

## Tutorial 1 Solutions

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### Problem 3

Suppose that  $x = 5$  and  $y = 2$ . Use MATLAB to compute the following, and check the results with a calculator.

a.  $(1 - \frac{1}{x^5})^{-1}$

b.  $3\pi x^2$

c.  $\frac{3y}{4x-8}$

d.  $\frac{4(y-5)}{3x-6}$

```
1 clear; clc;
2 x = 5;
3 y = 2;
4
5 % a. (1 - 1/x^5)^-1
6 result_a = (1 - 1/x^5)^-1;
7
8 % b. 3 * pi * x^2
9 result_b = 3 * pi * x^2;
10
11 % c. (3*y) / (4*x - 8)
12 result_c = (3*y) / (4*x - 8);
13
14 % d. (4*(y - 5)) / (3*x - 6)
15 result_d = (4*(y - 5)) / (3*x - 6);
16
17 % Display results
18 disp(table(result_a, result_b, result_c, result_d));
```

## Problem 5

Assuming that the variables  $a$ ,  $b$ ,  $c$ ,  $d$ , and  $f$  are scalars, write MATLAB statements to compute and display the following expressions. Test your statements for the values  $a = 1.12$ ,  $b = 2.34$ ,  $c = 0.72$ ,  $d = 0.81$  and  $f = 19.83$ .

- $x = 1 + \frac{a}{b} + \frac{c}{f^2}$

- $r = \frac{1}{\frac{1}{a} + \frac{1}{b} + \frac{1}{c} + \frac{1}{d}}$

- $s = \frac{b-a}{d-c}$

- $y = ab\frac{1}{c}\frac{f^2}{2}$

```
1 clear; clc;
2 a = 1.12;
3 b = 2.34;
4 c = 0.72;
5 d = 0.81;
6 f = 19.83;
7
8 % x = 1 + a/b + c/f^2
9 x = 1 + a/b + c/f^2;
10
11 % r = 1 / (1/a + 1/b + 1/c + 1/d)
12 r = 1 / (1/a + 1/b + 1/c + 1/d);
13
14 % s = (b - a) / (d - c)
15 s = (b - a) / (d - c);
16
17 % y = ab * (1/c) * (f^2/2)
18 y = a * b * (1/c) * (f^2/2);
19
20 disp(['x = ', num2str(x)]);
21 disp(['r = ', num2str(r)]);
22 disp(['s = ', num2str(s)]);
23 disp(['y = ', num2str(y)]);
```

## Problem 9

The functions `realmax` and `realmin` give the largest and smallest possible numbers that can be handled by MATLAB. Calculations generating numbers that are too large or too small result in overflow and underflow. Usually this does not present a problem if you arrange the calculation sequence properly. Type `realmax` and `realmin` in MATLAB to determine the upper and lower limits for your system.

For example, suppose you have the variables  $a = 3 \times 10^{150}$ ,  $b = 5 \times 10^{200}$ .

- Use MATLAB to calculate  $c = ab$ .
- Supposed  $d = 5 \times 10^{-200}$  use MATLAB to calculate  $f = d/a$ .
- Use MATLAB to calculate the product  $x = abd$  two ways, i) by calculating the product directly as  $x = a*b*d$  and then ii) by splitting up the calculation as  $y = b*d$  and then  $x = a*y$  Compare the results.

```
1 % Check limits
2 realmax
3 realmin
4
5 a = 3e150;
6 b = 5e200;
7
8 % a. Calculate c = a*b
9 % This will likely result in Inf (Overflow) because 10^150 * 10^200 = 10^350
10 c = a * b
11
12 % b. d = 5e-200, calculate f = d/a
13 % This will likely result in 0 (Underflow) or very small number
14 d = 5e-200;
15 f = d / a
16
17 % c. Calculate x = abd in two ways
18 x1 = a * b * d; % May fail due to intermediate overflow of (a*b)
19 y = b * d;      % Pre-calculating smaller product
20 x2 = a * y;     % Safer calculation
21
22 disp(['Method 1: ', num2str(x1)]);
23 disp(['Method 2: ', num2str(x2)]);
```

## Problem 22

Use MATLAB to calculate:

- $e^{(-2.1)^3} + 3.47 \log(14) + \sqrt[4]{287}$
- $(3.4)^7 \log(14) + \sqrt[4]{287}$
- $\cos^2\left(\frac{4.12\pi}{6}\right)$
- $\cos\left(\frac{4.12\pi}{6}\right)^2$

Check your answers with a calculator.

```

1 % a.  $e^{(-2.1)^3} + 3.47\log(14) + 287^{(1/4)}$ 
2 % Assuming log is log10 based on standard notation,
3 % though MATLAB log() is natural.
4 ans_a = exp((-2.1)^3) + 3.47 * log10(14) + nthroot(287, 4);
5
6 % b.  $(3.4)^7 * \log(14) + 287^{(1/4)}$ 
7 ans_b = (3.4)^7 * log10(14) + nthroot(287, 4);
8
9 % c.  $\cos^2(4.12\pi / 6)$ 
10 ans_c = cos((4.12 * pi) / 6)^2;
11
12 % d.  $\cos((4.12\pi / 6)^2)$ 
13 ans_d = cos(((4.12 * pi) / 6)^2);

```

## Problem 27

Use MATLAB to plot the function  $T = 7\ln t - 8e^{0.3t}$  over the interval  $1 \leq t \leq 3$ . Put a title on the plot and properly label the axes. The variable represents temperature in degrees Celsius: the variable t represents time in minutes.

```

1 t = 1:0.01:3; % Define interval
2
3 % Function definition (interpreted 'Int' from source as natural log 'ln')
4 T = 7 .* log(t) - 8 .* exp(0.3 .* t);
5
6 plot(t, T);
7 title('Temperature vs Time');
8 xlabel('Time (min)');
9 ylabel('Temperature (C)');
10 grid on;

```

## Problem 30

A cycloid is the curve described by a point P on the circumference of a circular wheel of radius r rolling along the x axis. The curve is described in parametric form by the equations:

- $x = r(\phi - \sin \phi)$
- $y = r(1 - \cos \phi)$

Use these equations to plot the cycloid for  $r = 10$  in. and  $0 \leq \phi \leq 4\pi$ .

```
1 r = 10;
2 phi = 0 : 0.01 : 4*pi; % Interval 0 to 4pi
3
4 % Parametric equations
5 x = r .* (phi - sin(phi));
6 y = r .* (1 - cos(phi));
7
8 plot(x, y);
9 title('Cycloid Plot (r=10)');
10 xlabel('x');
11 ylabel('y');
12 axis equal; % Ensures the curve looks correct proportionally
```

## Problem 34

The four-sided figure shown in Figure P34 consists of two triangles having a common side  $a$ . The law of cosines for the top triangle states that  $a^2 = b_1^2 + c_1^2 - 2b_1c_1 \cos A_1$  and a similar equation can be written for the bottom triangle. Develop a procedure for computing the length of side  $c_2$  if you are given the lengths of sides  $b_1$ ,  $b_2$  and  $c_1$  and the angles  $A_1$  and  $A_2$  in degrees. Write a script file to implement this procedure.

Test your script, using the following values:  $b_1 = 200$  m,  $b_2 = 1801$  m,  $c_1 = 1201$  m,  $A_1 = 120^\circ$  and  $A_2 = 100^\circ$ .

```
1 % Inputs (using values from source text)
2 b1 = 200; % meters
3 b2 = 1801; % meters (Likely OCR error for 180, but using source value)
4 c1 = 1201; % meters (Likely OCR error for 120, but using source value)
5 A1_deg = 120; % degrees
6 A2_deg = 100; % degrees
7
8 % Convert angles to radians
9 A1 = deg2rad(A1_deg);
10 A2 = deg2rad(A2_deg);
11
12 % 1. Find common side 'a' using Top Triangle (Law of Cosines)
13 % a^2 = b1^2 + c1^2 - 2*b1*c1*cos(A1)
14 a_sq = b1^2 + c1^2 - 2*b1*c1*cos(A1);
15 a = sqrt(a_sq);
16
17 % 2. Find c2 using Bottom Triangle
18 % a^2 = b2^2 + c2^2 - 2*b2*c2*cos(A2)
19 % Rearranging for c2: c2^2 - (2*b2*cos(A2))*c2 + (b2^2 - a^2) = 0
```

```

20 % This is a quadratic equation: Ax^2 + Bx + C = 0
21
22 coeff_A = 1;
23 coeff_B = -2 * b2 * cos(A2);
24 coeff_C = b2^2 - a_sq;
25
26 % Calculate roots for side c2
27 possible_c2 = roots([coeff_A, coeff_B, coeff_C]);
28
29 % Filter for positive real lengths
30 c2 = possible_c2(possible_c2 > 0);
31
32 disp(['Common side a: ', num2str(a)]);
33 disp(['Side c2: ', num2str(c2)]);

```

## Problem 35

Write a script file to compute the three roots of the cubic equation  $x^3 + ax^2 + bx + c = 0$ . Use the input function to let the user enter values for a, b, and c.

```

1 disp('Solving x^3 + ax^2 + bx + c = 0');
2
3 % Input from user
4 a = input('Enter value for a: ');
5 b = input('Enter value for b: ');
6 c = input('Enter value for c: ');
7
8 % Coefficient vector for [1, a, b, c]
9 coefficients = [1, a, b, c];
10
11 % Compute roots
12 solution_roots = roots(coefficients);
13
14 disp('The roots of the equation are:');
15 disp(solution_roots);

```