

## Course Notes

**February 11, 2026**

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# Tutorial 1: An Overview of MATLAB

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## Problem 3

Suppose that  $x = 5$  and  $y = 2$ . Use MATLAB to compute the following, and check the results with a calculator.

a.  $(1 - \frac{1}{x^5})^{-1}$

b.  $3\pi x^2$

c.  $\frac{3y}{4x-8}$

d.  $\frac{4(y-5)}{3x-6}$

```
1 clear; clc;
2 x = 5;
3 y = 2;
4
5 % a. (1 - 1/x^5)^-1
6 result_a = (1 - 1/x^5)^-1;
7
8 % b. 3 * pi * x^2
9 result_b = 3 * pi * x^2;
10
11 % c. (3*y) / (4*x - 8)
12 result_c = (3*y) / (4*x - 8);
13
14 % d. (4*(y - 5)) / (3*x - 6)
15 result_d = (4*(y - 5)) / (3*x - 6);
16
17 % Display results
18 disp(table(result_a, result_b, result_c, result_d));
```

## Problem 5

Assuming that the variables  $a$ ,  $b$ ,  $c$ ,  $d$ , and  $f$  are scalars, write MATLAB statements to compute and display the following expressions. Test your statements for the values  $a = 1.12$ ,  $b = 2.34$ ,  $c = 0.72$ ,  $d = 0.81$  and  $f = 19.83$ .

$$\bullet \quad x = 1 + \frac{a}{b} + \frac{c}{f^2}$$

$$\bullet \quad r = \frac{1}{\frac{1}{a} + \frac{1}{b} + \frac{1}{c} + \frac{1}{d}}$$

$$\bullet \quad s = \frac{b-a}{d-c}$$

$$\bullet \quad y = ab\frac{1}{c}\frac{f^2}{2}$$

```
1 clear; clc;
2 a = 1.12; b = 2.34; c = 0.72; d = 0.81; f = 19.83;
3
4 x = 1 + a/b + c/f^2;
5 r = 1 / (1/a + 1/b + 1/c + 1/d);
6 s = (b - a) / (d - c);
7 y = a * b * (1/c) * (f^2/2);
8
9 disp(['x = ', num2str(x)]);
10 disp(['r = ', num2str(r)]);
11 disp(['s = ', num2str(s)]);
12 disp(['y = ', num2str(y)]);
```

## Problem 9

The functions `realmax` and `realmin` give the largest and smallest possible numbers that can be handled by MATLAB. Suppose you have variables  $a = 3 \times 10^{150}$ ,  $b = 5 \times 10^{200}$ .

- Use MATLAB to calculate  $c = ab$ .
- Supposed  $d = 5 \times 10^{-200}$  use MATLAB to calculate  $f = d/a$ .
- Use MATLAB to calculate the product  $x = abd$  two ways.

```
1 % Check limits
2 realmax
3 realmin
4
5 a = 3e150;
6 b = 5e200;
7
8 % a. Calculate c = a*b (Expect Overflow)
9 c = a * b
10
```

```

11 % b. d = 5e-200, calculate f = d/a (Expect Underflow)
12 d = 5e-200;
13 f = d / a
14
15 % c. Calculate x = abd in two ways
16 x1 = a * b * d; % Risk of intermediate overflow
17 y = b * d;
18 x2 = a * y;      % Safer calculation
19
20 disp(['Method 1: ', num2str(x1)]);
21 disp(['Method 2: ', num2str(x2)]);

```

## Problem 22

Use MATLAB to calculate:

- a.  $e^{(-2.1)^3} + 3.47 \log(14) + \sqrt[4]{287}$
- b.  $(3.4)^7 \log(14) + \sqrt[4]{287}$
- c.  $\cos^2\left(\frac{4.12\pi}{6}\right)$
- d.  $\cos\left(\frac{4.12\pi}{6}\right)^2$

```

1 % Note: Source likely implies log base 10 for "log(14)" in standard notation,
2 % but MATLAB's log() is natural log. Using log10() for base 10.
3 ans_a = exp((-2.1)^3) + 3.47 * log10(14) + nthroot(287, 4);
4 ans_b = (3.4)^7 * log10(14) + nthroot(287, 4);
5 ans_c = cos((4.12 * pi) / 6)^2;
6 ans_d = cos(((4.12 * pi) / 6)^2);

```

## Problem 27

Use MATLAB to plot the function  $T = 7 \ln t - 8e^{0.3t}$  over the interval  $1 \leq t \leq 3$ .

```

1 t = 1:0.01:3;
2 T = 7 .* log(t) - 8 .* exp(0.3 .* t);
3
4 plot(t, T);
5 title('Temperature vs Time');
6 xlabel('Time (min)');
7 ylabel('Temperature (C)');
8 grid on;

```

## Problem 30

A cycloid is described by  $x = r(\phi - \sin \phi)$  and  $y = r(1 - \cos \phi)$ . Plot for  $r = 10$  and  $0 \leq \phi \leq 4\pi$ .

```
1 r = 10;
2 phi = 0 : 0.01 : 4*pi;
3 x = r .* (phi - sin(phi));
4 y = r .* (1 - cos(phi));
5
6 plot(x, y);
7 title('Cycloid Plot (r=10)');
8 xlabel('x'); ylabel('y');
9 axis equal;
```

## Problem 34

Develop a procedure for computing the length of side  $c_2$  of the two-triangle figure given sides  $b_1, b_2, c_1$  and angles  $A_1, A_2$ . Test with  $b_1 = 200, b_2 = 1801, c_1 = 1201, A_1 = 120^\circ, A_2 = 100^\circ$ .

```
1 % Inputs
2 b1 = 200; b2 = 1801; c1 = 1201;
3 A1_deg = 120; A2_deg = 100;
4 A1 = deg2rad(A1_deg); A2 = deg2rad(A2_deg);
5
6 % 1. Find common side 'a' (Top Triangle Law of Cosines)
7 a_sq = b1^2 + c1^2 - 2*b1*c1*cos(A1);
8 a = sqrt(a_sq);
9
10 % 2. Find c2 (Bottom Triangle) solving quadratic:
11 % c2^2 - (2*b2*cos(A2))*c2 + (b2^2 - a^2) = 0
12 coeff_A = 1;
13 coeff_B = -2 * b2 * cos(A2);
14 coeff_C = b2^2 - a_sq;
15
16 possible_c2 = roots([coeff_A, coeff_B, coeff_C]);
17 c2 = possible_c2(possible_c2 > 0); % Filter positive
18
19 disp(['Side c2: ', num2str(c2)]);
```

## Problem 35

Write a script to compute the three roots of  $x^3 + ax^2 + bx + c = 0$ .

```
1 a = input('Enter a: ');
2 b = input('Enter b: ');
3 c = input('Enter c: ');
4 disp(roots([1, a, b, c]));
```

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## Tutorial 2: Numeric, Cell and Structure Arrays

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### Problem 10

Consider the array  $A = \begin{bmatrix} 1 & 4 & 2 \\ 2 & 4 & 100 \\ 7 & 9 & 7 \\ 3 & \pi & 42 \end{bmatrix}$  and  $B = \ln(A)$ .

Write MATLAB expressions to do the following:

- a. Select just the second row of B.
- b. Evaluate the sum of the second row of B.
- c. Multiply the second column of B and the first column of A element by element.
- d. Evaluate the maximum value in the vector resulting from element-by-element multiplication of the second column of B with the first column of A.
- e. Use element-by-element division to divide the first row of A by the first three elements of the third column of B. Evaluate the sum of the elements of the resulting vector.

```
1 % Define Matrix A
2 A = [1, 4, 2;
3      2, 4, 100;
4      7, 9, 7;
5      3, pi, 42];
6
7 % Define Matrix B (Natural log is log() in MATLAB)
8 B = log(A);
9
10 % a. Select second row of B
11 part_a = B(2, :);
12
13 % b. Sum of second row of B
14 part_b = sum(B(2, :));
15
16 % c. Multiply 2nd col of B and 1st col of A element-wise
17 part_c = B(:, 2) .* A(:, 1);
18
19 % d. Max value of result from c
20 part_d = max(part_c);
```

```

21
22 % e. Divide 1st row of A by first 3 elements of 3rd col of B
23 % Note: A(1,:) is 1x3. B(1:3, 3) is 3x1.
24 % We must transpose B's slice to match dimensions.
25 vec_e = A(1, :) ./ B(1:3, 3)';
26 part_e = sum(vec_e);
27
28 disp(['Sum (Part b): ', num2str(part_b)]);
29 disp(['Max (Part d): ', num2str(part_d)]);
30 disp(['Sum (Part e): ', num2str(part_e)]);

```

## Problem 11

Create a three-dimensional array D whose three "layers" are matrices A, B, and C. Use MATLAB to find the largest element in each layer of D and the largest element in D.

```

1 A = [3, -2, 1; 6, 8, -5; 7, 9, 10];
2 B = [6, 9, -4; 7, 5, 3; -8, 2, 1];
3 C = [-7, -5, 2; 10, 6, 1; 3, -9, 8];
4
5 % Create 3D array D
6 D(:,:,1) = A;
7 D(:,:,2) = B;
8 D(:,:,3) = C;
9
10 % Largest element in each layer
11 max_layer_1 = max(max(D(:,:,1)));
12 max_layer_2 = max(max(D(:,:,2)));
13 max_layer_3 = max(max(D(:,:,3)));
14
15 % Largest element in D
16 max_total = max(D(:));
17
18 disp(['Max Total: ', num2str(max_total)]);

```

## Problem 15

Given matrices A, B, and C, verify the associative and commutative laws for addition.

```

1 A = [-7, 11; 4, 9];
2 B = [4, -5; 12, -2];
3 C = [-3, -9; 7, 8];
4
5 % a. A + B + C
6 res_a = A + B + C;
7

```

```

8 % b. A - B + C
9 res_b = A - B + C;
10
11 % c. Verify Associative Law: (A+B)+C = A+(B+C)
12 check_assoc = isequal((A+B)+C, A+(B+C));
13
14 % d. Verify Commutative Law: A+B+C = B+C+A = A+C+B
15 term1 = A + B + C;
16 term2 = B + C + A;
17 term3 = A + C + B;
18 check_comm = isequal(term1, term2) && isequal(term2, term3);
19
20 if check_assoc && check_comm
21     disp('Laws Verified');
22 else
23     disp('Verification Failed');
24 end

```

## Problem 19

Plot the function  $f(x) = \frac{4\cos x}{x+e^{-0.75x}}$  over the interval  $-2 \leq x \leq 16$ .

```

1 x = -2 : 0.05 : 16; % Smooth interval
2 f = (4 .* cos(x)) ./ (x + exp(-0.75 .* x));
3
4 plot(x, f);
5 title('Plot of f(x)');
6 xlabel('x');
7 ylabel('f(x)');
8 grid on;

```

## Problem 22

A ship travels on a straight line course described by  $y = (200 - 5x)/6$ . The ship starts when  $x = -20$  and ends when  $x = 40$ . Calculate the distance at closest approach to a lighthouse located at the origin  $(0,0)$  without using a plot.

```

1 % Define path range
2 x = -20 : 0.01 : 40;
3 y = (200 - 5 .* x) ./ 6;
4
5 % Distance formula d = sqrt(x^2 + y^2)
6 distances = sqrt(x.^2 + y.^2);
7
8 % Find minimum distance

```

```

9 min_dist = min(distances);
10
11 disp(['Closest approach distance: ', num2str(min_dist), ' km']);

```

## Problem 23

Calculate work done  $W = FD$  for five segments of a path given force and distance data. Find (a) work for each segment and (b) total work.

```

1 % Data vectors
2 Force = [400, 550, 700, 500, 600]; % Newtons
3 Distance = [3, 0.5, 0.75, 1.5, 5]; % Meters
4
5 % a. Work per segment (Element-wise multiplication)
6 Work_segments = Force .* Distance;
7
8 % b. Total work
9 Work_total = sum(Work_segments);
10
11 disp('Work per segment (J):');
12 disp(Work_segments);
13 disp(['Total Work (J): ', num2str(Work_total)]);

```

## Problem 27

Calculate compression  $x$  and potential energy  $PE = \frac{1}{2}kx^2$  for five springs given Force  $F = kx$  and spring constant  $k$ .

```

1 % Data
2 F = [11, 7, 8, 10, 9]; % Force (N)
3 k = [1000, 600, 900, 1300, 700]; % Constant (N/m)
4
5 % a. Compression x = F / k
6 x = F ./ k;
7
8 % b. Potential Energy PE = 0.5 * k * x^2
9 PE = 0.5 .* k .* (x.^2);
10
11 % Display results table
12 disp(table(F', k', x', PE', 'VariableNames', {'Force', 'k', 'Compression', 'PE'}));

```

## Problem 41

Solve the following system using the left-division method.

$$\begin{aligned}6x - 3y + 4z &= 41 \\12x + 5y - 7z &= -26 \\-5x + 2y - 6z &= 16\end{aligned}$$

```
1 % Coefficient Matrix A
2 A = [ 6, -3, 4;
3      12, 5, -7;
4      -5, 2, -6];
5
6 % Constant Vector B
7 B = [41; -26; 16];
8
9 % Solve for X = [x; y; z] using left division
10 Solution = A \ B;
11
12 disp('Solution [x; y; z]:');
13 disp(Solution);
```