

SPATIALLY VARIABLE DECONVOLUTION FOR LIGHTSHEET MICROSCOPY

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LIGHTSHEET MICROSCOPY

Light sheet microscopy is a type of fluorescence microscopy used in cell biology due to its fast acquisition times and low photo-damage to the sample. This is achieved by selectively illuminating a slice of the sample using a sheet of light and detecting the emitted fluorescence signal using a dedicated objective orthogonal to the plane of the sheet.

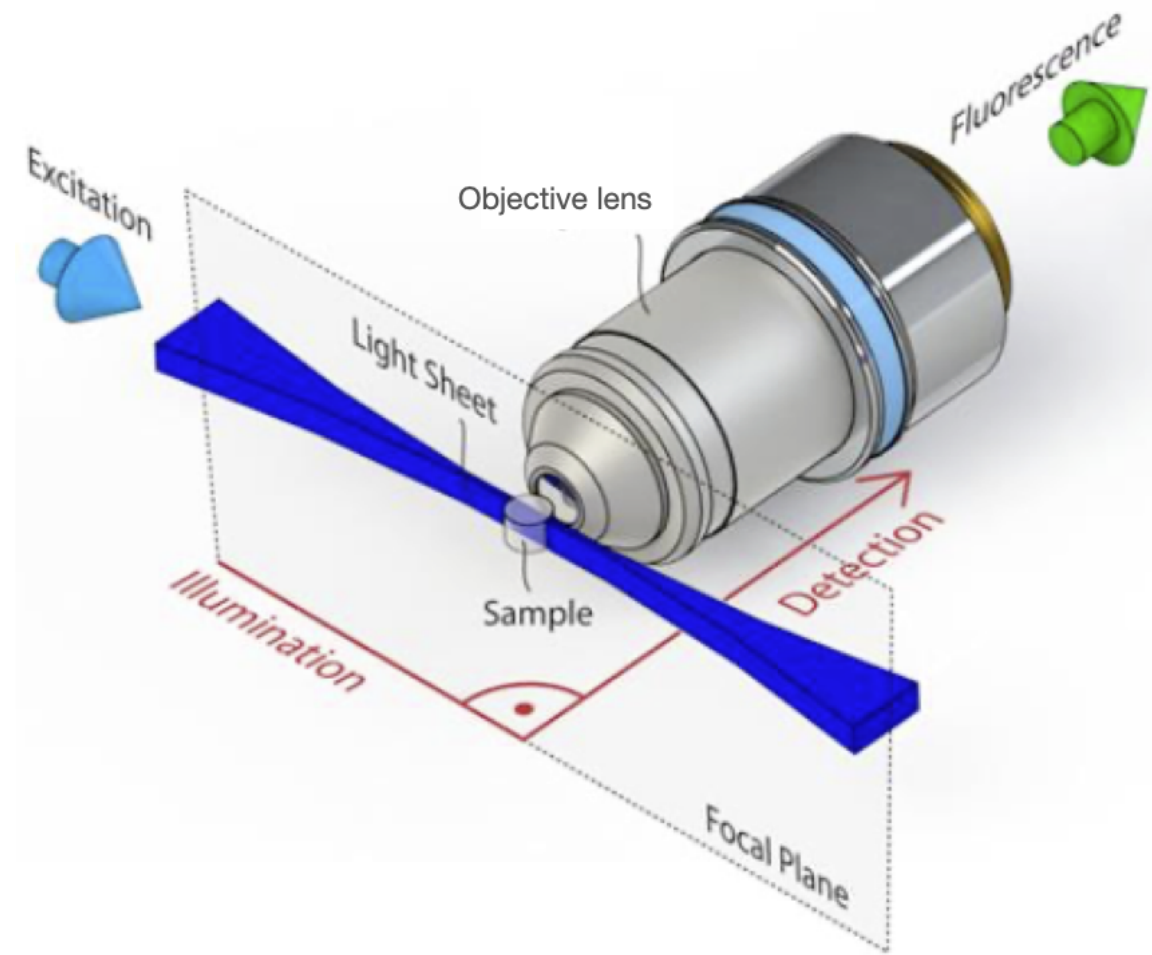
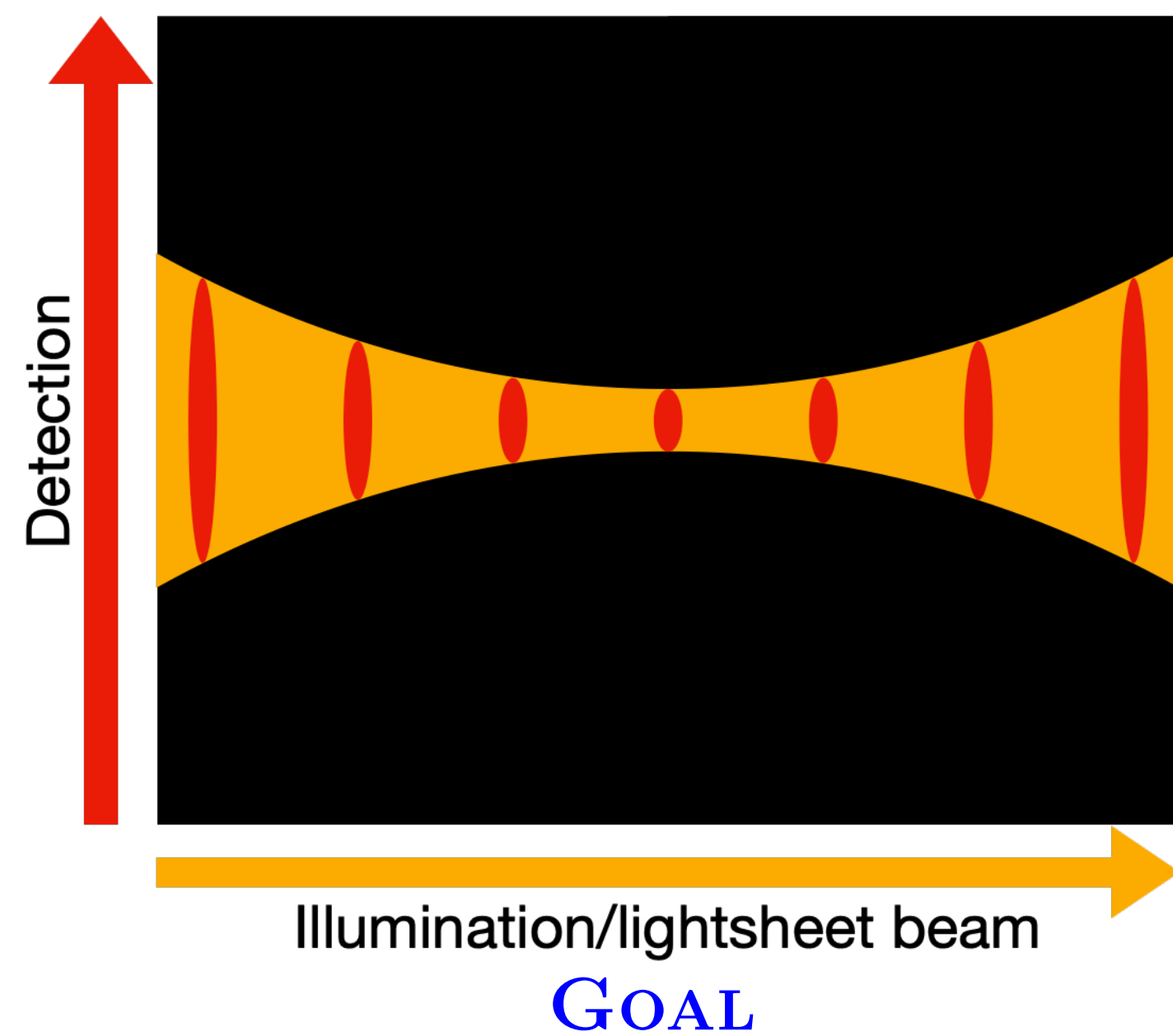


Figure credit: Jörg Ritter, PhD thesis (2011)

SPATIALLY VARYING PSF



PROBLEM

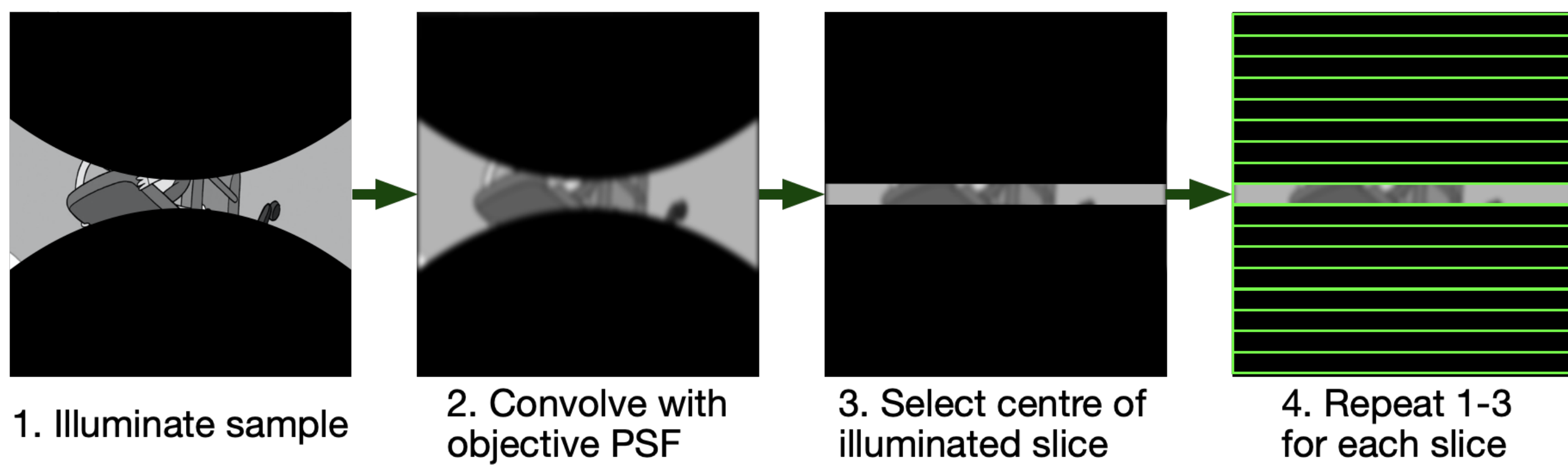
Due to the interaction of the lightsheet beam and the detection/objective point spread function (PSF), the effective PSF of the system is spatially varying, and therefore standard deconvolution approaches are not applicable.

GOAL

In this work, we propose a model for image formation that describes the interaction between the illumination PSF and the detection PSF which replicates the physics of the microscope while leading to a tractable inverse problem.

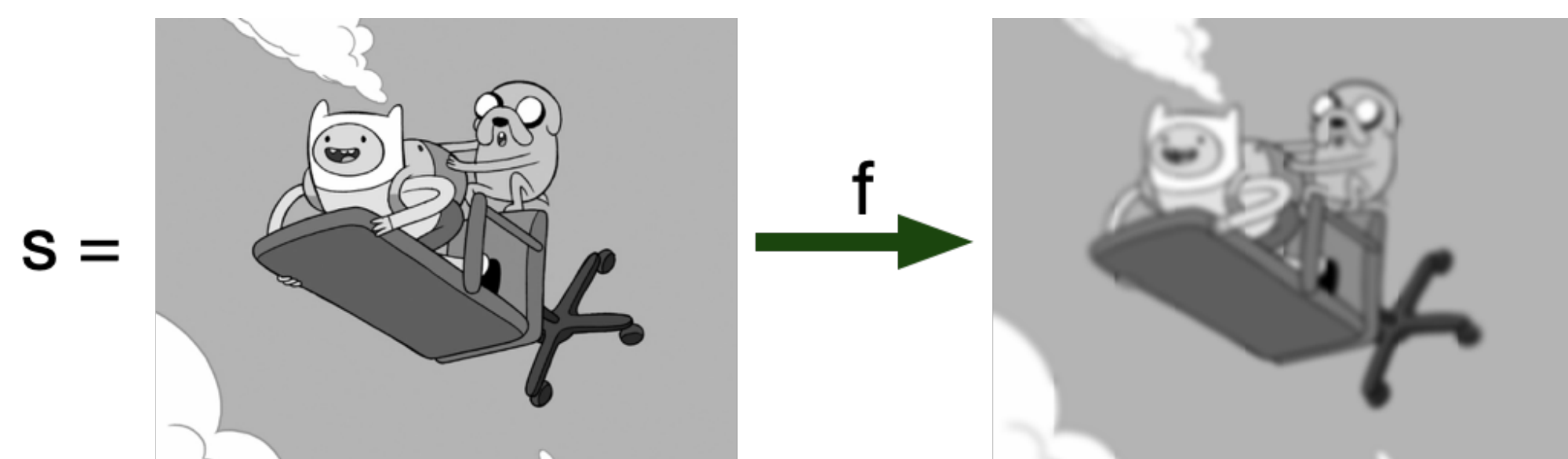
IMAGE FORMATION MODEL

The sample s illuminated at $z = z_0$ by the light-sheet l and the photons are collected by an objective with PSF h :



$$f(x, y, z_0) = \iiint l_{avg_y}(u, v, w) s(u, v, w - z_0) h(x - u, y - v, w) du dv dw \quad (3)$$

where h is the detection PSF, calculated using (1) and l_{avg_y} is the light-sheet, calculated by averaging the beam PSF obtained in a similar way to h , without Zernike polynomials.



PSF MODEL

The detection PSF h is modelled as the Fourier transform of the pupil function multiplied by defocus [3]:

$$h(x, y, z) = \left| \iint g_\sigma * p(\kappa_x, \kappa_y) e^{2i\pi z \sqrt{(n/\lambda)^2 - \kappa_x^2 - \kappa_y^2}} e^{2i\pi(\kappa_x x + \kappa_y y)} d\kappa_x d\kappa_y \right|^2 \quad (1)$$

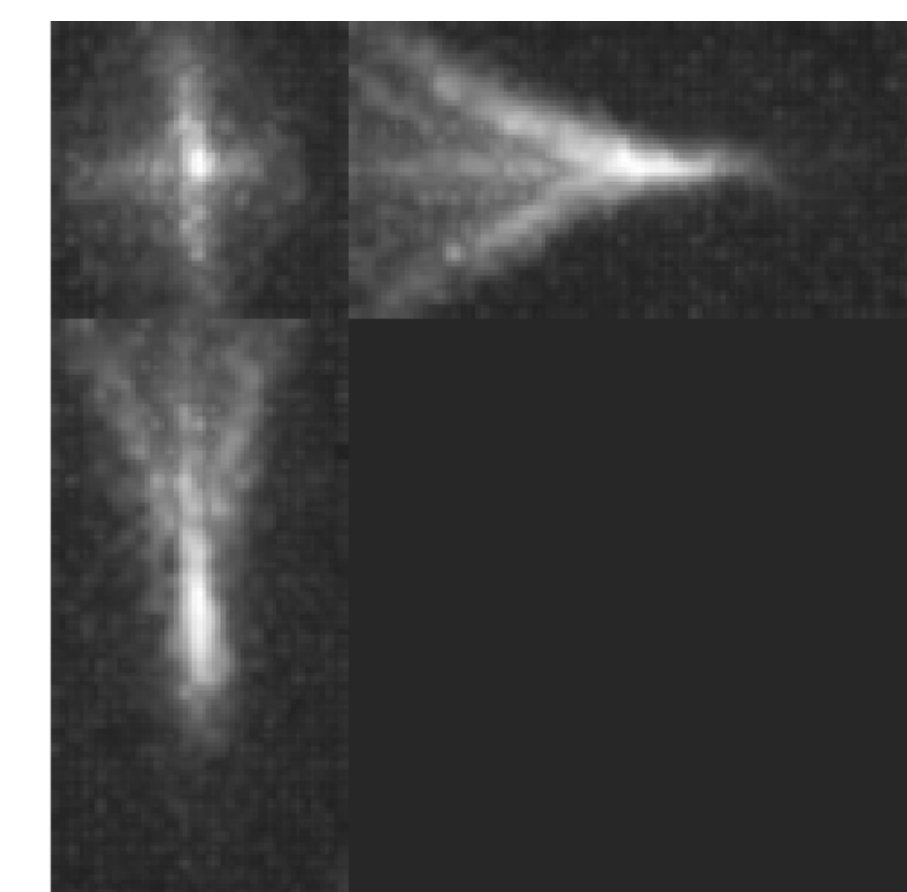
where p is the pupil function, defined as

$$p(\kappa_x, \kappa_y) = \begin{cases} e^{2i\pi \sum_{j=1}^{15} c_j Z_j(\kappa_x, \kappa_y)} & \text{for } \rho = \sqrt{\kappa_x^2 + \kappa_y^2} \leq NA/\lambda, \\ 0, & \text{otherwise.} \end{cases} \quad (2)$$

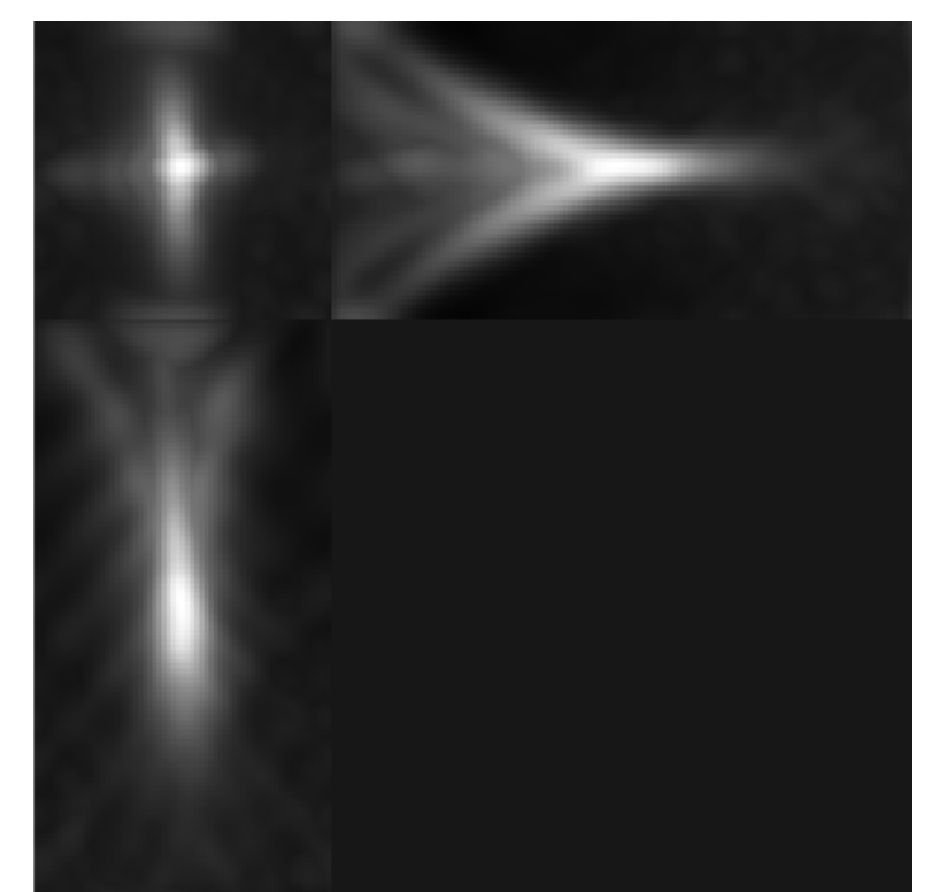
where the phase of the pupil function is computed by least-squares fitting of the coefficients of the first 15 Zernike polynomials using an image of a bead.

The parameters of the model are given by the experimental setup used to acquire the image:

- n - refractive index
- λ - wave length
- NA - numerical aperture
- g_σ Gaussian blur to take into account other properties not accounted for in our model



Bead image (MIP)

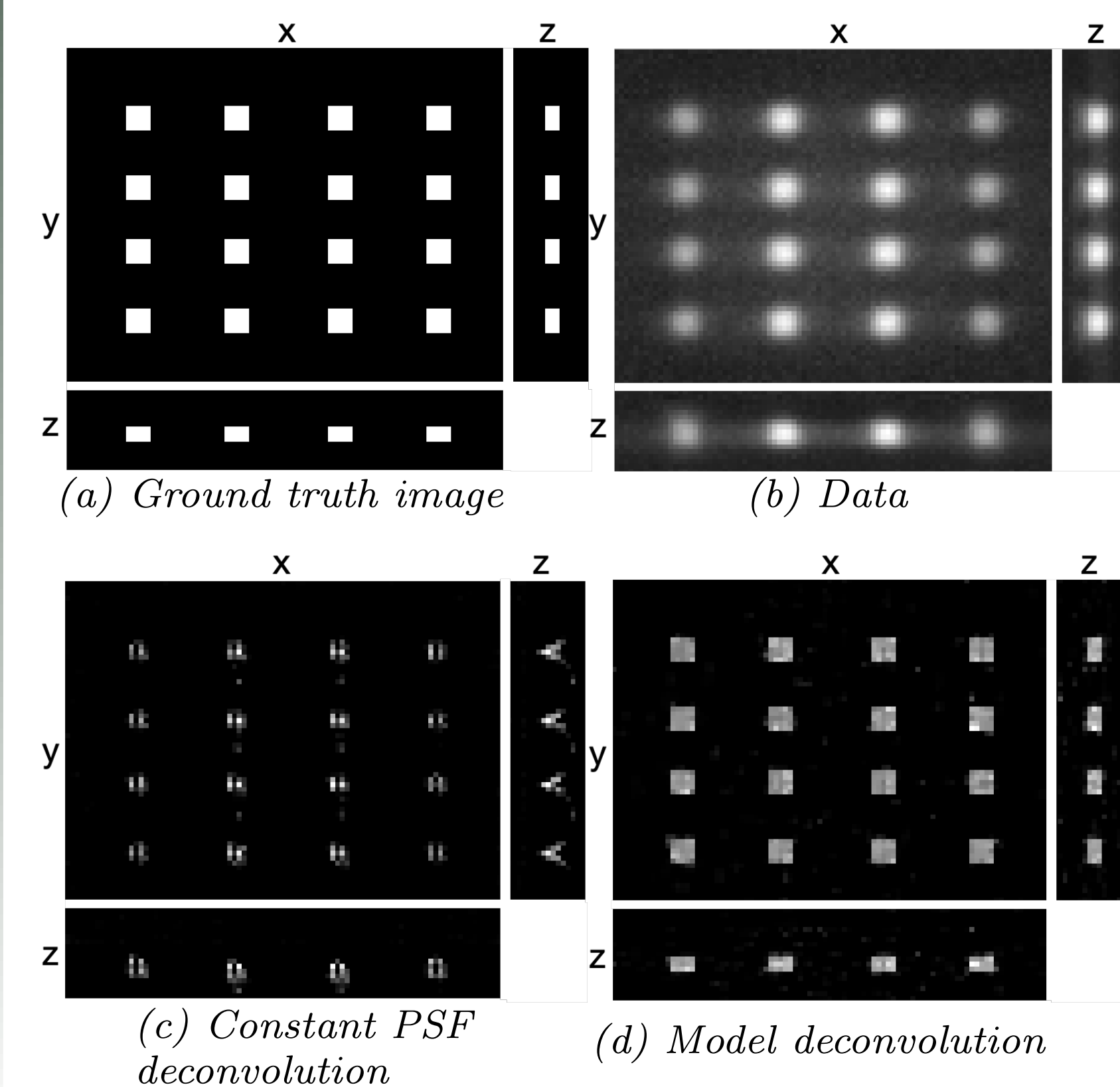


Estimated detection PSF (MIP)

RECONSTRUCTION

Let \hat{f} be the image data with Gaussian noise and $f(s)$ the result of applying the forward model (3) to the sample s . To recover s , we solve:

$$\text{Find } \hat{s} \in \operatorname{argmin}_s \left\{ \|\hat{f} - f(s)\|_{L_2} + \lambda TV(s) \right\}$$

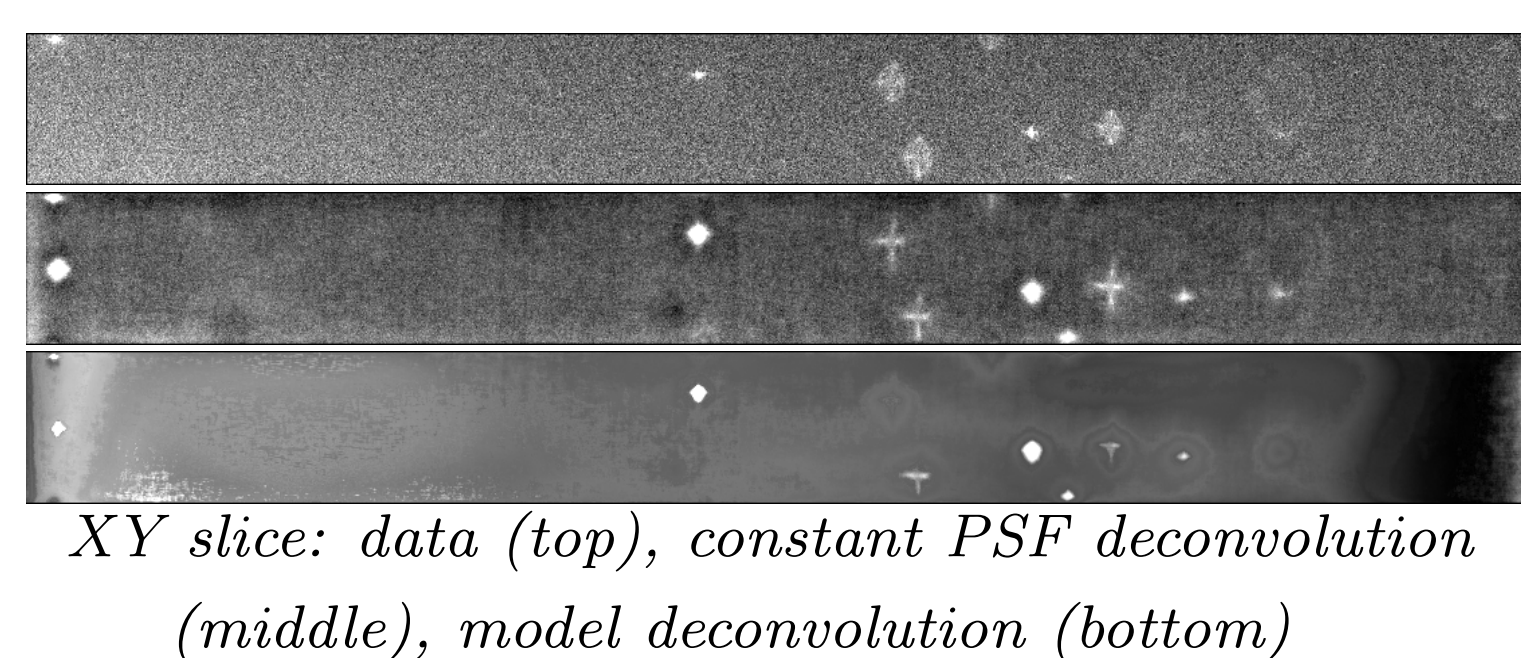


- We use the total variation regulariser $TV(s)$ and ℓ_2 fidelity term due to the Gaussian noise in the data.
- To solve the optimisation problem, we apply a version of the Primal Dual Hybrid Gradient (PDHG) algorithm from [1, 2].
- In the figure on the left, we show an example of a simulated sample (a) to which we apply the forward model with Gaussian noise (b) and the result of deconvolving using only a spatially varying PSF (c) and the full forward model (d).
- The images are shown using maximum intensity projection.

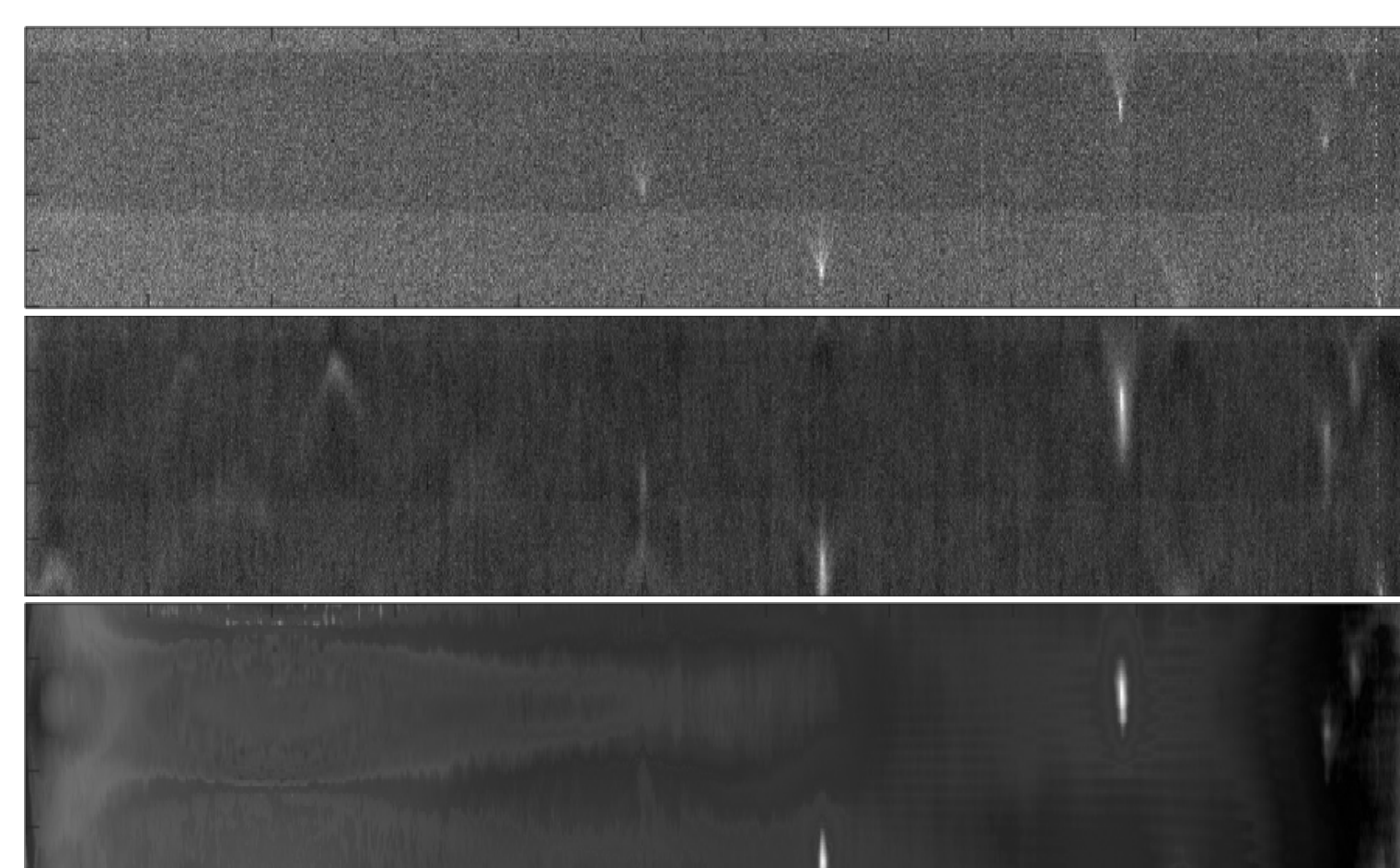
RESULTS

BEADS

- We apply the proposed method to a sample of beads in agarose.
- The dimensions of the sample are 1127 x 111 x 100 pixels.
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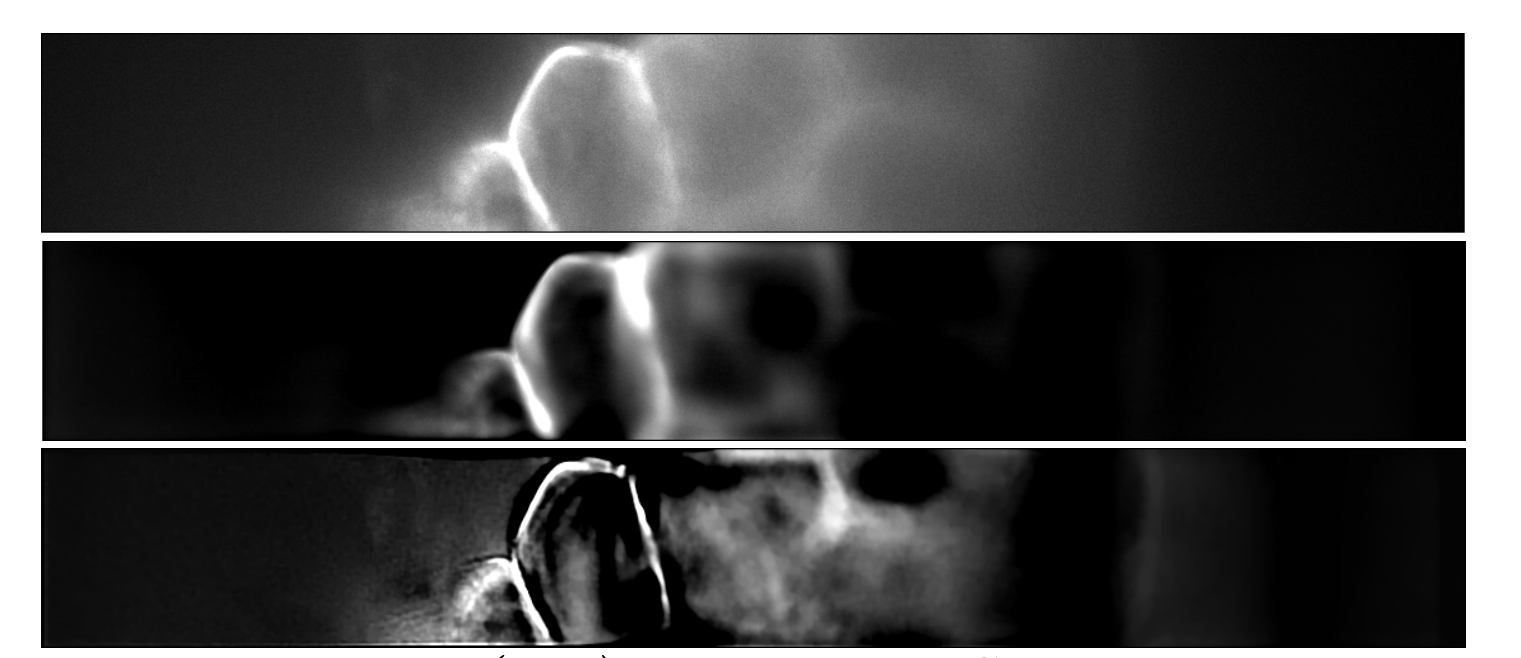
XY slice: data (top), constant PSF deconvolution (middle), model deconvolution (bottom)



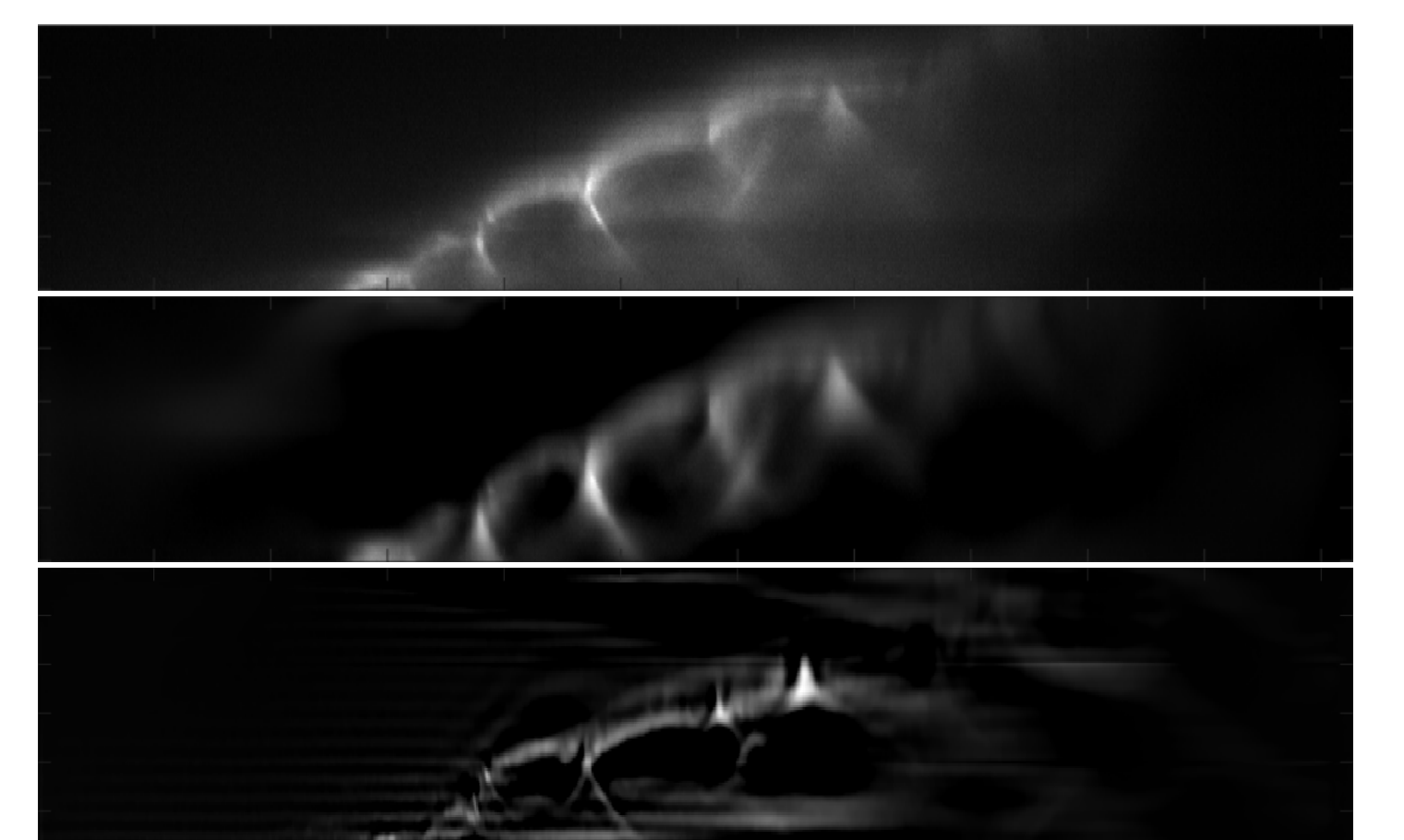
XZ slice: data (top), constant PSF deconvolution (middle), model deconvolution (bottom)

MARCHANTIA

- We apply the proposed method to a sample of Marchantia plant.
- The dimensions of the sample are 1127 x 155 x 100 pixels.
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XY slice: data (top), constant PSF deconvolution (middle), model deconvolution (bottom)



XZ slice: data (top), constant PSF deconvolution (middle), model deconvolution (bottom)

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ACKNOWLEDGMENTS

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