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**(結報) 實驗 5 Matlab 於基礎訊號運算之應用**

**DISCRETE-TIME SIGNALS: TIME-DOMAIN REPRESENTATION**

**1.1 GENERATION OF SEQUENCES**

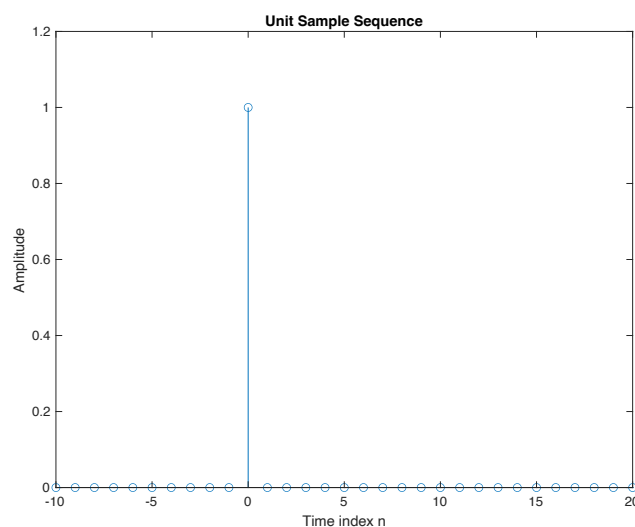
**Project 1.1 Unit sample and unit step sequences**

A copy of Program P1\_1 is given below.

```
% Program P1_1
% Generation of a Unit Sample Sequence
clf;
% Generate a vector from -10 to 20
n = -10:20;
% Generate the unit sample sequence
u = [zeros(1,10) 1 zeros(1,20)];
% Plot the unit sample sequence
stem(n,u);
xlabel('Time index n');ylabel('Amplitude');
title('Unit Sample Sequence');
axis([-10 20 0 1.2]);
```

**Answers:**

**Q1.1** The unit sample sequence  $u[n]$  generated by running Program P1\_1 is shown below:



**Q1.2** The purpose of `clf` command is – Clear current figure

The purpose of `axis` command is - Control axis scaling and appearance.

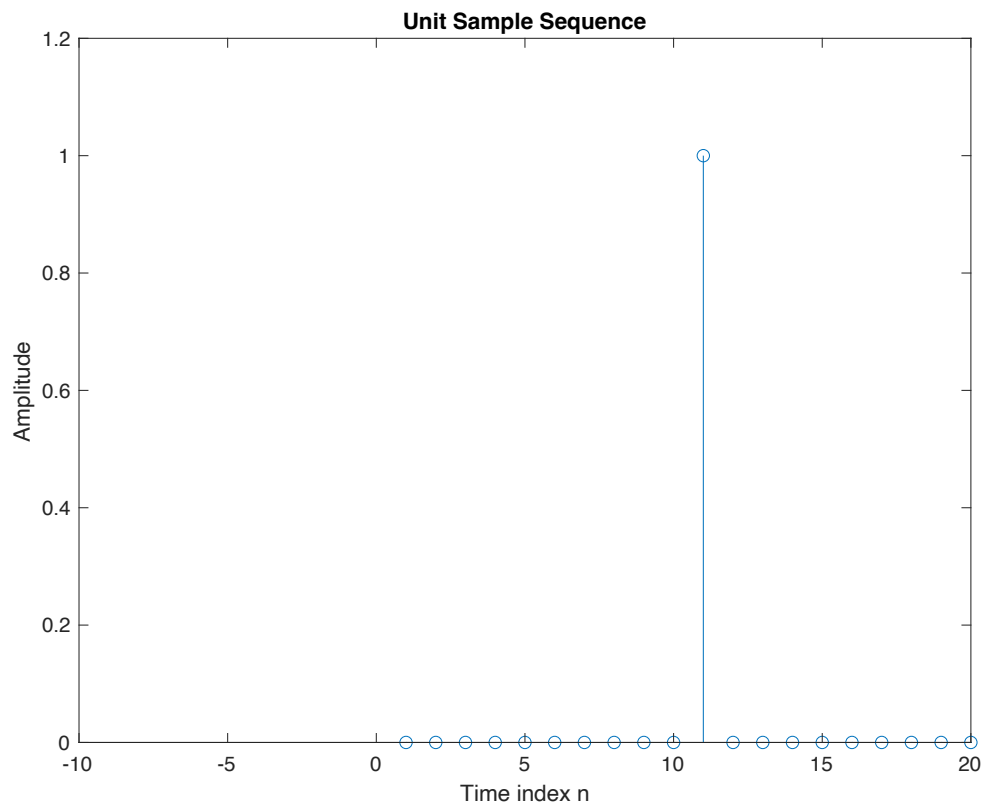
The purpose of `title` command is - input Graph title

The purpose of `xlabel` command is - X-axis label

The purpose of `ylabel` command is - Y-axis label

**Q1.3** The modified Program P1\_1 to generate a delayed unit sample sequence  $u_d[n]$  with a delay of 11 samples is given below along with the sequence generated by running this program.

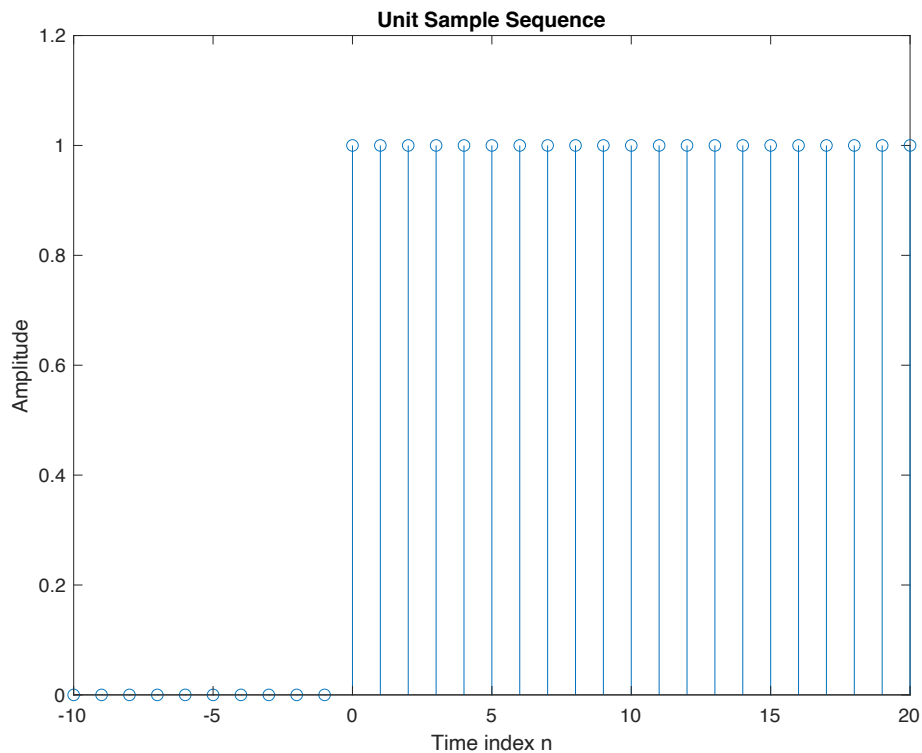
```
% Program P1_1
% Generation of a Unit Sample Sequence
clf;
% Generate a vector from -10 to 20
n = 1:31;
% Generate the unit sample sequence
u = [zeros(1,10) 1 zeros(1,20)];
% Plot the unit sample sequence
stem(n,u);
xlabel('Time index n');ylabel('Amplitude');
title('Unit Sample Sequence');
axis([-10 20 0 1.2]);
```



**Q1.4** The modified Program P1\_1 to generate a unit step sequence  $s[n]$  is given below along with the sequence generated by running this program. % Program P1\_1

```
% Generation of a Unit Sample Sequence
clf;
% Generate a vector from -10 to 20
n = -10:20;
% Generate the unit sample sequence
u = [zeros(1,10) 1 ones(1,20)];
% Plot the unit sample sequence
stem(n,u);
xlabel('Time index n');ylabel('Amplitude');
title('Unit Sample Sequence');
axis([-10 20 0 1.2]);
```

< Insert program code here. Copy from m-file(s) and paste. >



< Insert program code here. Copy from m-file(s) and paste. >

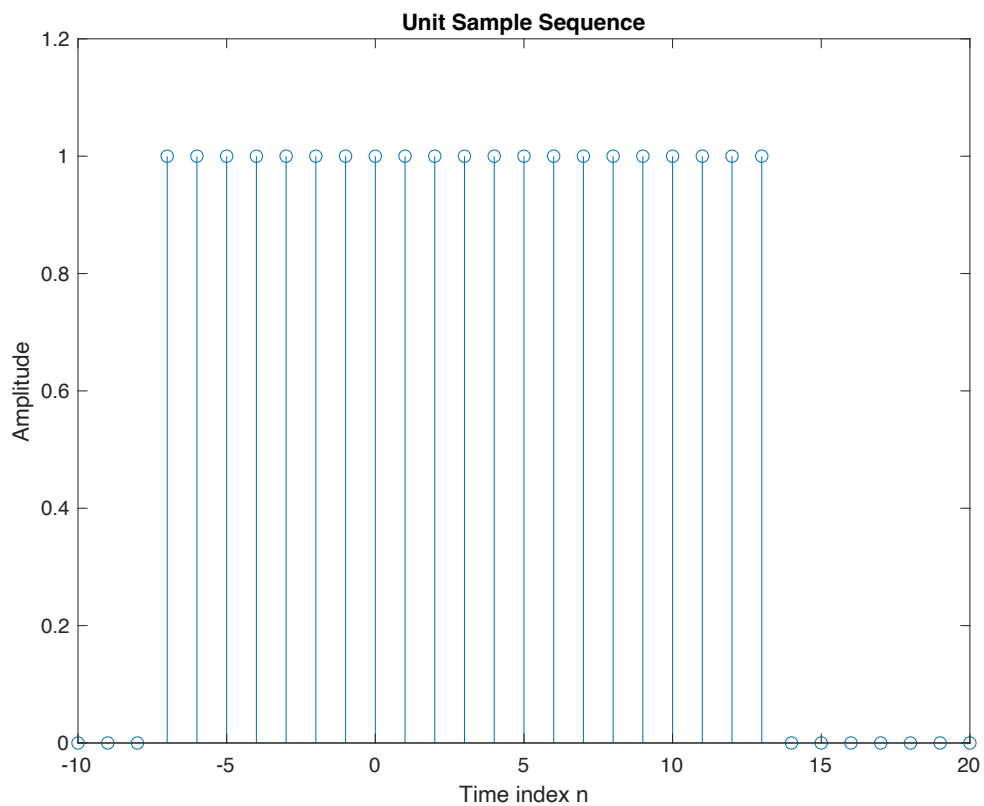
< Insert MATLAB figure(s) here. Copy from figure window(s) and paste. >

**Q1.5** The modified Program P1\_1 to generate a unit step sequence  $sd[n]$  with an advance of 7 samples is given below along with the sequence generated by running this program.

```

% Program P1_1
% Generation of a Unit Sample Sequence
clf;
% Generate a vector from -10 to 20
n = -10:20;
% Generate the unit sample sequence
u = [zeros(1,3) 1 ones(1,20) zeros(1,7)];
% Plot the unit sample sequence
stem(n,u);
xlabel('Time index n');ylabel('Amplitude');
title('Unit Sample Sequence');
axis([-10 20 0 1.2]);

```



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## Project 1.2 Exponential signals

A copy of Programs P1\_2 and P1\_3 are given below.

```

% Program P1_2
% Generation of a complex exponential sequence
clf;
c = -(1/12)+(pi/6)*i;

```

```

K = 2;
n = 0:40;
x = K*exp(c*n);
subplot(2,1,1);
stem(n,real(x));
xlabel('Time index n');ylabel('Amplitude');
title('Real part');
subplot(2,1,2);
stem(n,imag(x));
xlabel('Time index n');ylabel('Amplitude');
title('Imaginary part');

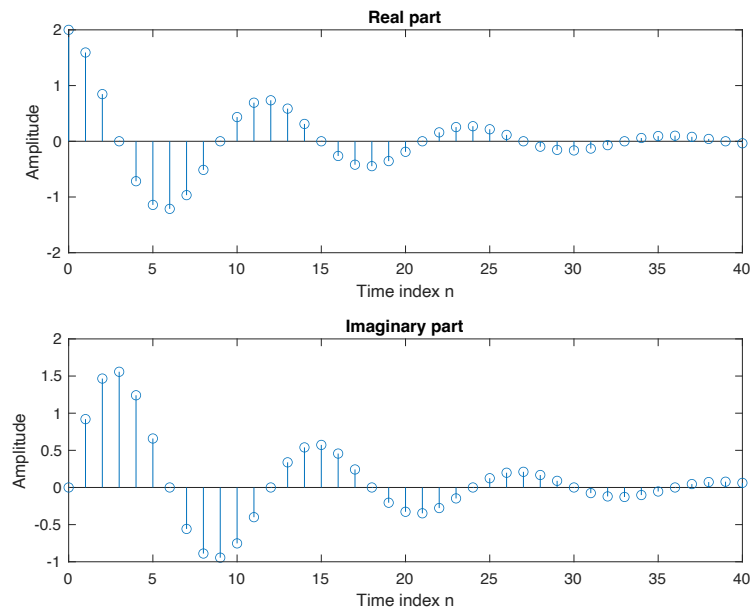
% Program P1_3
% Generation of a real exponential sequence
clf;
n = 0:35; a = 1.2; K = 0.2;
x = K*a.^n;
stem(n,x);
xlabel('Time index n');ylabel('Amplitude');

```

< Insert program code here. Copy from m-file(s) and paste. >

**Answers:**

**Q1.6** The complex-valued exponential sequence generated by running Program P1\_2 is shown below:

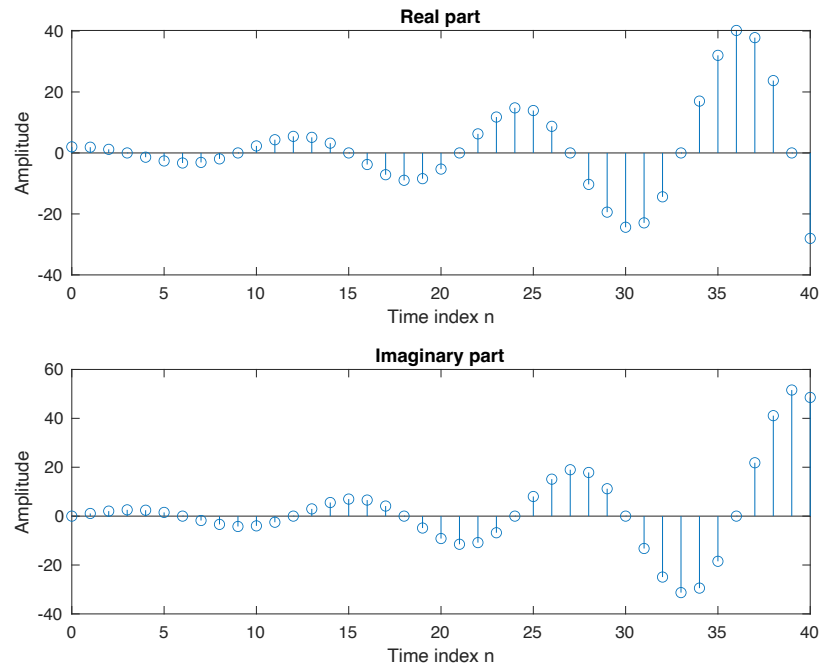


< Insert MATLAB figure(s) here. Copy from figure window(s) and paste. >

**Q1.7** The parameter controlling the rate of growth or decay of this sequence is -  $c$

The parameter controlling the amplitude of this sequence is -  $K$

**Q1.8** The result of changing the parameter  $c$  to  $(1/12) + (pi/6)*i$  is - disperse

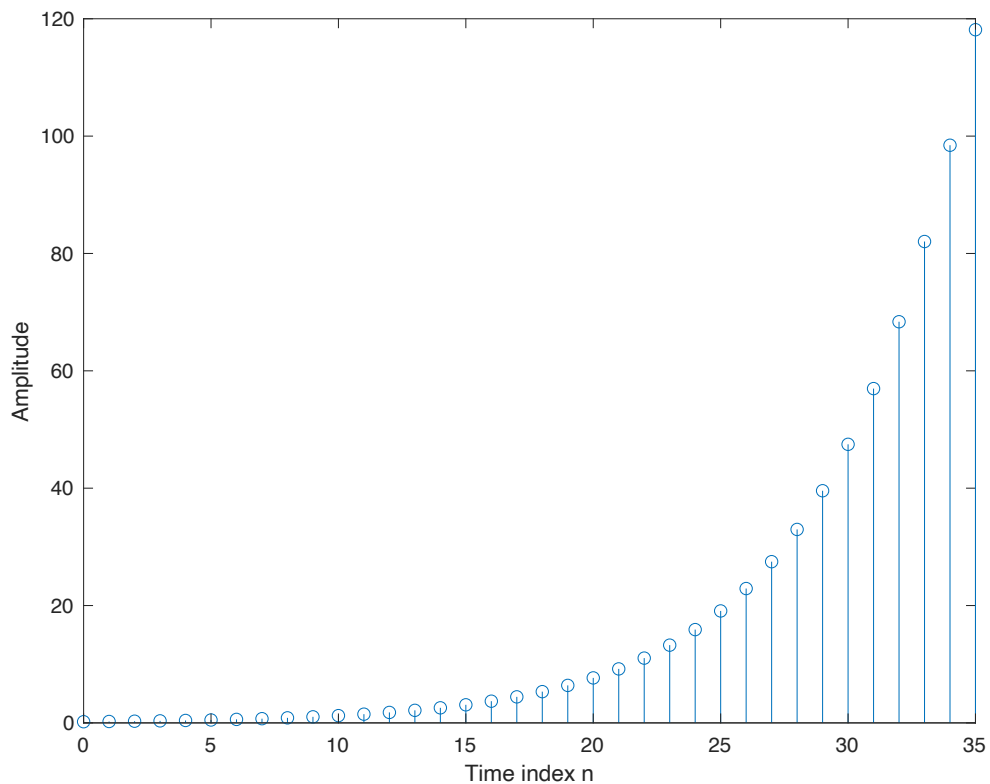


**Q1.9** The purpose of the operator `real` is - get real part of complex

The purpose of the operator `imag` is - get imaginary part of complex

**Q1.10** The purpose of the command `subplot` is - Create axes in tiled positions

**Q1.11** The real-valued exponential sequence generated by running Program P1\_3 is shown below:



< Insert MATLAB figure(s) here. Copy from figure window(s) and paste. >

**Q1.12** The parameter controlling the rate of growth or decay of this sequence is -a

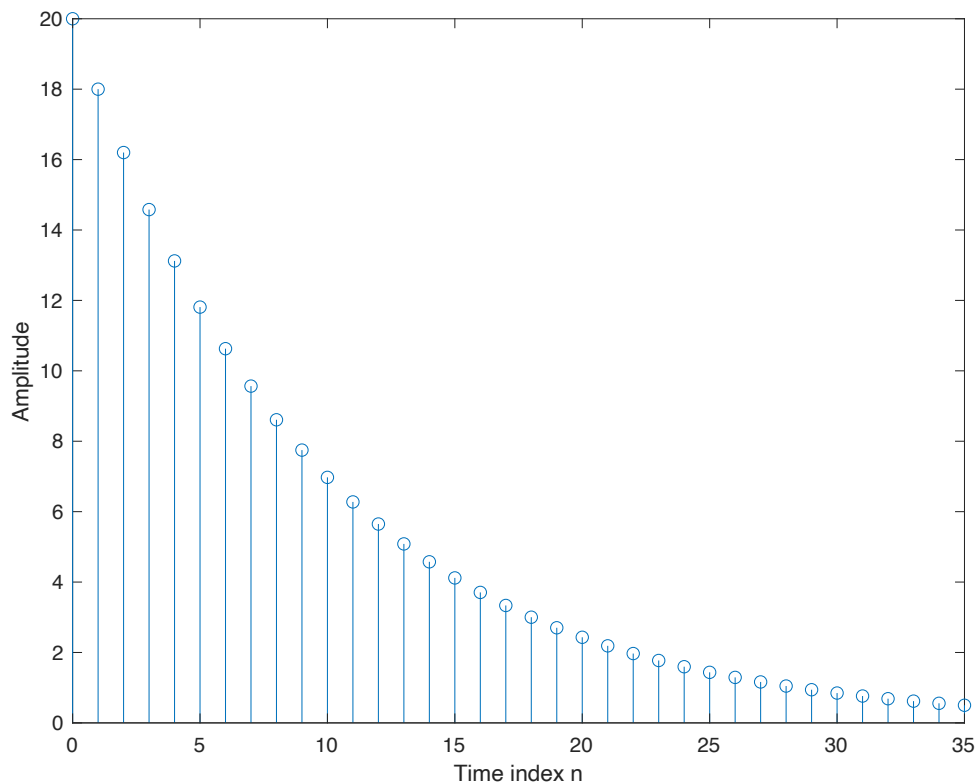
The parameter controlling the amplitude of this sequence is - k

**Q1.13** The difference between the arithmetic operators ^ and .^ is -

^ :  $X^y$  is X to the y power if y is a scalar and X is square

.^ denotes element-by-element powers

**Q1.14** The sequence generated by running Program P1\_3 with the parameter a changed to 0.9 and the parameter K changed to 20 is shown below:



< Insert MATLAB figure(s) here. Copy from figure window(s) and paste. >

**Q1.15** The length of this sequence is - 36

It is controlled by the following MATLAB command line: `n = 0:35;`

It can be changed to generate sequences with different lengths as follows (give an example command line and the corresponding length):

```
n = input("input sequence length");
```

```
m = 0:n-1;
```

length of m = n.

**Q1.16** The energies of the real-valued exponential sequences  $x[n]$  generated in Q1.11 and Q1.14 and computed using the command `sum` are -

Q1.11 energy = `sum(real(x).*real(x))` = 14.3373

Q1.14 energy = `sum(real(x).*real(x))` = 2.1042e+03



### Project 1.3 Sinusoidal sequences

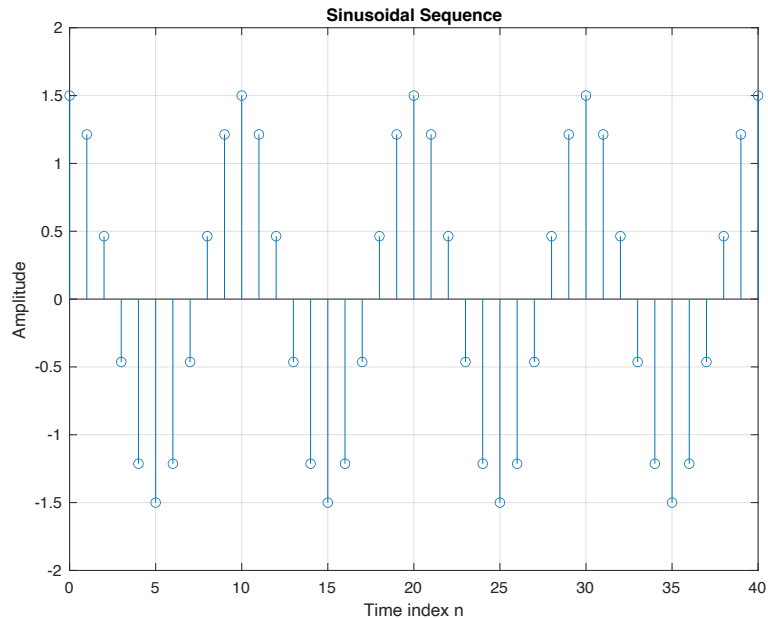
A copy of Program P1\_4 is given below.

```
% Program P1_4
% Generation of a sinusoidal sequence
n = 0:40;
f = 0.1;
phase = 0;
A = 1.5;
arg = 2*pi*f*n - phase;
x = A*cos(arg);
clf; % Clear old graph
stem(n,x); % Plot the generated sequence
axis([0 40 -2 2]);
grid;
title('Sinusoidal Sequence');
xlabel('Time index n');
ylabel('Amplitude');
axis;
```

< Insert program code here. Copy from m-file(s) and paste. >

Answers:

Q1.17 The sinusoidal sequence generated by running Program P1\_4 is displayed below.



< Insert MATLAB figure(s) here. Copy from figure window(s) and paste. >

**Q1.18** The frequency of this sequence is - 0.1

It is controlled by the following MATLAB command line:  $f = 0.1$ ;

A sequence with new frequency \_\_\_\_\_ can be generated by the following command line:  $f = \text{input}(\text{"input frequency"})$

The parameter controlling the phase of this sequence is -phase

The parameter controlling the amplitude of this sequence is -A

The period of this sequence is - 10

**Q1.19** The length of this sequence is - 41

It is controlled by the following MATLAB command line:  $n = 0:40$

A sequence with new length \_\_\_\_\_ can be generated by the following command line:  
 $\text{length} = \text{input}(\text{"input array length"});$   
 $n = 0:\text{length}-1;$

**Q1.20** The average power of the generated sinusoidal sequence is - 47.25

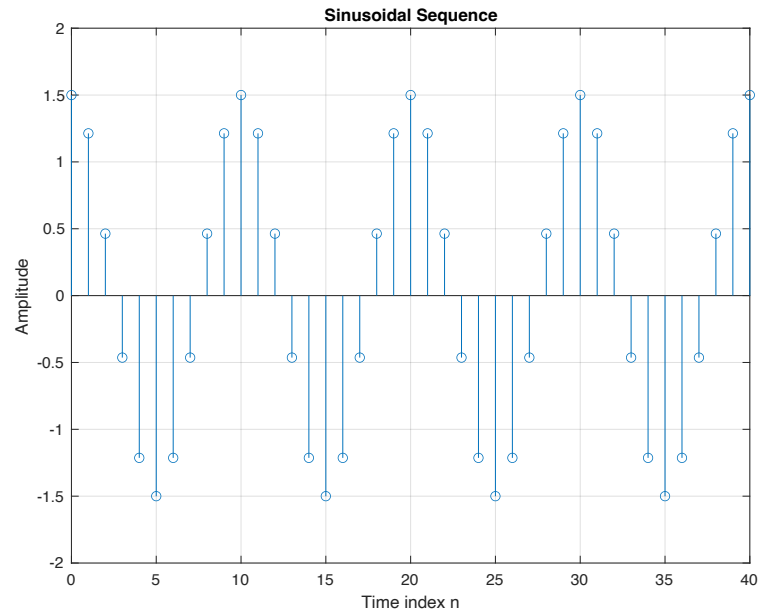
**Q1.21** The purpose of `axis` command is - Control axis scaling and appearance.

The purpose of `grid` command is - Grid lines.

**Q1.22** The modified Program P1\_4 to generate a sinusoidal sequence of frequency 0.9 is given below along with the sequence generated by running it.

```
% Program P1_4
% Generation of a sinusoidal sequence
n = 0:40;
%f = 0.1;
f = input("input frequency")
phase = 0;
A = 1.5;
arg = 2*pi*f*n - phase;
x = A*cos(arg);
clf; % Clear old graph
stem(n,x); % Plot the generated sequence
axis([0 40 -2 2]);
grid;
title('Sinusoidal Sequence');
xlabel('Time index n');
ylabel('Amplitude');
axis;
```

< Insert program code here. Copy from m-file(s) and paste. >

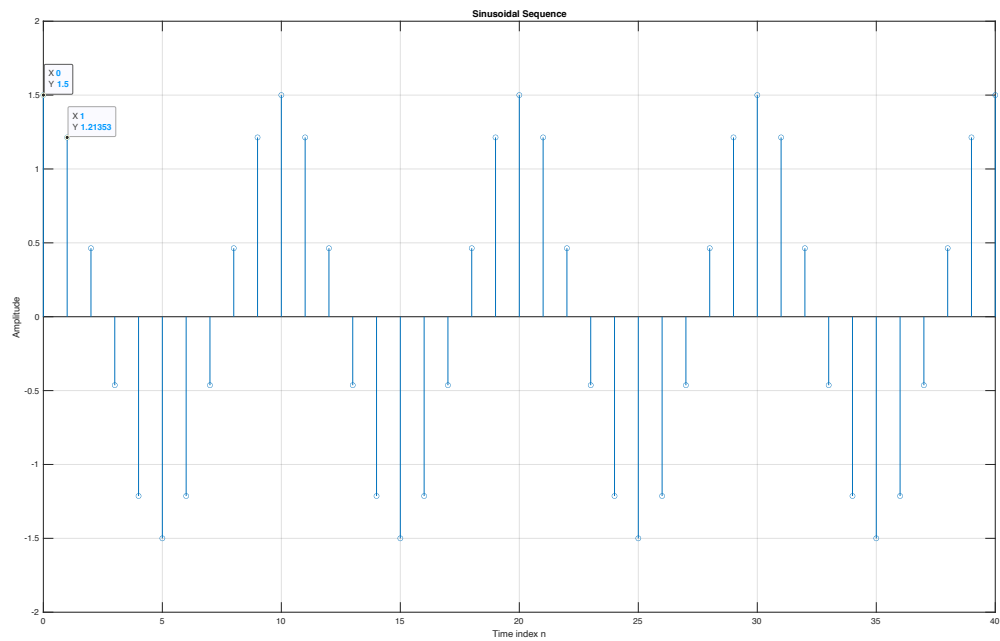


< Insert MATLAB figure(s) here. Copy from figure window(s) and paste. >

A comparison of this new sequence with the one generated in Question Q1.17 shows -

頻率不同，週期相同，x 值不同。

A sinusoidal sequence of frequency 1.1 generated by modifying Program P1\_4 is shown below.

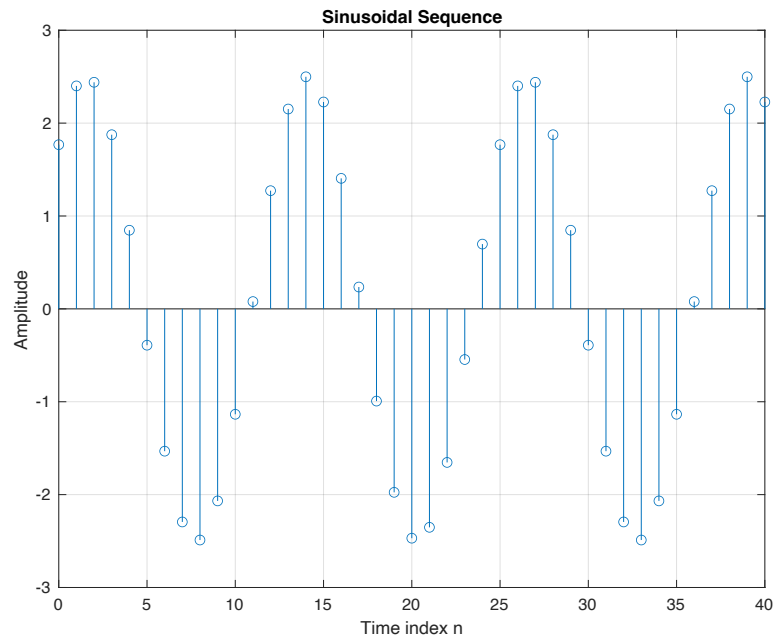


< Insert MATLAB figure(s) here. Copy from figure window(s) and paste. >

A comparison of this new sequence with the one generated in Question Q1.17 shows -

頻率不同，週期相同，x 值不同

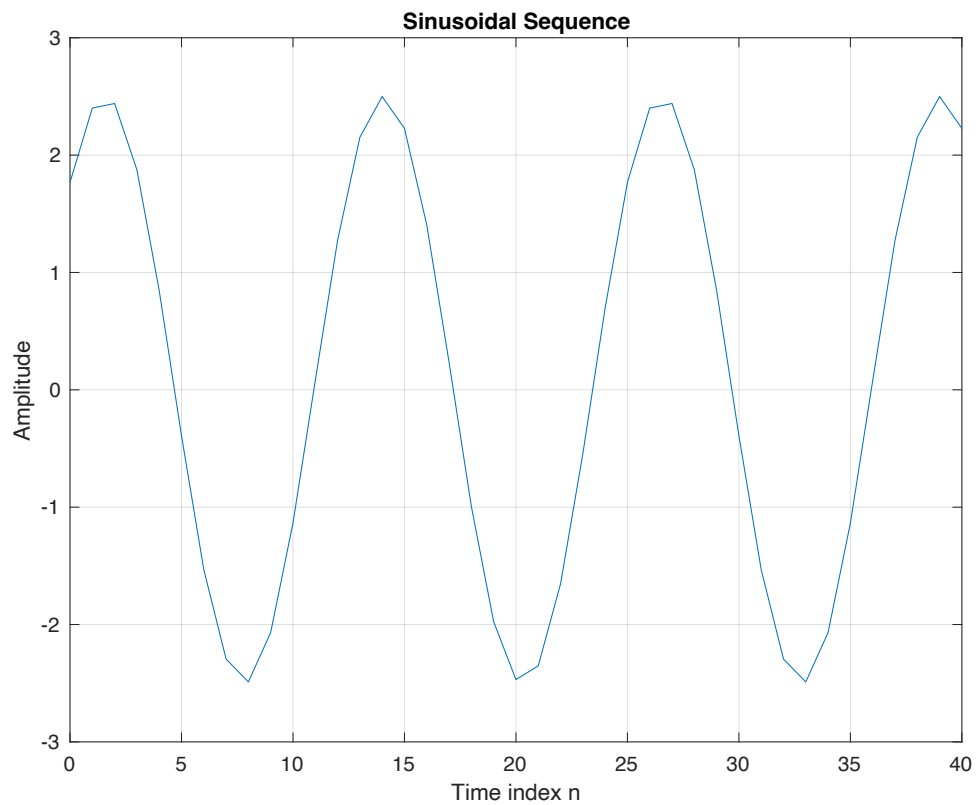
**Q1.23** The sinusoidal sequence of length 50, frequency 0.08, amplitude 2.5, and phase shift of 90 degrees generated by modifying Program P1\_4 is displayed below.



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The period of this sequence is - 25

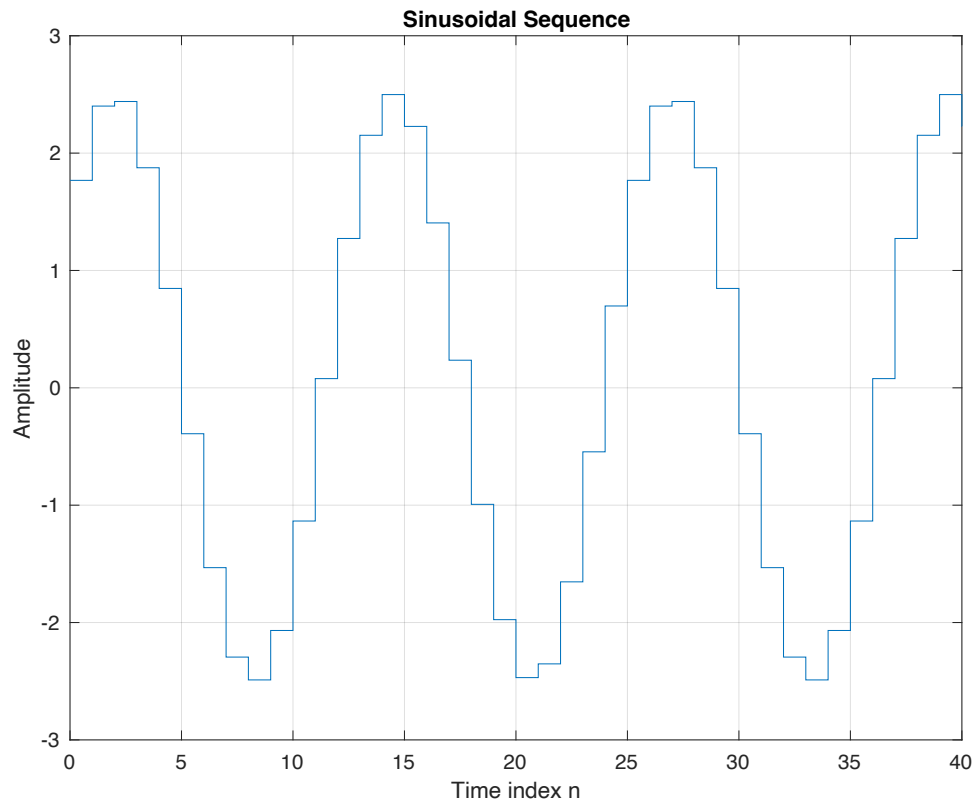
**Q1.24** By replacing the `stem` command in Program P1\_4 with the `plot` command, the plot obtained is as shown below:



< Insert MATLAB figure(s) here. Copy from figure window(s) and paste. >

The difference between the new plot and the one generated in Question Q1.17 is -

**Q1.25** By replacing the `stem` command in Program P1\_4 with the `stairs` command the plot obtained is as shown below;



< Insert MATLAB figure(s) here. Copy from figure window(s) and paste. >

The difference between the new plot and those generated in Questions Q1.17 and Q1.24 is – Plot displays figure by continuous line. Stem display figure by discrete impulse.

#### Project 1.4 Random signal

##### Answers:

**Q1.26** The MATLAB program to generate and display a random signal of length 100 with elements uniformly distributed in the interval  $[-2, 2]$  is given below along with the plot of the random sequence generated by running the program:

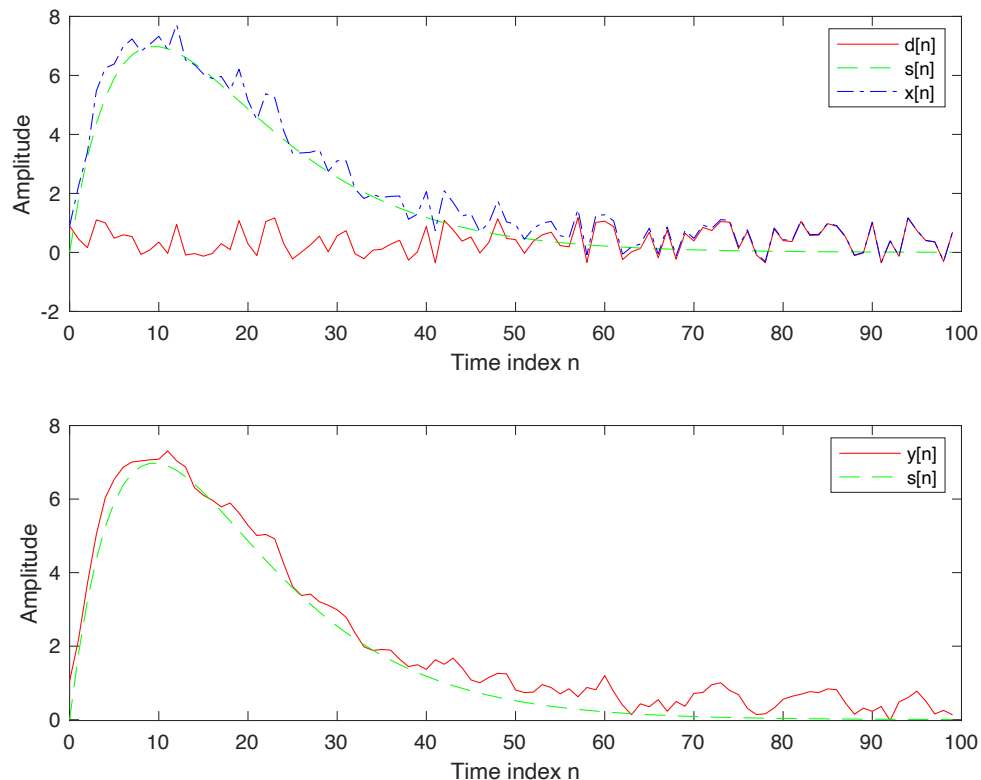
```
% Program P1_5
% Signal Smoothing by Averaging
clear;
clf;
R = 100;
r = 2*rand(R,1);
d = 0.8*(r - 0.5); % Generate random noise
m = 0:R-1;
s = 2*m.*(0.9.^m); % Generate uncorrupted signal
x = s + d'; % Generate noise corrupted signal
subplot(2,1,1);
plot(m,d','r-',m,s,'g--',m,x,'b-.');
```

```

xlabel('Time index n');ylabel('Amplitude');
legend('d[n] ','s[n] ','x[n] ');
x1 = [0 0 x];x2 = [0 x 0];x3 = [x 0 0];
y = (x1 + x2 + x3)/3;
subplot(2,1,2);
plot(m,y(2:R+1),'r-',m,s,'g--');
legend('y[n] ','s[n] ');
xlabel('Time index n');ylabel('Amplitude');

```

< Insert program code here. Copy from m-file(s) and paste. >



< Insert MATLAB figure(s) here. Copy from figure window(s) and paste. >

**Q1.27** The MATLAB program to generate and display a Gaussian random signal of length 75 with elements normally distributed with zero mean and a variance of 3 is given below along with the plot of the random sequence generated by running the program:

```

% Program P1_5
% Signal Smoothing by Averaging
clear;
clf;
R = 75;
r = 2*normrnd(0,sqrt(3),[R,1]);
d = 0.8*(r - 0.5); % Generate random noise
m = 0:R-1;
s = 2*m.*(0.9.^m); % Generate uncorrupted signal
x = s + d'; % Generate noise corrupted signal

```

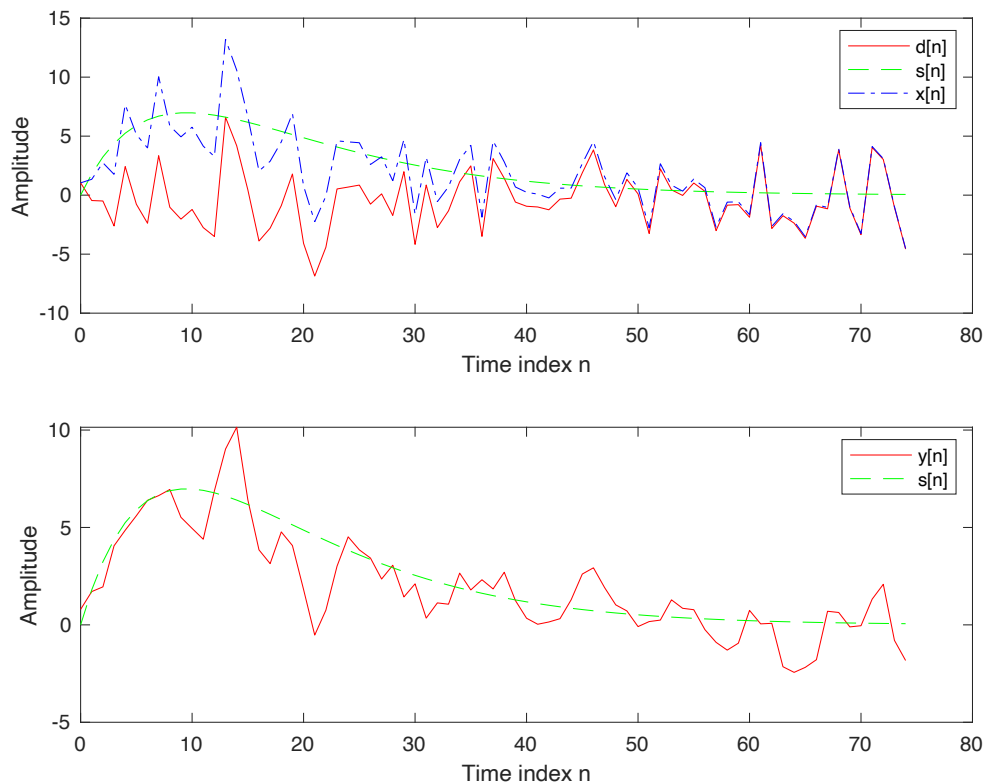


```

subplot(2,1,1);
plot(m,d','r-',m,s,'g--',m,x,'b-.');
xlabel('Time index n');ylabel('Amplitude');
legend('d[n] ','s[n] ','x[n] ');
x1 = [0 0 x];x2 = [0 x 0];x3 = [x 0 0];
y = (x1 + x2 + x3)/3;
subplot(2,1,2);
plot(m,y(2:R+1),'r-',m,s,'g--');
legend('y[n] ','s[n] ');
xlabel('Time index n');ylabel('Amplitude');

```

< Insert program code here. Copy from m-file(s) and paste. >



< Insert MATLAB figure(s) here. Copy from figure window(s) and paste. >

**Q1.28** The MATLAB program to generate and display five sample sequences of a random sinusoidal signal of length 31

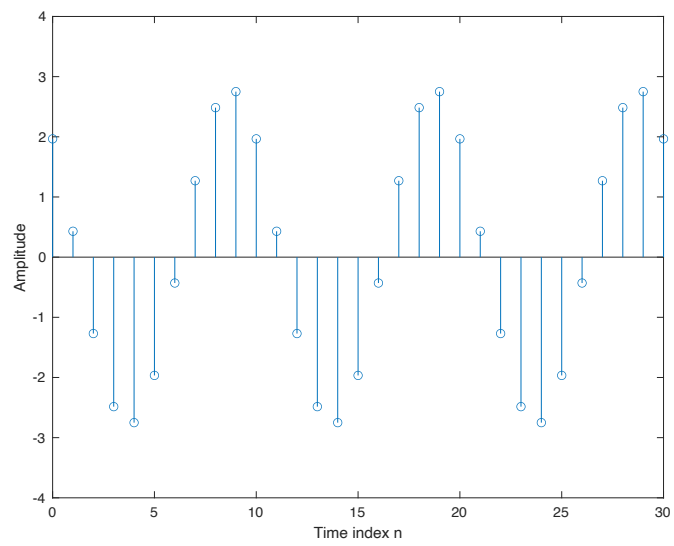
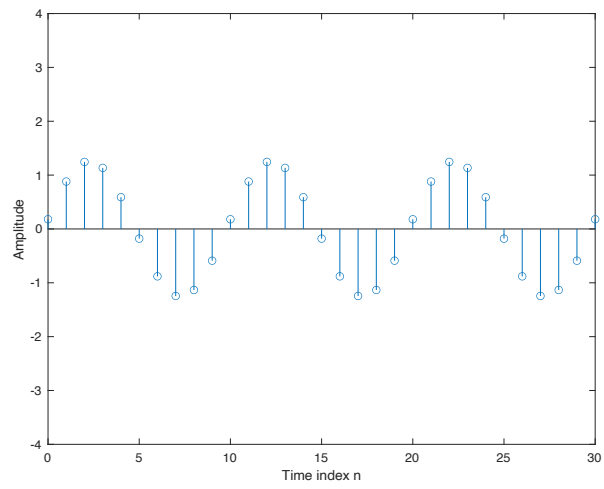
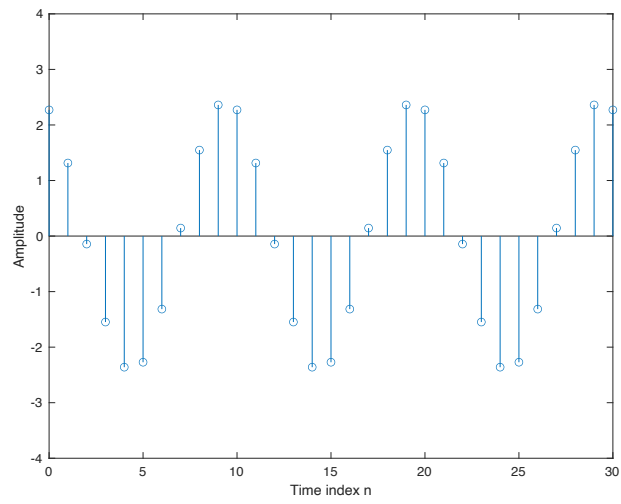
$$\{X[n]\} = \{A \cos(\omega_0 n + \phi)\}$$

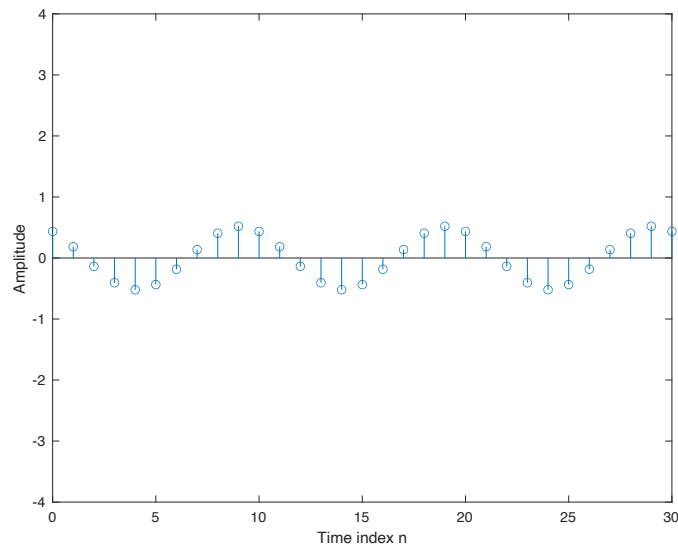
where the amplitude  $A$  and the phase  $\phi$  are statistically independent random variables with uniform probability distribution in the range  $0 \leq A \leq 4$  for the amplitude and in

```
clear; clc;
n = 0:30;
%Amplitude
a = 0;
b = 4;
A = a + (b-a).*rand(1);
%phase
a = 0;
b = 2*pi;
fi = a + (b-a).*rand(1);
%frequency
f = 0.1;

X = A*(cos(2*pi*f*n+fi));
%plot
stem(n,X);
axis([0,30,-4,4]);
xlabel('Time index n'); ylabel('Amplitude');
```

A stem plot of a discrete-time signal  $x[n]$  over the range  $n=0$  to  $30$ . The signal is periodic with a period of 10 samples. The amplitude values are 0, 1, and -1. The signal is zero for  $n=0, 4, 8, 12, 16, 20, 24, 28$ . It has a value of 1 for  $n=1, 5, 9, 13, 17, 21, 25, 29$  and a value of -1 for  $n=2, 6, 10, 14, 18, 22, 26, 30$ .





< Insert MATLAB figure(s) here. Copy from figure window(s) and paste. >

## 1.2 SIMPLE OPERATIONS ON SEQUENCES

### Project 1.5 Signal Smoothing

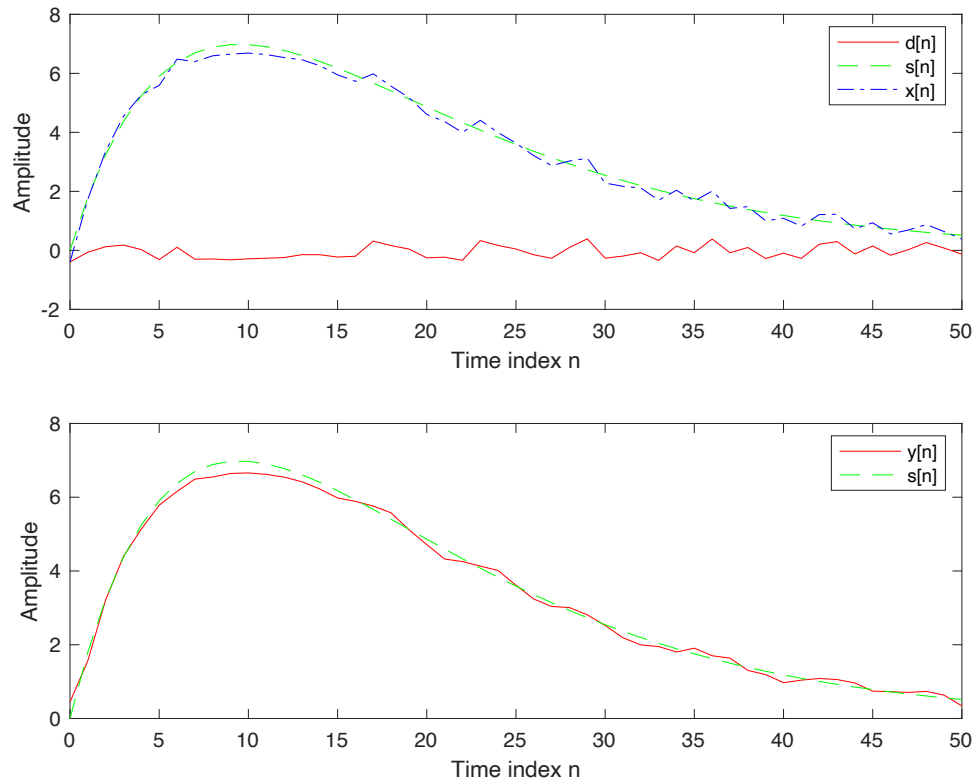
A copy of Program P1\_5 is given below.

```
% Program P1_5
% Signal Smoothing by Averaging
clear;
clf;
R = 51;
d = 0.8*(rand(R,1) - 0.5); % Generate random noise
m = 0:R-1;
s = 2*m.*(0.9.^m); % Generate uncorrupted signal
x = s + d'; % Generate noise corrupted signal
subplot(2,1,1);
plot(m,d','r-',m,s,'g--',m,x,'b-.');
xlabel('Time index n');ylabel('Amplitude');
legend('d[n] ','s[n] ','x[n] ');
x1 = [0 0 x];x2 = [0 x 0];x3 = [x 0 0];
y = (x1 + x2 + x3)/3;
subplot(2,1,2);
plot(m,y(2:R+1),'r-',m,s,'g--');
legend('y[n] ','s[n] ');
xlabel('Time index n');ylabel('Amplitude');
```

< Insert program code here. Copy from m-file(s) and paste. >

Answers:

**Q1.29** The signals generated by running Program P1\_5 are displayed below:



< Insert MATLAB figure(s) here. Copy from figure window(s) and paste. >

**Q1.30** The uncorrupted signal  $s[n]$  is -  $2 * m . * (0.9 . ^m)$  which is green line  
 The additive noise  $d[n]$  is -  $0.8 * (rand(R,1) - 0.5)$  which is red line

**Q1.31** The statement  $x = s + d$  CAN / CANNOT be used to generate the noise corrupted signal because - It can be used to generate the noise corrupted signal by additive noise.

**Q1.32** The relations between the signals  $x_1$ ,  $x_2$ , and  $x_3$ , and the signal  $x$  are -

$x$  adds two zero-sample to be  $x_1 \setminus x_2 \setminus x_3$ , if  $x_2$  is current signal,  $x_1$  would be delay 1 sample, and  $x_3$  would be advance 1 sample.

**Q1.33** The purpose of the legend command is - 在座標上添加圖例。