# Summary of Equations in Aerodynamics Lecture Notes

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1	${f F}$	undamental Aerodynamics Equations	
1.	1	Equation of State for a Gas (Ideal Gas Law)	
		$p = \rho RT$	(1)
		$p - \rho \iota \iota \iota$	(1)
wł	nere:		
	• p	= Pressure	
	• 0	= Density	
	P	= ~=~~ <i>y</i>	

# 1.2 Specific Volume

• T = Temperature (Kelvin)

$$v = \frac{1}{\rho} \tag{2}$$

where v is the specific volume (volume per unit mass).

## 1.3 Kinetic Energy and Temperature Relation

• R = Specific Gas Constant (e.g., 287 J/kg·K for air)

$$K_e = \frac{3}{2}kT\tag{3}$$

where:

- $K_e$  = Average kinetic energy of molecules
- $k = \text{Boltzmann constant } (1.38 \times 10^{-23} \text{ J/K})$
- T = Temperature (Kelvin)

#### 1.4 Shear Stress Due to Viscosity (Newton's Law of Friction)

$$\tau = \mu \frac{du}{dy} \tag{4}$$

where:

- $\tau = \text{Shear stress}$
- $\mu = \text{Dynamic viscosity}$
- $\frac{du}{dy}$  = Velocity gradient

#### 1.5 Reynolds Number (Flow Characterization)

$$Re = \frac{\rho V l}{\mu} = \frac{V l}{\nu} \tag{5}$$

where:

- Re =Reynolds number
- V = Flow velocity
- l = Characteristic length (e.g., airfoil chord)
- $\mu = \text{Dynamic viscosity}$
- $\nu = \text{Kinematic viscosity}$

#### 1.6 Mach Number (Compressibility Effects)

$$M = \frac{V}{a} \tag{6}$$

where:

- M = Mach number
- $\bullet$  V = Object speed
- $\bullet$  a =Speed of sound in the medium

# 2 Example Calculations

#### 2.1 Finding Temperature Using Ideal Gas Law

$$T = \frac{p}{\rho R} \tag{7}$$

Example:

$$T = \frac{8.9876 \times 10^4}{(1.1117)(287)} = 281K \tag{8}$$

#### 2.2 Air Weight in a Room

First, use the equation of state to find  $\rho$ :

$$\rho = \frac{p}{RT} \tag{9}$$

Then, find mass:

$$m = \rho V \tag{10}$$

Finally, weight:

$$W = mg (11)$$

## 2.3 Percentage Change in Air Weight Due to Temperature Drop

Since the temperature changes, we recalculate density:

$$\rho = \frac{2116}{(1716)(460 - 10)} = 0.00274 \frac{\text{slug}}{\text{ft}^3}$$
 (12)

Compare densities:

$$\Delta \rho = 0.00274 - 0.00237 = 0.00037 \frac{\text{slug}}{\text{ft}^3}$$
 (13)

Percentage change:

%change = 
$$\frac{\Delta \rho}{\rho} \times 100 = \frac{0.00037}{0.00237} \times 100 = 15.6\%$$
 increase (14)

Alternative solution:

$$\Delta W = \Delta m \cdot g = 0.888 \times 32.2 = 28.5936 \text{ lb}$$
 (15)

%change = 
$$\frac{\Delta W}{W_1} \times 100 = \frac{28.5936}{183} \times 100 = 15.6\%$$
 (16)