

# Tipping points in diversified farming systems

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## Abstract

The emergence and impact of tipping points are of great interest in both social and ecological research. Despite widespread recognition of the importance of feedbacks between human and environmental systems, it is often assumed that the observed nonlinear dynamics in these coupled systems rest within either underlying human or environmental processes. Using adoption of diversified farming practices as a case study, we show how bistability in ecosystem states and services can emerge purely from the temporal feedbacks between human decisions and ecological responses. We show that understanding temporal mechanisms of tipping points in social-environmental systems is critical to designing effective policy interventions in numerous environmental contexts.

**Keywords:** ecosystem services, tipping points, agriculture, diversification practices, decision-making

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## Introduction

Both ecosystems and social systems can change states abruptly as the result of crossing critical thresholds. Theories of ecological multistability have long described this phenomenon (Beisner, Haydon, and Cuddington (2003); Scheffer et al. (2001)) and explored how management impacts stability landscapes of these systems (Horan, Fenichel, Drury, et al. (2011a)). Tipping points in natural systems are generally assumed to stem from complex ecological processes like population dynamics and species interactions (Dai et al. (2012); Mumby, Hastings, and Edwards (2007); Scheffer (2010)). Similarly, examples of tipping points in social systems, ranging from the collapse of civilizations (Downey, Haas, and Shennan (2016)) to the spread of innovations through social network processes (Redmond (2003)) suggest that observed nonlinearities in

social systems can result from complex features of human decisions and economic structures (J. Vandermeer (1997a)).

In social-ecological systems (SES), human actions impact ecological processes and the resultant ecological changes create feedbacks that alter the scope and efficacy of future management actions (Liu et al. (2007); Ostrom (2009); Walker et al. (2004)). These coupled systems become increasingly complex when the dynamics of ecological processes do not align with the temporal scale of human decision-making (Cumming, Cumming, and Redman (2006)). Techniques previously used to investigate dynamic ecological processes and responsive decision-making have centered around one or the other, often overlooking the temporal complexity of decision-making (Lippe et al. (2019)). For example, agent based models often use single time-step decision rules rather than allowing for emergent decision strategies that maximize expected rewards over longer time horizons (CITE, CITE). Similarly, exploring both the time horizon of decisions and the rate of ecological processes is impossible using methods that rely on equilibrium analyses, such as dynamic equations (CITE).

Agriculture is a fundamental driver of anthropogenic ecological change (Foley et al. (2005); Foley et al. (2011); Stoate et al. (2009)) and its productivity is closely intertwined with ecosystems processes that provide valuable services presenting. Ecosystem services contribute to productivity of those agricultural activities and are integral to the long time potential of those practices. While adoption of sustainable farm management practices undoubtedly encompasses a continuum of actions and outcomes, suites of practices are often used together in a package, coalescing around distinct stable states or “syndromes” (Andow and Hidaka (1989); Ong and Liao (2020); J. Vandermeer (1997a)). However, the mechanisms driving these bistable patterns have been explained by both ecological (or production) dynamics and the decision functions that are non-monotonic. If either of these systems is approximated as monotonic, the system is necessarily characterized by either a single stable point or is itself monotonic, making alternative syndromes of production impossible to explain with dynamic equations (J. Vandermeer (1997a); J. Vandermeer and Perfecto (2012)). However, ecological processes that result in ecosystem services change over time as the result of sequential decisions. Multistable patterns could feasibly be the results not of complex nonmonotonic approximations, but of temporal interactions of decisions and ecosystem.

While it is increasingly recognized that effectively designing policies to promote agricultural sustainability require interdisciplinary approaches that jointly consider human decision-making and ecological factors (Alberti et al. (2011); Liu et al. (2007)). This paper presents a stylized model of the adoption of diversified agricultural practices (practices that bolster ecosystem services by promoting beneficial agrobiodiversity (Kremen, Iles, and Bacon (2012)) to explore the ecosystem service patterns that result specifically from

interactions between adaptive decision-making and an ever-changing environment. We find a mechanism for bistability, or two prevailing environmental (ecosystem service) states, that is the result not of complex structural assumptions within either the human or ecological system, but rather the rates at which the two systems interact. While our model necessarily simplifies both decision-making and environmental processes, it provides a framework to explore emergent properties in social-ecological systems. We show that our findings have important implications for agricultural policy implementation and social-ecological systems theory.

## Methods

### *Conceptual model description*

We explore the transition to and from diversified farming systems (low and high ecosystem service states) using a Markov Decision Process (MDP) in which a farmer makes a series of decisions about whether or not to employ diversified farming practices over time (Figure 1). In the context of diversified farming systems, diversification practices, such as the use of compost, crop rotation, intercrops, reduced tillage, and cover crops, are distinct from the concept of operational diversification (i.e., simply increasing the range of agricultural goods produced on a given farm). The model was developed through an iterative, collaborative process with an interdisciplinary team comprising plant and soil scientists, agricultural economists, ecologists, agricultural policy experts, social scientists, and farmers with the goal was to capture the core complexities stemming from the coupled human and natural dynamics of the modeled system (Figure 1).

In our model at each time step the farmer takes an “action” of 0% to 100% percent investment in adopting or maintaining diversification practices (Figure 1 A1). The “system state” corresponds to the level of benefit derived from the ecosystem services (Figure 1-A2) that result from those adoption decisions. Benefits may be financial, social, ideological, and/or aesthetic. A greater percent investment in diversification practices corresponds to a greater probability of transitioning to a higher (more beneficial) ecological state in the next year (Figure 1- A3). While higher ecological states are beneficial, investments in diversification practices also come with higher associated costs compared to non-diversified farms (Figure 1). By defining parameter values for cost, benefit, transition stochasticity, ecological change rate, and future discounting (Table 1), we can allow the optimal action strategy for the agent (farmer) to emerge based on expected rewards over either a finite (to represent short-tenure leased farms) or infinite (to represent longer-term leases and land ownership) time horizon (Figure 1 A4).

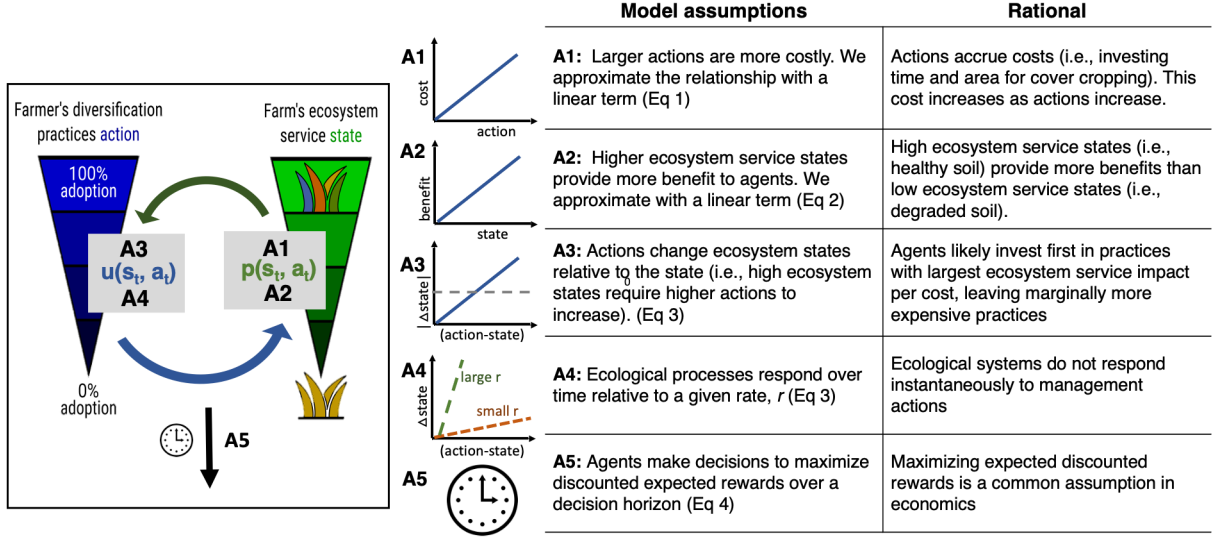


Figure 1: Conceptual diagram and model assumptions. The farmer's choice of how much to invest (time and money) into the adoption of diversification practices (blue), and the resulting ecosystem services state (green), with a more diversified ecosystem state at the top, and a more simplified ecosystem state at bottom. Each time step, the farmer chooses the optimal action for their current ecosystem service state based on the perceived utility function,  $u$ , and state transition probability function,  $p$ . For a given ecosystem service state and action at time  $t$ ,  $p$  describes how the ecosystem responds stochastically to result in an updated state at  $t + 1$ . The updated ecosystem service state then feeds back to influence the farmer's future choices, leading to tradeoffs arising from the coupling of ecological processes with consecutive diversification practice adoption decisions over time. Main model assumptions (A1-A5) are outlined along with the rational for each approximations.

### Mathematical description

The farmer's decision model can be expressed as

$$\max_{\{a_t\}} \mathbb{E} \left[ \sum_t^T u(s_t, a_t) \gamma^t \right]$$

where  $\{a_t\}$  is the set of available actions,  $\mathbb{E}$  the expected utility operator,  $u(s_t, a_t)$  the utility which the farmer associates with being in state  $s_t$  and taking action  $a_t$  at time  $t$ ,  $\gamma$  the myopic discount factor, and  $T$  the land tenure of the farm ( $T \rightarrow \infty$  if the farmer owns the land or has a long lease).

We assume a simple model of the farmer's perceived utility  $u(s_t, a_t)$  as a function of the difference between the cost  $c_a$  associated with diversification practice action  $a_t$ , versus expected benefits  $b_s$  derived from ecosystem state  $s_t$ , at time  $t$ , such that

$$u(s_t, a_t) = b_s s_t - c_a a_t$$

The ecosystem state is also dynamic, evolving according to the transition probability function  $p(s_t, a_t)$ , such that

Table 1: Baseline parameter values

Parameter	Value
Benefit $b$	1.57
Cost $c$	1.00
Noise $\sigma$	0.1
State response rate $r$	0.1
Discount factor $\gamma$	0.97

$$s_{t+1} = p(s_t, a_t) := s_t + r(a_t - s_t) + \epsilon$$

where  $\epsilon \sim N(0, \sigma)$ . This provides a minimal state transition model in which the parameter  $r$  sets the natural timescale at which the ecosystem can respond to changes in land management decisions, and  $\sigma$  defines the width of the state transition probability distribution, capturing the noise inherent to ecological system change. While we have assumed very basic transition and utility functions for this stylized model, in general more complicated nonlinear functions for both the ecosystem state transition and perceived utility are possible using this framework.

#### Parameterization

We have parameterized the model to illustrate the emergence of bistability in SES resulting from agroecological investment decision-making given stochastic ecological responses over time (Figure 1 and Figure 2). We explore a larger parameter space in the supplemental information, and explain why the choice of parameters does not change the main findings.

## Results

### Bistability in ecosystem services

Using the described model, we observe the behavior of agents' sequential choices and the resultant environmental outcomes through time. The decision strategy,  $\pi$ , describes the emergent optimal course of action for a given state and is the stationary optimal state-dependent decision strategy over an infinite time horizon (Figure 2A).

Agents' initial ecosystem states were distributed normally around a mean of  $s = 0.5$ . We find that after following the optimal decision strategy (infinite horizon) for 20 decision cycles, agents have largely settled into two stable ecosystem states, with some farms transitioning to more simplified (lower levels of ecosystem services) farming systems, and others to more diversified (higher levels ecosystem services) systems (Figure

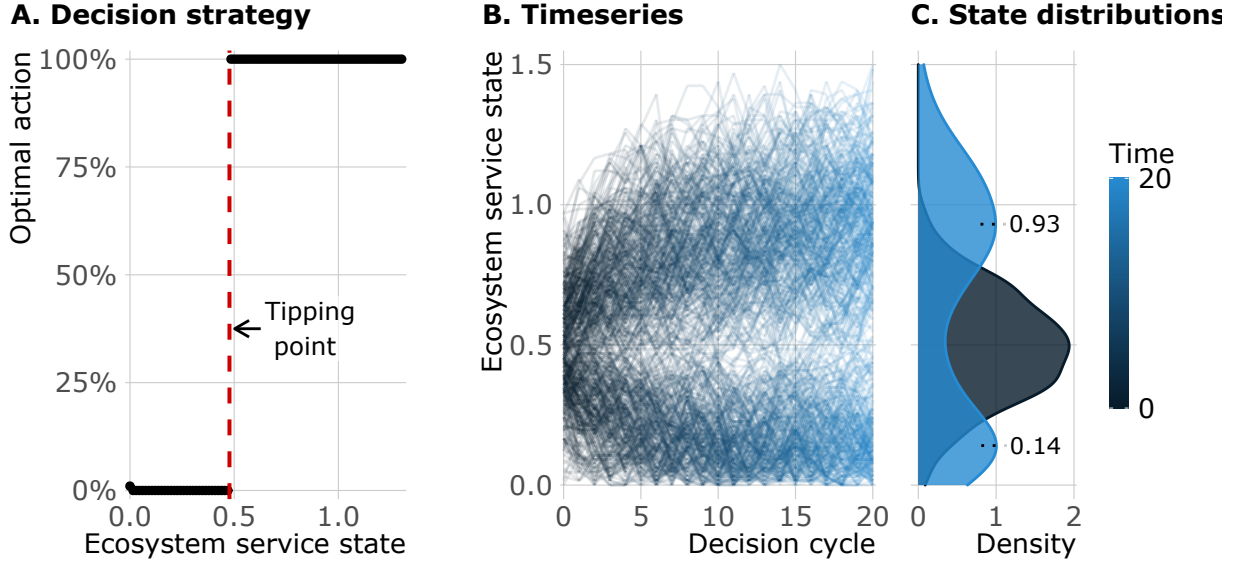


Figure 2: Initial ecosystem states are distributed normally (mean = 0.5; S.D. = 0.2; truncated at  $[0,1]$ ). (A) Agents follow decision strategy  $\pi$  until  $t = 20$ . (B) Ecosystem state of each agent over time (500 simulations). (C) Initial ES distribution (dark blue) and final bimodal distribution at  $t = 20$  (light blue).

2B and 2C). Further, we find strong path dependency, with only 17% of agents who started in a simplified ( $s < 0.5$ ) state concluding in a diversified ( $s > 0.5$ ) state, and only 7% initially in the diversified state transitioning to a simplified state.

#### Importance of temporal dynamics in coupled system trajectories

Our baseline model shows how a simple coupling of human choices and ecological response can result in bistable landscapes of high and low diversification practice adoption and, as a result, high and low levels of ecosystem services (Figure 2). By vary the time horizon of the decision process, the rate of the ecological response, and the cost/benefit ratio, we find that this tipping point disappears when the speed of response of either the ecological system or decision-making process overwhelms the coupling (a proxy for decoupling). Figure 3A shows that with temporal human/environment interactions, there exists a region of cost/benefit ratio within which various bimodal ecosystem state distributions exist (also exemplified in Figure 2). However, when ecological processes become fast enough that the ecosystem responds almost immediately to farmer actions ( $r = 0.95$ ), alternate stable states do not emerge, regardless of cost-benefit ratios (Fig 3C). Similarly, as decisions become temporally myopic (in this case, with a time horizon of 2 decision cycles), the potential for bistability in adoption trajectories disappears (Fig 3B). Only when both a gradually changing environment and a forward-looking decision-maker (i.e. a farmer who takes into account potential benefits over the long term) are coupled, do tipping point phenomena emerge in the decision strategy, leading to two

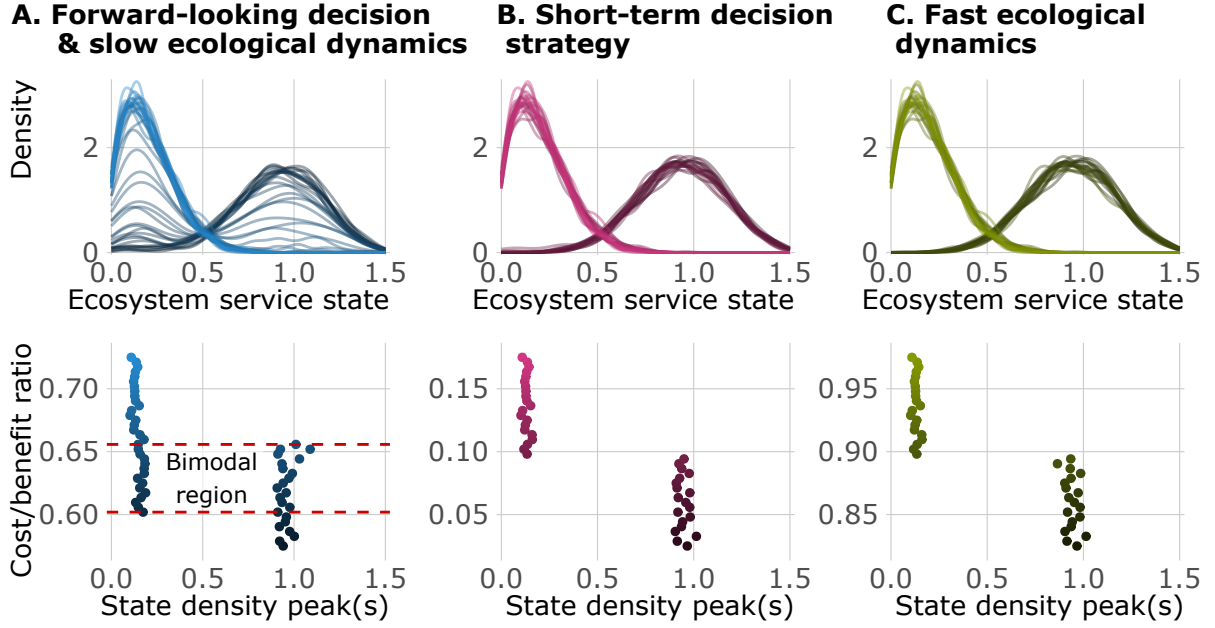


Figure 3: For three scenarios (coupled human/natural system, overly-myopic decision maker, and overly-fast ecological change), cost/benefit ratio was varied incrementally over 40 values, indicated by color shade, across a  $c : b$  range of width 0.15, encompassing the transition between a “never invest” to an “always invest” policy. For each  $c : b$ , 500 replicate simulations were conducted as in Fig 2. Upper plots show distribution of ES state at  $t = 20$  for each  $c : b$ . Lower plots show density curve peak(s). (A) By coupling a forward-looking decision-maker and a slowly-adapting environment, complex dynamics like alternate stable states can emerge. However, with (B) a short-term decision strategy (solving the MDP over a 2-year time horizon), or (C) a fast ecological change rate ( $r = 0.95$ ), no bimodality is observed.

stable ecosystem service states (Fig 3).

#### Implications for agricultural incentive design and land tenure policy

With approximately 39% of U.S. farmland under lease, land tenure is increasingly impacting agricultural management. For example, U.S. corn farmers who rent land are less likely than landowners to implement grassed waterways, strip cropping, contour farming, and conservation tillage (Soule, Tegene, and Wiebe (2000)).

We solve the MDP on a constrained time horizon (20-decision cycles, in comparison to an infinite time horizon in Fig 2), representing the shorter horizon on which tenant farmers often make decisions (Fig 4B). Comparing the final state distribution of the long-tenure (baseline) versus the short-tenure model shows that, as a farmer’s expected land tenure duration decreases, it becomes optimal to reduce diversification adoption across a wider range of ecosystem states. This results in ecosystem state degradation even among farm sites with an initially high ecosystem service value, with 94% of farmers ending up in the simplified state at  $t = 20$ .

While land tenure impacts the temporal horizon of land-use decisions, incentives that shift cost-benefit structures influence management practices and have become an integral part of farming over the past

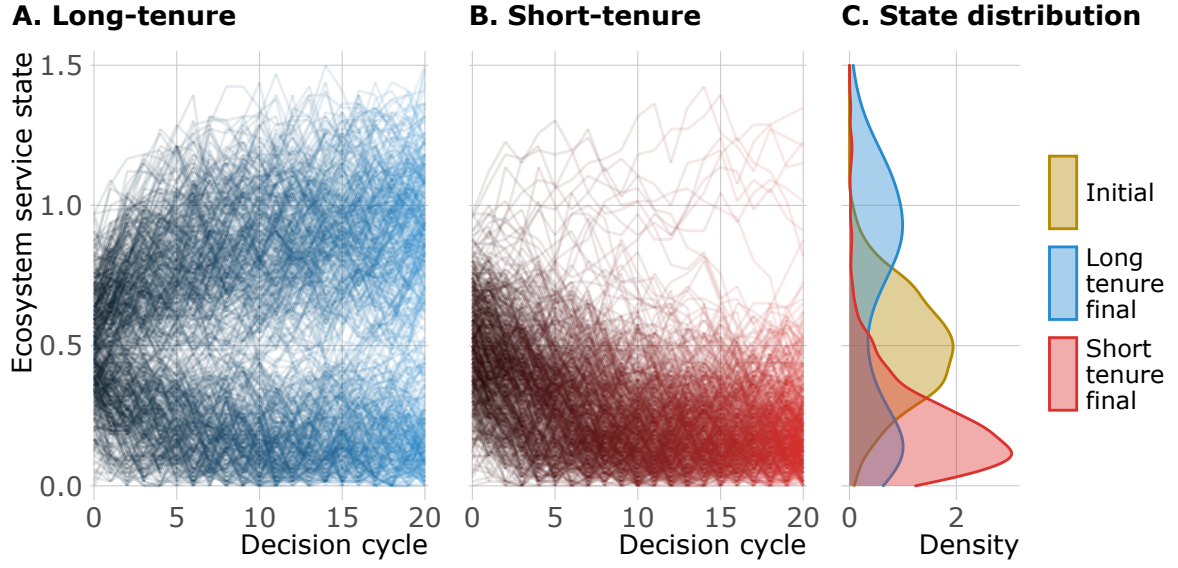


Figure 4: The simulation is identical to that in Fig 2, but the MDP is solved under a finite, 20-year time horizon. (A) Result of short land tenure on ES state over time. (B) Comparison between final state distribution of short- vs. long-tenure model runs.

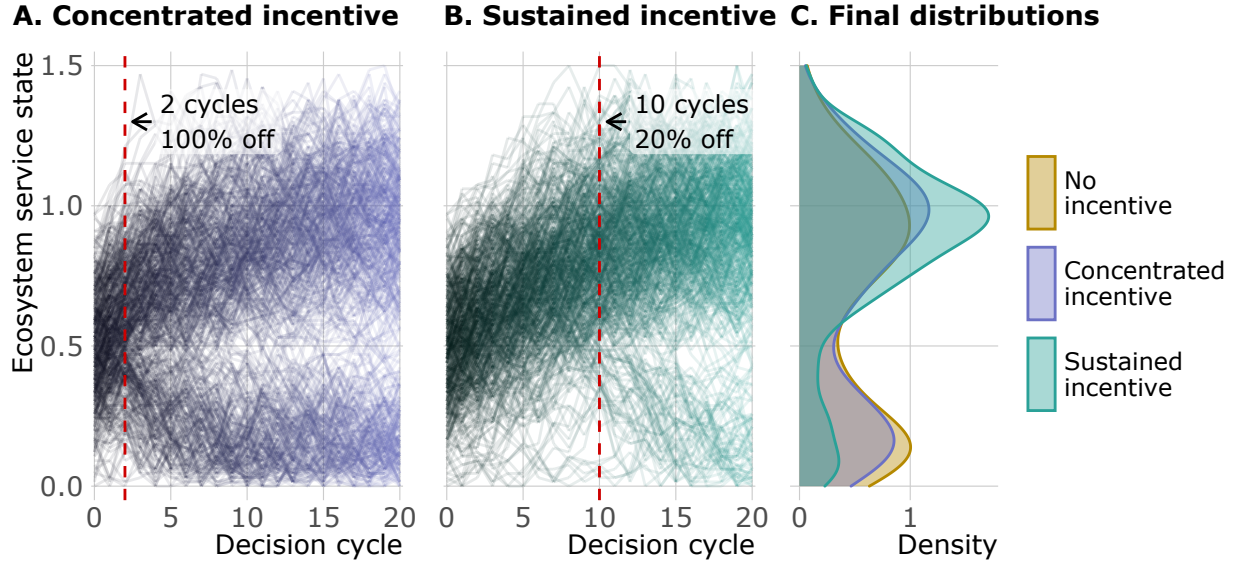


Figure 5: Starting from the same initial states as Fig 2, ES state timeseries are shown for (A) a large, abrupt incentive (100% of adoption expenses are covered for two years) vs. (B) a smaller, more sustained incentive (adoption cost is 80% of baseline for 10 years). Ignoring discounting, both packages have the same total cost to the funder (the equivalent of 2 years' worth of full adoption cost offsets). After the incentive period, agents adjust their decision rules to that of the base case (i.e. no incentive) until  $t = 20$ . (C) Shows that the sustained incentive ultimately drove more DP adoption.



half-century (Batáry et al. 2015; Graddy-Lovelace and Diamond 2017). We explore the impact of incentive duration on the efficacy of policies to promote adoption of diversification practices by implementing two competing publicly funded incentive schemes: a short-term (two-time step) incentive which fully covers the cost of adoption, versus a longer-term (ten-time step) incentive which only partially offsets the adoption costs over those time steps. Formally, the cost of each incentive package is equal. Within the model, agents adapt their optimal decision strategy for the given cost-benefit ratio during the incentive period, and at its conclusion they revert to the baseline strategy (i.e. without payments).

We find longer, more sustained incentive programs to be more effective at encouraging adoption behavior over the critical threshold toward diversified farming (Fig 5). Once a farmer has crossed the viable ecosystem state threshold, it becomes less likely that they will return to simplified systems, even after incentives are removed. Because it takes a series of investment actions for the ecosystem service state to cross the investment threshold, longer-term incentives ultimately result in more diversification practice adoption.

## Discussion

Our analysis suggests a mechanism for bistability in social-ecological systems that is the result of temporal interactions between forward-looking decisions and ecological processes rather than complex structural assumptions about either system alone (Figure 6 P1). While alternate stable states within social ecological systems, and farming systems in particular, have been previously explored and observed (Horan, Fenichel, Drury, et al. (2011b); J. Vandermeer (1997b); J. H. Vandermeer and Perfecto (2012)), our results shed light specifically on temporal feedbacks that might contribute to this pattern (Figure 6 P2). We show how this mechanism provides novel insights not only for social-ecological research (Fig 3), but also for agricultural policy (Fig 4 and Fig 5).

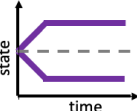
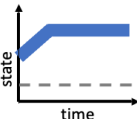
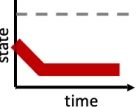
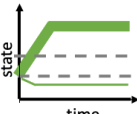
	Model predictions	Evidence in support of pattern	Value added
P1	 <p><b>P1:</b> Bistability in ecosystem states (ecosystem services) can emerge without complex structural assumptions about nonmonotonic cost structures or ecological dynamics (Fig 2)</p>	<b>E1:</b> Syndromes of production, or bistable patterns in the adoption of agricultural practices, have been both empirically and theoretically described (Vandermeer 2012, 1997)	<b>V1:</b> These patterns have historically been explained by complex non-monotonic assumptions that do not hold true in many systems
P2	 <p><b>P2:</b> As ecological processes become infinitely “fast” (in their response to management actions) bistability under simple assumptions no longer emerges.</p>	<b>E2:</b> Agricultural inputs that provide immediate benefits are not generally thought to display bistable patterns of adoption under a given condition.	<b>V2:</b> Considering the temporal component of ecological response to management is important for policy design (V4)
P3	 <p><b>P3:</b> Decision making over short time horizons decreases investment in ecosystem service promoting activities (Fig 4) and removes bistability as decision horizons become short (Fig 5B)</p>	<b>E3:</b> U.S. corn farmers who rent land are less likely than landowners to implement grassed waterways, strip cropping, contour farming, and conservation tillage	<b>V3:</b> Dynamic equilibrium models or hard-coded decisions in agent-based models do not explore the impact of decision horizons.
P4	 <p><b>P4:</b> Longer, more sustained incentive programs are more effective than short term incentive programs at encouraging adoption of processes with benefits that accrue slowly</p>	<i>(this is a model result that displays value of using these methods)</i>	<b>V5:</b> Effective policy design requires consideration of the temporal dynamics of decisions and ecosystem services.

Figure 6: Table of the four main model predictions, evidence in support of the pattern, value added of the temporal mechanism and minimal assumptions.

Policies designed to promote agricultural sustainability and ecosystem service in response to stressors such as climate change or soil degradation can have unintended consequences because when designed without explicit consideration of the feedback between human decision-making and ecosystem states. Our results suggest that long-term, sustained incentives, even when only partially covering the cost of adoption, may be more effective in shifting farmers from simplified ecological states to diversified states than more concentrated short-term incentives (Fig 6 P4). We show that the cost of interventions and the social-environmental benefit of those interventions are not necessarily equivalent. Rather, perceived stability of incentive programs over time may be an important driver of adoption, which can be overlooked if the temporal rates of coupled dynamics in social-environmental systems are not considered. This is particularly relevant to government payment programs and suggests that payments can be highly effective in encouraging adoption of diversification practices (or other ecosystem service promoting practices) when implemented over long time horizons. While the possibility of a policy discontinuation may contribute to the lack of impact for short-term incentives, reduced transaction costs that come with farmers making a longer-term commitment may also partially explain the greater impact of sustained incentives as compared to concentrated incentives.

In addition to incentive policies, our analysis shows how secure land tenure can impact decision strategies and consequently is integral to increasing the adoption of diversified farming practices. This finding complements sociological research documenting how security and length of land tenure affects adoption of

sustainable agricultural practices (Fraser (2004); Long et al. (2017); Richardson Jr (2015); Soule, Tegene, and Wiebe (2000)). Policies that increase land tenure duration, such as regulating lease agreement terms, providing low interest loans, or promoting stable farm succession plans, may represent a key lever to enable farmers to adopt more diversified agroecological practices.

By conceptualizing social environmental systems through lens, we offer new insights into important agricultural patterns. We present a flexible model framework that can be built on to address numerous questions in social-ecological systems research and policy design. Expanding the boundaries of the model to include the effect of other structural factors, such as agricultural regulations and network structures, could expand the scope of questions explored.

## Model implementation

The model was developed in the *R* programming language (R Core Team 2019). The *MDPtoolbox* library was used to set up and solve the MDP (Chades et al. 2017), *tidyverse* for data analysis (Wickham et al. 2019), and *ggplot2* to generate all figures (Wickham 2016). Code for our model and the experiments conducted in this paper is available freely at <https://github.com/boettiger-lab/dfs-mdp>.

## Author Contributions:

Conceptualization CB, MC, SW, PB, TB, LC, FC, KE, SG, AI, DK, CK, JL, EO, JO, MR, AS, JT, HW; Data curation: MC, SW, CB; Formal Analysis: MC, SW, CB; Funding acquisition: TB, AI, CK, DK, CB; Methodology: CB, MC, SW, PB, TB, LC, FC, KE, AI, DK, CK, EO, JT, HW; Code: MC, SW, CB; Visualization: MC, SW, CB; Writing – original draft: MC, SW, CB, LC; Writing – review & editing: CB, MC, SW, PB, TB, LC, FC, KE, SG, AI, DK, CK, JL, EO, JO, MR, AS, JT, HW

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