Sliding Window for Irdan Localization. 1. There is a cost term for each residual term e= /2 /1 r+ JAXI/Z $= \frac{1}{2} (r + J_{\Delta x})^T \Sigma^{-1} (r + J_{\Delta x})$ = となびプエリムス ナトアースス+ メトアエート $\frac{\partial e}{\partial \Delta x} = 0 \Rightarrow \int^{T} Z^{-1} J \Delta x = -\int^{T} Z^{-1} r$ -. Define $H_i = J_i^T \Sigma^T J_i$ bi = - Ji Zi ri The optimization problem can be formatted as: ZHi. DX = Zbi .. for each type of constraint we must define Tesidual, r

Jacobian of residual w.r.t panns, T

for real-time localization, the analytic expression for must be given to Ceres.

2. There are 3 types of constraints

a. pose from map matching (scan-context)
or
GINSS position

B. relative pose from lidar frontend (ICP/NDT/LOAM)

c. INVU pre-integration

For constraint type \underline{c} , the results from VIO can be readily used.

But for this project the extended pose will be parameterized using so3 rather than quaternion

Residual:

Jacobian:
$$\frac{\partial r_P}{\partial t} = I_3$$

Ir should be implemented.

3.b. relative pose from lidar frontend.

$$r_p = R_i^T(t_j - t_i) - t_{obs}$$

$$\frac{\partial P}{\partial r} = -P_i^T \qquad \frac{\partial P}{\partial r} = |I_{in}|$$

=
$$-J_r^-(r_q) exp(r_q^*).inverse()$$

Ir should be implemented.

3.c IMU pre-integration:

$$\frac{\partial r_{p}}{\partial k_{i}} = \left[R_{i}^{T} (P_{i} - P_{i} - V_{i}T + k_{g}T^{z}) \right]^{\Lambda} \qquad \frac{\partial r_{p}}{\partial r_{j}} = 0$$

$$\frac{\partial r_{i}}{\partial v_{i}} = -T \cdot R_{i}^{T} \qquad \frac{\partial r_{i}}{\partial v_{i}} = 0$$

$$T_{r} = \ln(R_{ij}^{T}R_{i}^{T}R_{j}^{T})$$

$$C T_{i}, b_{gi}$$

$$\frac{\partial Y_{r}}{\partial r_{i}} = \lim_{\phi \to 0} \ln(R_{ij}^{T}R_{i}^{T}R_{j}^{T}e^{\exp(-R_{ij}^{T}R_{i}\phi)}] - Y_{r} = -J_{r}^{-1}(Y_{r})R_{ij}^{T}R_{i}$$

$$T_{U} = R_{i}^{T}(V_{j} - V_{i} + gT) - \beta_{ij}$$
 C
 $K_{i}, V_{i}, D_{ai}, D_{gi}$

$$\frac{1}{2}: \frac{2}{2} = \left[R_{i}^{T}(y_{i} - V_{i} + gT) \right]^{\Lambda}$$

$$\frac{\partial r_g}{\partial bgi} = -\overline{1} \quad \frac{\partial r_g}{\partial bgj} = \overline{1}$$

4. In order to adapt Marginalization to Ceres Solver

a. When the sliding window has been filled, start to create Marginalization

factor for next optimization

b. In order to fit into Ceres solver marginalization has to be implemented as follows:

$$\begin{cases} H_{rr} - H_{rm}H_{mm} + H_{mr} = H = J^{T}J \\ J_{r} - H_{rm}H_{mm} + J_{m} = J = -J^{T}r \end{cases}$$

: 7=J-Tb=JN-1VTb->Nlarg. Res Block. Residuals.
c. Add the Marg. Factor directly to
next Ceres problem.

Marginalization Residual Block Building, PRVAG in SO3
for the to-be-marginalized param block m and its next param block h
a. Map Mate ing:
$J: m r_1 r_2 \rightarrow JJ m r_1 r_2$
e, //// e, //// /// /// /// /// ///
b. Relative Pose & IMU Pre Integration
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
P ₁ ////////////////////////////////////
The marginalization res. Block is only relevant to
Davam Harb r

should be computed using res. block (MapMatching (m) Relatrue Pose (m.r.)

IMU (m,r.)

Hrr, Hrm, Hmm, Hmr, Br, Bm

1/2(+Jax) (r+Jax) = /20xJJJax+rJax+rTL