How in tarnation do we show that the eigenvalues are

$$\alpha \pm |\boldsymbol{\beta}|$$
?