



## 基于滤波的融合方法



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- 第一部分：框架调试
- 第二部分：实现滤波算法

## ●说明：调试方法仅适用于第一版框架

```
r_localization/src/data_pretreat/lidar_preprocess_flow.cpp:6:  
/home/chongda517/catkin_chapter_6/src/07-filtering-advanced/src/lidar_localization/include  
/lidar_localization/publisher/lidar_measurement_publisher.hpp:10:49: fatal error: lidar_lo  
calization/LidarMeasurement.h: 没有那个文件或目录  
compilation terminated.  
make[2]: *** [CMakeFiles/data_pretreat_node.dir/src/data_pretreat/lidar_preprocess_flow.cpp  
p.o] Error 1  
make[1]: *** [CMakeFiles/data_pretreat_node.dir/all] Error 2  
In file included from /home/chongda517/catkin_chapter_6/src/07-filtering-advanced/src/lida  
r_localization/include/lidar_localization/data_pretreat/lidar_preprocess_flow.hpp:17:0,  
from /home/chongda517/catkin_chapter_6/src/07-filtering-advanced/src/lida  
r_localization/src/data_pretreat/lidar_preprocess_flow.cpp:6:  
/home/chongda517/catkin_chapter_6/src/07-filtering-advanced/src/lidar_localization/include  
/lidar_localization/publisher/lidar_measurement_publisher.hpp:10:49: fatal error: lidar_lo  
calization/LidarMeasurement.h: 没有那个文件或目录
```

图1.1

```
> ${ALL_SRCS})  
> ${PROJECT_NAME}_generate_messages_cpp)  
> ${ALL_TARGET_LIBRARIES})  
  
ode.cpp ${ALL_SRCS})  
ETS} ${PROJECT_NAME}_generate_messages_cpp)  
S} ${ALL_TARGET_LIBRARIES})  
  
ess_node.cpp ${ALL_SRCS})  
ARGETS} ${PROJECT_NAME}_generate_messages_cpp)  
RIES} ${ALL_TARGET_LIBRARIES})  
  
> ${ALL_SRCS})  
> ${PROJECT_NAME}_generate_messages_cpp)  
[ALL_TARGET_LIBRARIES])  
  
ALL_SRCS})  
> ${PROJECT_NAME}_generate_messages_cpp)  
ALL_TARGET_LIBRARIES})  
  
a.cpp ${ALL_SRCS})  
FS} ${PROJECT_NAME}_generate_messages_cpp)  
} ${ALL_TARGET_LIBRARIES})  
  
SRCS})  
PROJECT_NAME}_generate_messages_cpp)  
L_TARGET_LIBRARIES})  
  
rg_node.cpp ${ALL_SRCS})  
ARGETS} ${PROJECT_NAME}_generate_messages_cpp)  
IES} ${ALL_TARGET_LIBRARIES})  
  
ss_node.cpp ${ALL_SRCS})  
ARGETS} ${PROJECT_NAME}_generate_messages_cpp)  
IES} ${ALL_TARGET_LIBRARIES})  
  
ins_sim_preprocess_node.cpp ${ALL_SRCS})  
ORTED_TARGETS} ${PROJECT_NAME}_generate_messages_cpp)  
_LIBRARIES} ${ALL_TARGET_LIBRARIES})
```

图1.2

如若出现图1.1中的编译问题，修改目录/06-filtering-yc/src/lidar\_localization/下的CMakeLists文件，如图1.2。

## ●说明：调试方法仅适用于第一版框架

修改kitti\_filtering.yaml文件下的地图和回环检测所需文件的路径kitti\_filtering.yaml的路径如图1.3所示，修改后如图1.4。

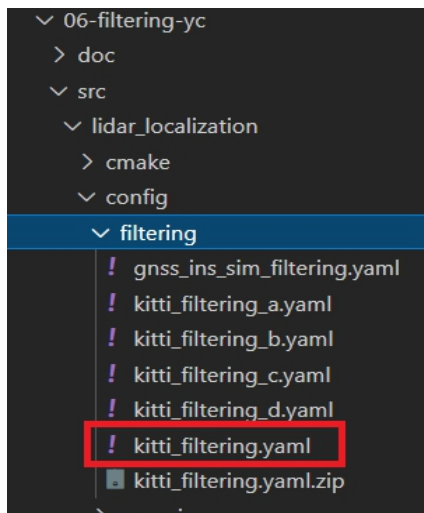


图1.3

```
# loop closure for localization initialization/re-initialization:
loop_closure_method: scan_context # 选择回环检测方法, 目前支持scan_context
scan_context_path: /home/chongda517/catkin_chapter_6/src/07-filtering-advanced/src/lidar_localization/slam_data/scan_context

# 配置

# 全局地图
map_path: /home/chongda517/catkin_chapter_6/src/07-filtering-advanced/src/lidar_localization/slam_data/map/filtered_map.pcd
global_map_filter: voxel_filter # 选择滑动窗口点云滤波方法, 目前支持: voxel_filter、no_filter

# 局部地图
```

图1.4

## ●说明：调试方法仅适用于第一版框架。

本地编译需要重新生成scan\_context需要的文件，如图1.5。在slam\_data/文件夹下新建trajectory，如图1.6

```
打开lidar_localization/config/scan_context文件夹，输入如下命令，生成pb文件
```bash
protoc --cpp_out=./ key_frames.proto
protoc --cpp_out=./ ring_keys.proto
protoc --cpp_out=./ scan_contexts.proto
mv key_frames.pb.cc key_frames.pb.cpp
mv ring_keys.pb.cc ring_keys.pb.cpp
mv scan_contexts.pb.cc scan_contexts.pb.cpp
```

分别修改生成的三个.pb.cpp文件。如下，以ring_keys.pb.cpp为例。
```C++
// Generated by the protocol buffer compiler.  DO NOT EDIT!
// source: ring_keys.proto

#define INTERNAL_SUPPRESS_PROTOBUF_FIELD_DEPRECATION
#include "ring_keys.pb.h" 替换为 #include "lidar_localization/models/
scan_context_manager/ring_keys.pb.h"

#include <algorithm>
```

之后，用以上步骤生成的.pb.h文件替换lidar_localization/include/
lidar_localization/models/scan_context_manager
中的同名文件。
将.pb.cpp文件替换lidar_localization/src/models/scan_context_manager中的同名
文件。
```

图1.5

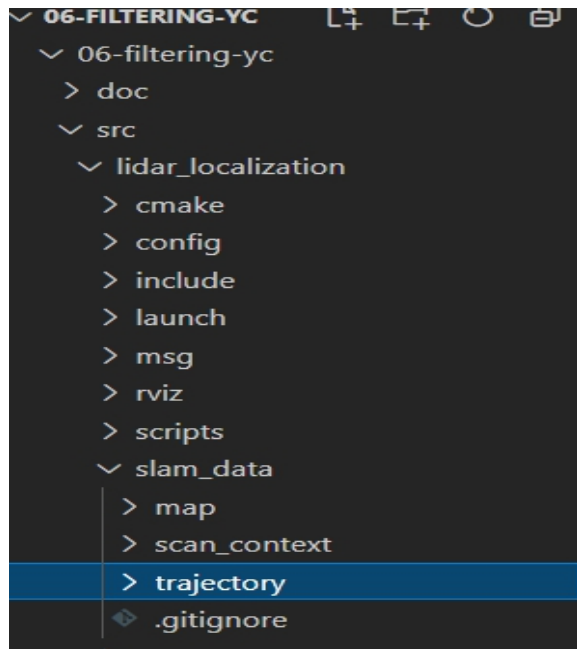
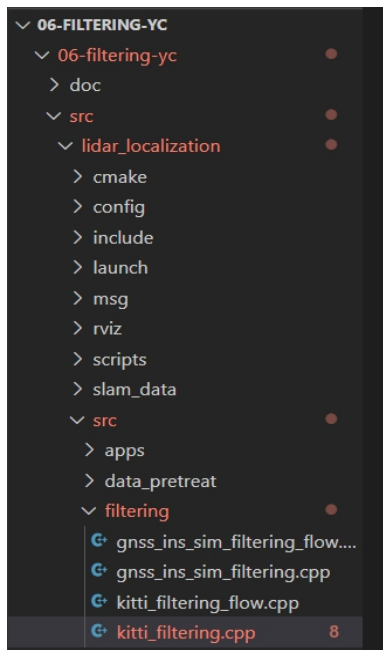


图1.6

## ●说明：调试方法仅适用于第一版框架。

修改kitti\_filtering.cpp。文件目录如左图，修改后如右图。



```
// Kalman correction:
if (
    /*kalman_filter_ptr_->Correct(
        imu_data,
        KalmanFilter::MeasurementType::POSE_VEL, current_measurement_
    )*/
    kalman_filter_ptr_->Correct(
        imu_data,
        KalmanFilter::MeasurementType::POSE, current_measurement_
    )
) {
```

➤ 第一部分： 框架调试

➤ 第二部分： 滤波实现

## 基于滤波器的融合

### 1. 状态方程

状态方程由误差方程得来，第6讲已经完成误差方程的推导：则误差方程可以写成状态方程的通用形式：

$$\delta \dot{x} = F_t \delta x + B_t w$$

其中

$$\delta \dot{p} = \delta v$$

$$\delta \dot{v} = -R_t [a_t - b_{a_t}]_x \delta \theta + R_t (n_{a_t} - \delta b_{a_t})$$

$$\delta \dot{\theta} = -[\omega_t - b_{\omega_t}]_x \delta \theta + n_{\omega_t} - \delta b_{\omega_t}$$

$$\delta \dot{b}_{a_t} = n_{b_{a_t}} \quad \delta \dot{b}_{a_t} = 0$$

或

$$\delta \dot{b}_{\omega_t} = n_{b_{\omega_t}} \quad \delta \dot{b}_{\omega_t} = 0$$

$$F_t = \begin{bmatrix} 0 & I_3 & 0 & 0 & 0 \\ 0 & 0 & -R_t [a_t]_x & -R_t & 0 \\ 0 & 0 & -[\omega_t]_x & 0 & -I_3 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \end{bmatrix} \quad \begin{aligned} \tilde{a}_t &= a_t - b_{a_t} \\ \tilde{\omega}_t &= \omega_t - b_{\omega_t} \end{aligned}$$

$$B_t = \begin{bmatrix} 0 & 0 & 0 & 0 \\ R_t & 0 & 0 & 0 \\ 0 & I_3 & 0 & 0 \\ 0 & 0 & I_3 & 0 \\ 0 & 0 & 0 & I_3 \end{bmatrix}$$

$$\text{令 } \delta x = \begin{bmatrix} \delta p \\ \delta v \\ \delta \theta \\ \delta b_{a_t} \\ \delta b_{\omega_t} \end{bmatrix}, W = \begin{bmatrix} n_{a_t} \\ n_{\omega_t} \\ n_{b_{a_t}} \\ n_{b_{\omega_t}} \end{bmatrix}$$

注：当选择  $\delta \dot{b}_{a_t} = 0, \delta \dot{b}_{\omega_t} = 0$  时，矩阵形式不一样，请各位自行推导。

预测状态方程的  $F_t$  矩阵需要加速度和旋转角速度信息。而第一期框架的解算函数输出了速度信息，我们可以添加旋转角速度信息，**注意修改源文件后同时修改头文件和相关函数。**

```
void ErrorStateKalmanFilter::UpdateOdomEstimation(Eigen::Vector3d &linear_acc_mid, Eigen::Vector3d &mid_w) {  
    //  
    // TODO: this is one possible solution to previous chapter, IMU Navigation, assignment  
    //  
    static Eigen::Vector3d w_b = Eigen::Vector3d::Zero();  
  
    // get deltas:  
    Eigen::Vector3d angular_delta;  
    GetAngularDelta(1, 0, angular_delta, mid_w);  
}
```

修改后

```
void ErrorStateKalmanFilter::UpdateOdomEstimation(Eigen::Vector3d &linear_acc_mid) {  
    //  
    // TODO: this is one possible solution to previous chapter, IMU Navigation, assignment  
    //  
    static Eigen::Vector3d w_b = Eigen::Vector3d::Zero();  
  
    // get deltas:  
    Eigen::Vector3d angular_delta;  
    GetAngularDelta(1, 0, angular_delta, mid_w);  
}
```

修改前



## 基于滤波器的融合

### 1. 状态方程

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$$\delta \dot{x} = F_t \delta x + B_t w$$

其中

$$F_t = \begin{bmatrix} 0 & I_3 & 0 & 0 & 0 \\ 0 & 0 & -R_t [a_t]_{\times} & -R_t & 0 \\ 0 & 0 & -[\tilde{\omega}_t]_{\times} & 0 & -I_3 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \end{bmatrix} \quad \begin{matrix} \tilde{a}_t = a_t - b_{a_t} \\ \tilde{\omega}_t = \omega_t - b_{\omega_t} \end{matrix}$$

$$B_t = \begin{bmatrix} 0 & 0 & 0 & 0 \\ R_t & 0 & 0 & 0 \\ 0 & I_3 & 0 & 0 \\ 0 & 0 & I_3 & 0 \\ 0 & 0 & 0 & I_3 \end{bmatrix}$$

$$\begin{aligned} \delta \dot{p} &= \delta v \\ \delta \dot{v} &= -R_t [a_t - b_{a_t}]_{\times} \delta \theta + R_t (n_a - \delta b_{a_t}) \\ \delta \dot{\theta} &= -[\omega_t - b_{\omega_t}]_{\times} \delta \theta + n_{\omega} - \delta b_{\omega} \\ \delta \dot{b}_{a_t} &= n_{b_{a_t}} \quad \delta \dot{b}_{\omega_t} = 0 \\ \text{或} \\ \delta \dot{b}_{\omega_t} &= n_{b_{\omega_t}} \quad \delta \dot{b}_{a_t} = 0 \end{aligned}$$

$$\text{令 } \delta x = \begin{bmatrix} \delta p \\ \delta v \\ \delta \theta \\ \delta b_{a_t} \\ \delta b_{\omega_t} \end{bmatrix}, W = \begin{bmatrix} n_a \\ n_{\omega} \\ n_{b_{a_t}} \\ n_{b_{\omega_t}} \end{bmatrix}$$

注：当选择  $\delta \dot{b}_{a_t} = 0, \delta \dot{b}_{\omega_t} = 0$  时，矩阵形式不一样，请各位自行推导。

接下来将  $F_t$  的初始化。首先在 `ErrorStateKalmanFilter` 的构造函数里面初始  $F_t$  的单位矩阵。

```
// e. process equation:
//F_.block<3, 3>( INDEX_ERROR_POS, INDEX_ERROR_VEL) = Eigen::Matrix3d::Identity();
//F_.block<3, 3>( INDEX_ERROR_ORI, INDEX_ERROR_ORI) = Sophus::SO3d::hat(-w_).matrix();
F_.block<3, 3>( 0, INDEX_ERROR_POS) = Eigen::Matrix3d::Identity();
F_.block<3, 3>( INDEX_ERROR_ORI, INDEX_ERROR_ACCEL) = Eigen::Matrix3d::Identity();
```

# 滤波实现

## 基于滤波器的融合

### 1. 状态方程

状态方程由误差方程得来，第6讲已经完成误差方程的推导：

$$\delta \dot{p} = \delta v$$

$$\delta \dot{v} = -R_t[a_t - b_{a_t}]_x \delta \theta + R_t[n_a - \delta b_a]$$

$$\delta \dot{\theta} = -[\omega_t - b_{\omega_t}]_x \delta \theta + n_{\omega} - \delta b_{\omega}$$

$$\delta \dot{b}_a = n_{b_a} \quad \delta \dot{b}_a = 0$$

或

$$\delta \dot{b}_{\omega} = n_{b_{\omega}} \quad \delta \dot{b}_{\omega} = 0$$

$$\text{令 } \delta x = \begin{bmatrix} \delta p \\ \delta v \\ \delta \theta \\ \delta b_a \\ \delta b_{\omega} \end{bmatrix}, W = \begin{bmatrix} n_a \\ n_{\omega} \\ n_{b_a} \\ n_{b_{\omega}} \end{bmatrix}$$

其中

$$F_t = \begin{bmatrix} 0 & I_3 & 0 & 0 & 0 \\ 0 & 0 & -R_t[a_t]_x & -R_t & 0 \\ 0 & 0 & -[\omega_t]_x & 0 & -I_3 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \end{bmatrix} \quad \begin{matrix} \bar{a}_t = a_t - b_{a_t} \\ \bar{\omega}_t = \omega_t - b_{\omega_t} \end{matrix}$$

$$B_t = \begin{bmatrix} 0 & 0 & 0 & 0 \\ R_t & 0 & 0 & 0 \\ 0 & I_3 & 0 & 0 \\ 0 & 0 & I_3 & 0 \\ 0 & 0 & 0 & I_3 \end{bmatrix}$$

注：当选择  $\delta \dot{b}_a = 0$ ,  $\delta \dot{b}_{\omega} = 0$  时，矩阵形式不一样，请各位自行推导。

然后在ErrorStateKalmanFilter的Update()成员函数里面使用修改后解算函数。并且修改滤波更新函数UpdateErrorEstimation()使其参数里面包含旋转角速度。

```
bool ErrorStateKalmanFilter::Update(const IMUData &imu_data) {  
    // update IMU buff:  
    if (time_ < imu_data.time) {  
        // update IMU odometry:  
        Eigen::Vector3d linear_acc_mid;  
        Eigen::Vector3d mid_w;  
        imu_data_buff_.push_back(imu_data);  
  
        UpdateOdomEstimation(linear_acc_mid, mid_w);  
        imu_data_buff_.pop_front();  
  
        // update error estimation:  
        double T = imu_data.time - time_;  
        UpdateErrorEstimation(T, linear_acc_mid, mid_w);  
    }  
}
```

## 基于滤波器的融合

### 1. 状态方程

状态方程由误差方程得来，第6讲已经完成误差方程的推导：

则误差方程可以写成状态方程的通用形式：

$$\delta \dot{\mathbf{x}} = \mathbf{F}_t \delta \mathbf{x} + \mathbf{B}_t \mathbf{w}$$

$$\delta \dot{\mathbf{p}} = \delta \mathbf{v}$$

$$\delta \dot{\mathbf{v}} = -\mathbf{R}_t[\mathbf{a}_t - \mathbf{b}_{a_t}]_x \delta \theta + \mathbf{R}_t(\mathbf{n}_a - \delta \mathbf{b}_{a_t})$$

$$\delta \dot{\theta} = -[\omega_t - \mathbf{b}_{\omega_t}]_x \delta \theta + \mathbf{n}_{\omega} - \delta \mathbf{b}_{\omega}$$

$$\delta \dot{\mathbf{b}}_a = \mathbf{n}_{b_a} \quad \delta \dot{\mathbf{b}}_a = 0$$

或

$$\delta \dot{\mathbf{b}}_{\omega} = \mathbf{n}_{b_{\omega}} \quad \delta \dot{\mathbf{b}}_{\omega} = 0$$

其中

$$\mathbf{F}_t = \begin{bmatrix} 0 & \mathbf{I}_3 & 0 & 0 & 0 \\ 0 & 0 & -\mathbf{R}_t[\mathbf{a}_t]_x & -\mathbf{R}_t & 0 \\ 0 & 0 & -[\omega_t]_x & 0 & -\mathbf{I}_3 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \end{bmatrix} \quad \begin{matrix} \bar{\mathbf{a}}_t = \mathbf{a}_t - \mathbf{b}_{a_t} \\ \bar{\omega}_t = \omega_t - \mathbf{b}_{\omega_t} \end{matrix}$$

$$\mathbf{B}_t = \begin{bmatrix} 0 & 0 & 0 & 0 \\ \mathbf{R}_t & 0 & 0 & 0 \\ 0 & \mathbf{I}_3 & 0 & 0 \\ 0 & 0 & \mathbf{I}_3 & 0 \\ 0 & 0 & 0 & \mathbf{I}_3 \end{bmatrix}$$

$$\text{令 } \delta \mathbf{x} = \begin{bmatrix} \delta p \\ \delta v \\ \delta \theta \\ \delta b_a \\ \delta b_{\omega} \end{bmatrix}, \quad \mathbf{W} = \begin{bmatrix} \mathbf{n}_a \\ \mathbf{n}_{\omega} \\ \mathbf{n}_{b_a} \\ \mathbf{n}_{b_{\omega}} \end{bmatrix}$$

注：当选择  $\delta \dot{\mathbf{b}}_a = 0$ ,  $\delta \dot{\mathbf{b}}_{\omega} = 0$  时，矩阵形式不一样，请各位自行推导。

接下来需要在SetProcessEquation函数里面对Ft矩阵的非单位矩阵，即第二行和第三行进行赋值和矩阵B。

```
F_.block<3, 3>(INDEX_ERROR_VEL, INDEX_ERROR_ORI) = -C_nb * Sophus::SO3d::hat(f_n).matrix();
F_.block<3, 3>(INDEX_ERROR_VEL, INDEX_ERROR_GYRO) = -C_nb;

B_.block<3, 3>(INDEX_ERROR_VEL, INDEX_ERROR_POS) = C_nb;
B_.block<3, 3>(INDEX_ERROR_ORI, INDEX_ERROR_VEL) = Eigen::Matrix3d::Identity();
B_.block<3, 3>(INDEX_ERROR_GYRO, INDEX_ERROR_ORI) = Eigen::Matrix3d::Identity();
B_.block<3, 3>(INDEX_ERROR_ACCEL, INDEX_ERROR_GYRO) = Eigen::Matrix3d::Identity();

// b. set process equation for delta ori:
F_.block<3, 3>(INDEX_ERROR_ORI, INDEX_ERROR_ORI) = -Sophus::SO3d::hat(mid_angular_velocity).matrix();
F_.block<3, 3>(INDEX_ERROR_ORI, INDEX_ERROR_ACCEL) = -Eigen::Matrix3d::Identity();
```

# 滤波实现

最后就只需要修改框架代码里面提示的fix\_this部分，按照卡尔曼滤波公式直接补上去就ok。当不考虑Bias时，由于预测量减少，滤波更容易实现，推导公式也更简单，只需要在框架上稍加修改即可。相关噪音参数只需修改kitti\_filtering文件。

```
//X_ = F * X_ + B * w ; // fix this
X_ = F * X_;
P_ = F * P_ * F.transpose() + B * Q_ * B.transpose() ; // fix this
```

```
Eigen::Matrix<double, 6, 6> Ct = Eigen::Matrix<double, 6, 6>::Identity();
MatrixRPose R = RPose_; // fix this
K = P_ * G.transpose() * (G * P_ * G.transpose() + Ct * R * Ct.transpose()).inverse(); // fix this
```

```
P_ = (Eigen::Matrix<double, 15, 15>::Identity() - K * G) * P_; // fix this
X_ = X_ + K * (Y - G * X_); // fix this
```

```
pose_.block<3, 1>(0, 3) = pose_.block<3, 1>(0, 3) + X_.block<3,1>(0,0); // fix this
// b. velocity:
vel_ = vel_ + X_.block<3,1>(3,0); // fix this
// c. orientation:
Eigen::Matrix3d delta_rotation = Sophus::SO3d::hat(X_.block<3, 1>(6, 0)).matrix(); // fix this*/
pose_.block<3,3>(0,0) = pose_.block<3,3>(0,0) * (Eigen::Matrix3d::Identity() + delta_rotation);
```



**感谢各位聆听 !**  
Thanks for Listening

