

# Which rate are you on?

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# What is a "rate"



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## Rate

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(Redirected from [Rates](#))

**Rate** may refer to:

### Science and finance [[edit](#)]

- [Rate function](#), a function used to quantify the probabilities of a rare event
- [Rates \(tax\)](#), a type of taxation system used to fund local government
- [Reaction rate](#) in Chemistry
- [Exchange rate](#), specifies how much one currency is worth in terms of the other

### Human growth [[edit](#)]

- [Birth rate](#), the natality or childbirths per 1,000 people per year
- [Mortality rate](#), a measure of the number of deaths in some population

### Other uses [[edit](#)]

- [Rate \(mathematics\)](#), a specific kind of ratio, in which two measurements are related to each other (often with respect to time)
  - Rate of travel, or [velocity](#)
  - [Bit rate](#), number of bits that are conveyed or processed per unit of time
- [Naval rating](#) or rate, terms used to designate specialty or seniority of enlisted naval personnel
- [Rate of a ship](#), a term indicating a sail ship's firepower in the British Royal Navy
- [Rates \(Portuguese parish\)](#), a Portuguese parish and town located in the municipality of Póvoa de Varzim
- [RATE project](#), a young earth creationism research project

# Rates commonly occurring in BEAST

- Substitution model rates
  - ▶ CTMC
  - ▶ Covarion
  - ▶ Stochastic dollo
- Gamma rate heterogeneity
  - ▶ with
  - ▶ without
- Relative substitution rates
  - ▶ fixed to 1
  - ▶ estimated
- Clock rates
  - ▶ Strict
  - ▶ Relaxed
  - ▶ Random local

Which one to choose? Which combinations make sense?

# Database of cognates

## word list

| language  | hand | mother | father | ... |
|-----------|------|--------|--------|-----|
| English   | hand | mother | father | ... |
| Dutch     | hand | moeder | vader  | ... |
| German    | hand | mutter | vater  | ... |
| French    | main | mère   | père   | ... |
| Spanish   | mano | madre  | padre  | ... |
| Dhudhuroa | ?    | papa   | mama   | ... |

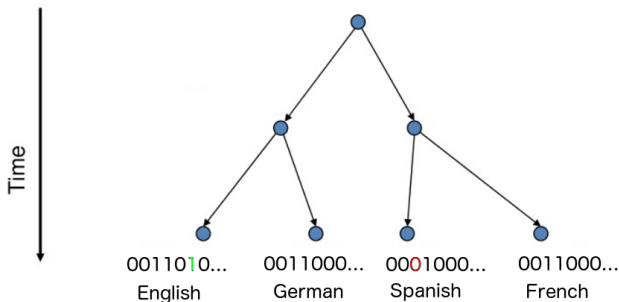
## cognate list

| language  | ascertainment | hand | mano | mother | papa | father | mama | ... |
|-----------|---------------|------|------|--------|------|--------|------|-----|
| English   | 0             | 1    | 0    | 1      | 0    | 1      | 0    | ... |
| Dutch     | 0             | 1    | 0    | 1      | 0    | 1      | 0    | ... |
| German    | 0             | 1    | 0    | 1      | 0    | 1      | 0    | ... |
| French    | 0             | 0    | 1    | 1      | 0    | 1      | 0    | ... |
| Spanish   | 0             | 0    | 1    | 1      | 0    | 1      | 0    | ... |
| Dhudhuroa | 0             | ?    | ?    | 0      | 1    | 0      | 1    | ... |

Sites: columns in the table

# Tree-likelihood

We want to calculate  $P(data|tree, rates)$

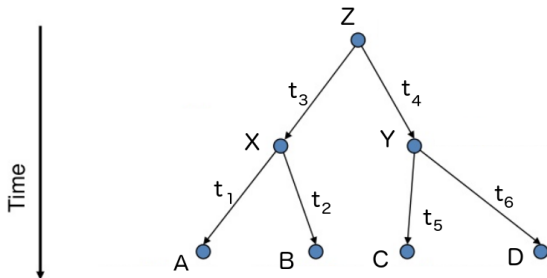


Assume sites are independent:

$$P(data|tree, rates) = \prod_{i \in \text{sites}} P(site_i|tree, rates)$$

# Substitution model

$P(\text{site}_i | \text{tree}, \text{rates}) = P(A|X, t_1, \theta)P(B|X, t_2, \theta)P(X|Z, t_3, \theta)P(C|Y, t_5, \theta)P(D|Y, t_6, \theta)P(Y|Z, t_4, \theta)P(Z)$   
= product over all branches  $\times$  root distribution.



$\theta$  the substitution model rates

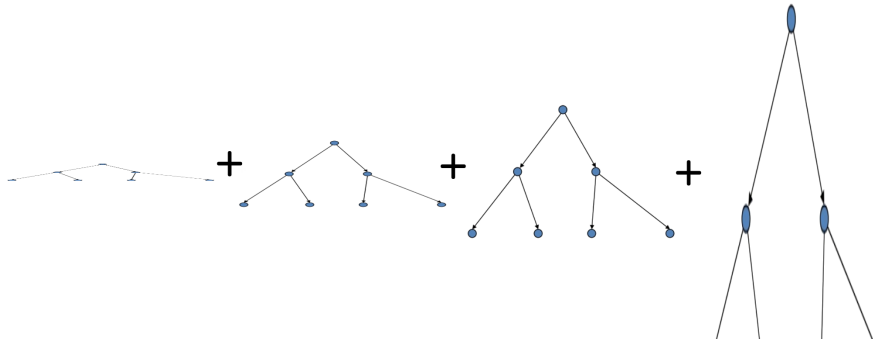
# Gamma rate heterogeneity

# Gamma rate heterogeneity



# Gamma rate heterogeneity

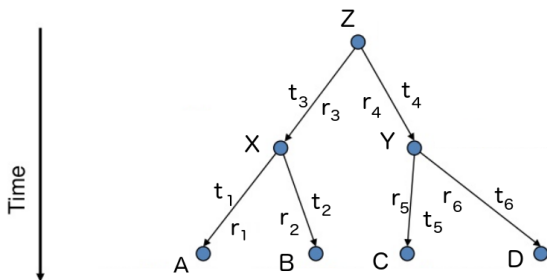
Mixture of tree likelihoods, trees scaled by gamma category rate



# Clock rates

Associate a rate  $r_j$  with each branch

Use  $r_i \times t_i$  instead of  $t_i$  for  $P(\text{site}_i | \text{tree}, \text{rates})$ .



- Strict clock: all rates equal
- Uncorrelated relaxed clock: all rates independent, drawn from common distribution
- Random local clock: some rates same as parent branch rates

# Summary so far

- Tree likelihood is product of likelihoods over sites
- Likelihood over sites is product of  $P(A|B, t, \theta)$  over branches
- Substitution model rates determine  $P(A|B, t, \theta)$
- Gamma rate heterogeneity: rate variation across sites
- Clock models: rate variation across branches

What about substitution rates?

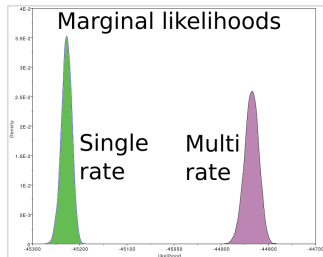
# Change et al's model

## word list

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| German    | 0             | 1    | 0    | 1      | 0    | 1      | 0    | ... |
| French    | 0             | 0    | 1    | 1      | 0    | 1      | 0    | ... |
| Spanish   | 0             | 0    | 1    | 1      | 0    | 1      | 0    | ... |
| Dhudhuroa | 0             | ?    | ?    | 0      | 1    | 0      | 1    | ... |

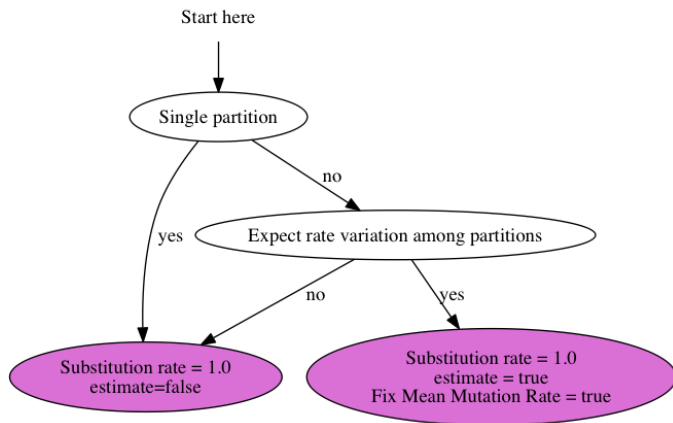


## cognate list

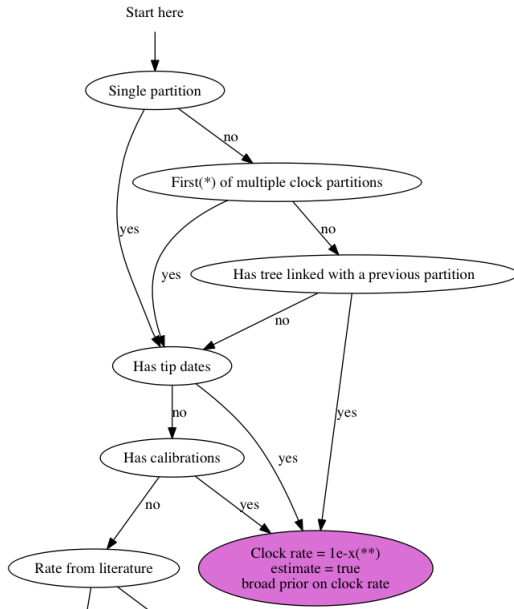
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| German    | 0             | 1    | 0    | 0             | 1      | 0    | 0             | 1      | 0    | ... |
| French    | 0             | 0    | 1    | 0             | 1      | 0    | 0             | 1      | 0    | ... |
| Spanish   | 0             | 0    | 1    | 0             | 1      | 0    | 0             | 1      | 0    | ... |
| Dhudhuroa | ?             | ?    | ?    | 0             | 0      | 1    | 0             | 0      | 1    | ... |

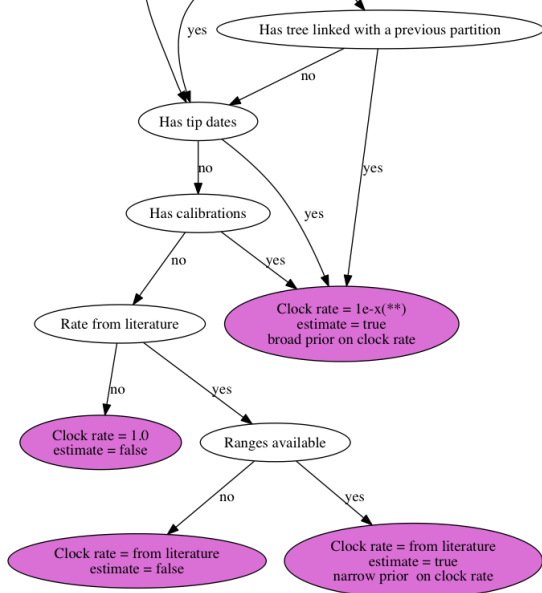
+ 1 relative rate for every meaning class = 207-1 extra parameters

# Setting up substitution rates



# Setting up clock rates





\*\* choose appropriate starting value

# Summary

- Tree likelihood is product of likelihoods over sites
- Likelihood over sites is product of  $P(A|B, t, \theta)$  over branches
- Substitution model rates determine  $P(A|B, t, \theta)$
- Gamma rate heterogeneity: rate variation across sites
- Clock models: rate variation across branches
- Substitution rates: rate variation across partitions