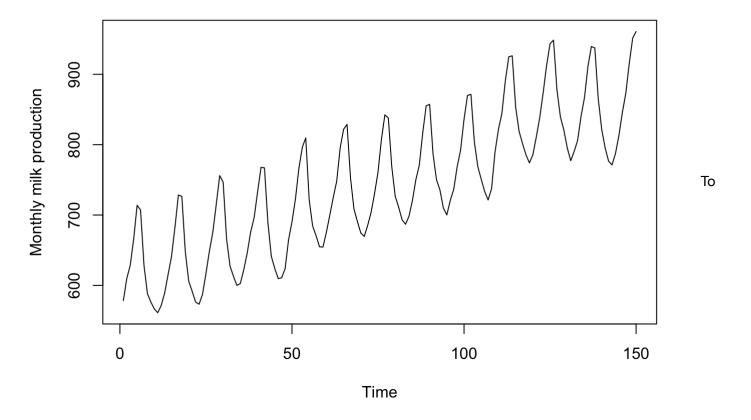
pstat274_lab07_aoxu

AO XU

2022-11-09

```
library(tsdl)
milk <- subset(tsdl, 12, "Agriculture")[[3]]
train <- milk[1:150]
test <- milk[151:156]
ts.plot(train, ylab = "Monthly milk production")</pre>
```



make it more stationary, we need to remove trend and seasonality:

```
dmilk <- diff(train, 12)
ddmilk <- diff(dmilk, 1)
dmilk</pre>
```

```
##
          10.8
                  5.5
                       12.8
                              17.2
                                     14.7
                                           19.2
                                                 19.6
                                                        17.7
                                                               15.2
                                                                       9.8
                                                                            12.1
                                                                                   15.7
     [1]
                        34.3
                              32.5
                                     27.5
                                           20.3
                                                  17.7
                                                         21.6
                                                               21.3
                                                                     23.6
                                                                            29.5
                                                                                   35.4
##
    [13]
          27.5
                 33.3
##
    [25]
          29.5
                 27.5
                        20.6
                              17.2
                                     11.8
                                           20.3
                                                  23.6
                                                         13.8
                                                               11.2
                                                                       9.8
                                                                              8.1
                                                                                    1.0
##
    [37]
          18.6
                 14.2
                        26.5
                              33.5
                                     28.5
                                           42.6
                                                  32.4
                                                         43.2
                                                               46.6
                                                                      45.2
                                                                            43.6
                                                                                   52.0
    [49]
          35.4
                 34.8
                        25.6
                              29.4
                                     25.5
                                           19.3
                                                  31.4
                                                         24.5
                                                               20.3
                                                                      19.6
                                                                            15.2
                                                                                    9.8
##
                                     20.6
##
    [61]
           3.9
                  5.4
                        12.7
                              12.2
                                             9.1
                                                  15.7
                                                        17.7
                                                               20.3
                                                                      18.7
                                                                            17.3
                                                                                   12.8
   [73]
                                     12.8
                                                  17.7
                                                                                   22.6
##
          16.7
                 19.6
                         9.9
                               9.1
                                           19.3
                                                         23.5
                                                               24.4
                                                                      16.7
                                                                            13.2
##
    [85]
          15.7
                 18.4
                        21.6
                              19.3
                                     14.7
                                           14.2
                                                  17.6
                                                         18.7
                                                               15.2
                                                                      23.5
                                                                            21.3
                                                                                   16.7
##
   [97]
          53.0
                 53.3
                        52.0
                              54.8
                                     55.0
                                           54.8
                                                  49.1
                                                         50.1
                                                               50.7
                                                                      52.1
                                                                            52.7
                                                                                   48.1
## [109]
          21.6
                        29.5
                                     18.7
                                           22.3
                                                 24.6
                                                         20.6
                                                               19.3
                                                                       9.8
                                                                                    4.9
                 16.8
                              22.3
                                                                              3.1
                                     -4.0 -11.1 -12.8 -17.7 -25.4 -18.7
## [121]
          -4.9
                  1.7
                        -6.9
                              -2.0
                                                                            -6.1
                                                                                   -3.0
## [133]
            6.9
                  5.4
                         5.9
                               4.1
                                     11.8 23.3
```

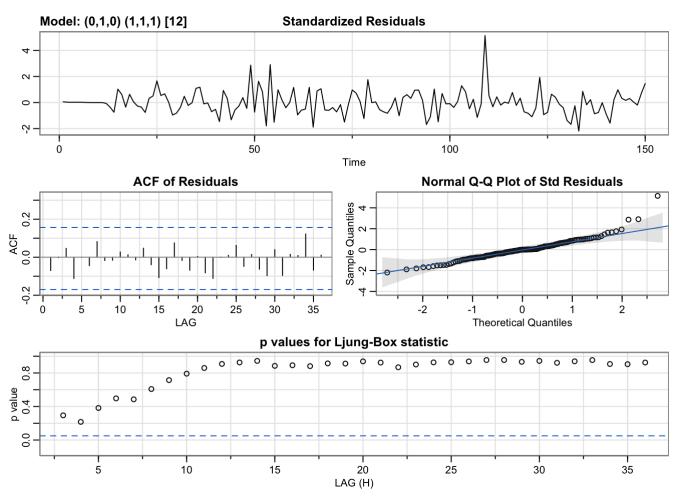
ddmilk

```
##
                              -2.5
                                             0.4
                                                         -2.5
                                                                -5.4
                                                                       2.3
          -5.3
                  7.3
                         4.4
                                      4.5
                                                  -1.9
                                                                              3.6
                                                                                    11.8
     [1]
##
    [13]
            5.8
                  1.0
                        -1.8
                              -5.0
                                     -7.2
                                            -2.6
                                                    3.9
                                                         -0.3
                                                                 2.3
                                                                       5.9
                                                                              5.9
                                                                                    -5.9
##
    [25]
          -2.0
                 -6.9
                        -3.4
                              -5.4
                                      8.5
                                             3.3
                                                  -9.8
                                                         -2.6
                                                                -1.4
                                                                      -1.7
                                                                             -7.1
                                                                                    17.6
##
    [37]
          -4.4
                 12.3
                         7.0
                              -5.0
                                     14.1 -10.2
                                                  10.8
                                                          3.4
                                                                -1.4
                                                                       -1.6
                                                                              8.4 -16.6
##
   [49]
          -0.6
                 -9.2
                         3.8
                              -3.9
                                     -6.2
                                            12.1
                                                  -6.9
                                                         -4.2
                                                                -0.7
                                                                       -4.4
                                                                             -5.4
                                                                                    -5.9
                  7.3
                       -0.5
                               8.4 -11.5
                                                    2.0
                                                          2.6
                                                                             -4.5
                                                                                     3.9
##
    [61]
            1.5
                                             6.6
                                                                -1.6
                                                                      -1.4
##
   [73]
            2.9
                 -9.7
                        -0.8
                                3.7
                                      6.5
                                            -1.6
                                                    5.8
                                                          0.9
                                                                -7.7
                                                                       -3.5
                                                                              9.4
                                                                                    -6.9
##
   [85]
            2.7
                  3.2
                       -2.3
                              -4.6
                                     -0.5
                                             3.4
                                                    1.1
                                                         -3.5
                                                                 8.3
                                                                      -2.2
                                                                             -4.6
                                                                                    36.3
##
   [97]
            0.3
                -1.3
                         2.8
                               0.2
                                     -0.2
                                            -5.7
                                                    1.0
                                                          0.6
                                                                 1.4
                                                                       0.6
                                                                             -4.6 - 26.5
                        -7.2
## [109]
          -4.8
                 12.7
                              -3.6
                                      3.6
                                             2.3
                                                  -4.0
                                                         -1.3
                                                                -9.5
                                                                      -6.7
                                                                              1.8
                                                                                    -9.8
## [121]
                         4.9
                              -2.0
                                     -7.1
                                           -1.7
                                                  -4.9
                                                         -7.7
                                                                       12.6
                                                                              3.1
            6.6
                 -8.6
                                                                 6.7
                                                                                     9.9
## [133]
          -1.5
                  0.5
                       -1.8
                               7.7
                                     11.5
```

library(astsa)

fit.i <- sarima(xdata=train, p=0, d=1, q=0, P=1, D=1, Q=1, S=12)

```
## initial
            value 1.989465
## iter
          2 value 1.850408
##
  iter
          3 value 1.824156
          4 value 1.800049
##
  iter
##
  iter
          5 value 1.791131
##
  iter
          6 value 1.789958
          7 value 1.789636
   iter
          8 value 1.789235
  iter
##
  iter
          9 value 1.789186
##
         10 value 1.789182
  iter
         10 value 1.789182
         10 value 1.789182
##
  iter
##
  final
          value 1.789182
  converged
  initial
            value 1.803940
  iter
##
          2 value 1.803675
##
  iter
          3 value 1.803165
##
  iter
          4 value 1.803164
          5 value 1.803163
##
  iter
##
  iter
          6 value 1.803163
##
          6 value 1.803163
  iter
          value 1.803163
  final
## converged
```



```
# Residual plots:
res <- residuals(fit.i)
res</pre>
```

```
## NULL
```

a.

There is no residual since res is null.

From the ACF of residuals plot, we could get that residuals lie within the 95% CI, so it could be assumed as zero.

From QQ plot, we could get that all points lie on a line, meaning residuals are normally distributed.

Nearly all p-values are greater than 5%, so we fail to reject the hypothesis.

Therefore, the residuals are white noise.

b.

```
# Predict 6 future observations and plot
par(mfrow=c(1, 1))
mypred <- sarima.for(train, n.ahead = 6, p=0, d=1, q=0, P=1, D=1, Q=1, S=12)
#ts.plot(c(milk), xlim=c(1, length(milk) + 6), ylim=c(min(milk)*0.8, max(milk)*1.2))
#points((length(milk) + 1):(length(milk) + 6), col="red",(lambda*mypred$pred + 1)^(1/lambda))
#lines((length(wine) + 1):(length(wine) + 6),(lambda*mypred$pred + 1.96*mypred$se + 1)^(1/lambda), lty=2)
points(151:156, test, col="blue")</pre>
```

