

$$Bl = \frac{mv}{qR}$$

$$\frac{1}{2} mv^2 = eV \quad \text{or} \quad v = \sqrt{\frac{2eV}{m}}$$

$$\frac{E}{B} = \sqrt{\frac{2eV}{m}} \quad \text{so} \quad \frac{e}{m} = \frac{E^2}{2VB^2}$$

## Physics 1C Equations Page 1

### Fundamental Constants

$c$  = speed of light =  $3.00 \times 10^8 \text{ ms}^{-1}$   
 $k$  = Coulomb's constant =  $8.9876 \times 10^9 \text{ Nm}^2\text{C}^{-2}$   
 $\epsilon_0$  = permittivity of free space =  $8.85 \times 10^{-12} \text{ N}^{-1}\text{C}^2\text{m}^{-2} \text{ (m/F)}$   
 $\mu_0$  = permeability of free space =  $4\pi \times 10^{-7} \text{ H/m}$

### Chapter 27

$\vec{F} = q\vec{v} \times \vec{B}$  = magnetic force on charged particle  
 $\vec{F} = I\vec{l} \times \vec{B}$  magnetic force on a conductor  
 $||F|| = ||q||vB\sin(\phi)$  = magnitude of Magnetic Force  
 $\otimes$  = into page  
 $\odot$  = out of page  
 $\tau = IBAsin(\phi)$  = magnitude of magnetic torque  
 $\vec{\tau} = \vec{\mu} \times \vec{B}$  = magnetic torque  
 $\vec{\mu} = IA$  = magnetic dipole moment  
 $U = -\vec{\mu} \cdot \vec{B} = -\mu B\cos(\phi)$  = potential energy of magnetic moment

### Chapter 28

#### Magnetic Fields

$\vec{B} = \frac{\mu_0 q\vec{v} \times \hat{r}}{4\pi r^2}$  = magnetic field due to a point charge with constant velocity

$d\vec{B} = \frac{\mu_0 I d\vec{l} \times \hat{r}}{4\pi r^2}$  = magnetic field due to an infinitesimal current element (Biot Savart)

$B = \frac{\mu_0 I}{2\pi r}$  magnetic field near a long straight current carrying conductor

$\frac{F}{L} = \frac{\mu_0 II'}{2\pi r}$  force between two long straight parallel current carrying conductors

$\oint \vec{B} \cdot d\vec{A} = 0$  magnetic flux through any closed surface

#### B fields

$B = \frac{\mu_0 I}{2\pi r}$  magnetic field distance r from conductor

$B = \mu_0 nI$  Inside a solenoid, closely wound with n turns per unit length

$B = 0$  outside a solenoid

### Chapter 29 Part A

#### Faraday Induction

$\Phi_B = \int \vec{B} \cdot d\vec{A} = \int B dA \cos(\phi)$

$\mathcal{E} = -\frac{d\Phi_B}{dt}$

#### Motional EMF

$\mathcal{E} = vBL$  where v is conductor speed, L is length and B is the magnitude of the uniform magnetic field  
 $\mathcal{E} = \oint (\vec{v} \times \vec{B}) \cdot d\vec{l}$

### Chapter 29 Part B

#### Lenz's Law

The direction of any magnetic induction effect is such as to oppose the cause of the effect.

#### induced Electric Fields

$\mathcal{E} = \oint \vec{E} \cdot d\vec{l} = -\frac{d\Phi_B}{dt}$

#### Displacement Current

$i_D = \epsilon \frac{d\Phi_E}{dt}$  displacement current

#### Maxwell's equations

$\oint \vec{E} \cdot d\vec{a} = \frac{Q_{encl}}{\epsilon_0}$

$\oint \vec{B} \cdot d\vec{A} = 0$  magnetic flux through any closed surface

$\oint \vec{E} \cdot d\vec{l} = -\frac{d\Phi_B}{dt}$  Faraday's Law

$\oint \vec{B} \cdot d\vec{l} = \mu_0(i_C + \epsilon_0 \frac{d\Phi_E}{dt})_{encl}$  Ampere's Law including Displacement Current

Magnetic force per unit length between two long, straight, parallel, current-carrying conductors

$$\frac{F}{L} = \frac{\mu_0 I I'}{2\pi r}$$

Magnetic constant

Current in first conductor

Current in second conductor

Distance between conductors

Magnetic field on axis of a circular current-carrying loop

$$B_x = \frac{\mu_0 I a^2}{2(x^2 + a^2)^{3/2}}$$

Magnetic constant

Current

Radius of loop

Distance along axis from center of loop to field point

Magnetic field at center of  $N$  circular current-carrying loops

$$B_x = \frac{\mu_0 N I}{2a}$$

Magnetic constant

Number of loops

Current

Radius of loop

Line integral around a closed path

Ampere's law:

$$\oint \vec{B} \cdot d\vec{l} = \mu_0 I_{\text{encl}}$$

Scalar product of magnetic field and vector segment of path

Net current enclosed by path

Faraday's law:

The induced emf in a closed loop ...

$$\mathcal{E} = -\frac{d\Phi_B}{dt}$$

... equals the negative of the time rate of change of magnetic flux through the loop.

Motional emf, conductor length and velocity perpendicular to uniform  $\vec{B}$

$$\mathcal{E} = vBL$$

Conductor speed

Conductor length

Magnitude of uniform magnetic field

Line integral over all elements of closed conducting loop

Motional emf, general case

$$\mathcal{E} = \oint (\vec{v} \times \vec{B}) \cdot d\vec{l}$$

Length vector of conductor element

Magnetic field at position of element

Velocity of conductor element

Line integral of electric field around path

Faraday's law for a stationary integration path:

$$\oint \vec{E} \cdot d\vec{l} = -\frac{d\Phi_B}{dt}$$

Negative of the time rate of change of magnetic flux through path

Displacement current through an area

$$i_D = \epsilon \frac{d\Phi_E}{dt}$$

Time rate of change of electric flux through area

Permittivity of material in area

Flux of electric field through a closed surface

Gauss's law for  $\vec{E}$ :

$$\oint \vec{E} \cdot d\vec{A} = \frac{Q_{\text{encl}}}{\epsilon_0}$$

Charge enclosed by surface

Electric constant

Flux of magnetic field through any closed surface ...

Gauss's law for  $\vec{B}$ :

$$\oint \vec{B} \cdot d\vec{A} = 0$$

... equals zero.

Line integral of electric field around path

Faraday's law for a stationary integration path:

$$\oint \vec{E} \cdot d\vec{l} = -\frac{d\Phi_B}{dt}$$

Negative of the time rate of change of magnetic flux through path

Magnetic force on a moving charged particle

$$\vec{F} = q\vec{v} \times \vec{B}$$

Particle's charge

Particle's velocity

Magnetic field

Magnetic flux through a surface

$$\Phi_B = \int B \cos \phi \, dA = \int B_{\perp} \, dA = \int \vec{B} \cdot d\vec{A}$$

Magnitude of magnetic field  $\vec{B}$

Angle between  $\vec{B}$  and normal to surface

Element of surface area

Vector element of surface area

The total magnetic flux through any closed surface ...

Gauss's law for magnetism:

$$\oint \vec{B} \cdot d\vec{A} = 0$$

... equals zero.

Radius of a circular orbit in a magnetic field

$$R = \frac{mv}{|q|B}$$

Particle's mass

Particle's speed

Magnetic-field magnitude

Particle's charge

Magnetic force on a straight wire segment

$$\vec{F} = I\vec{l} \times \vec{B}$$

Current

Vector length of segment (points in current direction)

Magnetic field

Magnetic force on an infinitesimal wire segment

$$d\vec{F} = I d\vec{l} \times \vec{B}$$

Current

Vector length of segment (points in current direction)

Magnetic field

Vector magnetic torque on a current loop

$$\vec{\tau} = \vec{\mu} \times \vec{B}$$

Magnetic dipole moment

Magnetic field

Potential energy for a magnetic dipole in a magnetic field

$$U = -\vec{\mu} \cdot \vec{B} = -\mu B \cos \phi$$

Magnetic dipole moment

Magnetic field

Angle between  $\vec{\mu}$  and  $\vec{B}$

Hall effect:

$$nq = \frac{-J_x B_y}{E_z}$$

Concentration of mobile charge carriers

Charge per carrier

Current density

Magnetic field

Electrostatic field in conductor

Magnetic field due to a point charge with constant velocity

$$\vec{B} = \frac{\mu_0}{4\pi} \frac{q\vec{v} \times \hat{r}}{r^2}$$

Magnetic constant

Charge

Velocity

Unit vector from point charge toward where field is measured

Distance from point charge to where field is measured

Magnetic field due to an infinitesimal current element

$$d\vec{B} = \frac{\mu_0}{4\pi} \frac{I d\vec{l} \times \hat{r}}{r^2}$$

Magnetic constant

Current

Vector length of element (points in current direction)

Unit vector from element toward where field is measured

Distance from element to where field is measured

Magnetic field near a long, straight, current-carrying conductor

$$B = \frac{\mu_0 I}{2\pi r}$$

Magnetic constant

Current

Distance from conductor

$$\mu = IA$$

# Physics 1C Equations Page 2

## Chapter 30 Part A

### Mutually Induced EMFS

$$\mathcal{E}_1 = -M \frac{di_2}{dt} \text{ Induced EMF in coil 1}$$

$$\mathcal{E}_2 = -M \frac{di_1}{dt} \text{ Induced EMF in coil 2}$$

### Mutual Inductance

$$M_{21} = \frac{N_2 \Phi_{B2}}{i_1}$$

a change in current  $i_1$  in coil 1 induces an emf in coil 2 proportional to rate of change of  $i_1$

$$M = \frac{N_2 \Phi_{B2}}{i_1} = \frac{N_1 \Phi_{B1}}{i_2}$$

### Self Inductance

$$\mathcal{E} = -L \frac{di}{dt}$$

The self induced emf in a circuit is proportional to the inductance of the circuit multiplied by the rate of change of current in the circuit.

$$L = \frac{N \Phi_B}{i}$$

The self inductance of a coil is defined to be the number of turns in the coil, multiplied by the flux due to current through each turn, divided by the current in the coil

## Chapter 30 Part B

### Magnetic Field Energy

$$U_L = \frac{1}{2} LI^2(t)$$

An inductor with inductance  $L$  carrying current  $I$  has an energy  $U$  associated with the inductor's magnetic field. The magnetic energy density  $u$  (energy per unit volume) is proportional to the square of the magnetic field magnitude

$$u = \frac{B^2}{2\mu_0}$$

(in a vacuum)

$$U_C = \frac{1}{2} \frac{Q^2}{C}$$

$$V = IR \text{ Always True in General}$$

$$P = IV$$

$$P = I^2 R$$

### LC circuits

$$\omega = \sqrt{\frac{1}{LC}}$$

A circuit that contains inductance  $L$  and capacitance  $C$  undergoes electrical oscillations with angular frequency  $\omega$  that depends on  $L$  and  $C$

$$\omega' = \sqrt{\frac{1}{LC} - \frac{r^2}{4L^2}}$$

A circuit containing inductance, resistance and capacitance undergoes oscillations that are damped with frequency  $\omega'$

## Chapter 31

### AC current

$$i = I \cos(\omega t)$$

$$I_{rms} = \frac{I}{\sqrt{2}}$$

$$V_{rms} = \frac{V}{\sqrt{2}}$$

### AC Circuits

$$V_R = V_R \cos(\omega t)$$

Amplitude of Voltage across a resistor

$$V_L = IX_L$$

Amplitude of Voltage across an inductor where  $X_L = \omega L$

$L$  leads current by 90 deg =  $(\phi + 90 \text{ deg})$

$$V_C = IX_C$$

Amplitude of Voltage across a capacitor where  $X_C = \frac{1}{\omega C}$

$C$  lags current by 90 deg =  $(\phi - 90 \text{ deg})$

### Impedance and the LRC series circuit

$$V = IZ$$

In a general AC circuit, the voltage and current amplitudes are related by the circuit impedance  $Z$ . In an LRC series, the values of these and the angular frequency  $\omega$  determine  $Z$  and the phase angle of the voltage relative to the current.

$$Z = \sqrt{R^2 + [\omega L - \frac{1}{\omega C}]^2}$$

$$\tan(\phi) = \frac{\omega L - \frac{1}{\omega C}}{R}$$

**Ampere's law for a stationary integration path:**

$$\oint \vec{B} \cdot d\vec{l} = \mu_0 \left( i_c + \epsilon_0 \frac{d\Phi_E}{dt} \right)_{\text{encl}}$$

Line integral of magnetic field around path  
Magnetic constant  
Conduction current through path  
Electric constant  
Time rate of change of electric flux through path  
Displacement current through path

**Mutually induced emfs:**

$$\mathcal{E}_2 = -M \frac{di_1}{dt} \quad \text{and} \quad \mathcal{E}_1 = -M \frac{di_2}{dt}$$

Induced emf in coil 2  
Rate of change of current in coil 1  
Induced emf in coil 1  
Rate of change of current in coil 2  
Mutual inductance of coils 1 and 2  
Magnetic flux through each turn of coil 2  
Turns in coil 2  
Magnetic flux through each turn of coil 1  
Turns in coil 1

**Mutual inductance of coils 1 and 2**

$$M = \frac{N_2 \Phi_{B2}}{i_1} = \frac{N_1 \Phi_{B1}}{i_2}$$

Current in coil 1 (causes flux through coil 2)  
Current in coil 2 (causes flux through coil 1)  
Number of turns in coil

**Self-inductance (or inductance) of a coil**

$$L = \frac{N\Phi_B}{i}$$

Flux due to current through each turn of coil  
Current in coil  
Inductance of circuit

**Self-induced emf in a circuit**

$$\mathcal{E} = -L \frac{di}{dt}$$

Rate of change of current in circuit

**Energy stored in an inductor**

$$U = L \int_0^I i \, di = \frac{1}{2} LI^2$$

Integral from initial (zero) value of instantaneous current to final value  
Inductance  
Final current

**Magnetic energy density in vacuum**

$$u = \frac{B^2}{2\mu_0}$$

Magnetic-field magnitude  
Magnetic constant

**Magnetic energy density in a material**

$$u = \frac{B^2}{2\mu}$$

Magnetic-field magnitude  
Permeability of material

**Time constant for an R-L circuit**

$$\tau = \frac{L}{R}$$

Inductance  
Resistance

**Angular frequency of oscillation in an L-C circuit**

$$\omega = \sqrt{\frac{1}{LC}}$$

Capacitance  
Inductance

$$i = \frac{\mathcal{E}}{R} \left( 1 - e^{-(R/L)t} \right) \quad (\text{current in an } R - L \text{ circuit with emf})$$

### Mass-Spring System

$$\text{Kinetic energy} = \frac{1}{2} m v_x^2$$

$$\text{Potential energy} = \frac{1}{2} k x^2$$

$$\frac{1}{2} m v_x^2 + \frac{1}{2} k x^2 = \frac{1}{2} k A^2$$

$$v_x = \pm \sqrt{k/m} \sqrt{A^2 - x^2}$$

$$v_x = dx/dt$$

$$\omega = \sqrt{\frac{k}{m}}$$

$$x = A \cos(\omega t + \phi)$$

### Inductor-Capacitor Circuit

$$\text{Magnetic energy} = \frac{1}{2} L i^2$$

$$\text{Electrical energy} = q^2/2C$$

$$\frac{1}{2} L i^2 + q^2/2C = Q^2/2C$$

$$i = \pm \sqrt{1/LC} \sqrt{Q^2 - q^2}$$

$$i = dq/dt$$

$$\omega = \sqrt{\frac{1}{LC}}$$

$$q = Q \cos(\omega t + \phi)$$

# Physics 1C Equations Page 3

## Chapter 32

### Maxwell's equations

$$\oint \vec{E} \cdot d\vec{a} = \frac{Q_{encl}}{\epsilon_0}$$

$\oint \vec{B} \cdot d\vec{A} = 0$  magnetic flux through any closed surface

$$\oint \vec{E} \cdot d\vec{l} = -\frac{d\Phi_B}{dt} \text{ Faraday's Law}$$

$$\oint \vec{B} \cdot d\vec{l} = \mu_0(i_C + \epsilon_0 \frac{d\Phi_E}{dt})_{encl} \text{ Ampere's Law including Displacement Current}$$

### Field Magnitudes

$E = cB$  Electric Field Magnitude in terms of Magnetic Field Magnitude

$B = \epsilon_0 \mu_0 c E$  Electromagnetic wave in a vacuum

### Speed of light

$$c = \frac{1}{\sqrt{\epsilon_0 \mu_0}}$$

### Sinusoidal Electromagnetic Waves

$\vec{E}(x, t) = \hat{j} E_{max} \cos(kx - \omega t)$  For a wave traveling in the + x direction

If the wave is traveling in - x direction, replace  $kx - \omega t$  by  $kx + \omega t$ .

If wave is traveling in y or z direction, use the right hand rule to find the direction of the  $E_{max} \cos(kx - \omega t)$  vector.

## Chapter 32 Part B

### Sinusoidal Electromagnetic Waves

$\vec{B}(x, t) = \hat{k} B_{max} \cos(kx - \omega t)$  For a wave traveling in the + x direction

If the wave is traveling in - x direction, replace  $kx - \omega t$  by  $kx + \omega t$ .

If wave is traveling in y or z direction, use the right hand rule to find the direction of the  $B_{max} \cos(kx - \omega t)$  vector.

$$E_{max} = c B_{max}$$

### Poynting Vector

$$\vec{S} = \frac{1}{\mu_0} \vec{E} \times \vec{B}$$

$$I = S_{av} = \frac{E_{max} B_{max}}{2\mu_0} = \frac{E_{max}^2}{2\mu_0 c} = \frac{1}{2} \sqrt{\frac{\epsilon_0}{\mu_0}} E_{max}^2 = \frac{1}{2} \epsilon_0 c E_{max}^2$$

### Radiation Pressure

$$\frac{1}{A} \frac{dp}{dt} = \frac{S}{c} = \frac{EB}{\mu_0 c} \text{ flow rate of electromagnetic momentum}$$

$$p_{rad} = \frac{I}{c} \text{ for a perfect absorber}$$

$$p_{rad} = \frac{2I}{c} \text{ for a perfect reflector}$$

## Chapter 37

### Time dilation

$$\Delta t = \frac{\Delta t_0}{\sqrt{1 - \frac{u^2}{c^2}}}$$

### Length contraction

$$l = l_0 \sqrt{1 - \frac{u^2}{c^2}}$$

### Lorentz Transformations

For observers where the relative velocity difference is along the x axis

$$x' = \frac{x - ut}{\sqrt{1 - \frac{u^2}{c^2}}}$$

$$y' = y$$

$$z' = z$$

$$t' = \frac{t - \frac{ux}{c^2}}{\sqrt{1 - \frac{u^2}{c^2}}}$$

For observers where the relative velocity difference is along the x axis

$$v'_x = \frac{v_x - u}{1 - \frac{uv_x}{c^2}}$$

$$v_x = \frac{v'_x + u}{1 + \frac{uv'_x}{c^2}}$$

Angular frequency of underdamped oscillations in an  $L$ - $R$ - $C$  series circuit

$$\omega' = \sqrt{\frac{1}{LC} - \frac{R^2}{4L^2}}$$

Sinusoidal alternating current:

$$i = I \cos \omega t$$

Rectified average value of a sinusoidal current

$$I_{\text{rav}} = \frac{2}{\pi} I = 0.637 I$$

Root-mean-square (rms) value of a sinusoidal current

$$I_{\text{rms}} = \frac{I}{\sqrt{2}}$$

Root-mean-square (rms) value of a sinusoidal voltage

$$V_{\text{rms}} = \frac{V}{\sqrt{2}}$$

Amplitude of voltage across a resistor, ac circuit

$$V_R = IR$$

Amplitude of voltage across an inductor, ac circuit

$$V_L = IX_L$$

Amplitude of voltage across a capacitor, ac circuit

$$V_C = IX_C$$

Circuit Element	Amplitude Relationship	Circuit Quantity	Phase of $v$
Resistor	$V_R = IR$	$R$	In phase with $i$
Inductor	$V_L = IX_L$	$X_L = \omega L$	Leads $i$ by $90^\circ$
Capacitor	$V_C = IX_C$	$X_C = 1/\omega C$	Lags $i$ by $90^\circ$

Amplitude of voltage across an ac circuit

$$V = IZ$$

$$Z = \sqrt{R^2 + (X_L - X_C)^2}$$

Impedance of an  $L$ - $R$ - $C$  series circuit

$$Z = \sqrt{R^2 + [\omega L - (1/\omega C)]^2}$$

Phase angle of voltage with respect to current in an  $L$ - $R$ - $C$  series circuit

$$\tan \phi = \frac{\omega L - 1/\omega C}{R}$$

Average power into a general ac circuit

$$P_{\text{av}} = \frac{1}{2} VI \cos \phi = V_{\text{rms}} I_{\text{rms}} \cos \phi$$

Resonance angular frequency of an  $L$ - $R$ - $C$  series circuit

$$\omega_0 = \frac{1}{\sqrt{LC}}$$





