Extra Problems on Limits

1) Prove that
$$\lim_{n\to\infty} \frac{2n+11}{n+3} = 2$$
 using the definition of convergence.

2) Prove that
$$\lim_{n\to\infty} \sqrt{\frac{5n+3}{n}} = \sqrt{5}$$
 using the definition of convergence.

3) Prove that
$$a_n = \frac{5}{\sqrt{n}} + 3$$
 converges using the definition of convergence.

4) Prove that
$$a_n = \frac{(-3)^n}{4^n + 7}$$
 converges using the definition of convergence.

(note that
$$(-3)^n = (-1)^n 3^n$$
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