

Tipping points in diversified farming systems

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Abstract

The emergence and impact of tipping points are of great interest in both social and ecological research. Despite widespread recognition of the importance of feedbacks between human and environmental systems, it is often assumed that the observed nonlinear dynamics in these coupled systems are the result of dynamics in either the underlying human or environmental processes. Using the adoption of diversified farming practices as a case study, we show how bistability in ecosystem states and corresponding ecosystem services can emerge purely from the temporal feedbacks between human decisions and ecological responses. We leverage interview data to inform a stylized model, showing how understanding the temporal mechanisms of tipping points in social-environmental systems is critical to designing effective policy interventions in sustainable agriculture.

Keywords: ecosystem services, tipping points, agriculture, diversification practices, decision-making

Introduction

Both ecosystems and social systems can change states abruptly as the result of crossing critical thresholds. Often referred to as “tipping points”, states where small perturbations can trigger large responses have garnered extensive academic and public attention (Gladwell 2006; Rockström et al. 2009). Theories of ecological multistability have long described tipping points and critical thresholds (Beisner, Haydon, and Cuddington 2003; Scheffer et al. (2001)) and explored how management impacts stability landscapes of social ecological systems (Horan, Fenichel, Drury, et al. (2011a)). Tipping points in natural systems are generally assumed to stem from complex ecological processes like population dynamics and species interactions (Dai et al. (2012); Mumby, Hastings, and Edwards (2007); Scheffer (2010)). Similarly, examples of tipping points in social systems, ranging from the collapse of civilizations (Downey, Haas, and Shennan (2016)) to the spread

of innovations through social network processes (Redmond (2003)) suggest that observed nonlinearities in social systems can result from complex features of human decisions and economic structures (J. Vandermeer (1997a)).

In social-ecological systems (SES), human actions impact ecological processes and the resultant ecological changes create feedbacks that alter the scope and efficacy of future management actions (Liu et al. (2007); Ostrom (2009); Walker et al. (2004)). These coupled systems become increasingly complex when the dynamics of ecological processes do not align with the temporal scale of human decision-making (Cumming, Cumming, and Redman (2006)). Techniques previously used to investigate dynamic ecological processes and responsive decision-making have centered around one or the other, often overlooking the temporal complexity of decision-making (Lippe et al. (2019)). For example, agent based models often use single time-step decision rules rather than allowing for emergent decision strategies that maximize expected rewards over longer time horizons (Lippe et al. (2019)). Similarly, exploring both the time horizon of decisions and the rate of ecological processes is impossible using methods that rely on equilibrium analyses, such as dynamic equations.

While variations of models and data have been used to explain and explore tipping points in numerous systems, from ecological to climate (Muradian (2001); Lenton et al. (2008)), we focus here on agricultural systems. Agriculture is a fundamental driver of anthropogenic ecological change (Foley et al. (2005); Foley et al. (2011); Stoate et al. (2009)) and its productivity is closely intertwined with ecosystem processes that provide valuable services. While adoption of sustainable farm management practices undoubtedly encompasses a continuum of actions and outcomes, suites of practices are often used together in a package, coalescing around distinct stable states or “syndromes” (Andow and Hidaka (1989); Ong and Liao (2020); J. Vandermeer (1997a)). However, similar to the aforementioned issues, the mechanisms currently used to explain these bistable patterns have relied on the assumption that both ecological (or production) and decision (or economic) dynamics are non-monotonic. If either of these systems is approximated as monotonic, the larger social environmental system is characterized by a single stable point, making alternative syndromes of production impossible to explain with dynamic equations (J. Vandermeer (1997a); J. Vandermeer and Perfecto (2012)). While non-monotonic assumptions are sometimes reasonable, these explanations overlook the temporal component of both the ecological and decision process. As we explore here, multistable patterns could feasibly be the result not of complex non-monotonic approximations, but of temporal interactions of decisions and ecosystem.

This paper presents a stylized model of the adoption of diversified agricultural practices, or practices that bolster ecosystem services by promoting beneficial agrobiodiversity (Kremen, Iles, and Bacon (2012)), to ex-

plore the ecosystem service patterns that result specifically from interactions between adaptive decision-making and an ever-changing environment. We find a mechanism for bistability, or two prevailing environmental (ecosystem service) states, that is the result not of complex structural assumptions within either the human or ecological system, but rather the rates at which the two systems interact. While our model necessarily simplifies both decision-making and environmental processes, it provides a framework to explore emergent properties in social-ecological systems. We inform assumptions and important structural attributes of our model with interview data which. Finally, we show that our findings have important implications for agricultural policy implementation and social-ecological systems theory.

Methods

We explore the transition to and from diversified farming systems (low and high ecosystem service states) using a Markov Decision Process (MDP) in which a farmer makes a series of decisions about whether or not to employ diversified farming practices over time (Figure 1). In the context of diversified farming systems, diversification practices, such as the use of compost, crop rotation, intercropping, reduced tillage, and cover crops, are distinct from the concept of operational diversification (i.e., simply increasing the range of agricultural goods produced on a given farm). The model was developed through an iterative, collaborative process with an interdisciplinary team comprising plant and soil scientists, agricultural economists, ecologists, agricultural policy experts, social scientists, and farmers with the goal was to capture the core complexities stemming from the coupled human and natural dynamics of the modeled system (Figure 1).

Interview data

From February 2018 - August 2020, we interviewed 25 lettuce growers and 17 almond growers from California using a snowball sampling method and referrals. We focused on the almonds and leafy greens/lettuce sectors because these are among the most valuable crops in California. We selected interviewees to represent a range of growers (small to large scale; organic to conventional, early adopters of diversification practices to late adopters/laggards, family run to corporate management, and direct-to-consumer marketing to wholesale). Interviews were conducted in person or over the phone in situations where in-person interviews were not possible due to farmer schedules or the need to social distance during COVID-19 restrictions. Most interviews were audio recorded and transcribed. If recording was not possible, careful notes were taken to create a transcript.

We performed coding for key themes and keyword searches of the transcripts to inform key assumptions and provide quotes used in this paper.

Conceptual model description

In our model at each time step the farmer takes an “action” of 0% to 100% percent investment in adopting or maintaining diversification practices (Figure 1 A1). The “system state” corresponds to the level of benefit derived from the ecosystem services (Figure 1-A2) that result from those adoption decisions. Benefits may be financial, social, ideological, and/or aesthetic. A greater percent investment in diversification practices corresponds to a greater probability of transitioning to a higher (more beneficial) ecological state in the next year (Figure 1- A3). While higher ecological states are beneficial, investments in diversification practices also come with higher associated costs compared to non-diversified farms (Figure 1). By defining parameter values for cost, benefit, transition stochasticity, ecological change rate, and future discounting (Table 1), we can allow the optimal action strategy for the agent (farmer) to emerge based on expected rewards over either a finite (to represent short-tenure leased farms) or infinite (to represent longer-term leases and land ownership) time horizon (Figure 1 A4).

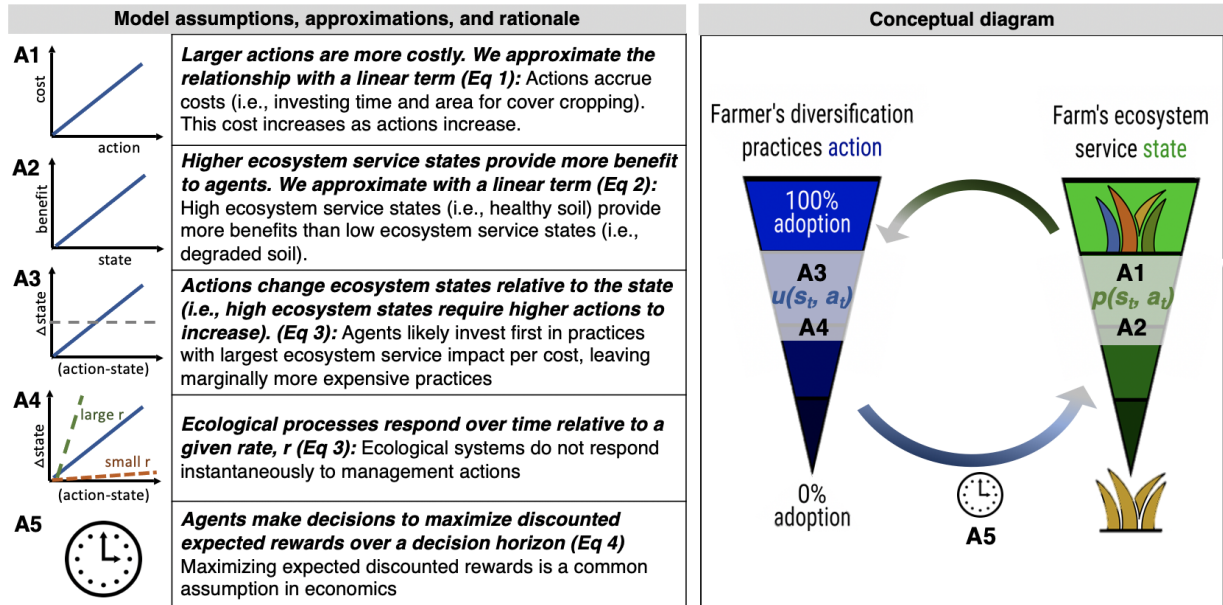


Figure 1: Conceptual diagram and model assumptions. The farmer’s choice of how much to invest (time and money) into the adoption of diversification practices (blue), and the resulting ecosystem services state (green), with a more diversified ecosystem state at the top, and a more simplified ecosystem state at bottom. Each time step, the farmer chooses the optimal action for their current ecosystem service state based on the perceived utility function, u , and state transition probability function, p . For a given ecosystem service state and action at time t , p describes how the ecosystem responds stochastically to result in an updated state at $t + 1$. The updated ecosystem service state then feeds back to influence the farmer’s future choices, leading to tradeoffs arising from the coupling of ecological processes with consecutive diversification practice adoption decisions over time. Main model assumptions (A1-A5) are outlined along with a brief rational for each approximation.

Mathematical description

The farmer’s decision model can be expressed as

$$\max_{\{a_t\}} \mathbb{E} \left[\sum_t^T u(s_t, a_t) \gamma^t \right]$$

where $\{a_t\}$ is the set of available actions, \mathbb{E} the expected utility operator, $u(s_t, a_t)$ the utility which the farmer associates with being in state s_t and taking action a_t at time t , γ the myopic discount factor, and T the land tenure of the farm ($T \rightarrow \infty$ if the farmer owns the land or has a long lease).

We assume a simple model of the farmer's perceived utility $u(s_t, a_t)$ as a function of the difference between the cost c_a associated with diversification practice action a_t , versus expected benefits b_s derived from ecosystem state s_t , at time t , such that

$$u(s_t, a_t) = b_s s_t - c_a a_t$$

The ecosystem state is also dynamic, evolving according to the transition probability function $p(s_t, a_t)$, such that

$$s_{t+1} = p(s_t, a_t) := s_t + r(a_t - s_t) + \epsilon$$

where $\epsilon \sim N(0, \sigma)$. This provides a minimal state transition model in which the parameter r sets the natural timescale at which the ecosystem can respond to changes in land management decisions, and σ defines the width of the state transition probability distribution, capturing the noise inherent to ecological system change. While we have assumed very basic transition and utility functions for this stylized model, in general more complicated nonlinear functions for both the ecosystem state transition and perceived utility are possible using this framework.

Parameterization

We have parameterized the model to illustrate the emergence of bistability in SES resulting from agroecological investment decision-making given stochastic ecological responses over time (Figure 1 and Figure 2; Parameter values in Supporting information). We explore a larger parameter space in the supporting information, and explain why the choice of parameters does not change the main findings.

Results

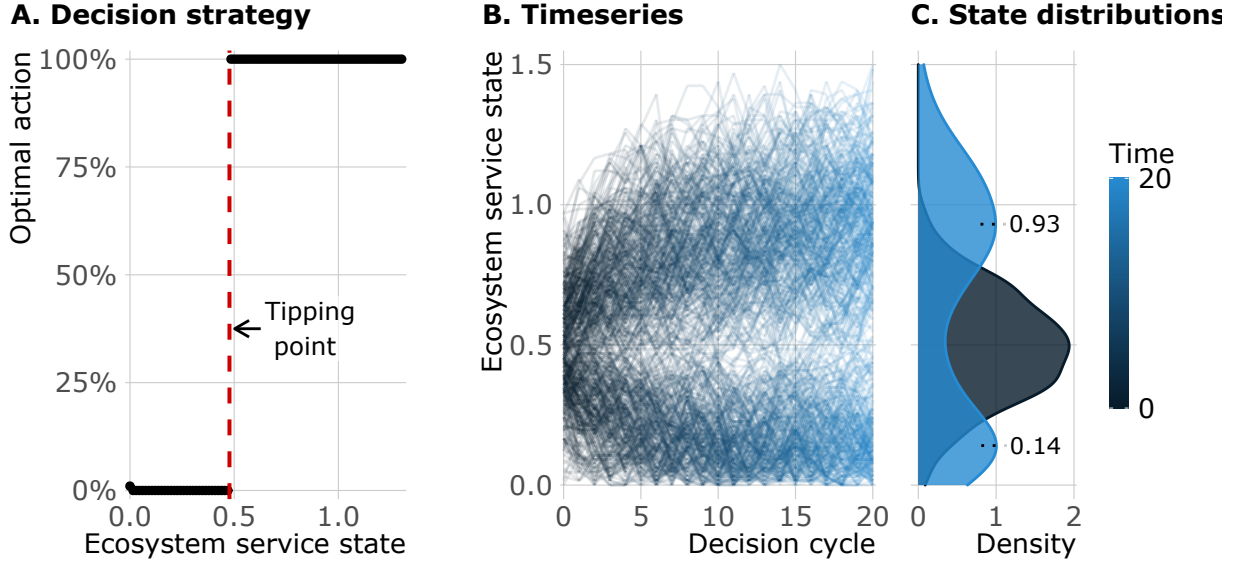


Figure 2: Initial ecosystem states are distributed normally (mean = 0.5; S.D. = 0.2; truncated at [0,1]). (A) Agents follow decision strategy π until $t = 20$. (B) Ecosystem state of each agent over time (500 simulations). (C) Initial ES distribution (dark blue) and final bimodal distribution at $t = 20$ (light blue).

Bistability in ecosystem services

Using the described model, we observe the behavior of agents' sequential choices and the resultant environmental outcomes through time. The decision strategy, π , describes the emergent optimal course of action for a given state and is the stationary optimal state-dependent decision strategy over an infinite time horizon (Figure 2A).

Agents' initial ecosystem states were distributed normally around a mean of $s = 0.5$. We find that after following the optimal decision strategy (infinite horizon) for 20 decision cycles, agents have largely settled into two stable ecosystem states, with some farms transitioning to more simplified (lower levels of ecosystem services) farming systems, and others to more diversified (higher levels ecosystem services) systems (Figure 2B and 2C). Further, we find strong path dependency, with only 17% of agents who started in a simplified ($s < 0.5$) state concluding in a diversified ($s > 0.5$) state, and only 7% initially in the diversified state transitioning to a simplified state.

Importance of temporal dynamics in coupled systems

Our baseline model shows how a simple coupling of human choices and ecological response can result in bistable landscapes of high and low diversification practice adoption and, as a result, high and low levels of ecosystem services (Figure 2). By vary the time horizon of the decision process, the rate of the ecological response, and the cost/benefit ratio, we find that this tipping point disappears when the speed of response of

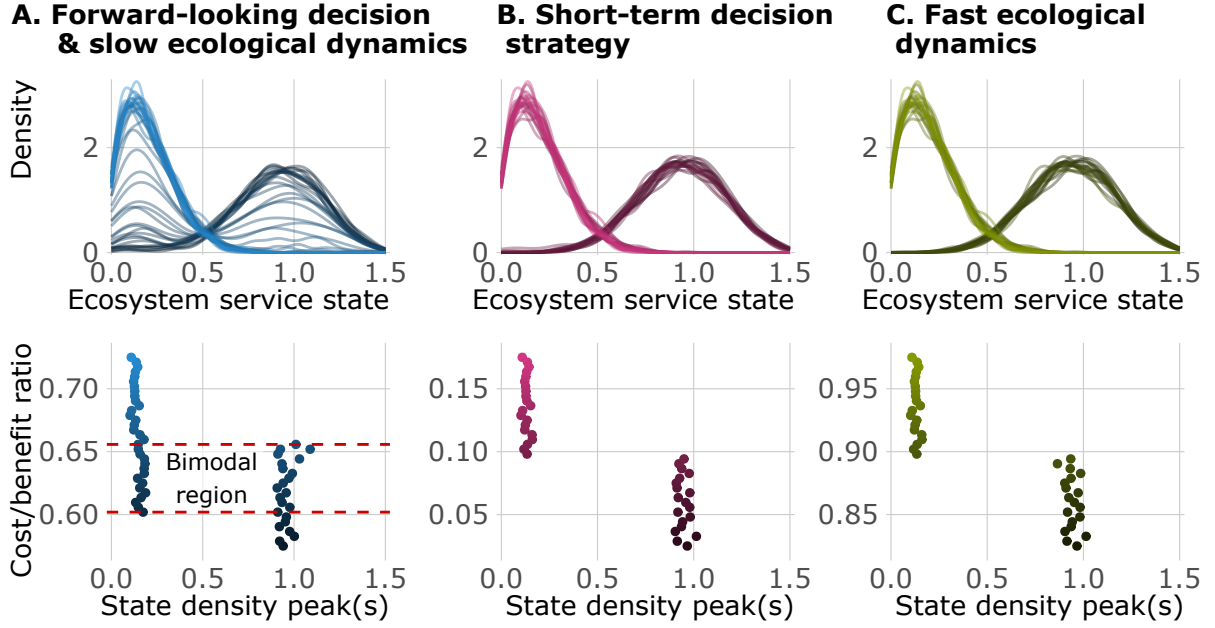


Figure 3: For three scenarios (coupled human/natural system, overly-myopic decision maker, and overly-fast ecological change), cost/benefit ratio was varied incrementally over 40 values, indicated by color shade, across a $c : b$ range of width 0.15, encompassing the transition between a “never invest” to an “always invest” policy. For each $c : b$, 500 replicate simulations were conducted as in Fig 2. Upper plots show distribution of ES state at $t = 20$ for each $c : b$. Lower plots show density curve peak(s). (A) By coupling a forward-looking decision-maker and a slowly-adapting environment, complex dynamics like alternate stable states can emerge. However, with (B) a short-term decision strategy (solving the MDP over a 2-year time horizon), or (C) a fast ecological change rate ($r = 0.95$), no bimodality is observed.

either the ecological system or decision-making process overwhelms the coupling (a proxy for decoupling). This is expected given the linear approximations of costs, benefits, and ecological processes (J. Vandermeer (1997a); J. Vandermeer and Perfecto (2012)). Figure 3A shows that with temporal human/environment interactions, there exists a region of cost/benefit ratio within which various bimodal ecosystem state distributions exist (also exemplified in Figure 2). However, when ecological processes become fast enough that the ecosystem responds almost immediately to farmer actions ($r = 0.95$), alternate stable states do not emerge, regardless of cost-benefit ratios (Fig 3C). Similarly, as decisions become temporally myopic (in this case, with a time horizon of 2 decision cycles), the potential for bistability in adoption trajectories disappears (Fig 3B). Only when both a gradually changing environment and a forward-looking decision-maker (i.e. a farmer who takes into account potential benefits over the long term) are coupled, do tipping point phenomena emerge in the decision strategy (without non-monotonic assumptions), leading to two stable ecosystem service states (Fig 3).

Decision horizons	Costs	Rates of ecological process
"Cover crops cost money. And (there is resistance at our company because) some people don't believe they see the benefit right away. That's an internal discussion we try to have (at our company). I'm for the cover crop. It takes time. It takes time."		
"I own the land. I want to make the soil as good or better when I give it to my son. Since I own it, I do care about it. But even if I leased, I believe that you should take care of the soil. But I know others that lease who do not do that. "		
"If you have a good source of compost and start incorporating those practices, I would hope that you would see something in five years. Not that there's anything magical about five years, but realizing that it's not going to happen necessarily in a year or two."		
"Sometimes the cost of doing things is a barrier. Sometimes getting out of your box of thinking is a barrier to doing things. I mean, you're used to doing something a certain way, and to change it very dramatically...how much effort does it take to do that as opposed to what you know kind of works now?"		
"The biggest thing (that's a challenge for soil health) is the economic pressure. The pressure to make money off of a given piece of ground, which means using it too intensively, which is quite common around here."		
"I think a lot of those are Band-Aids for people that don't look more long-term and are not willing to put the investment into the ground, and so they look for Band-Aids"		

Figure 4: My Flowchart

Implications for agricultural incentive design and land tenure policy

While approximations of coarse mechanisms that can explain bistability in agricultural system may seem inconsequential, the temporal component of ecology processes and decision horizons were central themes emerging from our interview data about adoption patterns (Table 1). And with approximately 39% of U.S. farmland under lease, the impact of land tenure on decision making is important for understanding agricultural management more broadly. For example, U.S. corn farmers who rent land are less likely than landowners to implement grassed waterways, strip cropping, contour farming, and conservation tillage (Soule, Tegene, and Wiebe (2000)).

We solve the MDP on a constrained time horizon (20-decision cycles, in comparison to an infinite time horizon in Fig 2), representing the shorter horizon on which tenant farmers might make decisions (Fig 4B).

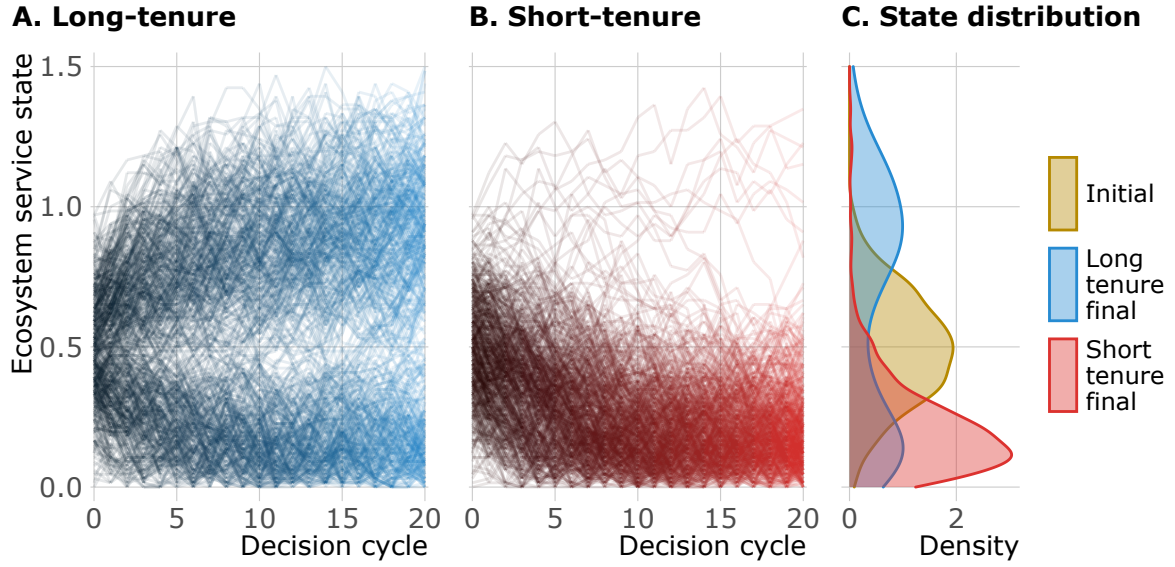


Figure 5: The simulation is identical to that in Fig 2, but the MDP is solved under a finite, 20-year time horizon. (A) Result of short land tenure on ES state over time. (B) Comparison between final state distribution of short- vs. long-tenure model runs.

Comparing the final state distribution of the long-tenure (baseline) versus the short-tenure model shows that, as a farmer’s expected land tenure duration decreases, it becomes optimal to reduce diversification adoption across a wider range of ecosystem states. This results in ecosystem state degradation even among farm sites with an initially high ecosystem service value, with 94% of farmers ending up in the simplified state at $t = 20$. It’s worth noting that land tenure itself does not necessarily define decision horizons, there are numerous factors (i.e. cultural, familial, economic) that might also impact decision horizons.

While the temporal horizon of land-use decisions has impacts on the predicted trajectories of those system, incentives that shift cost-benefit structures influence management practices are also a critical component to those trajectories and have become an integral part of farming over the past half-century (Batáry et al. (2015); Graddy-Lovelace and Diamond (2017)). We explore the impact of incentive duration on the efficacy of policies to promote adoption of diversification practices by implementing two competing publicly funded incentive schemes: a short-term (two-time step) incentive which fully covers the cost of adoption, versus a longer-term (ten-time step) incentive which only partially offsets the adoption costs over those time steps. Formally, the cost of each incentive package is equal. Within the model, agents adapt their optimal decision strategy for the given cost-benefit ratio during the incentive period, and at its conclusion they revert to the baseline strategy (i.e. without payments).

We find longer, more sustained incentive programs to be more effective at encouraging adoption behavior over the critical threshold toward diversified farming (Fig 5). Once a farmer has crossed the viable ecosystem

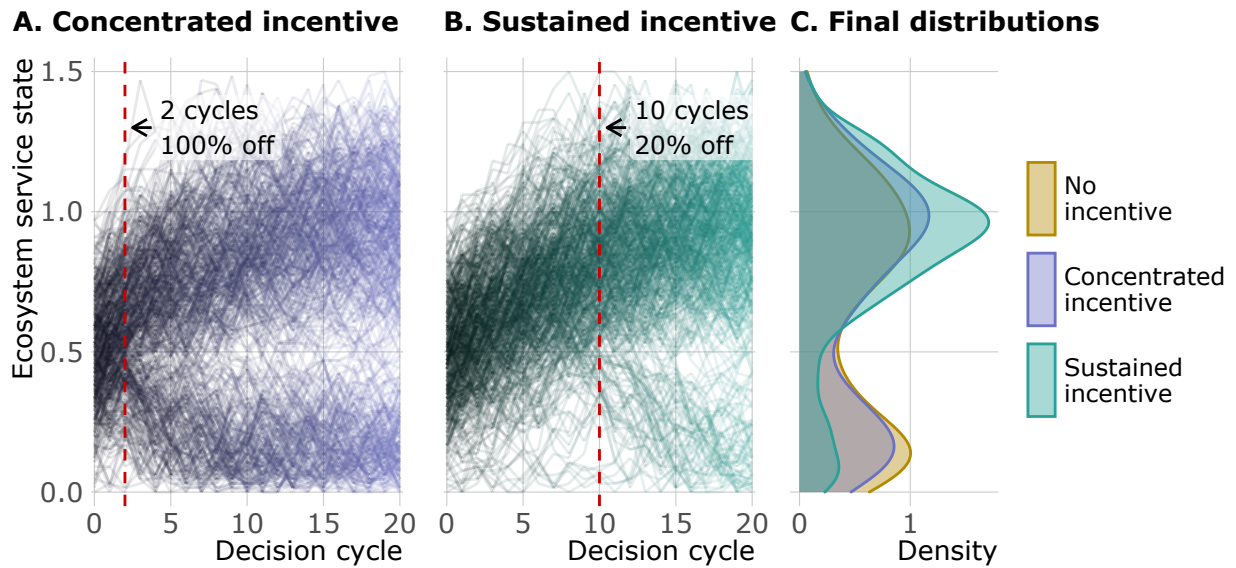


Figure 6: Starting from the same initial states as Fig 2, ES state timeseries are shown for (A) a large, abrupt incentive (100% of adoption expenses are covered for two years) vs. (B) a smaller, more sustained incentive (adoption cost is 80% of baseline for 10 years). Ignoring discounting, both packages have the same total cost to the funder (the equivalent of 2 years' worth of full adoption cost offsets). After the incentive period, agents adjust their decision rules to that of the base case (i.e. no incentive) until $t = 20$. (C) Shows that the sustained incentive ultimately drove more DP adoption.

state threshold, it becomes less likely that they will return to simplified systems, even after incentives are removed. Because it takes a series of investment actions for the ecosystem service state to cross the investment threshold, longer-term incentives ultimately result in more diversification practice adoption.

Discussion

Our analysis suggests a mechanism for bistability in social-ecological systems that is the result of temporal interactions between forward-looking decisions and ecological processes rather than complex structural assumptions about either system alone. While alternate stable states within social ecological systems, and farming systems in particular, have been previously explored and observed (Horan, Fenichel, Drury, et al. (2011b); J. Vandermeer (1997b); J. H. Vandermeer and Perfecto (2012)), our results shed light specifically on temporal feedbacks that might contribute to this pattern (Figure 6). We show how this mechanism provides novel insights not only for social-ecological research (Fig 3), but also for agricultural policy (Fig 4 and Fig 5).

In contrast to equilibrium models (J. H. Vandermeer and Perfecto 2012), our model assumptions [Table 1] reflects the delay between adopting a diversified practice and seeing the benefits. This reality is supported by our interviews with farmers, for example, one states, “Cover crops cost money. And (there is resistance at our company because) some people don’t believe they see the benefit right away. That’s an internal discussion we try to have (at our company). I’m for the cover crop. It takes time. It takes time”. The

time required to see these benefits influences the adoption patterns seen across short and long term tenants. One farmer explains, “We do have hedge rows on several of the ranches, more where we have long-term leases.” Our model similarly reflects why secure land tenure can impact decision strategies and consequently is integral to increasing the adoption of diversified farming practices. This finding complements a larger body of sociological research documenting how security and length of land tenure affects adoption of sustainable agricultural practices (Fraser (2004); Long et al. (2017); Richardson Jr (2015); Soule, Tegene, and Wiebe (2000)). Policies that increase land tenure duration, such as regulating lease agreement terms, providing low interest loans, or promoting stable farm succession plans, may represent a key lever to enable farmers to adopt more diversified agroecological practices.

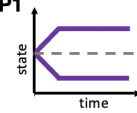
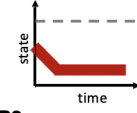
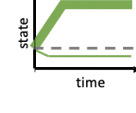
	Model predictions	Evidence in support of pattern	Value of MDP method
P1 	Bistability in ecosystem states (ecosystem services) can emerge without structural assumptions about non-monotonic cost structures and ecological dynamics (Fig 2)	Syndromes of production, or bistable patterns in adoption of agricultural practices, have been both empirically documented and theoretically described (Vandermeer 2012, 1997)	The temporal mechanism for bistability leads to different suggested intervention strategies than mechanisms that require nonmonotonic assumptions about individual system dynamics
P2 	Decision making over short time horizons decreases investment in ecosystem service promoting activities (Fig 4) and removes bistability as decision horizons become infinitely short (Fig 3B)	U.S. corn farmers who rent land are less likely than landowners to implement grassed waterways, strip cropping, contour farming, and conservation tillage (Soule, 2000)	Decision horizons are less intuitive to explore in equilibrium models. Including these attributes of decision making important for understanding the impact of tenure systems.
P3 	Longer, more sustained incentive programs are more effective than short term policies at encouraging adoption of practices for which benefits accrue slowly (Fig 5)	<i>Untested prediction</i>	Tradeoffs between incentive duration and magnitude remain unresolved. MDPs allows us to explore these policy scenarios unlike equilibrium models.

Figure 7: Table of the four main model predictions, evidence in support of the pattern, value added of the temporal mechanism and minimal assumptions.

Policies designed to promote agricultural sustainability and ecosystem services by reducing the costs of practice adoption are particularly interesting to explore with this model. Our results suggest that long-term, sustained incentives, even when only partially covering the cost of adoption, may be more effective in shifting farmers from simplified ecological states to diversified states than more concentrated short-term incentives (Fig 6 P4). We show that the cost of interventions and the social-environmental benefit of those interventions are not necessarily equivalent. Rather, perceived stability of incentive programs over time may be an important driver of adoption, which can be overlooked if the temporal rates of coupled dynamics in social-environmental systems are not considered. This is particularly relevant to government payment programs and suggests that payments can be highly effective in encouraging adoption of diversification practices (or other ecosystem service promoting practices) when implemented over long time horizons. While the possibility of a policy discontinuation may contribute to the lack of impact for short-term incentives,

reduced transaction costs that come with farmers making a longer-term commitment may also partially explain the greater impact of sustained incentives as compared to concentrated incentives.

By conceptualizing social environmental systems through lens, we offer insights into important agricultural patterns and thier implications for policy. We present a flexible model framework that can be built on to address numerous questions in social-ecological systems research and policy design. Expanding the boundaries of the model to include the effect of factors such as agricultural regulations and network structures would extend the scope of questions explored.

Model implementation

The model was developed in the *R* programming language (R Core Team 2019). The *MDPtoolbox* library was used to set up and solve the MDP (Chades et al. 2017), *tidyverse* for data analysis (Wickham et al. 2019), and *ggplot2* to generate all figures (Wickham 2016). Code for our model and the experiments conducted in this paper is available freely at <https://github.com/boettiger-lab/dfs-mdp>.

Author Contributions:

Conceptualization CB, MC, SW, PB, TB, LC, FC, KE, SG, AI, DK, CK, JL, EO, JO, MR, AS, JT, HW; Data curation: MC, SW, CB; Formal Analysis: MC, SW, CB; Funding acquisition: TB, AI, CK, DK, CB; Methodology: CB, MC, SW, PB, TB, LC, FC, KE, AI, DK, CK, EO, JT, HW; Code: MC, SW, CB; Visualization: MC, SW, CB; Writing – original draft: MC, SW, CB, LC; Writing – review & editing: CB, MC, SW, PB, TB, LC, FC, KE, SG, AI, DK, CK, JL, EO, JO, MR, AS, JT, HW

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