Language Models as Compilers: Simulating Pseudocode Execution Improves Algorithmic Reasoning in Language Models

Anonymous ACL submission

Abstract

Algorithmic reasoning tasks that involve complex logical patterns, such as completing Dyck language, pose challenges for large language models (LLMs), despite their recent success. Prior work has used LLMs to generate *programming language* and applied external compilers for such tasks. Yet, when on the fly, it is hard to generate an executable code with the correct logic for the solution. Even so, code for one instance cannot be reused for others, although they might require the same logic to solve. We present **THINK-AND-EXECUTE**, a novel framework that improves LLMs' algorithmic reasoning: (1) In THINK, we discover task-level logic shared across all instances, and express such logic with ***pseudocode***; (2) In EXECUTE, we tailor the task-level pseudocode to each instance and simulate the execution of it. THINK-AND-EXECUTE outperforms several strong baselines (including CoT and PoT) in diverse algorithmic reasoning tasks. We manifest the advantage of using task-level pseudocode over generating instance-specific solutions one by one. Also, we show that pseudocode can better improve LMs' reasoning than natural language (NL) guidance, even though they are trained with NL instructions.

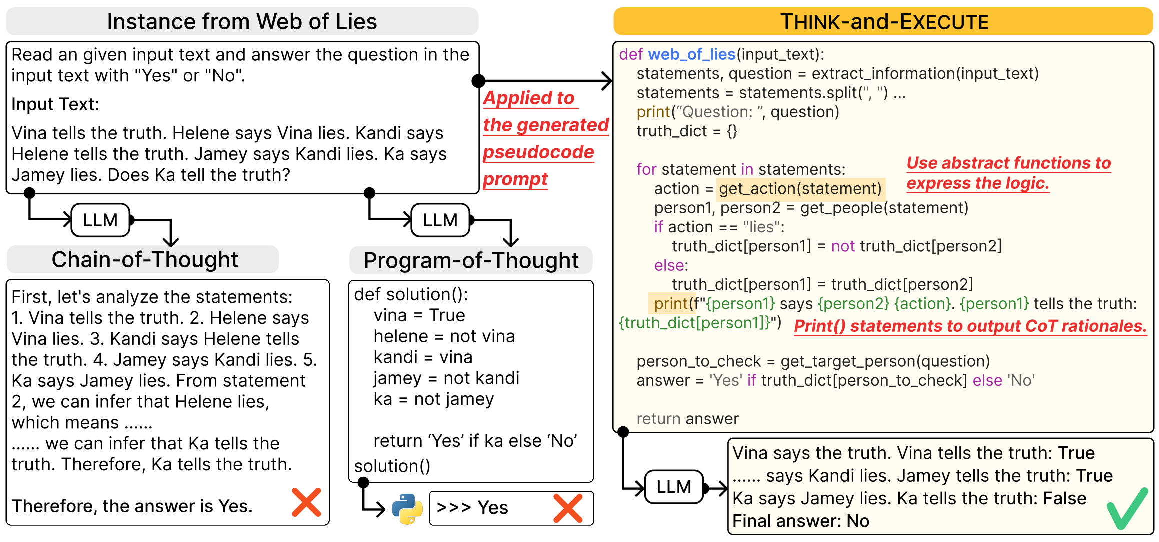
1 Introduction

Reasoning in large language models (LLMs) typically entails analyzing the logical structure underlying a problem and realizing the logic into a sequence of reasoning steps to derive the final answer (Zhou et al., 2022a,b; Hao et al., 2023). In particular, algorithmic reasoning has long been a formidable challenge for LLMs, as it requires to scrutinize a complicated reasoning pattern and to translate it into a long sequence of reasoning steps (Suzgun et al., 2022; Valmeekam et al., 2022; Pan et al., 2023).

To improve the reasoning capabilities of LLMs, prior works have primarily pursued two directions. The first direction includes enhancing the reasoning execution step by generating a rationale in natural language (*e.g.*, Chain-of-Thought (Wei et al., 2022; Kojima et al., 2022)) or a piece of code (*e.g.*, Program-of-Thought (Chen et al., 2023), Program-Aided LMs (Gao et al., 2023)). However, such approaches perform step-by-step reasoning on-the-fly, without a dedicated phase for planning. This necessitates that the LLM analyze the logic and execute it within a single inference call, which constrains its expressiveness. Moreover, when encountering a similar problem, the LLM should solve it without being able to reuse the logic previously understood.

The second direction involves explicitly generating a plan described in natural language with LLMs. The plan describes the logic of the task and the LLM would subsequently concretize it into a sequence of reasoning steps (*e.g.*, Least-to-Most (Zhou et al., 2022b), Plan-and-Solve (Wang et al., 2023)). Yet, as prior works have mentioned, during our preliminary experiments, we find that natural language might not be the optimal medium to describe the logic of the problem (Li et al., 2023). In addition, prior works mostly rely on generating a plan by observing a single instance, which hinders analyzing the core reasoning pattern shared across similar instances within a single task (Zhou et al., 2024).

To address these issues, we introduce THINK-AND-EXECUTE, an algorithmic framework that discovers a logic that reflects the shared reasoning pattern behind a given task, and conducts reasoning by tailoring the logic into each instance. THINK-AND-EXECUTE consists of three distinctive steps; We first ask an LLM to THINK about common reasoning patterns of a task by providing it with a few example questions. Then, the LLM translates the natural language description of the logic in a pseudocode format. The pseudocode format allows more flexibility in applying the logic to each instance compared to programming language such as


Instance from Web of Lies
THINK-and-EXECUTE
Applied to the generated pseudocode prompt
Use abstract functions to express the logic.
Print() statements to output CoT rationales.
LLM
LLM
LLM
Chain-of-Thought
Program-of-Thought

Read an given input text and answer the question in the input text with "Yes" or "No".

Input Text:

Vina tells the truth. Helene says Vina lies. Kandi says Helene tells the truth. Jamey says Kandi lies. Ka says Jamey lies. Does Ka tell the truth?

```
def web_of_lies(input_text):
    statements, question = extract_information(input_text)
    statements = statements.split(", ") ...
    print("Question: ", question)
    truth_dict = {}

    for statement in statements:
        action = get_action(statement)
        person1, person2 = get_people(statement)
        if action == "lies":
            truth_dict[person1] = not truth_dict[person2]
        else:
            truth_dict[person1] = truth_dict[person2]
        print(f"{person1} says {person2} {action}. {person1} tells the truth:
{truth_dict[person1]}")

    person_to_check = get_target_person(question)
    answer = 'Yes' if truth_dict[person_to_check] else 'No'

    return answer
```

First, let's analyze the statements: 1. Vina tells the truth. 2. Helene says Vina lies. 3. Kandi says Helene tells the truth. 4. Jamey says Kandi lies. 5. Ka says Jamey lies. From statement 2, we can infer that Helene lies, which means ......
...... we can infer that Ka tells the truth. Therefore, Ka tells the truth.

Therefore, the answer is Yes. ✗

```
def solution():
    vina = True
    helene = not vina
    kandi = vina
    jamey = not kandi
    ka = not jamey

    return 'Yes' if ka else 'No'
solution()
```

```
>>> Yes
```
✗

```
Vina says the truth. Vina tells the truth: True
...... says Kandi lies. Jamey tells the truth: True
Ka says Jamey lies. Ka tells the truth: False
Final answer: No
```
✓

Figure 1: An illustration of THINK-AND-EXECUTE, compared with Zero-shot Chain-of-Thought (Kojima et al., 2022) and Program-of-Thoughts (Chen et al., 2023).

Python. Finally, in EXECUTE step, the LLM simulates the execution of the task-level pseudocode to follow the logic in it and predicts the output result of the pseudocode.

Through extensive experiments on 7 algorithmic reasoning tasks from Big-Bench Hard (Suzgun et al., 2022), we show the effectiveness of THINK-AND-EXECUTE over the challenging baselines. The superior performance of THINK-AND-EXECUTE over PoT suggests that discovering the common logic for a given task and applying it to each instance would be more helpful than writing instance-specific code for every instance. Noteworthily, simulating the execution of pseudocode is shown to improve LMs' reasoning more than planning with natural language (NL), even though they are trained to follow NL instructions. Furthermore, we empirically show that the pseudocode prompt discovered by an LLM can be applied to small LMs (SLMs), such as CodeLlama-7B, to boost their reasoning ability. This indicates the efficiency of THINK-AND-EXECUTE over other code prompting methods that require the LLM to generate instance-specific code every time (*e.g.*, PoT).

To summarize, our contributions are as follows:

- We introduce THINK-AND-EXECUTE, a framework that performs reasoning with a pseudocode that contains the common logical structure of a given task.
- We show that THINK-AND-EXECUTE achieves notable improvements over strong baselines, including Chain-of-Thought and Program-of-Thought prompting, across various algorithmic tasks in Big-Bench Hard.
- We demonstrate that the pseudocode written by an LLM can be transferred to SLMs, showing the efficiency of our approach.

2 THINK-AND-EXECUTE

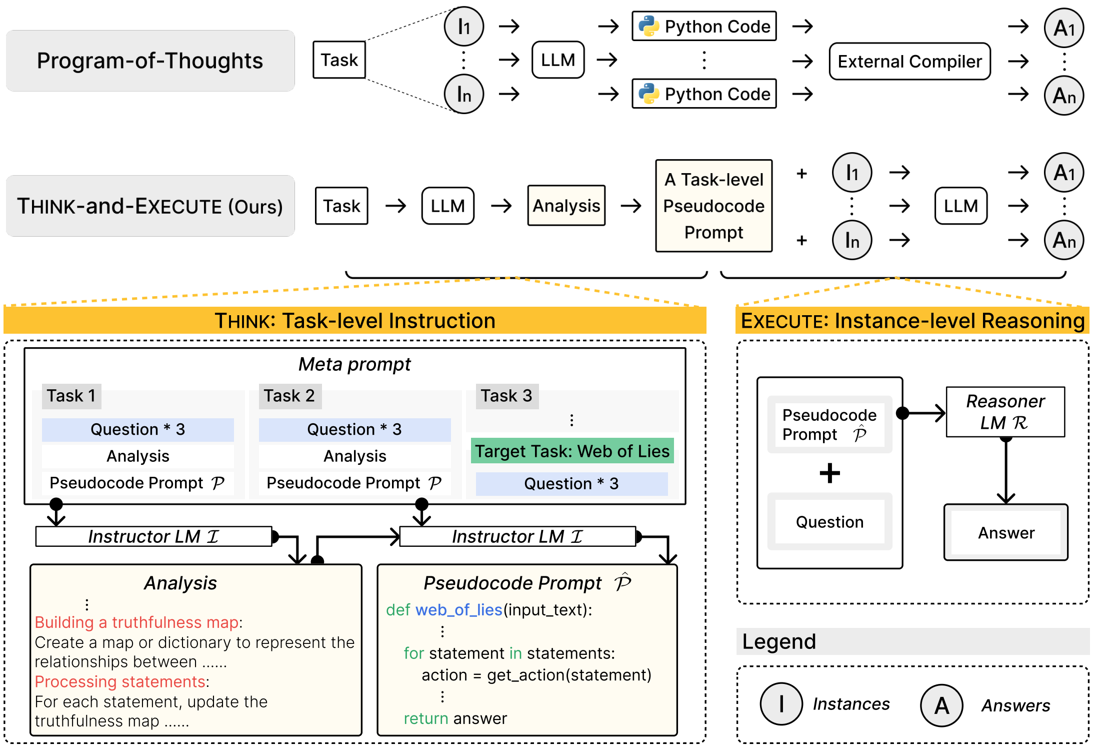
In this section, we introduce THINK-AND-EXECUTE and provide a detailed explanation of how LLMs perform reasoning with it. We incorporate an Instructor LM $\mathcal{I}$ and a Reasoner LM $\mathcal{R}$, for THINK and EXECUTE, respectively. Figure 2 shows the overview of our framework.

2.1 THINK: Describing the Underlying Logic of a Task in a Pseudocode Format

The goal for the Instructor LM $\mathcal{I}$ in this phase is to discover the underlying logic for solving a given task t, and generate a prompt describing the logic, which will be further applied to all instances of the task (in EXECUTE). This prompt is constructed with **pseudocode** rather than natural language, which is used in prior work to guide the LM to perform step-by-step reasoning (Kojima et al., 2022; Wang et al., 2023).

Step 1: Constructing a meta prompt. To prompt the Instructor LM $\mathcal{I}$ to generate a task-level pseudocode for the given target task t, we provide $\mathcal{P}$ of other tasks as demonstrations in a meta prompt.[1] In practice, we construct the meta

[1]We manually annotate $\mathcal{P}$ for each task in $\mathcal{T}$ in advance. See Appendix B.1 for examples.


Program-of-Thoughts
Task
I1
In
LLM
Python Code
Python Code
External Compiler
A1
An
THINK-and-EXECUTE (Ours)
Task
LLM
Analysis
A Task-level Pseudocode Prompt
+
I1
In
LLM
A1
An
THINK: Task-level Instruction
Meta prompt
Task 1
Question * 3
Analysis
Pseudocode Prompt $\mathcal{P}$
Task 2
Question * 3
Analysis
Pseudocode Prompt $\mathcal{P}$
Task 3
Target Task: Web of Lies
Question * 3
Instructor LM $\mathcal{I}$
Instructor LM $\mathcal{I}$
Analysis
Pseudocode Prompt $\hat{\mathcal{P}}$
EXECUTE: Instance-level Reasoning
Pseudocode Prompt $\hat{\mathcal{P}}$
+
Question
Reasoner LM $\mathcal{R}$
Answer
Legend
I Instances
A Answers

Building a truthfulness map:
Create a map or dictionary to represent the relationships between ......
Processing statements:
For each statement, update the truthfulness map ......

```
def web_of_lies(input_text):
    ⋮
    for statement in statements:
        action = get_action(statement)
    ⋮
    return answer
```

Figure 2: An overview of THINK-AND-EXECUTE. In THINK (Top), an LLM analyzes the given task provided in the meta prompt and generates a pseudocode prompt that describes the necessary logic for solving the task. Then, in EXECUTE (Bottom), the LLM conducts reasoning for each instance by simulating the execution of the pseudocode prompt.

prompt with 3 randomly sampled tasks (3 example questions, analysis, and $\mathcal{P}$ for each task) from $\mathcal{T}$ as demonstrations and the target task t (3 example questions without the answers).[2]

Step 2: Analyzing the target task. Given the meta prompt, $\mathcal{I}$ generates an analysis containing key reasoning logic that is required to solve the target task regardless of the instances (questions). For example, in Figure 2 (Top), the generated analysis points out that *building a truthfulness map* and updating it by *processing statements* are needed to solve the task, *i.e.*, Web of Lies. This step guides $\mathcal{I}$ to focus on the reasoning process shared among all the instances, which would be crucial in making a task-level prompt.

Step 3: Generating a pseudocode prompt based on the analysis. Next, based on the analysis, $\mathcal{I}$ writes a prompt $\mathcal{P}$ in the form of pseudocode, which breaks down the necessary reasoning steps for solving the target task. We choose to use the pseudocode format over the form of natural language plan (Kojima et al., 2022; Wang et al., 2023) for two main reasons: (1) the efficiency of it in describing the logic behind a task (*e.g.*, avoid using repetitive instructions via `for` loop), and (2) the guidance of what and when to generate rationales via the argument in `print()` statement and the location within the execution of code. For example, in Figure 2, the $\mathcal{P}$ contains the statement, print(f"{person1} says {person2} {action}. {person1} tells the truth: {truth_dict[person1]}"), which instructs the Reasoner LM to generate a rationale that is helpful in keep tracking of the truth map containing the truthfulness of each person, during the execution of $\mathcal{P}$. We provide more examples in Appendix G.

[2]We use the questions of the examples instances in the few-shot prompt in Big-Bench Hard.

2.2 EXECUTE: Simulating the Execution of Pseudocode Prompt for an Instance

The reasoner LM $\mathcal{R}$ then conducts reasoning with the generated pseudocode prompt $\mathcal{P}$, tailoring the logic in $\mathcal{P}$ for the given instance. Following Wei et al. (2022), we aim to maximize the reasoning abilities of the LM by instructing them to explicitly generate intermediate reasoning steps, known as chain-of-thought (CoT) reasoning. $\mathcal{R}$ is instructed to predict not only the final output result of the

Reasoner/Method	DL	GS	Nav	CO	TS	SO	WL	Avg
CodeLlama-7B								
Direct Prompting	0.0	9.0	39.0	24.4	4.4	11.2	47.6	19.4
Zero-shot CoT (Kojima et al., 2022)	0.0	**16.8**	26.0	10.8	**20.0**	10.4	44.8	18.4
NL Planning	0.0	10.0	52.0	0.4	7.6	18.8	**50.4**	19.9
Zero-shot PoT (Chen et al., 2023)	0.0	10.0	47.2	23.6	4.4	3.2	45.2	19.1
THINK-AND-EXECUTE	**2.0**	13.2	**70.8**	**49.6**	19.2	**22.0**	38.8	**30.8**
CodeLlama-13B								
Direct prompting	0.0	3.2	39.0	28.8	0.0	6.8	37.2	16.4
Zero-shot CoT (Kojima et al., 2022)	0.0	**24.8**	62.4	28.0	21.6	15.6	44.8	28.2
NL Planning	1.2	8.8	24.8	28.8	7.2	17.6	**53.6**	20.3
Zero-shot PoT (Chen et al., 2023)	1.2	16.4	45.6	38.8	10.8	**35.6**	20.4	24.1
THINK-AND-EXECUTE	**8.0**	18.4	**70.4**	**50.4**	**25.2**	32.4	49.6	**36.3**
GPT-3.5-Turbo								
Direct prompting	1.0	33.0	57.0	52.4	41.2	20.0	54.0	36.9
Zero-shot CoT (Kojima et al., 2022)	4.4	**46.8**	73.2	70.4	44.4	37.6	59.2	48.0
NL Planning	1.2	35.6	58.8	46.8	32.0	40.0	50.4	37.8
Zero-shot PoT (Chen et al., 2023)	0.4	21.2	77.2	45.6	0.4	28.0	54.0	32.4
Chain-of-Code (Li et al., 2023)	2.8	17.6	57.2	26.0	16.8	29.6	46.4	28.1
Plan-and-Solve (Wang et al., 2023)	4.0	41.2	84.8	**74.8**	52.4	37.2	58.0	50.3
THINK-AND-EXECUTE	**6.0**	41.6	**96.8**	72.0	**68.0**	**65.6**	**72.8**	**60.4**

Table 1: Zero-shot performance of THINK-AND-EXECUTE and baselines on seven algorithmic reasoning tasks, including Dyck Languages (DL), Geometric Shapes (GS), Navigate (Nav), Reasoning about Colored Objects (CO), Temporal Sequences (TS), Tracking Shuffled Objectives (SO), and Web of Lies (WL) from Big-Bench Hard (Suzgun et al., 2022).

code, but also the intermediate execution outputs as rationales. Specifically, $\mathcal{R}$ predicts a list of outputs $O = \{o_1, o_2, ..., o_k\}$ of the pseudocode by simulating the execution process of $\mathcal{P}$, where o_i denotes the i-th system output from `print()` statements, and $\{o_1\}_1^{k-1}$ are CoT rationales toward the final answer o_k. We assume that tracking intermediate execution results would benefit $\mathcal{R}$ to keep track of the state of variables while they change over the execution of the code. We enable $\mathcal{R}$ to mimic the behavior of a compiler with a system message "`Generate the expected outputs (from all print() functions) of the code.`". The final answer for a given question is outputted with "`print("Final answer:{answer}")`" command as the last system output o_k.

3 Experimental Setup

3.1 Datasets

We curate seven algorithmic reasoning tasks from Big-Bench Hard (Suzgun et al., 2022), including: dyck languages; geometric shapes; navigate; reasoning about colored objects; temporal sequence;tracking shuffled objectives; web of lies. These are specifically designed to measure the step-by-step reasoning capability of LLMs. Model performance on evaluated in **zero-shot** settings, where we do not provide demonstrations in the prompt. We provide detailed explanations in Appendix A.5.

3.2 Baselines

We consider the following baselines: (1) **Direct prompting**: Directly predicting the answer without generating any rationales. (2) **Zero-shot CoT** (Kojima et al., 2022): A setting where LLMs are evoked to generate the reasoning steps with "*Let's think step by step*", before the answer. (3) **Zero-shot PoT** (Chen et al., 2023): A setting where an LLM generates an instance-specific Python code that can be executed with a Python interpreter. Then, the execution result is used as the final answer. (4) **NL planning**: A variation of THINK-AND-EXECUTE, where the task-level instruction is generated in *natural language*, instead of pseudocode.

3.3 Models

For the Reasoner LM $\mathcal{R}$, we adopt GPT-3.5-Turbo (OpenAI, 2023), which shows strong performance in various reasoning benchmarks and code generation tasks (Zellers et al., 2019; Cobbe et al., 2021; Muennighoff et al., 2024), as well as the 7B and 13B versions of CodeLlama (Roziere et al., 2023), which are trained on both code and natural language corpora and further fine-tuned to follow natural language instructions. As for the Instructor LM $\mathcal{I}$, we choose GPT-3.5-Turbo.

4 Results

4.1 THINK-AND-EXECUTE Improves Algorithmic Reasoning

We start by comparing our framework with direct prompting and zero-shot CoT (Kojima et al., 2022) in Table 1. We find that zero-shot CoT performs better than direct prompting with average improvements of 11.1% with GPT-3.5-Turbo, respectively, suggesting zero-shot CoT to be a strong baseline. Our THINK-AND-EXECUTE, however, further outperforms both of them significantly regardless of model sizes, which indicates that explicitly generating a plan is an effective way to improve the LLM's reasoning capabilities than simply encouraging LLMs to generate their intermediate reasoning steps.

4.2 Task-level Pseudocode Prompts Benefits a Wider Range of Algorithmic Reasoning Tasks than Instance-specific Python Code

In Table 1, PoT shows performance gains in some tasks over direct prompting (*e.g.*, Navigate; Tracking Shuffled Objects) with Python code generated specifically for each instance and the corresponding interpreter output as the answer. However, such improvement is difficult to generalize to all tasks, *e.g.*, 0.4% accuracy in both Dyck Language and Temporal Sequences, with GPT-3.5-Turbo. By contrast, THINK-AND-EXECUTE outperforms PoT and direct prompting in all tasks with GPT-3.5-Turbo. This suggests that making the task-level strategy with pseudocode and applying it to each instance can benefit LLM's reasoning in a wider range of algorithmic reasoning tasks than generating instance-specific Python codes.

4.3 The Logic Discovered by an LLM can be Transferred to SLMs

We further explore if the pseudocode prompt written by an LLM (*i.e.*, GPT-3.5-Turbo as the instructor) can be applied to smaller LMs: the CodeLlama family in Table 1. When applying the pseudocode prompts generated by GPT-3.5-Turbo, CodeLlama-7B and -13B significantly outperform direct prompting. Moreover, THINK-AND-EXECUTE with CodeLlama-13B shows comparable performance with GPT-3.5-Turbo with PoT and direct prompting.

Method	Avg
w/o Analysis	21.8
THINK-AND-EXECUTE	**60.4**

Table 2: Ablation on Step2 of THINK phase.

4.4 Pseudocode Better Describes the Logic for Solving a Task than Natural Language

We also compare our approach with NL planning, a variant of ours that utilizes natural language to write the task-level instruction, instead of pseudocode. In practice, we provide human-written NL plans that contain a similar amount of information to $\mathcal{P}$ in the meta prompt and use it to generate the task-level NL plan for the given task. Surprisingly, although the LMs are fine-tuned to follow natural language instructions, we find that task-level pseudocode prompts can boost their performance more than NL plans (Table 1).

4.5 Ablation Studies

Components of the pseudocode prompt. We conduct an ablation study on each component of the pseudocode prompt. For that, we prepare four types of pseudocode prompts: (1) **Human-written pseudocode**; (2) Human-written prompt **w/o comments and semantics** by removing the comments that explain the code and replacing variable names with meaningless alphabets, such as X, Y, and Z; (3) Human-written prompt **w/ for loop** and (4) **w/ intermediate print()** statements. The results are in Figure 3. Model performance decreases significantly when applying prompts w/o comments and semantics, especially in Temporal Sequences. This implies that semantics play an important role in guiding the LLMs to apply the discovered logic and reasoning with it accordingly. Also, we find that printing out the intermediate execution steps with `print()` is crucial in reasoning, which is consistent with the finding from Wei et al. (2022).

Generating the analysis before the pseudocode prompt. Table 2 shows a notable decrease in model performance when generating pseudocode

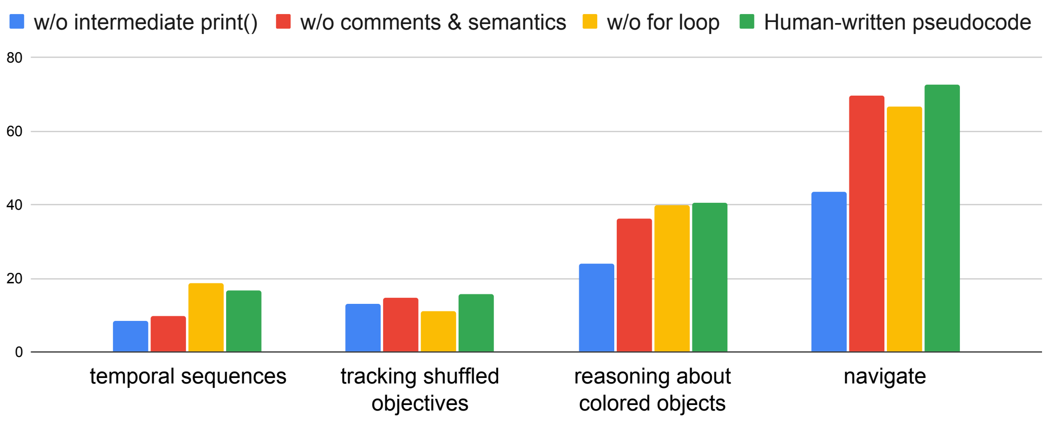


Figure 3: Ablation study of the components of pseudocode prompt using GPT-3.5-Turbo.

Method	Avg
Self-Discover w/ GPT-4	77.9
THINK-AND-EXECUTE w/ GPT-4	**81.7**

Table 3: Comparison of THINK-AND-EXECUTE and Self-Discover (Zhou et al., 2024) using GPT-4 on Big-Bench Hard. The results of Self-Discover are obtained from the original paper, because the code and prompts are not provided. The full results are in Appendix A.4.

prompts without conducting the analysis first. This suggests that explicitly generating analysis on the task can elicit a better pseudocode prompt that contains the necessary logic for solving the task.

4.6 Comparison with other Baselines

We further compare THINK-AND-EXECUTE with another three baselines: (1) Plan-and-Solve (Wang et al., 2023), where an LLM sequentially generates a natural language plan for solving the given instance, step-by-step reasoning according to the plan, and the final answer; (2) Chain-of-Code (Li et al., 2023), where Python code is generated as a part of intermediate reasoning steps specifically for a given instance; (3) Self-Discover (Zhou et al., 2024), a concurrent work that devises a task-level reasoning structure in a JSON format before inferencing the instance. First, as presented in Table 3 (Left), we find THINK-AND-EXECUTE largely outperforms Plan-and-Solve and Chain-of-Code by 10.9 and 32.3 percentage points in terms of accuracy, respectively. Second, while Self-Discover also incorporate task-level instruction, in Table 3 (Right), our THINK-AND-EXECUTE with pseudocode prompts shows better performance when using GPT-4 (Achiam et al., 2023).[3] These findings indicate that generating (1) task-level instruction with (2) pseudocode can better represent the necessary logic for solving a task and benefit LLM's algorithmic ability.

5 Analysis

We conduct experiments to address the following research questions:

- **RQ1**: Is task-level pseudocode more helpful than instance-specific pseudocode?
- **RQ2**: Does pre-training on code corpora improve reasoning?
- **RQ3**: How is the quality of the logic discovered by THINK-AND-EXECUTE compared to human-written logic?

5.1 Implementing the Underlying Logic is more Effective than Instance-specific Logic in Pseudocode (RQ1)

We conduct an analysis to check if the improvement of THINK-AND-EXECUTE is contributed by our chosen format for the task-level instruction, *i.e.*, pseudocode. We compare THINK-AND-EXECUTE with a concurrent work, Chain-of-Code (CoC) (Li et al., 2023). In Table 1, THINK-AND-EXECUTE outperforms CoC, showing about 2x improvement in the average score. The main difference between THINK-AND-EXECUTE and CoC is that we use pseudocodes which are generated to express logic shared among the tasks instances, while CoC incorporates pseudocode as part of the intermediate reasoning steps towards the solution of a

[3]We use `gpt-4-0613` for GPT-4.

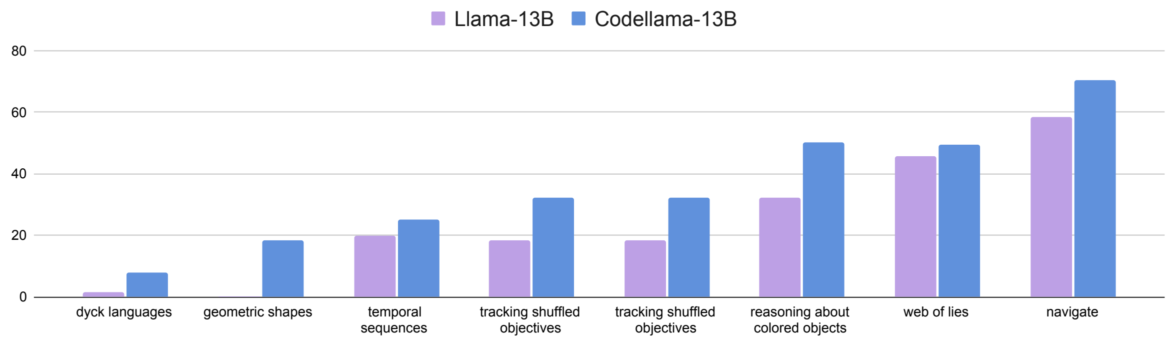


Figure 4: Analysis on the effect of code pre-training on the reasoning capability in applying THINK-AND-EXECUTE. Without pre-training on code corpora the accuracies drop notably.

Reasoner/Method	DL	GS	Nav	CO	TS	SO	WL	Avg
CodeLlama-7B								
Human-written $\mathcal{P}$	**2.4**	0.0	40.4	29.6	12.0	18.0	**52.8**	22.2
THINK-AND-EXECUTE	2.0	**13.2**	**70.8**	**49.6**	**19.2**	**22.0**	38.8	**30.8**
CodeLlama-13B								
Human-written $\mathcal{P}$	2.8	14.8	**72.8**	40.4	16.8	15.6	**49.6**	30.4
THINK-AND-EXECUTE	**8.0**	**18.4**	70.4	**50.4**	**25.2**	**32.4**	**49.6**	**36.3**
GPT-3.5-Turbo								
Human-written $\mathcal{P}$	**12.4**	**50.0**	86.0	50.8	**84.0**	32.4	**74.4**	55.7
THINK-AND-EXECUTE	6.0	41.6	**96.8**	**72.0**	68.0	**65.6**	72.8	**60.4**

Table 4: Comparison between THINK-AND-EXECUTE and Human-written $\mathcal{P}$.

given instance. Hence, the results indicate the advantages of applying pseudocode for the generation of task-level instruction over solely using them as a part of rationales.

5.2 THINK-AND-EXECUTE Requires Knowledge in Code (RQ2)

To understand whether SLMs acquire the ability to understand the task-level logic written in pseudocode during pre-training on code corpora, we compare the performance of CodeLlama-13B with Llama-13B using THINK-AND-EXECUTE. In Figure 4, CodeLlama-13B shows better reasoning capabilities compared to Llama-13B in all tasks. These results suggest that the improvement from using THINK-AND-EXECUTE could depend on the knowledge of code, which is usually obtained by pre-training with code corpora. Writing code usually involves understanding the logic behind the given problem and expecting the execution results of a code, which resemble the same reasoning process of THINK-AND-EXECUTE.

5.3 Models Prefer Pseudocode from THINK-AND-EXECUTE Compared to Human's (RQ3)

To gauge LLMs' capabilities in discerning the underlying logic of a task, we compare THINK-AND-EXECUTE (using GPT-3.5-Turbo as the Instructor) with human-written pseudocode prompts. The results are shown in Table 4. Using the GPT-3.5-Turbo the Reasoner, THINK-AND-EXECUTE scores 60.4% in terms of accuracy, which is superior to the human-written $\mathcal{P}$ (with an accuracy of 55.7%). Especially, in the tasks of Navigate and Tracking Shuffled Objectives, pseudocode prompts generated by THINK-AND-EXECUTE elicit better performance. This also holds true when adopting CodeLlama-7B and -13B as the Reasoner, further suggesting the effectiveness of our THINK step over human writers.

5.4 Impact of LLMs' Capability on THINK-AND-EXECUTE

In examining the impact of LLMs' capabilities within our framework, we investigate the influence of both the Reasoner and Instructor compo-

Reasoner	Instructor		
	CodeLlama-13B	CodeLlama-34B	GPT-3.5-Turbo
CodeLlama-13B	30.9	33.0	36.4
CodeLlama-34B	32.5	34.2	39.1
GPT-3.5-Turbo	33.9	35.9	60.4

Table 5: Analysis of the effect of the capability of Reasoner and Instructor on the performance. We report the average performance on the 7 tasks.

nents on performance, as depicted in Table 5. Notably, higher accuracy scores are observed when utilizing GPT-3.5-Turbo as Reasoners compared to CodeLlama-13B and CodeLlama-34B. Additionally, the effectiveness of the Instructor also plays a crucial role, with GPT-3.5-Turbo exhibiting the highest accuracy scores across all configurations. These results underscore the significance of both the Reasoner and Instructor components in enhancing the performance of THINK-AND-EXECUTE.

6 Related Work

Chain-of-Thought (CoT) prompting. CoT prompting evokes LMs to generate intermediate reasoning steps that guide and explain the solution (Wei et al., 2022; Wang et al., 2022; Wu et al., 2023). One common paradigm of this is zero-shot CoT prompting (Kojima et al., 2022). Without specifically designed question-explanation-answer triplets as demonstrations, zero-shot CoT prompting elicits a plausible reasoning path towards the final answer with simple instruction, such as *"Let's think step-by-step"*, eliciting better model performance in tasks that require multi-step reasoning.

In the context of improving zero-shot CoT, Wang et al. (2023) propose to first generate a plan breaking down the target task into smaller subtasks, and then solve each subtask according to the plan. Similar to our approach, a concurrent work (Zhou et al., 2024) devises a task-level reasoning structure that can be applied to each instance (question) of the target task. The most significant distinction between these prior studies and ours is that our THINK-AND-EXECUTE adopts **pseudocode** (as opposed to natural language) to express the necessary logic for solving the task. We demonstrate that our task-level pseudocode prompt empowers LMs with better ability of zero-shot reasoning than natural language plans under various settings in Section 5.

Incorporation of code in reasoning. With unambiguous syntax and strict structure, programming languages such as Python have been applied to LLM-based systems to improve system performance in solving tasks. For instance, Gao et al. (2023) and Chen et al. (2023) use LLMs to generate Python code for given mathematical questions, and run the generated code on external compilers to obtain/calculate the answers.

Besides, there has been a line of work on improving LLMs' capabilities with pseudocode (Zelikman et al., 2023; Mishra et al., 2023). Concurrently with our work, Li et al. (2023) present chain-of-code (CoC), where pseudocode is also incorporated along with the Python code for solving a given question (instance). While this approach generates instance-specific code as intermediate reasoning steps for each individual instance, our THINK-AND-EXECUTE, by contrast, focus on the task-level pseudocode prompt that can be applied to all instances. We compare CoC and THINK-AND-EXECUTE in Section 4. Another concurrent work (Weir et al., 2024), inspired by our study, delves into training LLMs that are specialized to generate task-level pseudocodes.

7 Conclusion

In this paper, we present THINK-AND-EXECUTE, an algorithmic reasoning framework that generates a logic for solving the given task into a pseudocode and performs reasoning by simulating the execution of the pseudocode with language models. Through extensive experiments, we show the effectiveness of THINK-AND-EXECUTE, over the strong baselines. These results underscore not only the usefulness of pseudocode in eliciting language models' reasoning capabilities but also the efficiency of our framework in discovering the high-quality logic behind a given task.

8 Limitations and Discussion

A possible limitation of our approach is that we focus on algorithmic reasoning, as we believe it is the best setting to assess LLMs' capabilities in understanding a complex logic and carrying out a sequence of reasoning step, following the logic. However, we believe that THINK-AND-EXECUTE can be applied to other domains of reasoning that require following a long sequence of reasoning steps, such as multi-hop reasoning (Ji et al., 2020) and symbolic reasoning (Madaan and Yazdanbakhsh, 2022).

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A Experimental Details

A.1 Models

We use several LLMs, including GPT-3.5-Turbo (OpenAI, 2023) and GPT-4 (Achiam et al., 2023), which are available via OpenAI API[4], and open-source LLM, CodeLlama (Roziere et al., 2023) as the Instructor LM $\mathcal{I}$ and the Reasoner LM $\mathcal{R}$.

- **GPT-3.5-Turbo**: `gpt-3.5-turbo-0125`
- **GPT-4**: `gpt-4-0613`
- **CodeLlama**: CodeLlama encompasses variations of LLaMA2 fine-tuned for code domains using code corpus. This comprehensive collection features models of various sizes (7B, 13B, 34B, and 70B) and diverse types, including the foundation model, Python-focused model, and instruction-following model. In our study, we employ the CodeLlama-Instruct model (7B[5], 13B[6]).

A.2 Inference

We use vLLM to improve inference throughput.[7] During our experiments, we adopt temperature sampling with $T = 0.0$ (*i.e.*, greedy decoding) to efficiently generate outputs. For a task comprising 250 instances, GPT-3.5-Turbo achieves an inference time of 30 seconds. Additionally, utilizing 2 A100 GPUs, CodeLlama achieves inference times of approximately 2 and 5 minutes for 7B and 13B models, respectively.

A.3 Evaluation

To extract answers for evaluation, LLMs generate the final answer triggered by the phrase "Final answer: ". Following Suzgun et al. (2022), we provide all multiple-choice options to LLMs as input, then measure accuracy using exact match (EM), which compares the generated output with the ground-truth label. To ensure fair comparison between PoT and other baselines, we also admit the prediction that includes the text of correct choice, *e.g.*, blue, but without a choice tag, *e.g.*, "(A)".

A.4 Experimental Results

We provide the full result of comparison with Self-Discover (Zhou et al., 2024).

[4]`https://openai.com/blog/openai-api`
[5]`https://huggingface.co/codellama/CodeLlama-7b-Instruct-hf`
[6]`https://huggingface.co/codellama/CodeLlama-13b-Instruct-hf`
[7]`https://github.com/vllm-project/vllm`

A.5 Datasets

We take 7 algorithmic benchmarks from Big-Bench Hard (Suzgun et al., 2022) dataset. All datasets contain 250 examples respectively. We provide the descriptions of each dataset regarding the goals and contexts.

- **Dyck Languages (DL)**: Complete a partially given Dyck-4 sequence by predicting the necessary sequence of closing brackets that are missing at the end.
- **Geometric Shapes (GS)**: Determine the geometric figure formed by following all the instructions in a specified SVG path element containing several commands.
- **Navigate (Nav)**: Evaluate whether a set of directional commands will return a navigator to the starting point.
- **Reasoning about Colored Objects (CO)**: Given a scenario, deduce the color of a specific object placed on a surface, using the provided context for guidance.
- **Temporal Sequences (TS)**: Examine a chronology of a person's daily activities to find when they could fit an additional activity into their schedule.
- **Tracking Shuffled Objectives (SO)**: Ascertain the final positions of several objects after they have been moved from their original locations through a sequence of exchanges. We use the version of the task with 5 objectives.
- **Web of Lies (WL)**: Assess the veracity of a Boolean function presented within a narrative problem to establish its truthfulness.

B Details of THINK-AND-EXECUTE

B.1 Human-annotation on the Tasks in the Task Pool

Please see Appendix D for human-written pseudocode prompts.

B.2 Components of a Pseudocode Prompt

We highlight some components of code prompt that would be helpful in describing the underlying reasoning logic.

Reasoner/Method	DL	GS	Nav	CO	TS	SO	WL	Avg
Self-Discover	**77.0**	60.0	**90.0**	79.0	**100.0**	68.0	71.0	77.9
THINK-AND-EXECUTE	55.6	**72.8**	70.0	**96.0**	97.2	**99.6**	**88.4**	**82.8**

Table 6: Comparison between THINK-AND-EXECUTE and Self-Discover (Zhou et al., 2024) using GPT-4.

- **Conditional branch**: To allow the reasoning model to take different reasoning paths based on the condition, we use `if` and `else` statement to describe the logic.

- **Loop**: We can efficiently present repetitive instructions that iterate over a list of items by using loops, such as `for` and `while` loop.

- **Abstraction**: In programming, we can encapsulate a complex logic into a single function. Focusing on this, we adopt modular design in constructing pseudocode prompts by encapsulating complex and repetitive process into an abstract function.

- **Variables**: Variables are essential in programming languages as they store data values to execute instructions. Similarly, in reasoning, keeping track of variables is crucial for maintaining state, passing data, and for general data manipulation tasks.

- **Comments and docstrings**: As human programmers can rely on the assistance of comments to better understand codes, we provide more detailed explanations on the intent of code via comments. Also, comments and docstrings can compensate the limitation when some semantics cannot be directly expressed with programming language.

B.3 Comparison to Related Work

Table 7 summarizes some related approaches to ours.

Method	**Granularity of plan/logic**	**Use of pseudocode**	**Transferability to SLMs**
Plan-and-Solve (Wang et al., 2023)	Instance-level	✗	✗
Self-Discover (Zhou et al., 2024)	Task-level	✗	✗
Chain-of-Code (Li et al., 2023)	Intance-level	✅	✗
THINK-AND-EXECUTE (this work)	Task-level	✅	✅

Table 7: A comparison of THINK-AND-EXECUTE to closely related prior approaches.

C Prompts Used in Our Experiments

C.1 Meta Prompt for generating an analysis (THINK: Step 2).

```
Generate an explanation, analyzation,
and plan to generate code prompt for
the last task considering the example
task instances. Your plan should show
enough intermediate reasoning steps
towards the answer. Construct the plan
as much as you can and describe the
logic specifically. When constructing
the plan for the code prompt, actively
use 'if else statement' to take
different reasoning paths based on the
condition, 'loop' to efficiently
process the repititive instructions, '
dictionary' to keep track of
connections between important variables
.

[Example 1]
Example task instances:
{example_instances_of_task1}

Output format:
{output_format_of_task1}

Explanation:
{analysis_of_task1}

...

[Example 4]
Example task instances:
{example_instances_of_target_task}

Output format:
{output_format_of_target_task}

Explanation:
```

C.2 Meta Prompt for pseudocode prompt genration (THINK: Step 3).

```
Generate the code prompt for the last
task using the similar style of the
example codes. Add enough print()
functions following the provided steps
 in the provided explanation to output
intermediate reasoning steps towards
the answer and keep track of important
variables. Implement the code prompt as
 much as you can and describe the logic
 in code following the provided
explanation but do not make a code that
 is biased toward a single task example
 instance. For example, do not use hard
-coded variables that are obtained from
 task instances (e.g., using specific
name of person in the question). The
code prompt must be able to be applied
to various instances of same task. When
 returning the final answer, carefully
consider the output format. Especially,
 for the multiple choice questions, the
 final answer should be one of the
given options. The main function name
should be '{function_name}'. Along with
 the main function, you may want to
define some helper functions that might
 be helpful for implementing the '{
function_name}'. But you don't have to
explicitly implement the helper
functions, but just define them with
function name and a single-line
explanation in comment. When
constructing the main function, ...

[Example 1]
Task description:
{description_of_task1}

Example task instances and the code
usage:
{
example_task_instances_and_code_usages_of_targ
}

Format of the Final answer:
{output_format_of_task1}

Explanation:
{analysis_of_task1}

Code prompt:
{code_prompt_of_task1}

...

[Example 4]
Task description:
{description_of_target_task}

Example task instances and the code
usage:
{
example_task_instances_and_code_usages_of_targ
}

Format of the Final answer:
{output_format_of_target_task}

Explanation:
{analysis_of_target_task}

Code prompt:
```

C.3 Prompt for NL Planning

```
Generate a plan for the last task
considering the example task instances.
 Your plan should show enough
intermediate reasoning steps towards
the answer. Construct the plan as much
as you can and describe the logic
specifically.

[Example 1]
Task description:
{description_of_task1}

[Example 1]
Example task instances:
{example_instances_of_task1}

Output format:
{output_format_of_task1}

Plan:
{analysis_of_task1}

...

[Example 4]
Example task instances: {
example_instances_of_target_task}

Output format:
{output_format_of_target_task}

Plan:
```

C.4 Prompt for EXECUTE phase

```
{prompt}
input_text = "{input_text}"
final_answer = {function_name}(
input_text)
print("Final answer:"+ final_answer)
Generate the expected execution output
(output from all print() functions) of
the code. You don't have to actually
run the code and do not care about 'not
 implemented error'.
```

C.5 Prompt for evaluating Direct Prompting

```
{prompt}
text for the task: {input_text}
Final answer should be at the end of
your answer and its format should be
like "Final answer: your_answer".
Generate output following the task
description above.
Output:
```

C.6 Prompt for evaluating Zero-shot CoT

```
{prompt}
text for the task: {input_text}
Final answer should be at the end of
your answer and its format should be
like "Final answer: your_answer".
Generate output following the task
description above.
Output:
Let's think step by step.
```

C.7 Prompt for evaluating Zero-shot PoT

```
You will write python program to solve
the below problem. You will only write
code blocks. Your python promgram must
be executable and returns the right
answer for the problem.

Q: {question}

# solution using Python:

def solution():
    """{question}"""
```

C.8 Prompt for evaluating Plan-and-Solve

```
{prompt}
text for the task: {input_text}
Final answer should be at the end of
your answer and its format should be
like "Final answer: your_answer".
Generate output following the task
description above.
Output:
Let's first understand the problem and
devise a plan to solve the problem.
Then, let's carry out the plan and
solve the problem step by step.
```

D Human-written Pseudocode Prompts

D.1 Human-written $\mathcal{P}$ of Dyck Languages

```
def complete_dyck_languages(input_text)
:
    # Step 1: Initialize a stack to
keep track of open parentheses and
split the input text to identify and
define all types of open parentheses in
 the text.
    stack = []
    character_list = input_text.split()
    open_to_close_parenthesis_dict = {"
(": ")", "<": ">", "{": "}", "[": "]"}
    opening_parenthesis = ["(", "<", "{
", "["]
    print(f"Parse characters in the
input and initialize a stack to track
of open parentheses. \nCurrent stack: {
stack}. Parsed characters: {
character_list}")


    # Step 2: Through iteration over
the input characters, identify opening
parentheses among the input characters
and add them to the stack.
    print("Check if a character is an
opening parenthesis while iterating
over the input characters.")
    for char in character_list:
        if char in opening_parenthesis:
                print(f"
Iteration {i+1}: Current character {
char} is an opening parenthesis.")
            stack.append(char)
            print(f"Thus, we append {
char} to the stack. Current stack after
 insertion: {', '.join(stack)}")

        # Step 3: For each open
parentheses, find the corresponding
closing parentheses and close the open
parentheses.
        else:
            print(f"Iteration {i+1}:
Current character {char} is not an
opening parenthesis.\n Thus we delete
the last item {stack[-1]} from the
stack\n current stack before deletion:
{" ".join(stack)} -> updated stack
after deletion: {' '.join(stack[:-1])
if stack else 'empty'}")
            stack.pop() # Remove the
last added open parentheses assuming a
correct match.

    # Step 4: Generate the sequence of
closing parentheses based on remaining
open parentheses in the stack.
    print(f"The resulting stack is {'
'.join(stack)}.")
    print(f"We will need to pop out {'
'.join(stack[::-1])} one by one in that
 order.")
    closing_list = [parentheses_pairs[
opening] for opening in stack[::-1]]

    # Step 5: Output the completed
sequence. Generate the input sequence
concatenated with the generated closing
 sequence of parentheses, ensuring a
well-formed structure.
    return " ".join(closing_list)
```

D.2 Human-written $\mathcal{P}$ of Geometric Shapes

```
def recognize_shape_from_svg(input_text
):
    # Step 1: Get the SVG path data
from the input text and generate the
extracted SVG path.
```

```
    paths = parse_path(input_text)
    print("SVG paths:\n ", paths)

    # Step 2: Initialize a coordinate
map that maps each coordinate with the
other connected coordinates and the
connection type.
    coordinate_map = dict()

    # Step 3: Update the coordinate map
 referring to the each SVG path.
    for i, path in enumerate(paths):
      coordinate_map =
update_coordinate_map(coordinate_map,
path)
      print(f"Step {i} - path: {path},
updated coordinate map: {coordinate_map
}")

    # Step 4: Conduct calculation to
analyze each characteristic of the
shape.
    analysis_results_dict =
analyze_characteristics(coordinate_map)
    print(f"Anlysis results: {
analysis_results_dict}")

    # Step 5: Identify a geometric
shape with reasons using the completed
coordinates map and the analysis
results.
    reason_for_the_decision,
name_of_the_shape =
identify_shape_with_explanation(
coordinate_map, analysis_results_dict)
    print(f"Reason for the decision: {
reason_for_the_decision}")
    print(f"Thus, the shape of the path
 is {name_of_the_shape}.")

    # Step 6: Find the corresponding
option from the given options and only
output the label of the option as the
final answer to the question.
    options = parse_options(input_text)
    print(f"Options: {options}")
    answer = None
    for option in options:
      if name_of_the_shape in option:
        answer = option[:3]

    return answer
```

D.3 Human-written $\mathcal{P}$ of Navigate

```
def ends_up_at_start(input_text):
    # Step 1: Initialize coordinates
and direction by setting the starting
point at (0, 0) and face north.
    cur_x, cur_y = 0, 0
    cur_direction = 0

    # Step 2: Identify and list up
instructions from the input text.
    instructions = parse_instructions(
input_text)

    # Step 3: Process each instruction
and update the current coordinates and
direction. In order to keep track of
changes, output the instruction,
current and updated coordinates and
direction.
    for i, instruction in enumerate(
instructions):
        new_x, new_y, new_direction =
process_instruction(instruction, cur_x,
 cur_y, cur_direction) # process
instruction to calculate new position
and direction
        print(f"Step {i}: {instruction}
 - current coordinates: ({cur_x}, {
cur_y}), current direction: {
cur_direction} -> updated coordinates:
({new_x}, {new_y}), updated direction:
{new_direction}")
        cur_x, cur_y, cur_direction =
new_x, new_y, new_direction

    # Step 4: Return "yes" if the final
 coordinates are (0, 0). Otherwise,
return "no" as the final answer.
    return 'yes' if cur_x == 0 and
cur_y == 0 else 'no'
```

D.4 Human-written $\mathcal{P}$ of Reasoning about Colored Objects

```
def solve_colored_objects(input_text):
    # Step 1: Start by identifying the
objects along with their associated
properties, such as color and spatial
positioning from the input text. Show
the list of objects.
    objects_list = extract_objects(
input_text)
    print("Objects and their properties
:", objects_list)

    # Step 2: Identify the specific
question asked. Determine whether the
question is about identifying the color
 of a specific object, counting objects
 of a certain color, or reasoning about
 the spatial arrangement of objects and
 output the question type.
    question = extract_question(
input_text)
    print("Question specifics:",
question)

    # Step 3: Identify and list up
available options provided in the input
 text.
    options = input_text.split("\n")
[-5:]

    # Step 4: Process according to the
question type and show what the
question type is:
    # If the question is about
identifying color, identify and ouput
the target object the question is
asking for the color of. Determine and
output its color.
    if question['type'] == '
identify_color':
        print("Question type is =
identify_color")
        print(f"Identifying color for:
{question['details']}")
        target_object = target(
objects_list, question['details'])
        print(f"The question is asking
for the color of : {target_object}")
        pre_answer = extract_color(
target_object, question['details'])
        print(f"Identified color: {
pre_answer}")

    # If the question is about counting
 objects, identify and ouput the
objects the question is asking for the
number of. Go through each object in
the list in steps and count each object
. Show the counting steps. Output the
final number of objects that meet the
specified criteria (e.g., a specific
color).
    elif question['type'] == '
count_objects':
        print("Question type is =
count_objects")
        print(f"Counting objects for: {
question['details']}")
        print("Total iterations:", len(
objects_list))
        for i, object in enumerate(
objects_list):
            single_object_count =
count_single_object(object, question['
details'])
            intermediate_count +=
single_object_count
            print(f"Step ({i}) - {
object}: {single_object_count},
Intermediate count: {intermediate_count
}")
        pre_answer = count_objects(
objects_list, question['details'])
        print(f"Objects count: {
pre_answer}")

    # If the question is about spatial
reasoning, identify and ouput the
relative positions the question is
asking for. Arrange the objects from
left to right and output the order.
Determine the relative positions of
objects and output the result.
    elif question['type'] == '
spatial_reasoning':
        print("Question type is =
spatial_reasoning")
        print(f"Applying spatial
reasoning for: {question['details']}")
        arranged_object =
arrange_from_left_to_right(objects_list
)
        print(f"Arraged objects: {
arranged_object})
        pre_answer = spatial_reasoning(
arranged_object, question['details'])
        print(f"Spatial reasoning
result: {pre_answer}")

    # Step 5: Recall the identified
options and match the outcome of Step 4
 (the identified color, the count of
objects, or the result of spatial
reasoning) with the provided options to
 determine the correct answer.
    answer = find_correct_option(
pre_answer, options)

    # Step 6: Return the final answer
chosen at Step 5.
    return answer
```

D.5 Human-written $\mathcal{P}$ of Temporal Sequences

```
def solve_temporal_sequences_quiz(
input_text):
    # Step 1: Identify statements and
options from the input_text and output
the statements.
    statement_text, option_text =
input_text.split("\nOptions:\n")
    parts = statement_text.split("\n")
    statements = parts[1:-2]
    options = option_text.split("\n")
    print("Statements:", statements)

    # Step 2: Check the start and end
of the possible time.
    print("Start of the possible time:
", parts[0])
    print("End of the possible time: ",
 parts[-2])

    # Step 3: Initialize an available
time map with the time slots in the
options and output it. The time slots
are marked as 'free' initially.
    available_time_map = {option[4:]: "
free" for option in options}
    print(f"Initial available time
dictionary: {available_time_map}")

    # Step 4: Sequentially go through
each statement, marking the times when
the individual was seen or known to be
engaged in specific activities. In this
 step, you should generate the target
time slots and the updated available
time map according to the statement.
    for i, statement in enumerate(
statements):
        event, time_span =
extract_information(statement)
        print(f"\nStep {i}: {statement}
")
```

```
        print(f"current time occupation
: {available_time_map}")
        print(f"Time span to be
occupied: {time_span}")
        available_time_map[time_span] =
 "not available"
        print(f"updated time occupation
: {available_time_map}")

    # Step 5: By checking the available
 time map, identify which time slot is
marked as 'free'. For each time slot,
output the time slot is free or not
available.
    for key in available_time_map:
        if available_time_map[key] == "
free":
            print(f"{key} is free.")
            free_time = key
        else:
            print(f"{key} is not
available.")
    # Step 6: Review the provided
options and return the one that matches
 the identified free time slot in Step
5.
    print(f"Options:\n{option_text}")
    for option in options:
        if free_time in option:
            return option
```

D.6 Human-written $\mathcal{P}$ of Tracking Shuffled Objectives

```
def track_swaps(input_text):
    # Step 1: Identify Initial State.
Begin by identifying and outputing the
initial state of all objectives (e.g.,
who holds which ball or who is dancing
with whom) from the input text before
any swaps happen.
    state_dict = find_initial_state(
input_text)
    print(f"Initial state: {state_dict}
")

    # Step 2: Identify and output the
sequences of swaps from the input text.
 Each swap should be understood in
terms of who exchanges with whom.
    swap_sequences_list =
find_swap_sequences(input_text)
    print("Swap sequences: ",
swap_sequences_list)
    print("Total iterations: ", len(
swap_sequences_list))

    # Step 3: Carry out the swaps. For
each swap in swap sequences,
sequentially update and output the
current status of objectives by
exchanging them between the two
participants involved in the swap.
    for i, sequence in enumerate(
swap_sequences_list):
        player1, player2 =
extract_player(sequence)
        state_dict[player1], state_dict
[player2] = state_dict[player2],
state_dict[player1]
        print(f"({i}) {sequence} -> {
state_dict}")

    Step 4: Understand the Question.
After processing all swaps, identify
what the question is asking for in the
input text and output the question.
    question = extract_question(
input_text)
    print("Question:", question)

    Step 5: Analyze Options. Examine
and output the provided options in the
input text.
    options = input_text.split("\n")
[-5:]
    print("Options:", options)

    Step 6: Determine the Correct
Option. Using the updated state after
all swaps, determine which option
correctly answers the question and
output the answer.
    answer = find_correct_option(
question, options, state_dict)

    return answer
```

D.7 Human-written $\mathcal{P}$ of Web of Lies

```
def evaluate_boolean_word_problem(
input_text):
    # Step 1: Divide the input text
into individual statements and the
final question. Output each statements.
    statements = input_text.split("")
[:-1]
    question = input_text.split("")[-1]
    print("Parsed statements:",
statements)

    # Step 2: Create a Truth Map to
keep track of the assumed truthfulness
of each person mentioned in the
statements. No truth values are
assigned initially.
    truth_map = {statement.split()[0]:
None for statement in statements}

    # Step 3: Analyze Each Statement.
For each statement, first output the
statement number and the statement.
identify the subject person (who makes
the statement), the object person (who
the statement is about), and the
expected truth value (whether the
object person is said to tell the truth
 or lie). Output the current statement
under analysis along with the object
person and the expected truth value for
```

```
 clarity.
    for i, statement in enumerate(
statements):
        print(f"({i}): {statement}")
        speaker, target_person,
expected_truth_value_of_target_person =
 extract_person_and_truth_value(
statement) # speaker - says -
target_person -
expected_truth_value_of_target_person

        print(f"{speaker} says : {
target_person} - {
expected_truth_value_of_target_person}"
)
        print(f"Truth value of {
target_person}: {truth_map[
target_person]}")

        # Step 4: Update the Truth Map
based on the analysis of each statement
. If the statement's claim aligns with
the current assumption about the object
 person's truthfulness, mark the
subject person as truthful. Otherwise,
mark them as untruthful. After each
update, print the name of the person
being updated, their determined truth
value, and the updated truth map to
track changes.
        if truth_map[target_person] ==
None: # if the statement does not need
to be checked
            print(f"{
expected_truth_value_of_target_person}
matches {truth_map[target_person]}")
            truth_map[target_person] =
expected_truth_value_of_target_person
        else:
            print(f"{
expected_truth_value_of_target_person}
does not match {truth_map[target_person
]}")
            if truth_map[target_person]
 ==
expected_truth_value_of_target_person:
# the speaker tells the truth
                truth_map[speaker] =
True
            else: # the speaker lies
                truth_map[speaker] =
False

        print(f"Person to update: {
speaker} - {truth_map[speaker]}")

        print(f"updated truth_map: {
truth_map}")
        print("\n\n")

    # Step 5: Using the completed truth
 map, determine the truthfulness of the
 person in the final question. Output
the question for reference before
making the determination.
    print("question:", question)
    target_person_in_question =
extract_target_person_from_question(
question)
    target_truth_value = truth_map[
target_person_in_question]
    print(f"{target_person_in_question
}: {target_truth_value})

    # Step 6: Based on the evaluation,
output "Yes" if the person in the final
 question is determined to tell the
truth, otherwise output "No".
    answer = "Yes" if
target_truth_value else "No"

    return answer
```

E Generated Analyses

E.1 Generated Analysis of Dyck Languages

```
Explanation:
This task involves completing a
sequence of parentheses to ensure they
are closed properly. The challenge is
to understand the nesting structure of
the parentheses and add the appropriate
 closing brackets to match each opening
 bracket.

Analyzing the Task:
1. Parentheses Matching: Each opening
parenthesis should have a corresponding
 closing parenthesis to ensure the
sequence is valid.

2. Nested Parentheses: The parentheses
can be nested within each other, so it'
s crucial to maintain the correct
nesting structure.

3. Proper Closure: The goal is to add
the necessary closing brackets to
complete the sequence and make sure all
 parentheses are closed properly.

Constructing the Code Prompt:
1. Parsing Input: Extract the sequence
of parentheses from the input text.

2. Stack Implementation: Use a stack
data structure to keep track of the
opening parentheses that need closing.

3. Iterating Over the Sequence: Iterate
 over each character in the sequence
and push opening parentheses onto the
stack.

4. [Important] Closing Parentheses:
When encountering a closing parenthesis
, pop the corresponding opening
parenthesis from the stack to ensure
proper closure.

5. Generating Output: After processing
the entire sequence, the stack should
be empty if all parentheses are closed
```

```
properly. If not, add the necessary
closing brackets to match the remaining
 opening brackets.

6. Returning the Result: Output the
generated closing brackets as a string,
 separated by spaces, to complete the
sequence.
```

E.2 Generated Analysis of Geometric Shapes

```
Explanation:
This task involves analyzing SVG path
elements to determine the shape that is
 being drawn. The path elements consist
 of a series of commands that define
the movements and curves in the SVG
image. By understanding these commands
and their implications, we can identify
 the shape being drawn.

Analyzing the Task:
1. SVG Path Commands: The SVG path
element contains commands like M (move
to), L (line to), A (arc), etc., each
of which contributes to the overall
shape being drawn.

2. Interpreting Path Commands: Each
command in the path element corresponds
 to a specific action, such as moving
to a point, drawing a line, or creating
 an arc. Understanding these commands
is crucial to identifying the shape.

3. Recognizing Geometric Shapes:
Different combinations of path commands
 result in different geometric shapes
like circles, triangles, rectangles,
etc. We need to match the commands to
the shapes they represent.

Constructing the Code Prompt:
1. Parsing SVG Path Element: Extract
the path commands from the SVG path
element provided in the task. This
involves splitting the string and
identifying each command.

2. Processing Path Commands: Iterate
over each command in the path element
and execute the corresponding action.
This involves:
- Moving to a new point (M command).
- Drawing a line to a point (L command)
.
- Drawing an arc (A command).
- Other commands as necessary.

3. [Important] Tracking Coordinates:
Keep track of the coordinates as the
path commands are executed. This
involves updating the current position
based on the commands.
```

```
4. Determining the Shape: After
processing all commands, analyze the
resulting path to determine the shape
being drawn. This can be done by
comparing the final path with the
characteristics of known shapes.

5. Matching with Provided Options:
Compare the identified shape with the
options provided in the task to select
the correct answer.

6. Returning the Result: Return the
identified shape as the output in the
specified format ('(A)', '(B)', '(C)',
...).

By following these steps and accurately
 interpreting the SVG path commands, we
 can determine the shape being drawn
and select the correct option from the
given choices.
```

E.3 Generated Analysis of Navigate

```
Explanation:
This task involves following a series
of instructions related to movement and
 direction to determine if the final
position is the same as the starting
point. The challenge lies in accurately
 tracking the movements and rotations
to deduce the final position.

Analyzing the Task:
1. Movement Tracking: Keep track of the
 steps taken in each direction (forward
, backward, left, right) to determine
the final position.

2. Directional Changes: Account for any
 rotations (turning left or right) that
 may alter the orientation during
movement.

3. Spatial Reasoning: Apply logical
reasoning to calculate the final
position based on the cumulative effect
 of the movements and rotations.

Constructing the Code Prompt:
1. Extracting Instructions: Parse the
input text to extract the sequence of
movements and rotations.

2. Processing Movements:
   - Initialize variables to track the
current position (x, y coordinates) and
 orientation (direction faced).
   - Iterate over each instruction,
updating the position and orientation
accordingly.

3. [Important] Determining the Final
Position:
   - Calculate the final position based
 on the cumulative effect of movements
and rotations.
   - Check if the final position
matches the starting point to determine
 if the participant returns to the
starting point.

4. Matching with Options: Compare the
final position with the starting point
to determine if the participant returns
 to the starting point.

5. Returning the Final Answer: Output '
Yes' if the participant returns to the
starting point, 'No' otherwise.
```

E.4 Generated Analysis for Reasoning about Colored Objects

```
Explanation:
This task involves identifying specific
 attributes of items based on their
descriptions and positions relative to
each other. The task requires careful
reading of the descriptions and
analyzing the spatial relationships
between the items.

Analyzing the Task:
The task involves interpreting the
descriptions of items and their spatial
 relationships to answer specific
questions. This task does not require
variable tracking but rather a free
format reasoning approach to extract
the necessary information and make
logical deductions.

Constructing the Code Prompt:

1. Parse the descriptions: Extract the
descriptions of items and their colors
from the input text.

2. Identify the spatial relationships:
Determine the positions of items
relative to each other based on the
descriptions provided.

3. [Free format reasoning] Derive the
answer with explanation: Analyze the
descriptions and spatial relationships
to answer the specific question posed
in the task. Use a function like '
derive_answer_with_explanation' to
provide both the reasoning and the
correct answer.

4. Match the answer with the options:
Compare the derived answer with the
given options and select the correct
one.
```

```
5. Return the final answer: Output the
final answer in the specified format.

By following these steps, the task can
be effectively solved by reasoning
through the descriptions and spatial
relationships of the items provided in
the task instances.
```

E.5 Generated Analysis of Temporal Sequences

```
Explanation:
This task involves determining the
possible time intervals during which a
person could have visited a specific
location based on the given schedule of
 events throughout the day. The goal is
 to identify the time frames that are
not conflicting with other activities.

Analyzing the Task:
1. Establishing the Timeline:
Understanding the sequence of events
and the times at which they occurred is
 crucial for determining the available
time slots.

2. Identifying Conflicting Activities:
Recognizing the time intervals during
which the person was engaged in other
activities that would prevent them from
 visiting the specified location.

3. Determining Possible Visitation
Times: By eliminating conflicting time
intervals, the remaining time slots
represent the possible visitation times
.

Constructing the Code Prompt:
1. Extracting Event Information: Parse
the given schedule of events to extract
 the times at which each activity
occurred. This may involve creating a
data structure to store this
information.

2. Identifying Conflicting Time
Intervals: Determine the time intervals
 during which the person was occupied
with other activities that would
prevent them from visiting the
specified location.

3. [Important] Calculating Available
Time Slots: By subtracting the
conflicting time intervals from the
total day duration, identify the time
frames during which the person could
have visited the specified location.

4. Matching with Options: Compare the
possible visitation times with the
provided options to determine the
```

```
correct answer.

5. Returning the Correct Option: Return
 the letter corresponding to the time
interval that matches the calculated
possible visitation times.

This task involves a logical deduction
process based on the given schedule of
events to determine the feasible time
intervals for visiting the specified
location. By systematically analyzing
the timeline and eliminating
conflicting activities, the correct
answer can be identified. The solution
should provide a clear and accurate
assessment of the available time slots
for the visitation.
```

E.6 Generated Analysis of Tracking Shuffled Objectives

```
Explanation:
This task involves tracking the
positions or gifts of individuals as
they swap with each other in a sequence
 of exchanges. The challenge is to keep
 track of the swaps accurately and
determine the final position or gift of
 a specific individual at the end of
the sequence.

Analyzing the Task:
1. Initial Assignments: Understanding
the starting positions or gifts of each
 individual is crucial for tracking the
 swaps accurately.

2. Pairwise Swaps: Identifying the
pairs of individuals who swap positions
 or gifts at each step in the sequence.

3. Tracking Changes: Keeping a record
of the swaps and updating the positions
 or gifts of individuals accordingly.

Constructing the Code Prompt:
1. Initialize Positions or Gifts: Set
up a dictionary mapping each individual
 to their initial position or gift.

2. Define Swap Pairs: Create a list of
tuples representing the pairs of
individuals who swap positions or gifts
 at each step.

3. [Important] Process Swaps: Iterate
over the swap pairs, update the
positions or gifts of the individuals
involved in each swap. Use an if-else
statement to handle different swap
scenarios.

4. Determine the Final Position or Gift
: After processing all swaps, identify
the final position or gift of the
specified individual.

5. Match and Output the Answer: Parse
the options from the input text, find
the corresponding option from the given
 options, and only output the label of
the option as the final answer to the
question.
```

E.7 Generated Analysis of Web of Lies

```
Explanation:
This task involves determining the
truthfulness of a statement made by one
 individual based on the statements
made by others in a chain. The task
requires understanding the
relationships between truth-tellers and
 liars and applying logical reasoning
to determine the final answer.

Analyzing the Task:
1. Establishing Truth Relationships:
Each person's statement about another
person can be categorized as either
true or false. This forms the basis of
determining who tells the truth and who
 lies.

2. Propagating Truthfulness: By
analyzing the statements in a
sequential manner, the truthfulness of
each person can be deduced based on the
 statements made by others.

3. Identifying the Final Question: The
task usually asks whether a specific
person tells the truth or not based on
the chain of statements.

Constructing the Code Prompt:
1. Parsing Statements: Extract the
statements made by each person from the
 input text. This involves identifying
who is talking about whom and whether
they are telling the truth or lying.

2. Establishing Truth Relationships:
Create a dictionary to store the
truthfulness of each person based on
the statements made by others. This
dictionary will be updated as the
statements are processed.

3. [Important] Analyzing Statements:
Iterate over each statement and update
the truthfulness of the individuals
involved based on the logic that if A
says B lies, then A is telling the
truth if B is a liar, and vice versa.
This step involves logical reasoning
and updating the truth dictionary.

4. Extracting the Final Question:
Identify the specific question asked in
```

```
 the input text regarding the
truthfulness of a particular person.

5. Determining the Answer: Based on the
 final truthfulness of the person in
question as determined by the logic and
 the statements provided, select 'Yes'
if the person tells the truth and 'No'
if they do not.

By following these steps and applying
logical reasoning to the statements
provided, the code can accurately
determine whether the specified
individual tells the truth or not.
```

F Generated Pseudocode Prompts

F.1 Generated $\mathcal{P}$ of Dyck Languages

```
def complete_dyck_languages(input_text)
:
    # Step 1: Parse the input text to
extract the sequence of parentheses.
    parentheses_sequence =
extract_parentheses(input_text)
    print("Parentheses sequence:",
parentheses_sequence)

    # Step 2: Initialize a stack to
keep track of opening parentheses that
need closing.
    stack = []

    # Step 3: Iterate over each
character in the sequence to handle
opening and closing parentheses.
    for i, char in enumerate(
parentheses_sequence):
        if char in ['(', '[', '{', '<'
]:
            stack.append(char)
            print(f"Step ({i}) - Pushed
 {char} to stack")
        elif char in [')', ']', '}', '>
']:
            if len(stack) == 0:
                print(f"Step ({i}) - No
 matching opening bracket for {char}")
            else:
                opening_bracket = stack
.pop()
                print(f"Step ({i}) -
Matched {opening_bracket} with {char}")

    # Step 4: Check if the stack is
empty after processing the entire
sequence.
    if len(stack) > 0:
        print("Remaining unmatched
brackets in stack:", stack)
        # Step 5: Generate the
necessary closing brackets to match the
 remaining opening brackets.
        closing_brackets =
generate_closing_brackets(stack)
        print("Generated closing
brackets:", closing_brackets)
    else:
        print("All brackets are
properly matched.")

    # Step 6: Return the generated
closing brackets as the final answer.
    return closing_brackets
```

F.2 Generated $\mathcal{P}$ of Geometric Shapes

```
def recognize_shape_from_svg(
svg_path_element):
    # Step 1: Parse the SVG path
element to extract the path commands.
Output the extracted path commands.
    path_commands =
extract_path_commands(svg_path_element)
    print("Extracted path commands:",
path_commands)

    # Step 2: Process each path command
 to execute the corresponding action.
Keep track of the coordinates as the
commands are executed.
    current_position = (0, 0)
    for command in path_commands:
        action, coordinates =
process_path_command(command,
current_position)
        print(f"Executing command: {
command} - Action: {action} - New
coordinates: {coordinates}")
        current_position = coordinates

    # Step 3: Determine the shape based
 on the processed path commands. This
involves analyzing the final path drawn
.
    identified_shape = identify_shape(
path_commands)
    print("Identified shape:",
identified_shape)

    # Step 4: Match the identified
shape with the provided options to
select the correct answer.
    options = extract_options(
svg_path_element)
    answer = match_shape_with_options(
identified_shape, options)

    # Step 5: Return the identified
shape as the final answer.
    return answer
```

F.3 Generated $\mathcal{P}$ of Navigate

```
def ends_up_at_start(input_text):
    # Step 1: Extract the sequence of
movements and rotations from the input
text.
```

```
    instructions = extract_instructions
(input_text)
    print("Instructions:", instructions
)

    # Step 2: Initialize variables to
track the current position and
orientation.
    x, y = 0, 0
    orientation = "N"
    print(f"Initial position: ({x}, {y
}), Orientation: {orientation}")

    # Step 3: Process each instruction
to update the position and orientation
accordingly.
    for instruction in instructions:
        x, y, orientation =
process_instruction(instruction, x, y,
orientation)
        print(f"Instruction: {
instruction} -> Position: ({x}, {y}),
Orientation: {orientation}")

    # Step 4: Determine the final
position after following all
instructions.
    final_position = (x, y)
    print("Final Position:",
final_position)

    # Step 5: Check if the final
position matches the starting point to
determine if the participant returns to
 the starting point.
    if final_position == (0, 0):
        return 'Yes'
    else:
        return 'No'
```

F.4 Generated $\mathcal{P}$ for Reasoning about Colored Objects

```
def solve_colored_objects(input_text):
    # Step 1: Extract the descriptions
of items and their colors from the
input text.
    items = parse_items(input_text)
    print("Items on the surface:\n",
items)

    # Step 2: Determine the positions
of items relative to each other based
on the descriptions provided.
    spatial_relationships =
analyze_spatial_relationships(items)
    print("Spatial relationships
between items:\n",
spatial_relationships)

    # Step 3: Derive the answer with
explanation by analyzing the
descriptions and spatial relationships.
    question = identify_question(
input_text)
```

```
    print("The question is:", question)
    reason, answer =
derive_answer_with_explanation(items,
spatial_relationships, question)
    print("Reasoning for the answer:",
reason)

    # Step 4: Compare the derived
answer with the given options and
select the correct one.
    options = extract_options(
input_text)
    print("Answer options:\n", options)
    final_answer = None
    for option in options:
        if answer in option:
            final_answer = option[:3]
            break

    # Step 5: Return the final answer.
    return final_answer
```

F.5 Generated $\mathcal{P}$ of Temporal Sequences

```
def solve_temporal_sequences_quiz(
input_text):
    # Step 1: Extract event information
 from the input text to understand the
timeline of activities throughout the
day.
    events_list = extract_events(
input_text)
    print("Events and their timings:",
events_list)

    # Step 2: Identify conflicting time
 intervals when the person was engaged
in other activities that would prevent
them from visiting the specified
location.
    conflicting_intervals =
find_conflicting_intervals(events_list)
    print("Conflicting time intervals:"
, conflicting_intervals)

    # Step 3: Calculate the available
time slots by subtracting conflicting
intervals from the total day duration.
    available_intervals =
calculate_available_intervals(
conflicting_intervals)
    print("Available time intervals for
 visitation:", available_intervals)

    # Step 4: Match the available time
slots with the provided options to
determine the correct answer.
    options = input_text.split("\n")
[-5:]

    # Step 5: Return the correct option
 corresponding to the time interval
that aligns with the calculated
possible visitation times.
    answer = find_correct_option(
available_intervals, options)
```

```
    return answer
```

F.6 Generated $\mathcal{P}$ of Tracking Shuffled Objectives

```
def track_swaps(input_text):
    # Step 1: Initialize Positions or
Gifts
    initial_assignments =
extract_initial_assignments(input_text)
    print("Initial assignments:",
initial_assignments)

    # Step 2: Define Swap Pairs
    swap_pairs = extract_swap_pairs(
input_text)
    print("Swap pairs:", swap_pairs)

    # Step 3: Process Swaps
    final_assignments =
initial_assignments.copy()
    for pair in swap_pairs:
        if pair[0] in final_assignments
 and pair[1] in final_assignments:
            temp = final_assignments[
pair[0]]
            final_assignments[pair[0]]
= final_assignments[pair[1]]
            final_assignments[pair[1]]
= temp
        print(f"After swapping {pair
[0]} and {pair[1]}: {final_assignments}
")

    # Step 4: Determine the Final
Position or Gift
    final_person =
identify_final_person(input_text)
    final_position = final_assignments[
final_person]
    print(f"The final position or gift
of {final_person} is: {final_position}"
)

    # Step 5: Match and Output the
Answer
    options = extract_options(
input_text)
    print("Options:", options)
    answer = None
    for option in options:
        if final_position in option:
            answer = option[:3]

    return answer
```

F.7 Generated $\mathcal{P}$ of Web of Lies

```
def evaluate_boolean_word_problem(
input_text):
    # Step 1: Identify the statements
and the question from the input text.
    statements, question = input_text.
split("?")
    statements = statements.split(". ")
    print("Statements:", statements)
    print("Question:", question)

    # Step 2: Initialize a truth
dictionary to keep track of who tells
the truth and who lies.
    truth_dict = {}

    # Step 3: Process each statement to
 update the truth dictionary based on
the logic provided.
    for statement in statements:
        person1, action, person2 =
statement.split(" ")
        if action == "lies":
            truth_dict[person1] = not
truth_dict[person2]
        else:
            truth_dict[person1] =
truth_dict[person2]
        print(f"{person1} says {person2
} {action}. {person1} tells the truth:
{truth_dict[person1]}")

    # Step 4: Determine the
truthfulness of the person in question
based on the truth dictionary.
    person_to_check = question.split("
")[-2]
    answer = 'Yes' if truth_dict[
person_to_check] else 'No'

    return answer
```

G Qualitative Analysis

We conduct a qualitative analysis by comparing the outputs of our approach (THINK-AND-EXECUTE) with those of the baseline methods. This comparison is presented across Tables8,9,10,11,12,13, and 14.

Example Instance	Complete the rest of the sequence, making sure that the parentheses are closed properly. Input: ({ { } }
Ground truth Answer	)

Method	**Output**
Direct Prompting	Final answer: { }) **(Wrong)**
Zero-shot Prompting	Step 1: ({ { } }) Step 2: ({ { } }) Therefore, the answer is } **(Wrong)**

PoT	def solution():
	    stack = []
	    sequence = "({ { } }"
	
	    for char in sequence:
	        if char == "(" or char == "{":
	            stack.append(char)
	        elif char == ")" and stack[-1] == "(":
	            stack.pop()
	        elif char == "}" and stack[-1] == "{":
	            stack.pop()
	
	    for char in stack:
	        if char == "(":
	            sequence += ")"
	        elif char == "{":
	            sequence += "}"
	
	    return sequence
	
	solution()
	»> ({ { } }) **(Wrong)**

NL Planning	Step 1: Opening brackets in the input sequence: ({ { Step 2: Corresponding closing brackets: (->) { -> } { -> } Step 3: Closing brackets in order:) } } Final answer:) } } **(Wrong)**

Ours	Bracket sequence: ['(', '{', '{', '}', '}']
	Step 0 - bracket: (
	Updated stack: ['(']
	Step 1 - bracket: {
	Updated stack: ['(', '{']
	Step 2 - bracket: {
	Updated stack: ['(', '{', '{']
	Step 3 - bracket: }
	Updated stack: ['(', '{']
	Step 4 - bracket: }
	Updated stack: ['(']
	Rest of sequence:)
	Stack is not empty. The sequence is not properly balanced.
	Final answer:) **(Correct)**

Table 8: A comparison of results for Dyck Languages between the baseline methods and THINK-AND-EXECUTE.

Example Instance	This SVG path element <path d="M 38.00,62.00 L 48.00,60.00 L 51.00,49.00 L 54.00,60.00 L 65.00,62.00 L 54.00,64.00 L 51.00,74.00 L 48.00,64.00 L 38.00,62.00"/> draws a Options: (A) circle (B) heptagon (C) hexagon (D) kite (E) line (F) octagon (G) pentagon (H) rectangle (I) sector (J) triangle
Ground truth Answer	**(F) octagon**

Method	**Output**
Direct Prompting	Final answer: (C) hexagon **(Wrong)**
Zero-shot Prompting	The given SVG path forms a shape with 8 sides, which is a hexagon. Therefore, the answer is (C) hexagon. **(Wrong)**

PoT	def solution():
	    return "C) hexagon"
	
	solution()
	»> C) hexagon **(Wrong)**

NL Planning	Step 1: Identify the SVG Path Element. The given SVG path element is <path d="M 38.00,62.00 L 48.00,60.00 L 51.00,49.00 L 54.00,60.00 L 65.00, 62.00 L 54.00,64.00 L 51.00,74.00 L 48.00,64.00 L 38.00,62.00"/> Step 2: Analyze the Path Data. The path data commands used are 'M' for move to and 'L' for line to. The sequence of points mentioned are (38.00,62.00), (48.00,60.00), (51.00,49.00), (54.00,60.00), (65.00,62.00), (54.00,64.00), (51.00,74.00), (48.00,64.00), (38.00,62.00). Step 3: Determine the Shape. Based on the sequence of points and movements, the shape drawn appears to be a kite. Step 4: Match with Options. The shape drawn matches with option (D) kite. Step 5: Output the Correct Option. Final answer: (D) kite **(Wrong)**
Ours	Extracted path commands: ['M 38.00,62.00', 'L 48.00,60.00', 'L 51.00,49.00', 'L 54.00,60.00', 'L 65.00,62.00', 'L 54.00,64.00', 'L 51.00,74.00', 'L 48.00,64.00', 'L 38.00,62.00'] Executing command: M 38.00,62.00 - Action: Move to (38.00, 62.00) - New coordinates: (38.00, 62.00) Executing command: L 48.00,60.00 - Action: Draw line to (48.00, 60.00) - New coordinates: (48.00, 60.00) Executing command: L 51.00,49.00 - Action: Draw line to (51.00, 49.00) - New coordinates: (51.00, 49.00) Executing command: L 54.00,60.00 - Action: Draw line to (54.00, 60.00) - New coordinates: (54.00, 60.00) Executing command: L 65.00,62.00 - Action: Draw line to (65.00, 62.00) - New coordinates: (65.00, 62.00) Executing command: L 54.00,64.00 - Action: Draw line to (54.00, 64.00) - New coordinates: (54.00, 64.00) Executing command: L 51.00,74.00 - Action: Draw line to (51.00, 74.00) - New coordinates: (51.00, 74.00) Executing command: L 48.00,64.00 - Action: Draw line to (48.00, 64.00) - New coordinates: (48.00, 64.00) Executing command: L 38.00,62.00 - Action: Draw line to (38.00, 62.00) - New coordinates: (38.00, 62.00) Identified shape: octagon Final answer: (F) octagon **(Correct)**

Table 9: A comparison of results for Geometric Shapes between the baseline methods and THINK-AND-EXECUTE.

Example Instance	If you follow these instructions, do you return to the starting point? Take 3 steps. Turn around. Take 5 steps. Turn right. Turn right. Take 1 step. Take 1 step.
Ground truth Answer	**Yes**
Method	**Output**
Direct Prompting	Final answer: no **(Wrong)**
Zero-shot Prompting	First, take 3 steps. Then, turn around and take 5 steps in the opposite direction. After that, turn right twice and take 1 step followed by another step. Therefore, the answer is no. **(Wrong)**

PoT	def solution():
	    x = 0
	    y = 0
	    direction = 0 # 0: North, 1: East, 2: South, 3: West
	
	    # Take 3 steps
	    for _ in range(3):
	        if direction == 0:
	            y += 1
	        elif direction == 1:
	            x += 1
	        elif direction == 2:
	            y -= 1
	        else:
	            x -= 1
	
	    # Turn around
	    direction = (direction + 2) % 4
	
	    # Take 5 steps
	    ...
	
	    return x == 0 and y == 0
	solution()
	»> True **(Wrong)**

NL Planning	Final answer: No **(Wrong)**
Ours	Instructions: ['Take 3 steps', 'Turn around', 'Take 5 steps', 'Turn right', 'Turn right', 'Take 1 step', 'Take 1 step'] Initial position: (0, 0), Orientation: N Instruction: Take 3 steps −> Position: (0, 3), Orientation: N Instruction: Turn around −> Position: (0, 3), Orientation: S Instruction: Take 5 steps −> Position: (0, -2), Orientation: S Instruction: Turn right −> Position: (0, -2), Orientation: W Instruction: Turn right −> Position: (0, -2), Orientation: N Instruction: Take 1 step −> Position: (0, -1), Orientation: N Instruction: Take 1 step −> Position: (0, 0), Orientation: N Final Position: (0, 0) Final answer: Yes **(Correct)**

Table 10: A comparison of results for Navigate between the baseline methods and THINK-AND-EXECUTE.

Example Instance	On the floor, there is one mauve cat toy, two purple cat toys, three grey cat toys, two mauve notebooks, three grey notebooks, three burgundy cat toys, and one purple notebook. If I remove all the notebooks from the floor, how many grey objects remain on it? Options: (A) zero (B) one (C) two (D) three (E) four (F) five (G) six (H) seven (I) eight (J) nine (K) ten (L) eleven (M) twelve (N) thirteen (O) fourteen (P) fifteen (Q) sixteen
Ground truth Answer	(D) three
Method	**Output**
Direct Prompting	Final answer: (C) two **(Wrong)**
Zero-shot Prompting	First, let's count the number of grey objects on the floor before removing the notebooks: - Three grey cat toys - Three grey notebooks Total grey objects before removing notebooks: 3 (grey cat toys) + 3 (grey notebooks) = 6 grey objects Now, let's remove the notebooks from the floor: - Two mauve notebooks - Three grey notebooks - One purple notebook Total notebooks removed: 2 (mauve notebooks) + 3 (grey notebooks) + 1 (purple notebook) = 6 notebooks Now, let's calculate how many grey objects remain on the floor after removing the notebooks: Total grey objects before removing notebooks: 6 grey objects Total notebooks removed: 6 notebooks Grey objects remaining on the floor: 6 (total grey objects) - 6 (notebooks removed) = 0 grey objects Therefore, the answer is (A) zero **(Wrong)**

PoT	def solution():
	    # Total number of grey objects on the floor
	    total_grey_objects = 3 + 3
	
	    # Removing notebooks from the floor
	    removed_notebooks = 2 + 3
	
	    # Number of grey objects remaining on the floor
	    remaining_grey_objects = total_grey_objects - removed_notebooks
	
	    return remaining_grey_objects
	
	solution()
	»> 1 **(Wrong)**

NL Planning	Step 1: - Mauve cat toy - Purple cat toys - Grey cat toys - Mauve notebooks - Grey notebooks - Burgundy cat toys - Purple notebook Step 2: - The question asks about the number of grey objects remaining on the floor after removing all the notebooks. Step 3: - There are three grey cat toys and three grey notebooks on the floor. Step 4: - After removing all the notebooks, there are three grey cat toys remaining. Step 5: - The answer to the question is (C) two. Final answer: (C) two **(Wrong)**
Ours	Items on the surface: 'mauve cat toy': 1, 'purple cat toy': 2, 'grey cat toy': 3, 'mauve notebook': 2, 'grey notebook': 3, 'burgundy cat toy': 3, 'purple notebook': 1 Spatial relationships between items: 'mauve cat toy': ['floor'], 'purple cat toy': ['floor'], 'grey cat toy': ['floor'], 'mauve notebook': ['floor'], 'grey notebook': ['floor'], 'burgundy cat toy': ['floor'], 'purple notebook': ['floor'] The question is: how many grey objects remain on it? Reasoning for the answer: After removing all the notebooks, only the grey cat toys remain on the floor. Answer options: ['(A) zero', '(B) one', '(C) two', '(D) three', '(E) four', '(F) five', '(G) six', '(H) seven', '(I) eight', '(J) nine', '(K) ten', '(L) eleven', '(M) twelve', '(N) thirteen', '(O) fourteen', '(P) fifteen', '(Q) sixteen'] Final answer: (D) three **(Correct)**

Table 11: A comparison of results for Reasoning about Colored Objects Shapes between the baseline methods and ours.

Example Instance	Today, Jason went to the movies. Between what times could they have gone? We know that: Jason woke up at 10am. Linda saw Jason getting a coffee at the cafe from 10am to 3pm. Jennifer saw Jason walking towards the Statue of Liberty from 6pm to 7pm. Sean saw Jason buying a phone at the electronics store from 7pm to 10pm. The movies was closed after 10pm. Between what times could Jason have gone to the movies? Options: (A) 3pm to 6pm (B) 10am to 3pm (C) 7pm to 10pm (D) 6pm to 7pm
Ground truth Answer	**(A) 3pm to 6pm**
Method	**Output**
Direct Prompting	Final answer: (C) 7pm to 10pm **(Wrong)**
Zero-shot Prompting	Jason could have gone to the movies between 7pm to 10pm, as the movies were closed after 10pm. Therefore, the answer is (C) 7pm to 10pm **(Wrong)**

PoT	
	```
	def solution():
	    possible_times = []

	    # Jason could have gone to the movies between 3pm to 6pm
	    if 3 <= 6:
	        possible_times.append("3pm to 6pm")

	    # Jason could have gone to the movies between 10am to 3pm
	    if 10 <= 3:
	        possible_times.append("10am to 3pm")

	    # Jason could have gone to the movies between 7pm to 10pm
	    if 7 <= 10:
	        possible_times.append("7pm to 10pm")

	    # Jason could have gone to the movies between 6pm to 7pm
	    if 6 <= 7:
	        possible_times.append("6pm to 7pm")

	    return possible_times

	solution()
	»> ['3pm to 6pm', '7pm to 10pm', '6pm to 7pm']
	```
	 (Wrong)

NL Planning	Step 1: - Jason woke up at 10am. - Linda saw Jason at the cafe from 10am to 3pm. - Jennifer saw Jason walking towards the Statue of Liberty from 6pm to 7pm. - Sean saw Jason at the electronics store from 7pm to 10pm. - The movies was closed after 10pm. Step 2: - The specific question is about the time range for Jason to have gone to the movies. Step 3: - Timeline: - 10am: Jason woke up - 10am to 3pm: Jason at the cafe - 6pm to 7pm: Jason walking towards the Statue of Liberty - 7pm to 10pm: Jason at the electronics store - After 10pm: Movies closed Step 4: - Events placed on the timeline accordingly. Step 5: - Possible time range for Jason to have gone to the movies is after 10pm. Step 6: - Comparison results: - Option (A) 3pm to 6pm: Not possible - Option (B) 10am to 3pm: Not possible - Option (C) 7pm to 10pm: Possible - Option (D) 6pm to 7pm: Not possible Step 7: - Final answer: Jason could have gone to the movies between 7pm to 10pm. (Option C) **(Wrong)**
Ours	Events and their timings: [('Jason woke up', '10am'), ('Linda saw Jason getting a coffee at the cafe', '10am to 3pm'), ('Jennifer saw Jason walking towards the Statue of Liberty', '6pm to 7pm'), ('Sean saw Jason buying a phone at the electronics store', '7pm to 10pm')] Conflicting time intervals: [('10am', '3pm'), ('6pm', '7pm'), ('7pm', '10pm')] Available time intervals for visitation: [('3pm', '6pm')] Final answer: (A) 3pm to 6pm **(Correct)**

Table 12: A comparison of results for Temporal Sequences between the baseline methods and THINK-AND-EXECUTE.

Example Instance	Alice, Bob, Claire, Dave, and Eve are playing a game. At the start of the game, they are each holding a ball: Alice has a orange ball, Bob has a black ball, Claire has a pink ball, Dave has a white ball, and Eve has a red ball. As the game progresses, pairs of players trade balls. First, Alice and Dave swap balls. Then, Bob and Claire swap balls. Then, Claire and Dave swap balls. Then, Dave and Bob swap balls. Finally, Alice and Eve swap balls. At the end of the game, Claire has the Options: (A) orange ball (B) black ball (C) pink ball (D) white ball (E) red ball
Ground truth Answer	**(A) orange ball**

Method	**Output**
Direct Prompting	Final answer: (D) white ball **(Wrong)**
Zero-shot Prompting	1. After Alice and Dave swap balls: Alice has a white ball, Bob has a black ball, Claire has a pink ball, Dave has an orange ball, Eve has a red ball. 2. After Bob and Claire swap balls: ... 5. After Alice and Eve swap balls: Alice has a red ball, Bob has an orange ball, Claire has a black ball, Dave has a pink ball, Eve has a white ball. Therefore, the answer is (B) black ball **(Wrong)**

PoT	def solution():
	    balls = {"Alice": "orange", "Bob": "black", "Claire": "pink",
	"Dave": "white", "Eve": "red"}
	
	    # Define the swaps
	    swaps = [("Alice", "Dave"), ("Bob", "Claire"), ("Claire", "Dave"),
	("Dave", "Bob"), ("Alice", "Eve")]
	
	    # Perform the swaps
	    for swap in swaps:
	        temp = balls[swap[0]]
	        balls[swap[0]] = balls[swap[1]]
	        balls[swap[1]] = temp
	
	    # Return the ball color Claire has at the end
	    return [key for key, value in balls.items() if value == "pink"][0]
	
	solution()
	»> Dave **(Wrong)**

NL Planning	Step 1: Alice - orange ball Bob - black ball Claire - pink ball Dave - white ball Eve - red ball Step 2: 1. Alice and Dave swap balls 2. Bob and Claire swap balls 3. Claire and Dave swap balls 4. Dave and Bob swap balls 5. Alice and Eve swap balls Step 3: Alice - white ball Bob - pink ball Claire - black ball Dave - black ball Eve - orange ball Step 4: Final book assignment for Claire: black ball Step 5: Options: ... Step 6: Final answer: (B) black ball **(Wrong)**
Ours	Initial assignments: ’Alice’: ’orange ball’, ’Bob’: ’black ball’, ’Claire’: ’pink ball’, ’Dave’: ’white ball’, ’Eve’: ’red ball’ Swap pairs: [(’Alice’, ’Dave’), (’Bob’, ’Claire’), (’Claire’, ’Dave’), (’Dave’, ’Bob’), (’Alice’, ’Eve’)] After swapping Alice and Dave: ’Alice’: ’white ball’, ’Bob’: ’black ball’, ’Claire’: ’pink ball’, ’Dave’: ’orange ball’, ’Eve’: ’red ball’ ... After swapping Alice and Eve: ’Alice’: ’red ball’, ’Bob’: ’black ball’, ’Claire’: ’orange ball’, ’Dave’: ’pink ball’, ’Eve’: ’white ball’ The final position or gift of Claire is: orange ball Options: [(’(A) orange ball’, ’(B) black ball’, ’(C) pink ball’, ’(D) white ball’, ’(E) red ball’] Final answer:(A) **(Correct)**

Table 13: A comparison of results for Tracking Shuffled Objectives between the baseline methods and THINK-AND-EXECUTE.

Example Instance	Vina tells the truth. Helene says Vina lies. Kandi says Helene tells the truth. Jamey says Kandi lies. Ka says Jamey lies. Does Ka tell the truth?
Ground truth Answer	**No**
Method	**Output**
Direct Prompting	Final answer: Yes **(Wrong)**
Zero-shot Prompting	First, let's analyze the statements: 1. Vina tells the truth. 2. Helene says Vina lies. 3. Kandi says Helene tells the truth. 4. Jamey says Kandi lies. 5. Ka says Jamey lies. From statement 2, we can infer that Helene lies, which means Vina actually tells the truth. From statement 3, we can infer that Kandi tells the truth. From statement 4, we can infer that Jamey lies. From statement 5, we can infer that Ka tells the truth. Therefore, Ka tells the truth. Therefore, the answer is Yes **(Wrong)**

PoT	def solution():
	    vina = True
	    helene = not vina
	    kandi = vina
	    jamey = not kandi
	    ka = not jamey
	
	    return ka
	
	solution()
	»> True **(Wrong)**

NL Planning	Step 1: - Vina tells the truth. - Helene says Vina lies. - Kandi says Helene tells the truth. - Jamey says Kandi lies. - Ka says Jamey lies. Step 2: Person — Truth-telling status Vina — True Helene — False Kandi — True Jamey — False Ka — False Step 3: - Based on Helene's statement, Vina is lying. Since Vina tells the truth, Helene is lying. - Based on Kandi's statement, Helene tells the truth. Since Helene lies, Kandi is lying. - Based on Jamey's statement, Kandi lies. Since Kandi tells the truth, Jamey is lying. - Based on Ka's statement, Jamey lies. Since Jamey lies, Ka is telling the truth. Step 4: Person — Truth-telling status Vina — True Helene — False Kandi — True Jamey — False Ka — True Step 5: - Ka tells the truth. Final answer: Yes **(Wrong)**
Ours	Statements: ['Vina tells the truth', 'Helene says Vina lies', 'Kandi says Helene tells the truth', 'Jamey says Kandi lies', 'Ka says Jamey lies'] Question: Does Ka tell the truth Vina says the truth. Vina tells the truth: True Helene says Vina lies. Helene tells the truth: False Kandi says Helene tells the truth. Kandi tells the truth: False Jamey says Kandi lies. Jamey tells the truth: True Ka says Jamey lies. Ka tells the truth: False Final answer: No **(Correct)**

Table 14: A comparison of results for Web of lies between the baseline methods and THINK-AND-EXECUTE.