

Summary of Equations in Aerodynamics Lecture

By Kelvin Le

23/02/2025

1 Fundamental Aerodynamics Equations

1.1 Equation of State for a Gas (Ideal Gas Law)

$$p = \rho RT \quad (1)$$

where:

- p = Pressure
- ρ = Density
- R = Specific Gas Constant (e.g., 287 J/kg·K for air)
- T = Temperature (Kelvin)

1.2 Specific Volume

$$v = \frac{1}{\rho} \quad (2)$$

where v is the specific volume (volume per unit mass).

1.3 Kinetic Energy and Temperature Relation

$$K_e = \frac{3}{2}kT \quad (3)$$

where:

- K_e = Average kinetic energy of molecules
- k = Boltzmann constant (1.38×10^{-23} J/K)
- T = Temperature (Kelvin)

1.4 Shear Stress Due to Viscosity (Newton's Law of Friction)

$$\tau = \mu \frac{du}{dy} \quad (4)$$

where:

- τ = Shear stress
- μ = Dynamic viscosity
- $\frac{du}{dy}$ = Velocity gradient

1.5 Reynolds Number (Flow Characterization)

$$Re = \frac{\rho V l}{\mu} = \frac{V l}{\nu} \quad (5)$$

where:

- Re = Reynolds number
- V = Flow velocity
- l = Characteristic length (e.g., airfoil chord)
- μ = Dynamic viscosity
- ν = Kinematic viscosity

1.6 Mach Number (Compressibility Effects)

$$M = \frac{V}{a} \quad (6)$$

where:

- M = Mach number
- V = Object speed
- a = Speed of sound in the medium

2 Example Calculations

2.1 Finding Temperature Using Ideal Gas Law

$$T = \frac{p}{\rho R} \quad (7)$$

Example:

$$T = \frac{8.9876 \times 10^4}{(1.1117)(287)} = 281K \quad (8)$$

2.2 Air Weight in a Room

First, use the equation of state to find ρ :

$$\rho = \frac{p}{RT} \quad (9)$$

Then, find mass:

$$m = \rho V \quad (10)$$

Finally, weight:

$$W = mg \quad (11)$$

2.3 Percentage Change in Air Weight Due to Temperature Drop

Since the temperature changes, we recalculate density:

$$\rho = \frac{2116}{(1716)(460 - 10)} = 0.00274 \frac{\text{slug}}{\text{ft}^3} \quad (12)$$

Compare densities:

$$\Delta\rho = 0.00274 - 0.00237 = 0.00037 \frac{\text{slug}}{\text{ft}^3} \quad (13)$$

Percentage change:

$$\% \text{change} = \frac{\Delta\rho}{\rho} \times 100 = \frac{0.00037}{0.00237} \times 100 = 15.6\% \text{ increase} \quad (14)$$

Alternative solution:

$$\Delta W = \Delta m \cdot g = 0.888 \times 32.2 = 28.5936 \text{ lb} \quad (15)$$

$$\% \text{change} = \frac{\Delta W}{W_1} \times 100 = \frac{28.5936}{183} \times 100 = 15.6\% \quad (16)$$