

7.2

$$(1) \quad X \sim N(\mu_x, 784) \quad Y \sim N(\mu_y, 627)$$

$$\bar{X} = 937.4 \quad n = 56 \quad \bar{Y} = 988.9 \quad n = 57$$

$$\alpha = 0.10$$

$$\bar{X} - \bar{Y} = -51.5$$

$$\xi_0 = Z_{\alpha/2} \sqrt{\frac{\sigma_x^2}{n} + \frac{\sigma_y^2}{n}}$$

$$= 1.65 \sqrt{\quad}$$

$$= 8.25$$

$$P(-59.75 < \bar{X} - \bar{Y} < -43.25) = 90\%$$

(5)

$$\bar{X} = 5.916 \quad \bar{Y} = 8.153$$

$$s_x = 0.663 \quad s_y = 1.187$$

$$\bar{X} - \bar{Y} = -2.2364$$

$$\xi = 0.40979$$

$$P(-\infty < \bar{X} - \bar{Y} < -1.82666) = 0.95$$

(10)

$$\mu_D \approx \bar{x} = 0.67875$$

$$s = 0.06498$$

$$t = t_{0.05}^{(23)} \frac{s}{\sqrt{24}}$$

(1.714)

$$= 0.089$$

$$P(-0.0104 < \mu_D < \infty) = 0.957.$$

No it is not helpful

7.3

$$(1) \quad a) \quad \hat{p} = \frac{24}{642} = 0.03738$$

$$b) \quad E = Z_{0.025} \sqrt{\frac{\bar{p}(1-\bar{p})}{n}}$$

$$= 1.96 \sqrt{5.665 \cdot 10^{-5}}$$

$$= 0.015$$

$$p(0.0227 < p < 0.052) = 95\%$$

$$(3) \quad a) \quad \bar{Y} = \frac{167}{330} = 0.506$$

$$b) \quad E = Z_{0.05} \sqrt{\frac{\bar{Y}(1-\bar{Y})}{n}}$$

$$1.65 \cdot 0.0225$$

$$= 0.037$$

$$p(0.46 < p < 0.55) = 90\%$$

(10)

$$\bar{p}_1 = \frac{28}{194} \approx 0.144 \quad \bar{p}_2 = \frac{11}{162} \approx 0.067$$

$$E_1 = \frac{Z_{0.025} \cdot 0.025}{1.96}$$

$$P(0.095 < p_1 < 0.194) = 95\%$$

$$\bar{p}_1 - \bar{p}_2 \approx 0.0764$$

$$E = Z_{0.05} \sqrt{\frac{\bar{y}_1(1-\bar{y}_1)}{n_1} + \frac{\bar{y}_2(1-\bar{y}_2)}{n_2}}$$
$$\approx 0.053$$

$$P(0.024 < p_1 - p_2 < 0.129) = 95\%$$

7,4

(3)

$$\mu = 6,09 \quad \sigma = 0,02$$

$$\epsilon = 0,001$$

$$\alpha = 0,1$$

$$n = \left\lceil \left(\frac{z_{\alpha/2} \sigma}{\epsilon} \right)^2 \right\rceil = 1083$$

$$n = 1219 \quad \bar{x} = 6,048 \quad s = 0,022 \quad \alpha = 0,1$$

$$\epsilon = z_{\alpha/2} \left(\frac{0,022}{\sqrt{1219}} \right)$$

$$= 0,00104$$

$$P(6,047 < \bar{x} < 6,049) = 80\%$$

$$\frac{6,049 - 6,048}{0,1} \cdot 14,000 = 58,8K$$

$$P(X < 6,0)$$

$$= P\left(Z < \frac{6,0 - \bar{x}}{s}\right)$$

$$= P(Z < -2,1814) = 0,0146$$

(8)

$$n = 137 \quad \bar{y} = \frac{54}{n} \approx 0,394$$

$$\epsilon = 0,04$$

$$\alpha = 0,1$$

$$n = \left\lceil \left(\frac{z_{\alpha/2}}{\epsilon} \right)^2 (\bar{y})(1-\bar{y}) \right\rceil$$

$$= 404$$

(11)

$$\bar{p} = 0.89$$

$$E = 0.1$$

$$\alpha = 0.05$$

$$n = \left[\left(\frac{z_{\alpha/2}}{E} \right)^2 (\bar{p})(1-\bar{p}) \right]$$

$$n = 38$$

$$\bar{Y} = \frac{44}{60} = 0.733$$

$$\alpha = 0.05$$

$$E = z_{0.025} \sqrt{\frac{\bar{Y}(1-\bar{Y})}{60}}$$
$$= 0.111$$

$$P(0.623 < p < 0.845) = 95\%$$

7.5

(2)

$n=12$

4.8 5.0 5.4 | 5.4 5.5 5.7 5.8 5.9
6.0 6.0 | 6.3 6.8

a) $P(5.4 < n < 6.3) = 96.19\%$

$$\sum_{n=3}^4 \binom{12}{n} \left(\frac{1}{6}\right)^n \left(\frac{5}{6}\right)^{12-n}$$

b) $\sum_{n=1}^6 \binom{12}{n} (0.3)^n (0.7)^{12-n} = 0.948$
 $= 94.8\%$

$$\begin{array}{cccccc}
 (3) & 5.99 & 6.31 & | & 6.58 & 6.78 \\
 & 7.05 & 7.12 & | & 7.40 & 7.80
 \end{array}$$

$$P(6.31 < m < 7.40) = 96\%$$

$$\sum_{n=3}^6 \binom{9}{n} \left(\frac{1}{2}\right)^{12} = 82\%$$

$$(6.58, 7.22)$$