0.1444 | 0.4 | 245 |
| 84348301 | 98 | .87 | 567.7 | | 0.2098 | 0.8 | 663 |
| 84358402 | 152 | .20 | 1575.0 | | 0.1374 | 0.20 | 050 |
| 843786 | 103 | .40 | 741.6 | | 0.1791 | 0.5 | 249 |
| | concavity_wo | rst cond | cave.poir | nts_worst | symmetry | _worst | |
| 842302 | 0.7 | 119 | | 0.2654 | (| 0.4601 | |
| 842517 | 0.2 | 416 | | 0.1860 | (| 0.2750 | |
| 84300903 | 0.4 | 504 | | 0.2430 | (| 0.3613 | |
| 84348301 | 0.6 | 869 | | 0.2575 | (| 0.6638 | |
| 84358402 | 0.4 | 000 | | 0.1625 | (| 0.2364 | |
| 843786 | 0.5 | 355 | | 0.1741 | (| 0.3985 | |
| | <pre>fractal_dime</pre> | nsion_wo | orst | | | | |
| 842302 | | 0.11 | 1890 | | | | |
| 842517 | | 0.08 | 3902 | | | | |
| 84300903 | | 0.08 | 3758 | | | | |
| 84348301 | | 0.17 | 7300 | | | | |
| 84358402 | | 0.07 | 7678 | | | | |
| 843786 | | 0.12 | 2440 | | | | |
| | | | | | | | |

```
wisc.data <- wisc.df[,-1]
```

Q1. How many observations are in this dataset?

```
nrow(wisc.data)
```

[1] 569

Q1A. There are 569 observations in this data set.

Q2. How many of the observations have a malignant diagnosis?

```
diagnosis <- c(wisc.df[,1])
sum(diagnosis == "M")</pre>
```

[1] 212

Q2A. There are 212 observations that have a malignant diagnosis.

Q3. How many variables/features in the data are suffixed with _mean?

```
library(stringr)
cn<-colnames(wisc.data, do.NULL = TRUE)
sum(str_count(cn, "_mean"))</pre>
```

[1] 10

Q3A. There are 10 variables in the data that are suffixed with "_mean".

Q4. From your results, what proportion of the original variance is captured by the first principal components (PC1)?

colMeans(wisc.data)

| perimeter_mean | texture_mean | radius_mean |
|------------------------------------|--------------------------|------------------------|
| 9.196903e+01 | 1.928965e+01 | 1.412729e+01 |
| compactness_mean | ${\tt smoothness_mean}$ | area_mean |
| 1.043410e-01 | 9.636028e-02 | 6.548891e+02 |
| symmetry_mean | concave.points_mean | concavity_mean |
| 1.811619e-01 | 4.891915e-02 | 8.879932e-02 |
| texture_se | radius_se | fractal_dimension_mean |
| 1.216853e+00 | 4.051721e-01 | 6.279761e-02 |
| smoothness_se | area_se | perimeter_se |
| 7.040979e-03 | 4.033708e+01 | 2.866059e+00 |
| concave.points_se | concavity_se | compactness_se |
| 1.179614e-02 | 3.189372e-02 | 2.547814e-02 |
| radius_worst | fractal_dimension_se | symmetry_se |
| 1.626919e+01 | 3.794904e-03 | 2.054230e-02 |
| area_worst | perimeter_worst | texture_worst |
| 8.805831e+02 | 1.072612e+02 | 2.567722e+01 |
| concavity_worst | compactness_worst | smoothness_worst |
| 2.721885e-01 | 2.542650e-01 | 1.323686e-01 |
| <pre>fractal_dimension_worst</pre> | symmetry_worst | concave.points_worst |
| 8.394582e-02 | 2.900756e-01 | 1.146062e-01 |
| | | |

apply(wisc.data, 2, sd)

```
radius_mean
                                   texture_mean
                                                          perimeter_mean
          3.524049e+00
                                   4.301036e+00
                                                            2.429898e+01
             area_mean
                                smoothness_mean
                                                        compactness_mean
          3.519141e+02
                                   1.406413e-02
                                                            5.281276e-02
        concavity mean
                            concave.points mean
                                                           symmetry_mean
          7.971981e-02
                                   3.880284e-02
                                                            2.741428e-02
fractal dimension mean
                                      radius se
                                                              texture se
          7.060363e-03
                                   2.773127e-01
                                                            5.516484e-01
          perimeter_se
                                                           smoothness se
                                        area se
          2.021855e+00
                                   4.549101e+01
                                                            3.002518e-03
        compactness_se
                                   concavity_se
                                                       concave.points_se
          1.790818e-02
                                   3.018606e-02
                                                            6.170285e-03
           symmetry_se
                           fractal_dimension_se
                                                            radius_worst
          8.266372e-03
                                   2.646071e-03
                                                            4.833242e+00
         texture_worst
                                perimeter_worst
                                                              area_worst
          6.146258e+00
                                   3.360254e+01
                                                            5.693570e+02
      smoothness_worst
                              compactness_worst
                                                         concavity_worst
          2.283243e-02
                                   1.573365e-01
                                                            2.086243e-01
  concave.points_worst
                                 symmetry_worst fractal_dimension_worst
          6.573234e-02
                                   6.186747e-02
                                                            1.806127e-02
```

wisc.pr <- prcomp(wisc.data, scale=TRUE)
summary(wisc.pr)</pre>

Importance of components:

PC2 PC3 PC4 PC5 PC6 PC7 PC1 Standard deviation 3.6444 2.3857 1.67867 1.40735 1.28403 1.09880 0.82172 Proportion of Variance 0.4427 0.1897 0.09393 0.06602 0.05496 0.04025 0.02251 Cumulative Proportion 0.4427 0.6324 0.72636 0.79239 0.84734 0.88759 0.91010 PC8 PC9 PC10 PC11 PC12 PC13 PC14 0.69037 0.6457 0.59219 0.5421 0.51104 0.49128 0.39624 Standard deviation Proportion of Variance 0.01589 0.0139 0.01169 0.0098 0.00871 0.00805 0.00523 0.92598 0.9399 0.95157 0.9614 0.97007 0.97812 0.98335 Cumulative Proportion PC16 PC17 PC18 PC19 PC20 Standard deviation 0.30681 0.28260 0.24372 0.22939 0.22244 0.17652 0.1731 Proportion of Variance 0.00314 0.00266 0.00198 0.00175 0.00165 0.00104 0.0010 Cumulative Proportion 0.98649 0.98915 0.99113 0.99288 0.99453 0.99557 0.9966

```
PC22
                                  PC23
                                         PC24
                                                  PC25
                                                          PC26
                                                                  PC27
                                                                          PC28
Standard deviation
                       0.16565 0.15602 0.1344 0.12442 0.09043 0.08307 0.03987
Proportion of Variance 0.00091 0.00081 0.0006 0.00052 0.00027 0.00023 0.00005
Cumulative Proportion 0.99749 0.99830 0.9989 0.99942 0.99969 0.99992 0.99997
                          PC29
                                  PC30
Standard deviation
                       0.02736 0.01153
Proportion of Variance 0.00002 0.00000
Cumulative Proportion 1.00000 1.00000
```

Q4A. PC1 captures a proportion of 0.4427 of the original variance.

Q5. How many principal components (PCs) are required to describe at least 70% of the original variance in the data?

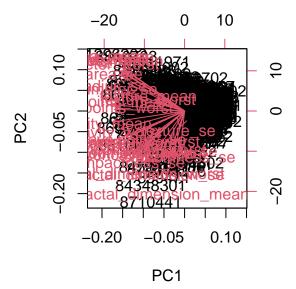
Q5A. 3 principal components are required to describe at least 70% of the original variance in the data.

Q6. How many principal components (PCs) are required to describe at least 90% of the original variance in the data?

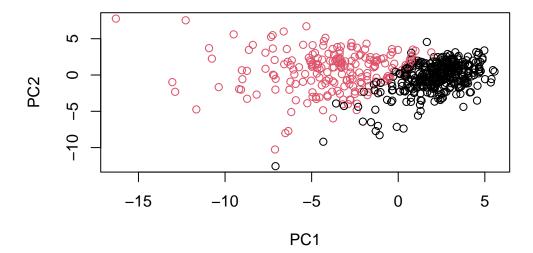
Q6A. 7 of the principal components are required to describe at least 90% of the original variance in the data.

Q7. What stands out to you about this plot? Is it easy or difficult to understand? Why?

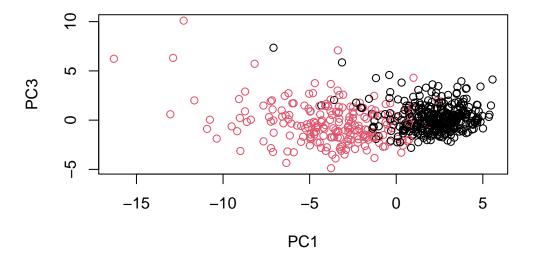
biplot(wisc.pr)



Q7A. There are too many variables in this plot, making it very difficult to understand. We will need to shorten the amount of variables to make it easier to digest.

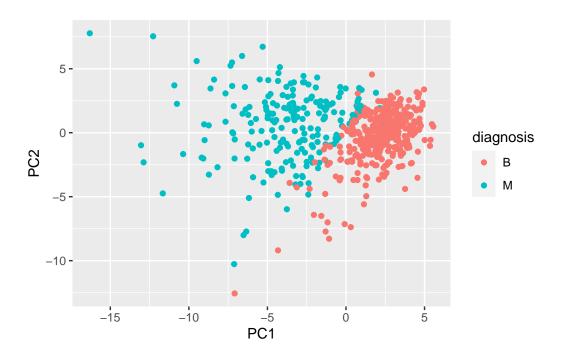


Q8. Generate a similar plot for principal components 1 and 3. What do you notice about these plots?



Q8A. There is a cleaner cut in the first plot because principal component 1 explains more variance in the original data than principal component 3.

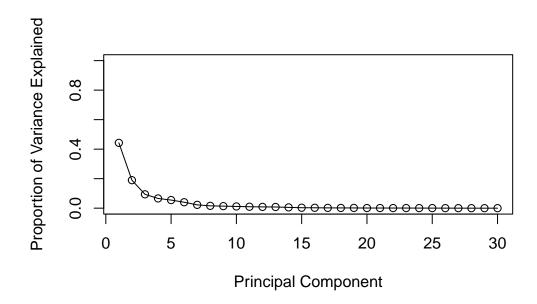
```
df <- as.data.frame(wisc.pr$x)
df$diagnosis <- diagnosis
library(ggplot2)
ggplot(df) +
   aes(PC1, PC2, col=diagnosis) + geom_point()</pre>
```

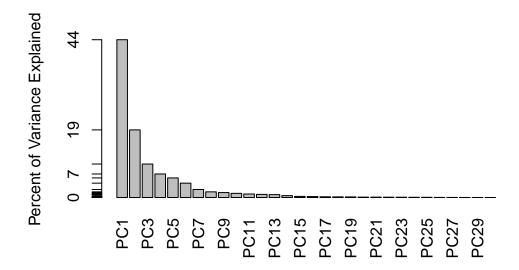


```
pr.var <- wisc.pr$sdev^2
head(pr.var)</pre>
```

[1] 13.281608 5.691355 2.817949 1.980640 1.648731 1.207357

```
pve <- pr.var / sum(pr.var)
plot(pve, xlab = "Principal Component",
    ylab = "Proportion of Variance Explained",
    ylim = c(0, 1), type = "o")</pre>
```





Q9. For the first principal component, what is the component of the loading vector (i.e. wisc.pr\$rotation[,1]) for the feature concave.points_mean?

wisc.pr\$rotation[,1]

| perimeter_mean | texture_mean | radius_mean |
|-------------------|--------------------------|-----------------------------------|
| -0.22753729 | -0.10372458 | -0.21890244 |
| compactness_mean | ${\tt smoothness_mean}$ | area_mean |
| -0.23928535 | -0.14258969 | -0.22099499 |
| symmetry_mean | concave.points_mean | concavity_mean |
| -0.13816696 | -0.26085376 | -0.25840048 |
| texture_se | radius_se | <pre>fractal_dimension_mean</pre> |
| -0.01742803 | -0.20597878 | -0.06436335 |
| smoothness_se | area_se | perimeter_se |
| -0.01453145 | -0.20286964 | -0.21132592 |
| concave.points_se | concavity_se | compactness_se |
| -0.18341740 | -0.15358979 | -0.17039345 |
| radius_worst | fractal_dimension_se | symmetry_se |
| -0.22799663 | -0.10256832 | -0.04249842 |
| area_worst | perimeter_worst | texture_worst |
| -0.22487053 | -0.23663968 | -0.10446933 |
| concavity_worst | compactness_worst | smoothness_worst |
| | | |

```
-0.12795256 -0.21009588 -0.22876753

concave.points_worst symmetry_worst fractal_dimension_worst

-0.25088597 -0.12290456 -0.13178394
```

Q9A. -0.26085376

Q10. What is the minimum number of principal components required to explain 80% of the variance of the data?

```
pve

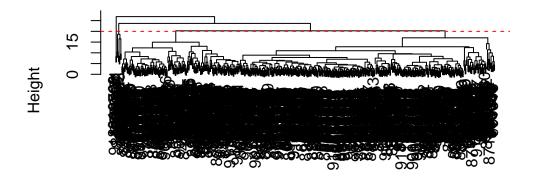
[1] 4.427203e-01 1.897118e-01 9.393163e-02 6.602135e-02 5.495768e-02 [6] 4.024522e-02 2.250734e-02 1.588724e-02 1.389649e-02 1.168978e-02 [11] 9.797190e-03 8.705379e-03 8.045250e-03 5.233657e-03 3.137832e-03 [16] 2.662093e-03 1.979968e-03 1.753959e-03 1.649253e-03 1.038647e-03 [21] 9.990965e-04 9.146468e-04 8.113613e-04 6.018336e-04 5.160424e-04 [26] 2.725880e-04 2.300155e-04 5.297793e-05 2.496010e-05 4.434827e-06 4.427203e-01 + 1.897118e-01 + 9.393163e-02 + 9.393163e-02
```

Q10A. 4 principal components is the minimum number required to explain 80% of the variance in the data.

```
data.scaled <- scale(wisc.data)
data.dist <- dist(data.scaled)
wisc.hclust <- hclust(data.dist, method = "complete")</pre>
```

Q11. Using the plot() and abline() functions, what is the height at which the clustering model has 4 clusters?

```
plot(wisc.hclust)
abline(h=20, col="red", lty=2)
```



data.dist hclust (*, "complete")

Q11A. The clustering model has 4 clusters at a height of 20.

```
wisc.hclust.clusters <- cutree(wisc.hclust, k = 4)
table(wisc.hclust.clusters, diagnosis)</pre>
```

diagnosis
wisc.hclust.clusters B M
1 12 165
2 2 5
3 343 40
4 0 2

Q12. Can you find a better cluster vs diagnoses match by cutting into a different number of clusters between 2 and 10?

```
wisc.hclust.clusters <- cutree(wisc.hclust, k = 8)
table(wisc.hclust.clusters, diagnosis)</pre>
```

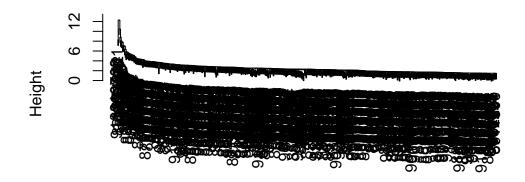
 $\begin{array}{cccc} & \text{diagnosis} \\ \text{wisc.hclust.clusters} & \text{B} & \text{M} \\ & 1 & 12 & 86 \end{array}$

Q12A. With 8 clusters, we can see that there is cluster 2, which contains only malignant diagnoses. This is a better separation than cluster 1 in the 4 cluster example, which had benign and malignant diagnoses.

Q13. Which method gives your favorite results for the same data.dist dataset? Explain your reasoning.

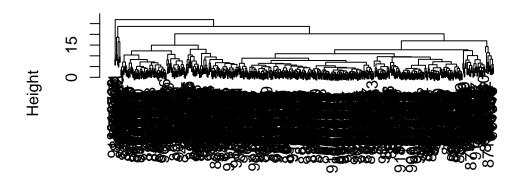
```
wisc.hclustS <- hclust(data.dist, method = "single")
plot(wisc.hclustS)</pre>
```

Cluster Dendrogram



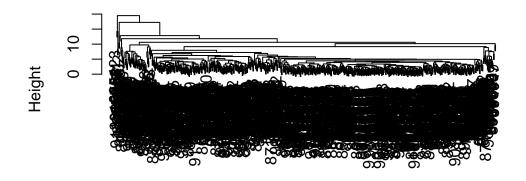
data.dist hclust (*, "single")

```
wisc.hclustC <- hclust(data.dist, method = "complete")
plot(wisc.hclustC)</pre>
```



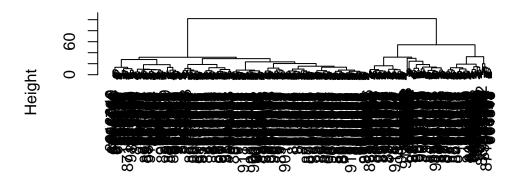
data.dist hclust (*, "complete")

```
wisc.hclustA <- hclust(data.dist, method = "average")
plot(wisc.hclustA)</pre>
```



data.dist hclust (*, "average")

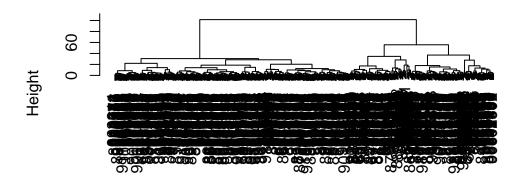
```
wisc.hclustD <- hclust(data.dist, method = "ward.D2")
plot(wisc.hclustD)</pre>
```



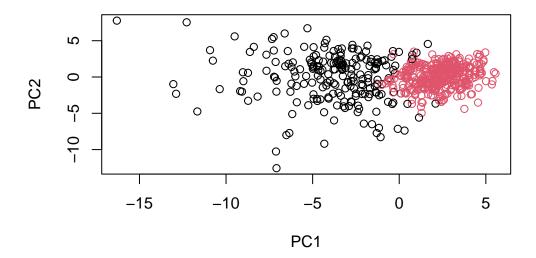
data.dist hclust (*, "ward.D2")

Q13A. I like the complete method of clustering the dataset because it looks cleaner and more neat than the other methods. It also uses more space on the plot, so more connections can be understood.

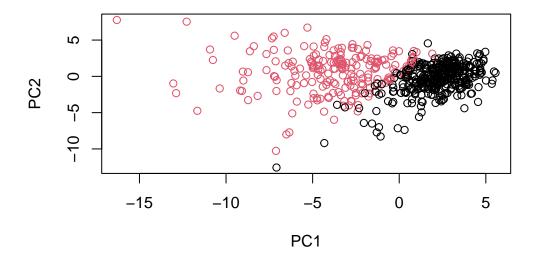
```
wisc.pr.hclust <- hclust(dist(wisc.pr$x[, 1:7]), method = "ward.D2")
plot(wisc.pr.hclust)</pre>
```



dist(wisc.pr\$x[, 1:7]) hclust (*, "ward.D2")



plot(wisc.pr\$x[,1:2], col=diagnosis)



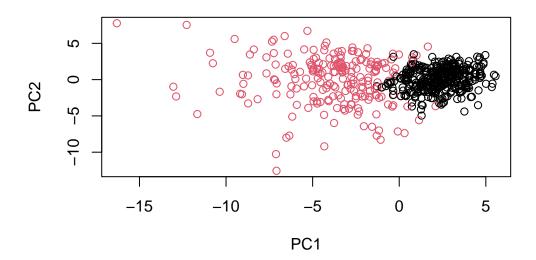
```
g <- as.factor(grps)
levels(g)

[1] "1" "2"

g <- relevel(g,2)
levels(g)

[1] "2" "1"

plot(wisc.pr$x[,1:2], col=g)</pre>
```



```
wisc.pr.hclust <- hclust(dist(wisc.pr$x[, 1:7]), method="ward.D2")
wisc.pr.hclust.clusters <- cutree(wisc.pr.hclust, k=2)
table(wisc.pr.hclust.clusters, diagnosis)</pre>
```

 $\begin{array}{ccc} & \text{diagnosis} \\ \text{wisc.pr.hclust.clusters} & \text{B} & \text{M} \end{array}$

28 188
 329 24

Q15. How well does the newly created model with four clusters separate out the two diagnoses?

Q15A. The newly created model does a good job of separating out the two diagnoses.

Q16. How well do the k-means and hierarchical clustering models you created in previous sections (i.e. before PCA) do in terms of separating the diagnoses? Again, use the table() function to compare the output of each model (wisc.km\$cluster and wisc.hclust.clusters) with the vector containing the actual diagnoses.

Q16A. The hierarchical clustering model I created in the previous section also does a good job in separating the diagnoses.

Q17. Which of your analysis procedures resulted in a clustering model with the best specificity? How about sensitivity?

```
## PCA Clustering
## Sensitivity
188 / (188 + 24)

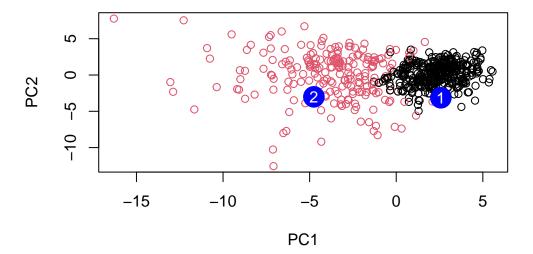
[1] 0.8867925

## Specificity
329 / (329 + 28)
```

[1] 0.9215686

```
## Before PCA Clustering
  ## Sensitivity
  165 / (165 + 5 + 40 + 2)
[1] 0.7783019
  ## Specificity
  343 / (343 + 2 + 12)
[1] 0.9607843
Q17A. The PCA model has a higher sensitivity while the hierarchical clustering model before
PCA has a higher specificity.
  url <- "https://tinyurl.com/new-samples-CSV"</pre>
  new <- read.csv(url)</pre>
  npc <- predict(wisc.pr, newdata=new)</pre>
  npc
           PC1
                     PC2
                                 PC3
                                            PC4
                                                       PC5
                                                                  PC6
                                                                              PC7
[1,] 2.576616 -3.135913 1.3990492 -0.7631950 2.781648 -0.8150185 -0.3959098
[2,] -4.754928 -3.009033 -0.1660946 -0.6052952 -1.140698 -1.2189945
                                                                       0.8193031
                      PC9
                                                      PC12
            PC8
                                 PC10
                                           PC11
                                                                PC13
                                                                          PC14
[1,] -0.2307350 0.1029569 -0.9272861 0.3411457 0.375921 0.1610764 1.187882
[2,] -0.3307423 0.5281896 -0.4855301 0.7173233 -1.185917 0.5893856 0.303029
          PC15
                     PC16
                                  PC17
                                              PC18
                                                           PC19
                                                                       PC20
[1,] 0.3216974 -0.1743616 -0.07875393 -0.11207028 -0.08802955 -0.2495216
[2,] 0.1299153 0.1448061 -0.40509706 0.06565549 0.25591230 -0.4289500
           PC21
                      PC22
                                  PC23
                                             PC24
                                                          PC25
                                                                        PC26
[1,] 0.1228233 0.09358453 0.08347651 0.1223396 0.02124121 0.078884581
[2,] -0.1224776 0.01732146 0.06316631 -0.2338618 -0.20755948 -0.009833238
             PC27
                          PC28
                                       PC29
                                                     PC30
[1,] 0.220199544 -0.02946023 -0.015620933 0.005269029
[2,] -0.001134152  0.09638361  0.002795349 -0.019015820
  plot(wisc.pr$x[,1:2], col=g)
```

```
points(npc[,1], npc[,2], col="blue", pch=16, cex=3)
text(npc[,1], npc[,2], c(1,2), col="white")
```



Q18. Which of these new patients should we prioritize for follow up based on your results?

Q18A. We should prioritize patient 2 for follow up because it is likely that they have a malignant condition. Furthermore, it is likely that patient 1 has a benign condition.