

# Summary of Equations in Aerodynamics Lecture Notes

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## 1 Fundamental Aerodynamics Equations

### 1.1 Equation of State for a Gas (Ideal Gas Law)

$$p = \rho RT \quad (1)$$

where:

- $p$  = Pressure
- $\rho$  = Density
- $R$  = Specific Gas Constant (e.g., 287 J/kg·K for air)
- $T$  = Temperature (Kelvin)

### 1.2 Specific Volume

$$v = \frac{1}{\rho} \quad (2)$$

where  $v$  is the specific volume (volume per unit mass).

### 1.3 Kinetic Energy and Temperature Relation

$$K_e = \frac{3}{2}kT \quad (3)$$

where:

- $K_e$  = Average kinetic energy of molecules
- $k$  = Boltzmann constant ( $1.38 \times 10^{-23}$  J/K)
- $T$  = Temperature (Kelvin)

### 1.4 Shear Stress Due to Viscosity (Newton's Law of Friction)

$$\tau = \mu \frac{du}{dy} \quad (4)$$

where:

- $\tau$  = Shear stress
- $\mu$  = Dynamic viscosity
- $\frac{du}{dy}$  = Velocity gradient

## 1.5 Reynolds Number (Flow Characterization)

$$Re = \frac{\rho V l}{\mu} = \frac{V l}{\nu} \quad (5)$$

where:

- $Re$  = Reynolds number
- $V$  = Flow velocity
- $l$  = Characteristic length (e.g., airfoil chord)
- $\mu$  = Dynamic viscosity
- $\nu$  = Kinematic viscosity

## 1.6 Mach Number (Compressibility Effects)

$$M = \frac{V}{a} \quad (6)$$

where:

- $M$  = Mach number
- $V$  = Object speed
- $a$  = Speed of sound in the medium

# 2 Example Calculations

## 2.1 Finding Temperature Using Ideal Gas Law

$$T = \frac{p}{\rho R} \quad (7)$$

Example:

$$T = \frac{8.9876 \times 10^4}{(1.1117)(287)} = 281K \quad (8)$$

## 2.2 Air Weight in a Room

First, use the equation of state to find  $\rho$ :

$$\rho = \frac{p}{RT} \quad (9)$$

Then, find mass:

$$m = \rho V \quad (10)$$

Finally, weight:

$$W = mg \quad (11)$$

## 2.3 Percentage Change in Air Weight Due to Temperature Drop

Since the temperature changes, we recalculate density:

$$\rho = \frac{2116}{(1716)(460 - 10)} = 0.00274 \frac{\text{slug}}{\text{ft}^3} \quad (12)$$

Compare densities:

$$\Delta\rho = 0.00274 - 0.00237 = 0.00037 \frac{\text{slug}}{\text{ft}^3} \quad (13)$$

Percentage change:

$$\% \text{change} = \frac{\Delta\rho}{\rho} \times 100 = \frac{0.00037}{0.00237} \times 100 = 15.6\% \text{ increase} \quad (14)$$

Alternative solution:

$$\Delta W = \Delta m \cdot g = 0.888 \times 32.2 = 28.5936 \text{ lb} \quad (15)$$

$$\% \text{change} = \frac{\Delta W}{W_1} \times 100 = \frac{28.5936}{183} \times 100 = 15.6\% \quad (16)$$