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# Modelling Energy-Aware Task Allocation in Mobile Workflows

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#### Rise of the Smart-Devices (Battery Limited)

	Nokia 8310, Ericsson T68,		830mAh 650mAh	
2003	Sony Ericsson P900:	156MHz	1000mAh	
2005	Nokia N91,	220 MHz	900mAh	
	Blackberry 8800: iPhone 1:	312MHz, 412MHz,	1400mAh 1400mAh	9:41
	HTC Hero: Palm Pre:	528MHz, 600MHz,	1350mAh 1150mAh	
	Sony Z1: iPhone 5S:	Quad-Core 2.2GHz, Dual-Core 1.3GhZ,	3000mAh 1560mAh	2.5
		(iPad Ai	r 8820mAh)	5 ¥ G



### **Battery Management Tools**

#### Hardware

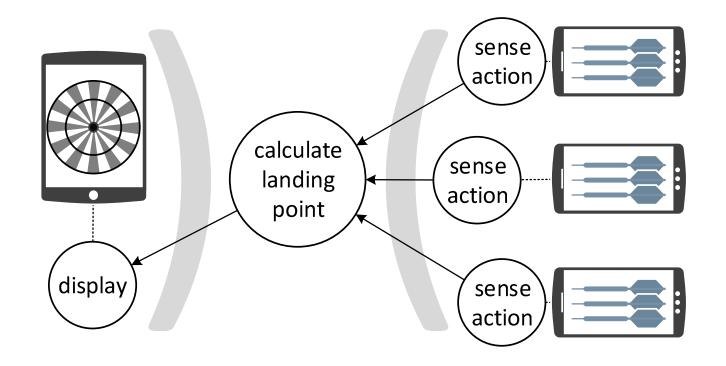
- Fast Charging
- Energy-Efficient Processors, Displays
- New Chemical Compound?

#### Software

- Energy Profiling
  - PowerTop, Trepn Profiler, PowerTutor, AppScope, etc.
- Workload Offload
  - Cuckoo, CloneCloud, MAUI, etc.

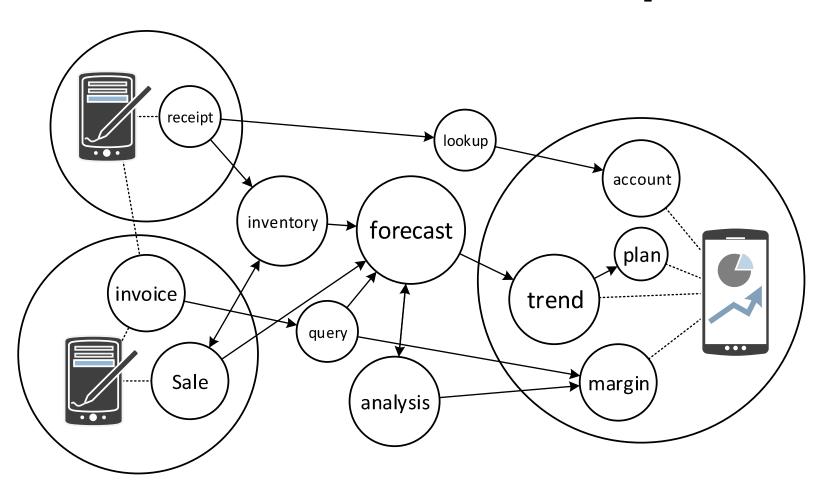


### **Mobile Workflow Example 1**





### **Mobile Workflow Example 2**



#### **Energy Model**

Given an allocation scheme  $\psi: T \to M$ , we first derive the energy cost of computing  $t_a, a \in \{1, \dots n\}$  to be

$$\mathcal{E}_{a\psi(a)}^{cmp} = e_{\psi(a)}^{cmp} \times \frac{c_a}{s_{\psi(a)}} \tag{1}$$

where  $\psi(a)$  is the device to which  $t_a$  is assigned. Secondly, we have the energy cost of transferring  $d_{ab}$ ,  $(t_a, t_b) \in R$  as

$$\mathcal{E}_{ab\psi(a)\psi(b)}^{tran} = \underbrace{e_{\psi(a)}^{snd} \times \frac{d_{ab}}{b_{\psi(a)\psi(b)}}}_{\text{sender's cost}} + \underbrace{e_{\psi(b)}^{rcv} \times \frac{d_{ab}}{b_{\psi(a)\psi(b)}}}_{\text{receiver's cost}} \tag{2}$$



#### **Formulation**

To represent an allocation scheme  $\psi$ , we first construct an  $n \times m$  binary matrix  $X = (x_{ai})$ , such that

$$x_{ai} = \begin{cases} 1 & \text{if } \psi(a) = i, \\ 0 & \text{otherwise.} \end{cases}$$
 (3)

We call matrix X an **assignment matrix** and a **valid** assignment must satisfy the following constraints

$$\sum_{i=1}^{m} x_{ai} = 1, \quad a = 1, 2, \dots, n,$$
(4)

$$x_{ai} \in \{0,1\}, \quad a = 1,2,\ldots,n, \quad i = 1,2,\ldots,m.$$
 (5)



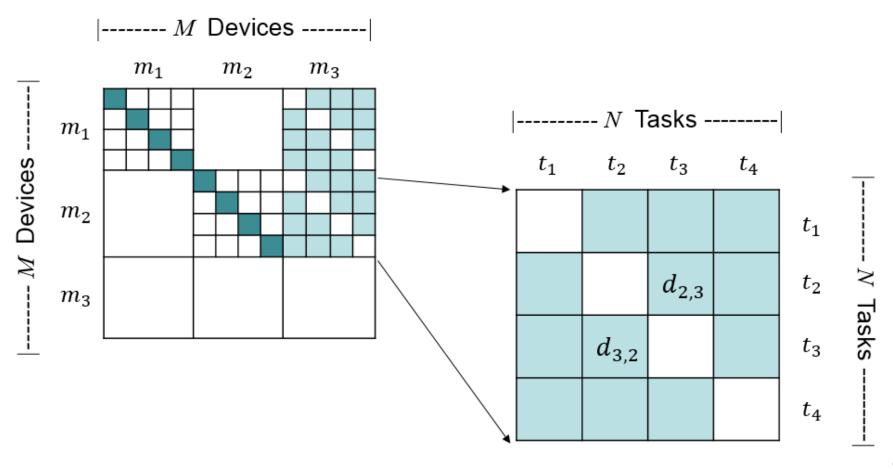
### Formulation (cont.)

Let coefficients  $q_{aibj}$  be the entries of an  $mn \times mn$  matrix Q, such that  $q_{aibj}$  is on row (i-1) n+a and column (j-1) n+b, and  $x = vec(X) = (x_{11}, x_{12}, \ldots, x_{1n}, x_{21}, \ldots, x_{mn})^T$  be the vector formed from the columns of X. Equivalent formulations for the minimum workflow energy cost problem's objective function are given by (8) and

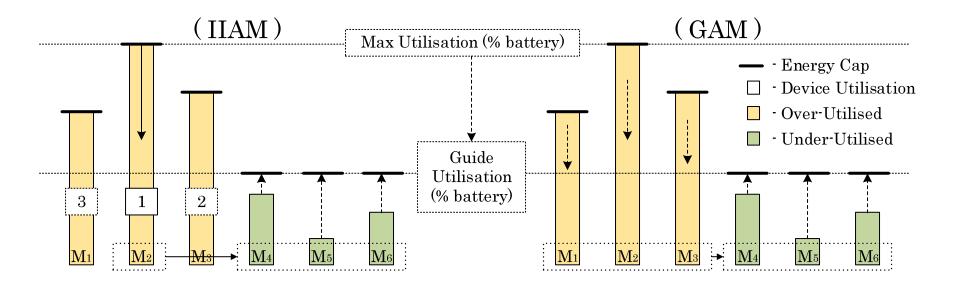
$$vec(X)^T Q vec(X)$$
 (9)



### Coefficient Matrix Q



### **Adjustment Algorithms**



#### **Simulation Definition**

#### Definition 3.

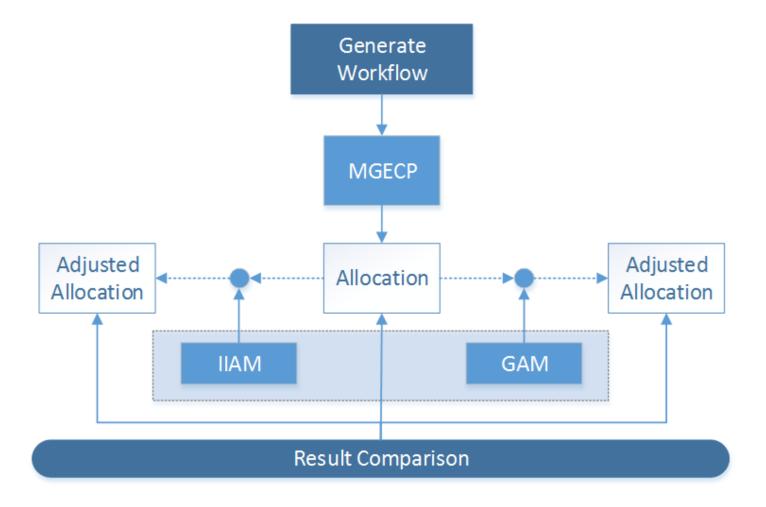
A **typical mobile device** has a battery capacity of 2000mAh, draws a current of 250-400mA during data transmission and 100-200mA when executing local computation tasks.

#### **Definition 4.**

A task has a **unit workload** if its execution takes 1 second to complete on a typical device.



### Simulation Definition (cont.)





#### **Simulation Results**

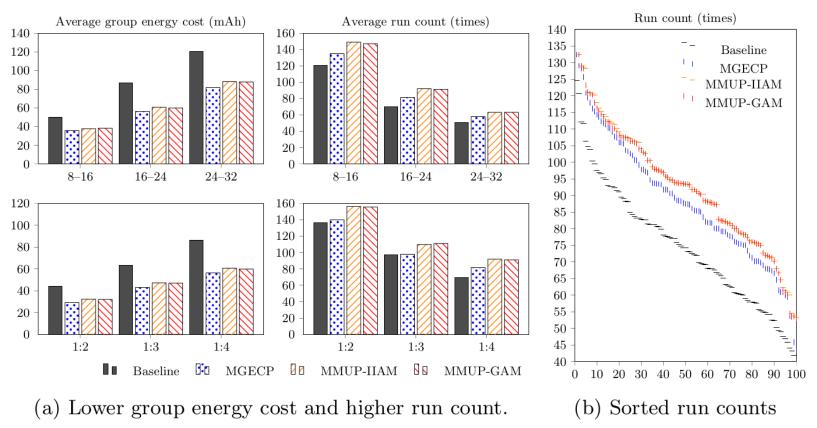


Fig. 3: Reduction in group energy cost and increase in workflow run count



#### **Simulation Results**

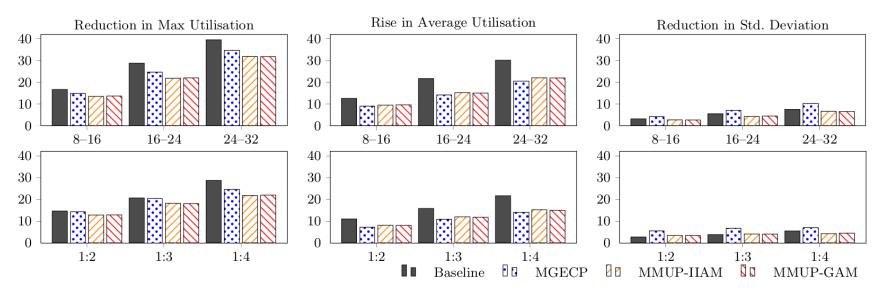


Fig. 4: Effect of adjustments within the MP.



## Summary

- Energy Cost Model
- Formulate Optimisation Problems
- Adjustment Algorithm
- Verified by Simulation

# Thank you



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