

Robot Autonomy

Lecture 11: Task Planning

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Complex Tasks

- Often need to perform **complex** tasks
 - ▶ Travel to another city
 - ▶ Replace the tire on a car
- **Difficult** to reasoning about tasks directly at c-space level
 - ▶ Matching nuts and bolts together
- Consist of **multiple steps** that need to be performed
 - ▶ Lift car, remove bolts, remove tire, place new tire...
 - ▶ Can use previous planners for individual steps
- Plan for entire task at the more abstract symbolic level

Task Planning Problem

- The robot is given:
 - ▶ An initial state
 - ▶ A goal characterisation (set of goal states)
 - ▶ A set of potential actions
- The robot needs to generate:
 - ▶ A sequence of actions that transforms the initial state into a goal state
- Need to model the state and the actions to plan

Representing States

- The state is represented by set of objects and predicates
- **Constant symbols** to represent objects in the domain
 - ▶ Table, LugNut1, LugNut2, Car, Tire, Axle, ...
 - ▶ Obj1, Obj2, Obj3, Obj4, ...
 - ▶ Assume unique names
- **Predicate symbols** to represent relations and properties
 - ▶ Bolt(a), On(a,b), Grasped(a,b), Metallic(a), Insertable(a,b,c)
 - ▶ Arity is the fixed number of arguments the predicate takes

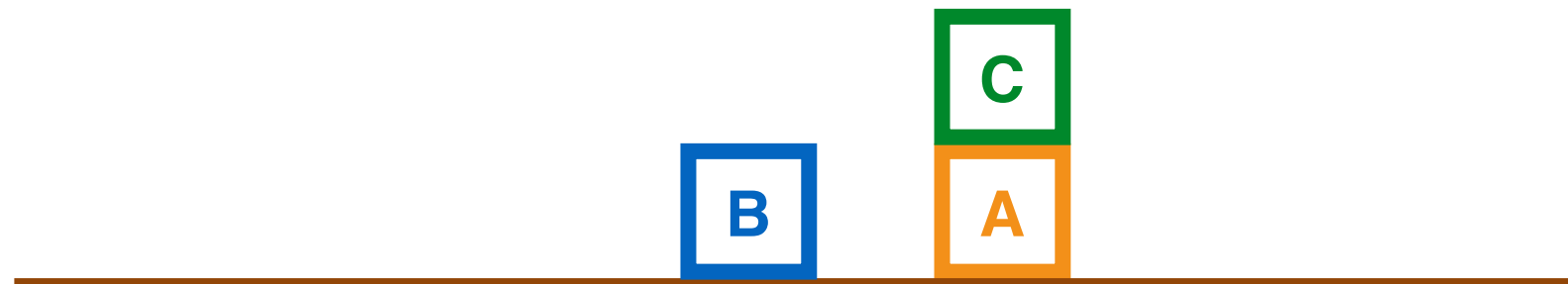
Representing States

- The **state** is defined by a set of **grounded predicates**

- ▶ $\text{Tire}(\text{Flat}) \wedge \text{Tire}(\text{Spare}) \wedge \text{At}(\text{Flat}, \text{Axle}) \wedge \text{At}(\text{Spare}, \text{Trunk})$



- ▶ $\text{On}(\text{A}, \text{Table}) \wedge \text{On}(\text{B}, \text{Table}) \wedge \text{On}(\text{C}, \text{A}) \wedge \text{Block}(\text{A}) \wedge \text{Block}(\text{B}) \wedge \text{Block}(\text{C}) \wedge \text{Clear}(\text{B}) \wedge \text{Clear}(\text{C}) \wedge \text{Clear}(\text{Table})$

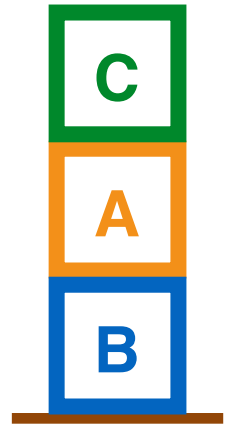
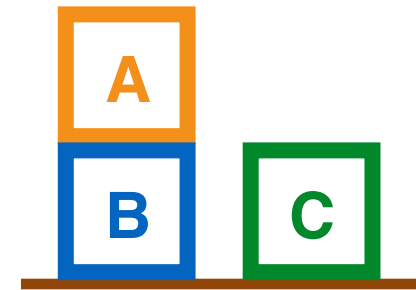


- **Closed-world assumption:**
 - ▶ Only include the positive predicates in the state list
 - ▶ All others are assumed to be negative

Goal Characterization

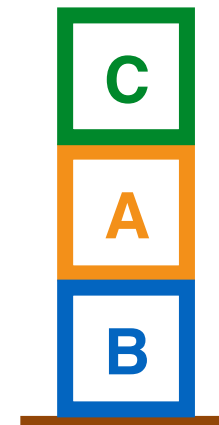
- **Goals** are characterised by a set of conditions

- ▶ $\text{On}(A,B) \wedge \text{Clear}(C)$
- ▶ Goal states entail these conditions



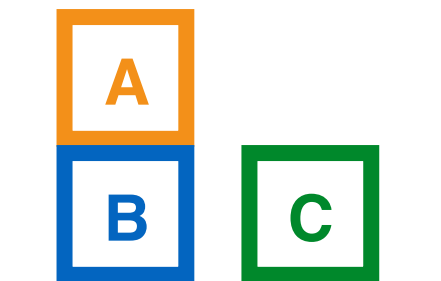
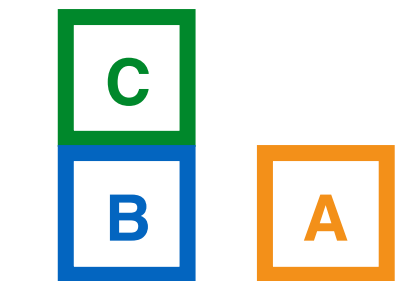
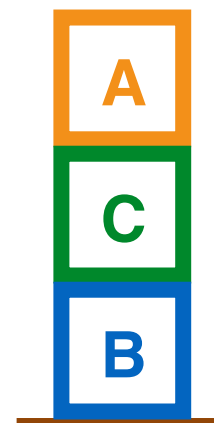
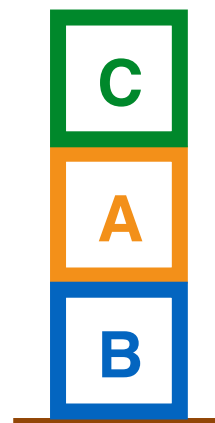
- Can include **positive and negated** conditions

- ▶ $\text{On}(A,B) \wedge \sim \text{Clear}(A)$



- Can include **variables** (true for any)

- ▶ $\text{On}(x,B) \wedge \text{Block}(x)$



Representing Actions

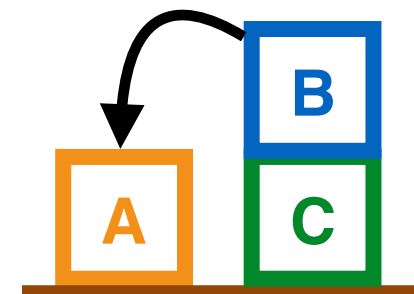
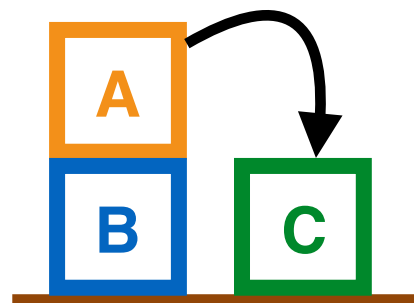
- Actions result in a change of state
 - ▶ Need to model the **effects** of the actions
- Actions are only applicable in certain states
 - ▶ Need to model the **preconditions of the actions**



- Use pre- and post- conditions to sequence actions
- Actions are often interpreted as skills and planners

Action Schemas

- Defining every possible action is exhausting
- Define **action schema**, i.e. lifted actions with variables
 - ▶ **Action Schema:** PutOn(t,Axle)
Action Examples: PutOn(Spare,Axle) or PutOn(Flat,Axle)
 - ▶ **Action Schema:** Move(b,x,y)
Action Examples: Move(A,B,C) or Move(B,C,A)



- Why not Move(Table,A,B) or PutOn(Axle,Axle)?

Preconditions

- **Precondition** define states in which the **action can be executed**
- Preconditions have the same form as goal representation

► Action Schema: PutOn(t,Axle)

Preconditions:

$\text{Tire}(t) \wedge \text{At}(t, \text{Ground}) \wedge \sim \text{At}(\text{Flat}, \text{Axle}) \wedge \sim \text{At}(\text{Spare}, \text{Axle})$

► Action: Move(b,x,y)

Preconditions:

$\text{On}(b, x) \wedge \text{Clear}(b) \wedge \text{Clear}(y) \wedge \text{Block}(b) \wedge \text{Block}(y) \wedge \text{Block}(x) \wedge (b \neq y) \wedge (b \neq x) \wedge (x \neq y)$

- Performing an action has an **effect** on the state
 - ▶ Action Schema: PutOn(t,Axle)
Effects:
 $\sim \text{At}(t, \text{Ground}) \wedge \text{At}(t, \text{Axle})$
 - ▶ Action: Move(b,x,y)
Effects:
 $\sim \text{On}(b, x) \wedge \sim \text{Clear}(y) \wedge \text{On}(b, y) \wedge \text{Clear}(x)$
- Often model effects as **delete and add lists**
- Variables in the effects must also be in the preconditions

Planning Domain Definition Language

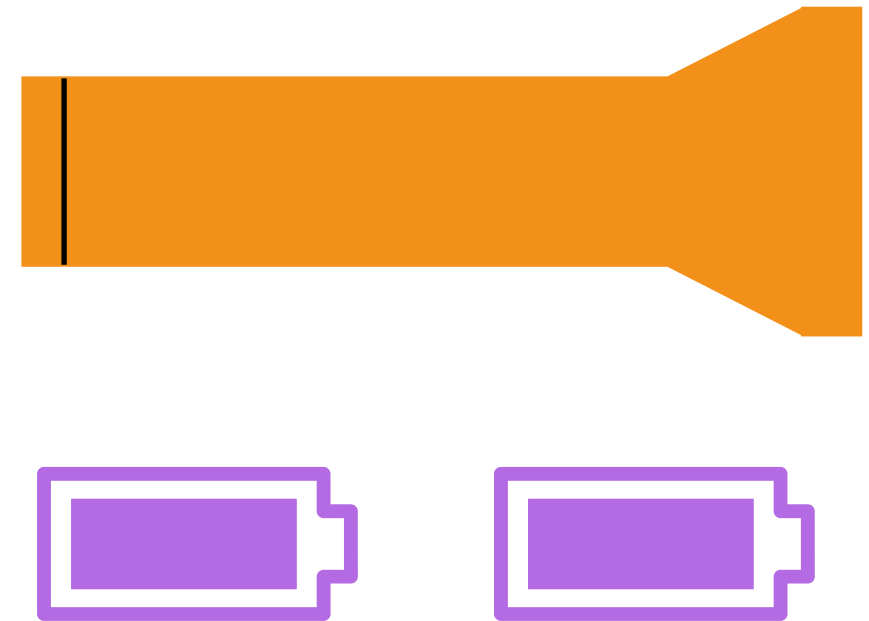
- In practice, define problem using **planning language**, e.g.,
Stanford Research Institute Problem Solver (STRIPS) '71
Action Description Language (ADL) '87
Planning Domain Definition Language (PDDL) '98
- **PDDL** is the standard AI planning language for the International Planning Competition
- PDDL includes ADL and STRIPS
- PDDL problems are defined using **two files**:
 - ▶ **Domain File**: Specifies predicates and action (schemas)
 - ▶ **Problem File**: Specifies objects, initial state, goal characterisation

```
(define (domain domain_name)  
  (:requirements :strips)  
  (:predicates (p1 ?x)  
               ....  
               (pn ?x ?y))  
  (:action action_name  
    :parameters (?v1 ?v2 ... ?vm)  
    :precondition (and (p2 ?v2 ?v3)  
                       ...  
                       (not(pk ?v1)))  
    :effect (and (p1 ?v1)  
                 ....))  
)  
(:action action_name2 ...)
```

```
(define (problem problem_name)  
  (:domain domain_name)  
  (:objects  $i_1, i_2, \dots, i_l$ )  
  (:init (p1 i2 ib)  
        ...  
        (pd i1))  
  (:goal (and (p2 i2 i6)  
             ...  
             (pd i5))  
  )))
```

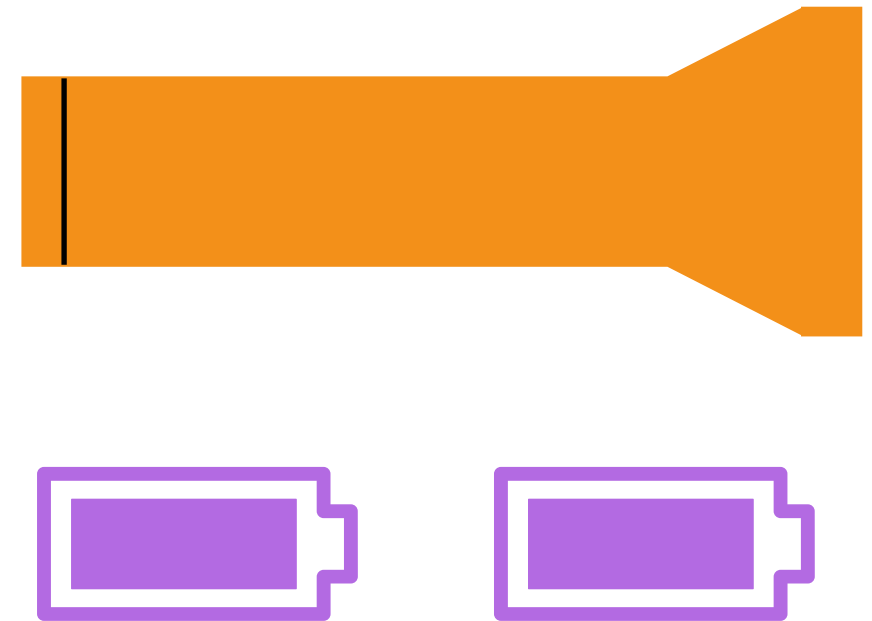
Flashlight Example

```
(define (domain flash_light)
  (:requirements :strips)
  (:predicates (on ?x ?y)
                (in ?x ?y))
  (:action remove_cap
   :parameters (?cap ?flash)
   :precondition ((on ?cap ?flash))
   :effect (not (on ?cap ?flash))
  ))
  (:action insert
   :parameters (?bat ?flash ?cap))
   :precondition (and (not(in ?bat,?flash))
                      (not(on ?cap,?flash)))
   :effect (in ?bat,?flash))
```



Flashlight Example

```
(define (problem flash_light_1)  
  (:domain flash_light)  
  (:objects cap, flash, bat1, bat2)  
  (:init (on cap flash))  
  )  
  (:goal (and (in bat1 flash)  
              (in bat2 flash)  
              (on cap flash))  
  )))
```



Planning as a Search Problem

- Discrete state (defined by symbols)

$$x \in X$$

- Discrete actions (defined by preconditions)

$$u \in U(x)$$

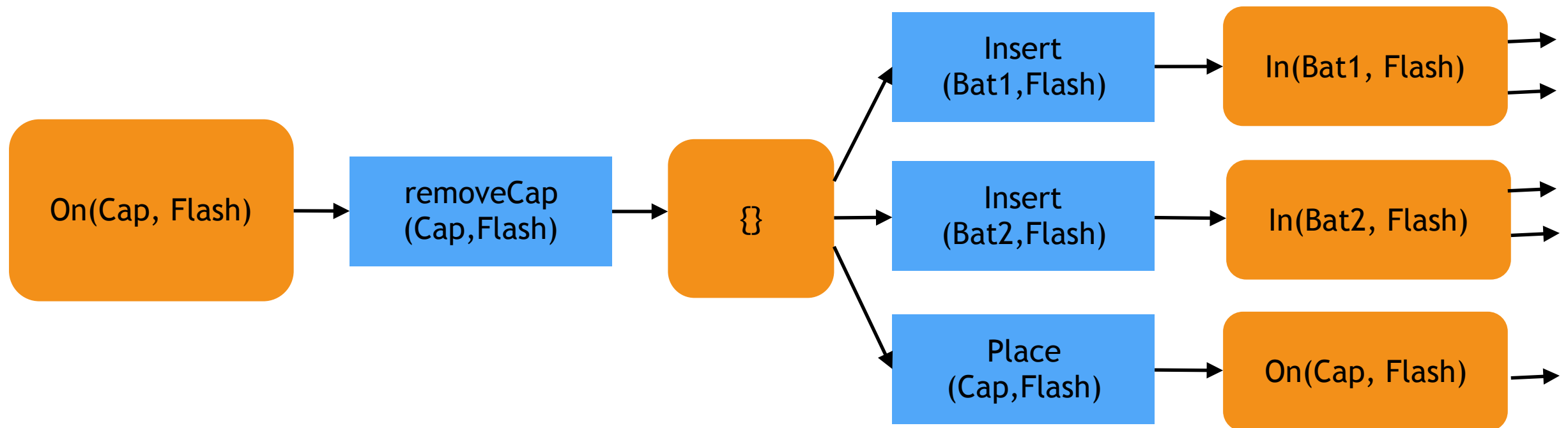
- State transition function (defined by effects)

$$f(x, u) = x'$$

- Treat the planning problem as a discrete search problem

Forward Search (Progression)

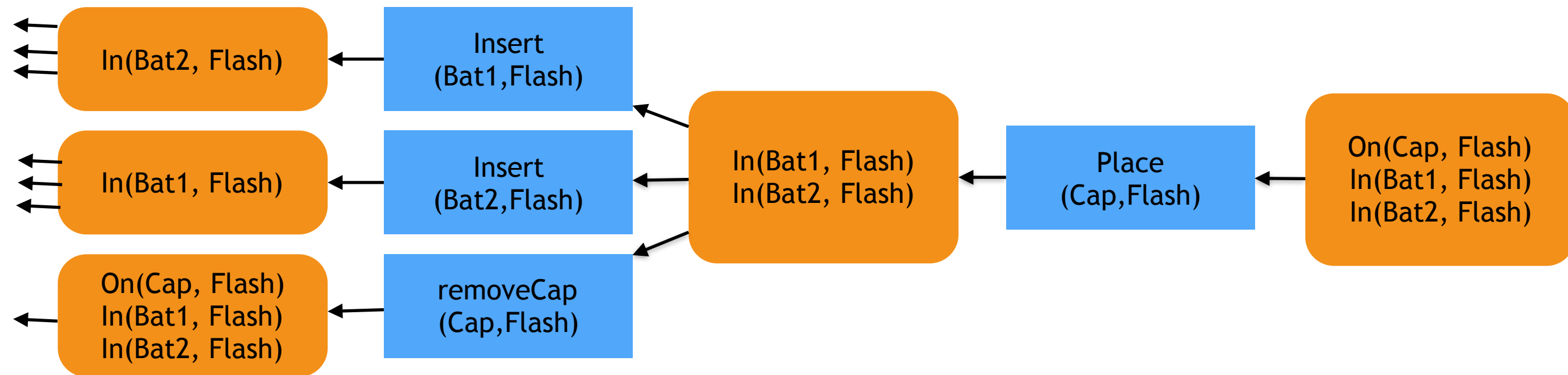
- Start with initial state and search actions forward



- Can have massive branching factor given many actions
- May try many irrelevant actions in search of goal
- Needs a good heuristic to guide action selection

Backward Search (Regression)

- Start with goal state and search actions backwards



- Reverse add/delete and ensure all preconditions met
- Focus on relevant actions - lower branching factor
- May need to consider set of multiple goal states
- Difficult to design heuristics

Heuristic Search

- Search can be very inefficient without some guidance
- Use heuristic to estimate distance from goal for A^*
- Use relaxed problems to estimate cost-to-go
- Ignore preconditions
 - ▶ All actions applicable from any state
 - ▶ Quickly achieve goals directly
- Ignore delete list
 - ▶ Ensure that all goals and preconditions are defined as positive
 - ▶ Monotonic progress towards goal
- (Learn) heuristic for specific domains (e.g., TD-gammon)

Planning Graph

- **Planning graphs** are powerful tools for planning
- Consider the cake problem

Init(Have(Cake))

Goal(Have(Cake) \wedge Eaten(Cake))

Action(Eat(Cake))

PRECOND: *Have(Cake)*

EFFECT: \neg *Have(Cake) \wedge Eaten(Cake)*

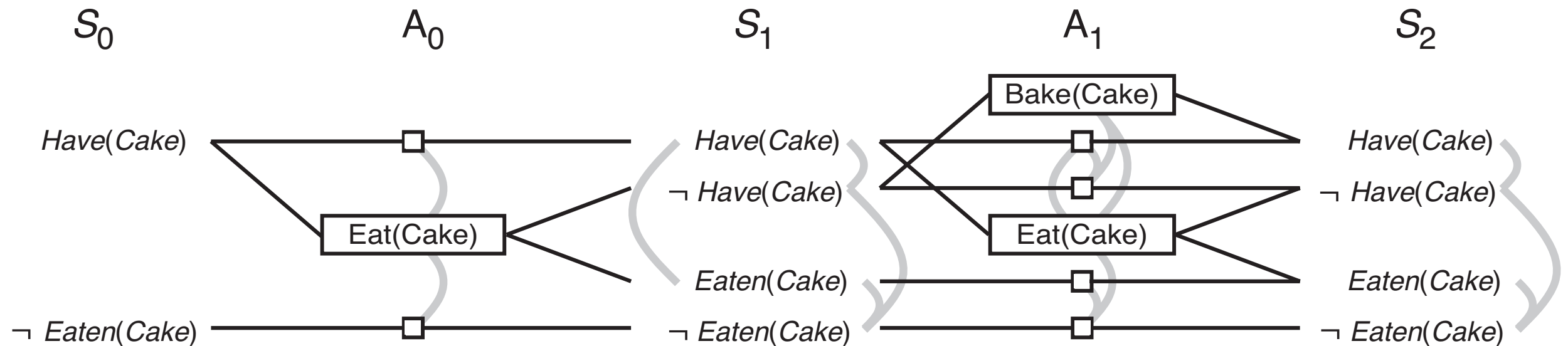
Action(Bake(Cake))

PRECOND: \neg *Have(Cake)*

EFFECT: *Have(Cake)*

Planning Graph

- Planning graph for the cake problem



- Each layer indicates the achievable symbols/actions
- Curves indicate (some) mutual exclusions (mutex)
- Small squares are no-op/persistence actions
- n layers, a actions, l literals: $O(n(a+l)^2)$ time and size

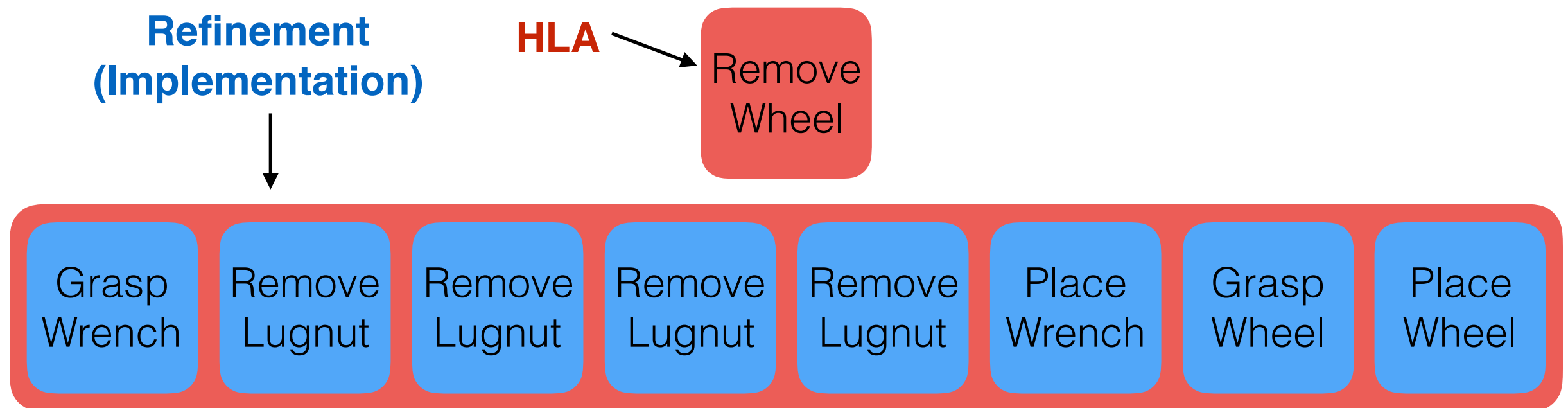
- Actions are mutex if:
 - ▶ An action negates the effect of the other (eat+persist cake)
 - ▶ An effect of one action negates precondition of the other
 - ▶ Preconditions of the actions are mutually exclusive
- State literals are mutex if:
 - ▶ One is the negation of the other
 - ▶ Each pair of actions that could achieve them are mutex
- Over time
 - ▶ Literals and actions increase monotonically
 - ▶ Mutexes decrease monotonically

Planning Graph

- Use planning graph to **generate heuristics**
 - ▶ **Max-level**
 - ▶ Max of level numbers for which each goal symbol first appears
 - ▶ **Level sum**
 - ▶ Sum of level numbers for which each goal symbol first appears
 - ▶ **Set-level**
 - ▶ Level at which all goal conditions appear without mutex
- Use planning graph to **plan** by incremental growth
 - ▶ Extract (regress) solution when goals reached and not mutex
 - ▶ Expand further if search does not find a valid plan

Hierarchical Task Networks (HTNs)

- Many tasks have an inherent hierarchical structure
- Can define **high-level actions** (HLA) for performing tasks



- HLA can contain primitive actions and other HLA
- Implementation only has primitive actions
- Allows defining domain knowledge for faster planning

Hierarchical Task Networks

- Treat HLA with one implementation as macro action
- An HLA can have **multiple implementations**
 - ▶ **Goto airport:** take car, taxi, or bus
 - ▶ **Move block:** push or pick-and-place
- Implementations may have different effects
 - ▶ Model the **reachable** set of states
 - ▶ Set of states reachable given at least one implementation
 - ▶ Reach goal when reachable set of states overlaps goal states
 - ▶ Determine exact implementation by refining plan

Semantic Attachment

- What if action **not** possible in **some** configurations?
 - ▶ e.g., obstacles, joint limits
- Use predicates with **semantic attachment**
 - ▶ CanGrasp(Obj, ObjPose, Grasp, ArmConfig)
 - ▶ Reachable(RobotConfig1, RobotConfig2)
- Use c-space planner to **evaluate predicates** during planning
 - ▶ Provides **feedback from motion** to **symbolic task planner**
- For continuous variables, e.g., Grasp, sample finite set

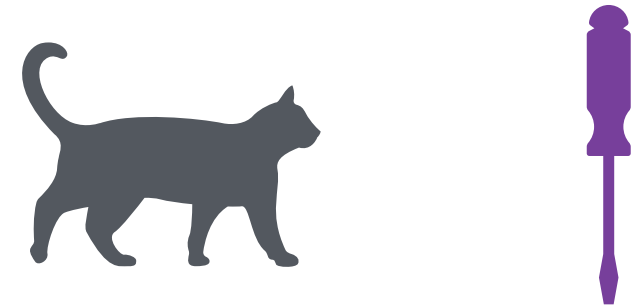
Grounding and Interpretation

- Ground Predicate
 - ▶ Ground predicate has constant syms assigned to it, no variables
 - ▶ e.g., $\text{At}(\text{Tire}, \text{Axle})$ is grounded, $\text{At}(a, b)$ is not, $\text{At}(a, b)$ is lifted
- Interpretation
 - ▶ Interpretation is what a symbol means in the real world
 - ▶ What does it mean to be block?
 - ▶ What does it mean for A to be on B?
- “Grounding” is often used to mean interpretation
 - ▶ Meaning may be obvious to us, but not to a robot
 - ▶ Define or learn groundings

Grounding and Interpretation

- Autonomous robot may need to interpret current state
- Grounding is often represented as a classifier

- ▶ Object recognition
Cat(Obj1), Screwdriver(Obj2)

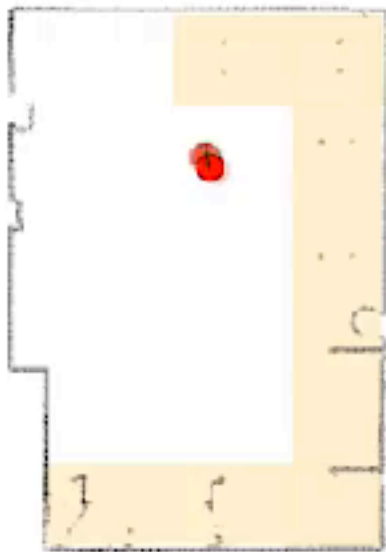


- ▶ Recognising relations
On(A,B), Grasped(Cup,Hand)



Learning Symbols

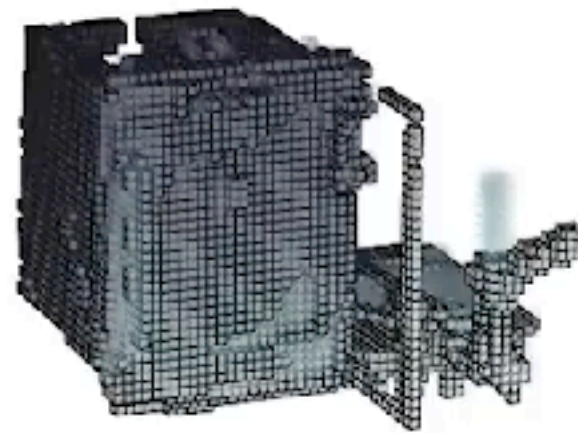
```
(:action cupboard_open1  
:parameters ()  
:precondition (and (symbol1) (symbol3) (symbol4))  
:effect       (and (symbol15) (not (symbol4))  
                  (decrease (reward) 67.44))  
)
```



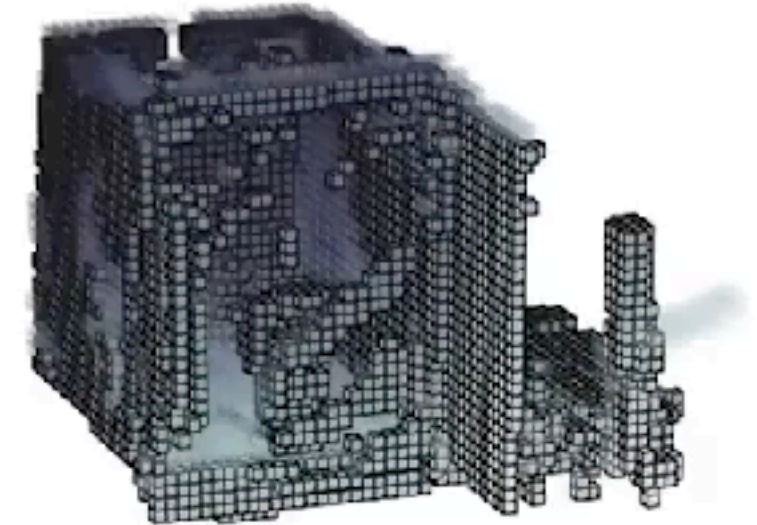
symbol1



symbol3



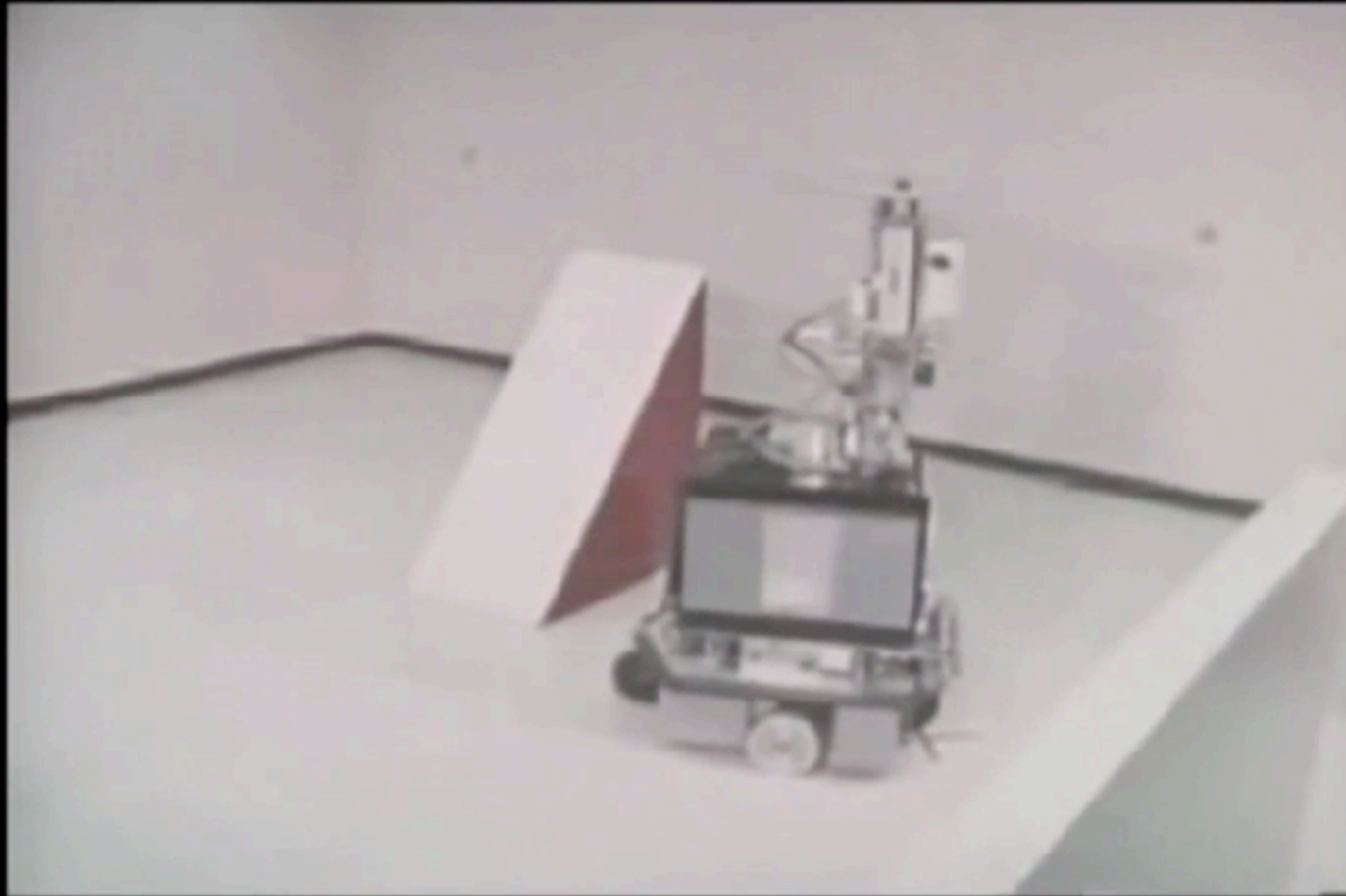
symbol4



Monitoring and Replanning

- Robust execution requires **execution monitoring**
- **Action monitoring:**
 - ▶ Check preconditions before executing an action
- **Plan monitoring:**
 - ▶ Check remaining plan will still succeed
- **Goal monitoring:**
 - ▶ Check if there is a better set of goals to achieve
- If **error** occurs:
 - ▶ **Replan** from the current state
 - ▶ **Repair** plan - plan to get back onto original plan

Shakey



Shakey the Robot - SRI, youtube.com/watch?v=qXdn6ynwpil

Questions?