

# Signal and System

## MATLAB Homework #2

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### 1 Problem 1

(a) Plot  $x[n]$ .

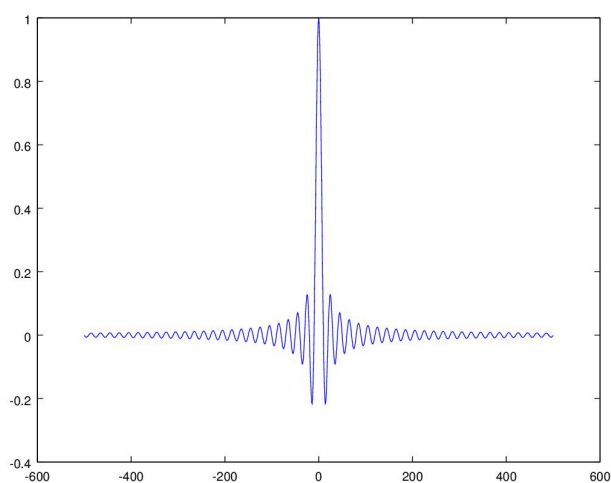


Figure 1: Plot of  $x[n]$ .

(b) Plot the magnitude response of the DFT of  $x$  during  $[-N_1, N_1]$ . The zero frequency should be centered in your plot. Observe the Gibbs phenomenon here.

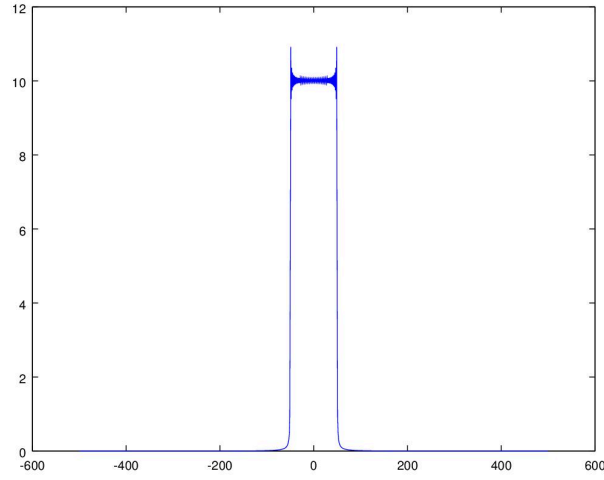
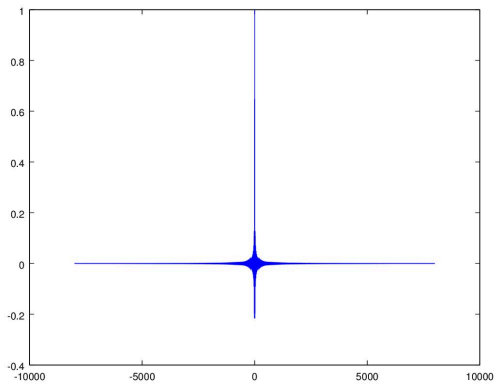
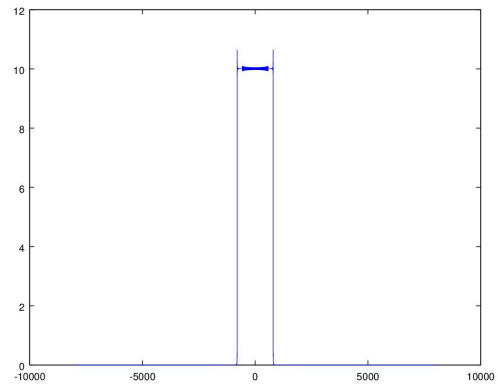


Figure 2: Plot of the magnitude response.

- (c) We define the overlapping factor  $K$  so that  $n \in \{-KN_1, -KN_1+1, \dots, 0, \dots, KN_1-1, KN_1\}$ . Please repeat part (a) and (b) with  $K = 16$  and fixed  $T_s$ , then compare the Gibbs phenomenon in (b).



(a) Plot of  $x[n]$ .



(b) Plot of the magnitude response.

The distortion width is smaller, but the maximum height (i.e the maximum error) remain the same.

## 2 Problem 2

- (a) Plot  $x[n]$  when  $n \in \mathcal{N}$ .

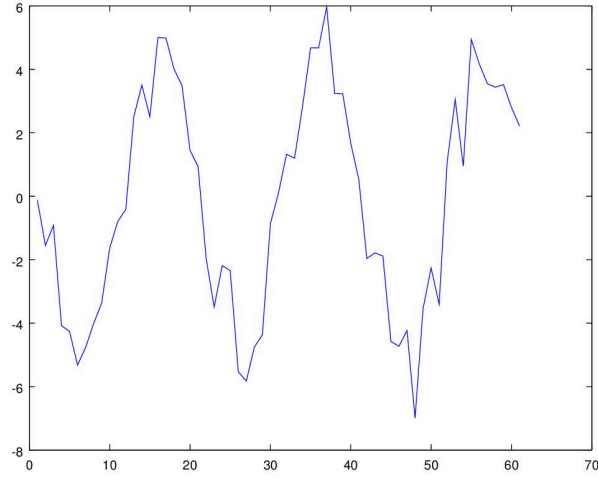


Figure 4: Plot of  $x[n]$ .

- (b) Now let  $b = 0.2$  and  $N = 3$ . Assuming that at  $n = 0$  and we initialize the EWMA filter with  $x[-1] = \dots = x[-N] = 0$ , plot the output of the filter for  $n \in \mathcal{N}$ .

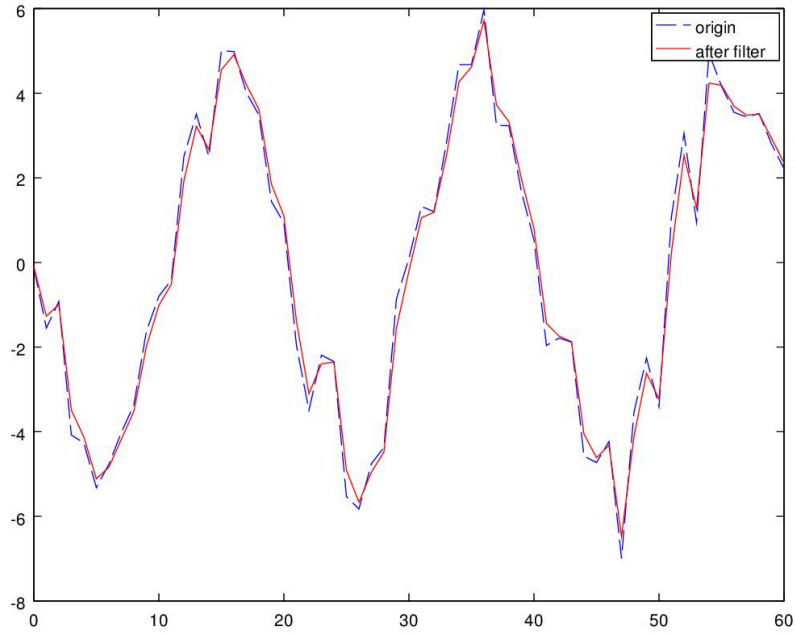


Figure 5: Plot of the output after filter.

(c) Repeat part (b) with  $b = 0.2$  and  $N = 10$ .

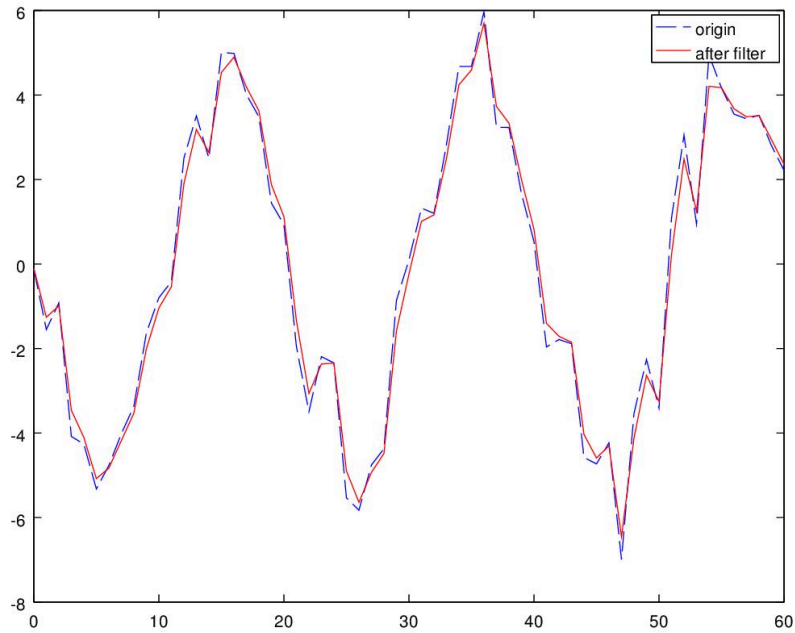


Figure 6: Plot of the output after filter.

(d) Comment on the relationship between the filter outputs in parts (b) and (c) with the original signal  $s[n]$ .

After the filter, the signal looks slightly smoother, but is still similar to the origin input, since the decay rate  $b$  is small (so it decay fast!).

Also because the decay rate  $b$  is too small,  $N = 3$  and  $N = 10$  gives almost the same result.

(e) Please repeat parts (b), and (d) with  $b = 0.5$  and  $N = 3$ .

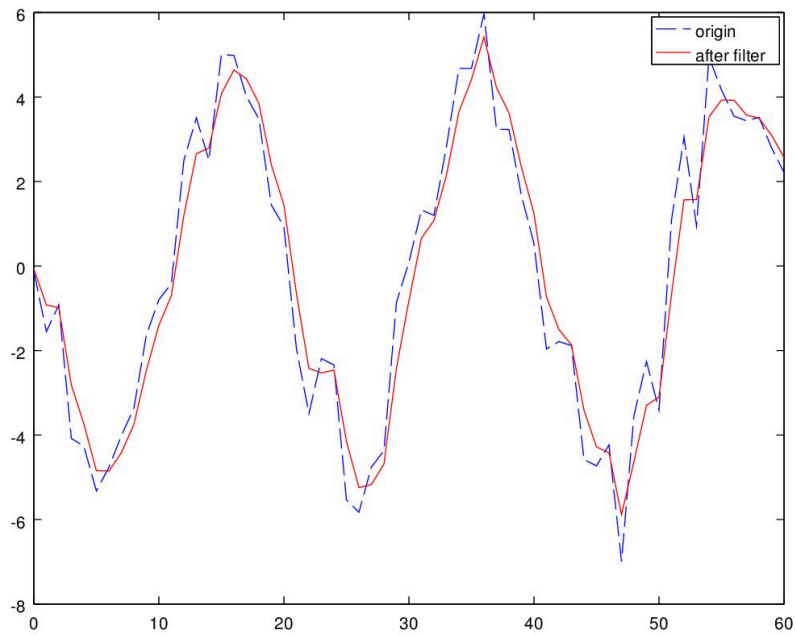


Figure 7: Plot of the output after filter.

The output is much smoother and closer to the signal without the noise compare to the input.

(f) **What is the effect of increasing  $b$ ? What about increasing  $N$ ?**

Increasing  $b$  tends to make the output smoother.

Increasing  $N$  at small  $N$  could also let the output become smoother, provided that  $b$  is not too small.