

# Middleman Finance and Product Market Distortions

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Jan 12, 2026

# Middlemen as Liquidity Providers

Middlemen, who purchase goods from suppliers and sell to consumers, provide liquidity support to suppliers.

Historically, middlemen and liquidity provision were closely related:

- ▶ *Colonial Trade*: The Dutch East India Company extended credit to local growers in the form of advanced payments
- ▶ *Input Financing*: Middlemen provide seeds, fertilizers, and farming equipment to small farmers

Nowadays, with advances in financial technologies, financing suppliers has become increasingly critical for middlemen, e.g., Walmart, Amazon, JD.com, etc.

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# The Co-op Partners with PrimeRevenue to Protect Suppliers Amid Economic Volatility



By [PrimeRevenue](#) • 4 minute read

*UK's sixth largest food retailer makes strategic transition to PrimeRevenue platform*

**Atlanta, GA – Manchester, UK, August 11, 2020** – PrimeRevenue, the leading platform for working capital finance solutions, and The Co-operative Group, today announce a new supply chain finance partnership. Barclays Bank PLC, who introduced The Co-op to PrimeRevenue, will be providing funding on the supply chain finance programme followed by other financial institutions as the programme grows.

Co-op has made the strategic decision to partner with PrimeRevenue for its new supply chain finance offering. Fueled by a highly challenging business climate heightened by the pandemic, the company aims to offer suppliers a simple method of early payment to help with their cash flow without having a detrimental impact to Co-op's own cash position. This is particularly relevant in the current environment where the old adage "cash is king" has never been truer.

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3. **Middlemen set product prices.** Upstream liquidity provision is linked to downstream pricing.

## Research questions:

- ▶ What are the economic rational behind **trade credit extension** and **supplier selection**?
- ▶ How does middleman finance affect retail prices and product market efficiency?

# Related literature

- ▶ Intersection of IO and Corporate Finance
  - ▶ Nocke & Thanassoulis JEEA 2014: Downstream financial constraint leads to risk-sharing between buyer and seller firms, resulting in double-marginalization.
- ▶ Multi-product Intermediaries
  - ▶ Rhodes, Watanabe & Zhou JPE 2021
  - ▶ Liquidity provision and intermediaries' retail advantages
- ▶ Diamond-Dybvig model and Trade Credit
  - ▶ Petersen & Rajan RFS 1997; Burkart & Ellingsen AER 2004; Cunat RFS 2007;
  - ▶ Reallocation of trade credit among suppliers

# 1. The Benchmark Model

# Agents

- ▶ A mass of suppliers:
- ▶ A mass of consumers:
- ▶ One intermediary:

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  - ▶ Each produces a unique and indivisible good
  - ▶ Constant marginal costs,  $c \in [\underline{c}, \bar{c}]$ , differ among suppliers
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  - ▶ trade surplus is split equally:  $p - c = (u - c)/2$

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# Trade and Liquidity Shocks

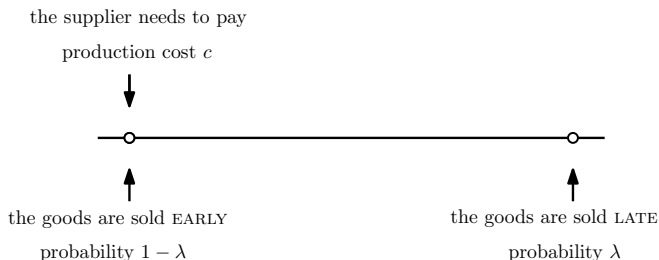
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- ▶ Suppliers face no liquidity issue in the textbook
  - ▶ retail revenue can be used to cover costs  $c$
- ▶ Supplier's liquidity issue matters when:
  - ▶ disparity exists in the timing between production and trade.



# Trade and Liquidity Shocks



- ▶ Two sub-periods: **early** and **late**
  - ▶ production occurs only in the **early** sub-period
  - ▶ suppliers may match with consumers **early or late**
- ▶ Prob.  $1 - \lambda$ : consumers arrive early,  $c$  can be paid by revenue
- ▶ Prob.  $\lambda$ : consumers arrive later,  $c$  can not be covered using revenue
- ▶ It is one micro-foundation for generating liquidity shocks.

# Ex ante heterogeneity of suppliers

- Suppliers are indexed by

$$(\lambda, c) \in \Omega = [0, 1] \times [\underline{c}, \bar{c}],$$

where  $\lambda$ : prob. of liquidity shock;

$c$ : marginal cost.

- The pair  $(\lambda, c)$  of each supplier is **publicly observable**.
- $(\lambda, c)$  follows some C.D.F.  $G(\lambda, c)$ .

# Intermediary

The intermediary selects suppliers into either mode:

- ▶ Middleman mode (M): pure middleman
- ▶ Finance mode (F): middleman *plus* liquidity provider

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Middleman matching advantage:

- ▶ The intermediary sells on behalf of suppliers
- ▶ prob. of liquidity shocks decreases to  $m \cdot \lambda$
- ▶  $m < 1$ : middlemen's matching advantage (Rubinstein and Wolinsky 1987)

## Middleman Mode (M)

- ▶ The intermediary gives Take-It-Or-Leave-It (TIOLI) offers:
  - ▶ Supplier pays  $c$  by himself;
  - ▶ Intermediary makes a transfer  $f_M(\lambda, c)$  **upon receipt of consumer payment.**
- ▶ Supplier  $(\lambda, c)$  contributes profit:

$$\begin{aligned}\pi_M(\lambda, c) &= (1 - m\lambda)p - \underbrace{(1 - \lambda)(u - c)/2}_{\text{direct-selling value}} \\ &= (1 - m)\lambda(u - c)/2 > 0 \text{ (since } m < 1\text{)}.\end{aligned}$$

## Finance Mode (F)

- ▶ The intermediary resells **and** provides liquidity.
- ▶ Financing supplier is costly: per-user cost  $k > 0$ .
- ▶ Intermediary gives TIOLI offers:
  - ▶  $c$  is covered by the intermediary in the early sub-period;
  - ▶ Intermediary pays  $f_F(\lambda, c)$  to supplier **by the end of the period**
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and contributes **liquidity** (at the time of production):

$$\theta_F(\lambda, c) = (1 - m\lambda)p - c$$

# The intermediary's problem

- ▶ The intermediary selects suppliers into one of the two modes:

$$\max_{q(\cdot) \in \{0,1\}} \int_{\Omega} \left( (1 - q(\lambda, c)) \pi_M(\lambda, c) + q(\lambda, c) \pi_F(\lambda, c) \right) dG$$

subject to the liquidity constraint:

$$\underbrace{\int_{\Omega} q(\lambda, c) \theta_F(\lambda, c) dG}_{\text{total liquidity}} + L \geq 0.$$

- ▶ Define  $\Delta\pi(\cdot) = \pi_F(\cdot) - \pi_M(\cdot)$ . The objective is equivalent to

$$\max_{q(\cdot)} \int_{\Omega} \left( \pi_M(\lambda, c) + q(\lambda, c) \Delta\pi(\lambda, c) \right) dG,$$



# Profit-maximizing selection rule

- Solve the problem using Lagrangian:

$$\mathcal{L} = \int_{\Omega} \left[ \pi_M(\cdot) + q(\cdot) \left( \Delta\pi(\cdot) + \mu\theta_F(\cdot) \right) \right] dG(\lambda, c)$$

$\mu \geq 0$ : The shadow value of liquidity

- The optimal selection rule is:

$$q(\lambda, c, \mu) = \begin{cases} 1 & \text{if } \Delta\pi(\lambda, c) + \mu\theta_F(\lambda, c) \geq 0 \\ 0 & \text{otherwise} \end{cases}$$

## Proposition (Selecting Suppliers)

*The intermediary optimally selects suppliers from three regions*

- ▶ *Region A: **positive** profit and **positive** liquidity contributions*

$$\Delta\pi(\lambda, c) \geq 0, \quad \theta_F(\lambda, c) \geq 0$$

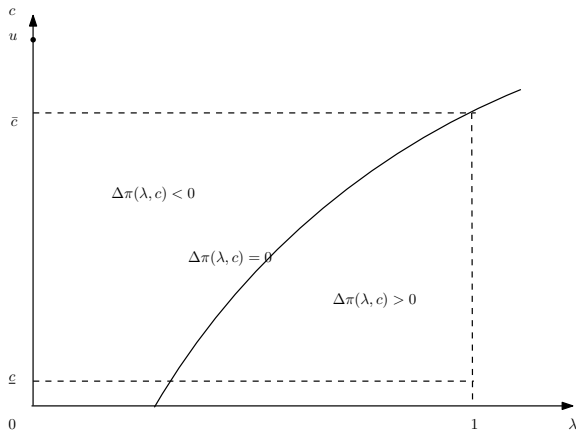
- ▶ *Region B: **positive** profit and **negative** liquidity*

$$\Delta\pi(\lambda, c) > 0, \quad \theta_F(\lambda, c) < 0, \quad \underbrace{-\Delta\pi/\theta_F}_{\text{returns}} \geq \mu$$

- ▶ *Region C: **negative** profit and **positive** liquidity*

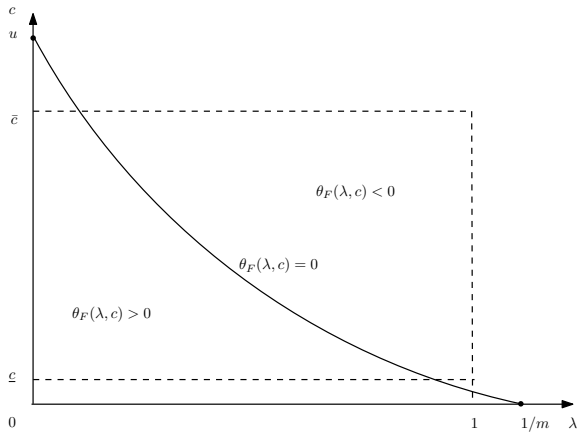
$$\Delta\pi(\lambda, c) < 0, \quad \theta_F(\lambda, c) > 0, \quad \underbrace{-\Delta\pi/\theta_F}_{\text{costs}} \leq \mu$$

## $\Delta\pi$ in the space of $\lambda$ and $c$



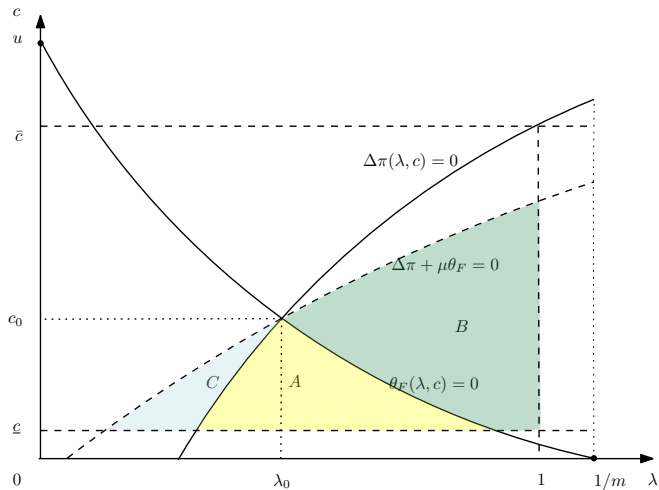
$$\Delta\pi(\lambda, c) = m\lambda(u - c)/2 - k$$

## $\theta_F$ in the space of $\lambda$ and $c$



$$\theta_F(\lambda, c) = (1 - m\lambda)(u + c)/2 - c$$

# Profit-based liquidity cross-subsidization



# Profit-maximizing selection rule

- ▶  $\mu$  is determined by

$$L = -\Theta(\mu) \equiv - \int_{\Omega} q(\lambda, c, \mu) \theta_F(\lambda, c) dG. \quad (1)$$

If liquidity constraint is slack, i.e.,  $-\Theta(0) \leq L$ , then  $\mu = 0$ .

## Proposition

Given liquidity endowment  $L \geq 0$  and  $k/m < (u - \underline{c})/2$ , the intermediary's profit-maximizing strategy involves *active F mode*, which is characterized by

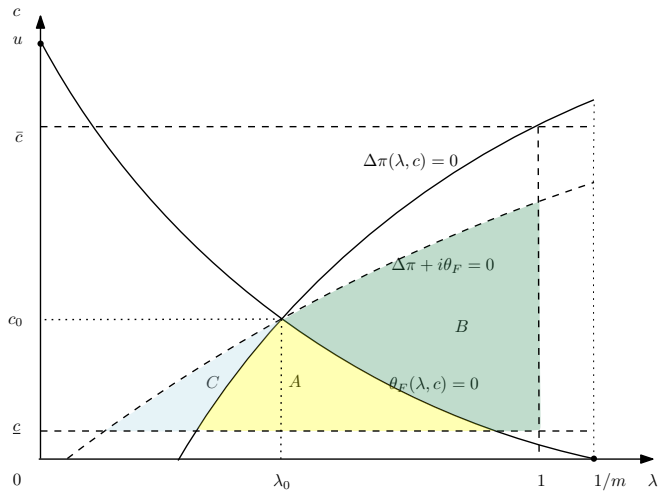
$$\{q(\lambda, c, \mu), f_F(\lambda, c), f_M(\lambda, c), \mu(L)\}.$$

# Endogenize $L$

- ▶ So far, a downward sloping demand curve for liquidity  $\mu(L)$
- ▶ Suppose the intermediary faces a liquidity cost  $i$
- ▶ The intermediary's liquidity holdings  $L \geq 0$  satisfy

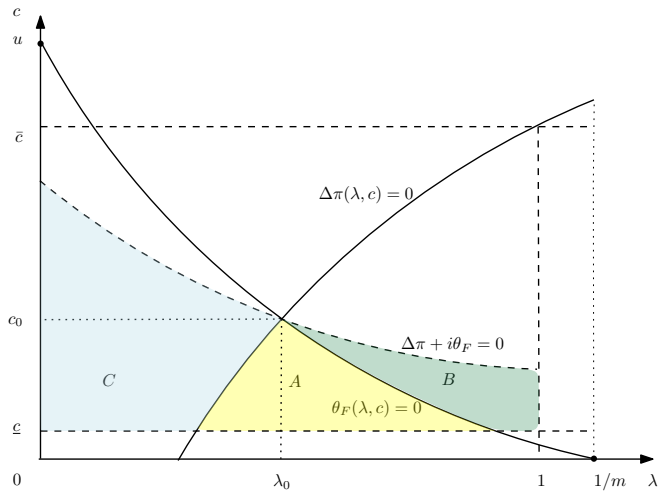
$$\begin{cases} \mu(L) = i & \text{if } i < \mu(0); \\ L = 0 & \text{if } i \geq \mu(0). \end{cases}$$

- ▶ The equilibrium liquidity value  $\mu = \min\{\mu(0), i\}$  is shaped by
  - ▶ richness of suppliers' liquidity:  $\mu(0)$
  - ▶ cost of external liquidity:  $i$



Positively-sloped selection curve





Negatively-sloped selection curve

## Generalize suppliers' direct selling value

- ▶ Let suppliers' direct selling value be  $\Phi(\lambda, c) \geq 0$ .
- ▶ We have profit contributions of F and M contracts:

$$\pi_F(\lambda, c) = (u - c)/2 - \Phi(\lambda, c) - k,$$

$$\pi_M(\lambda, c) = (1 - m\lambda)(u - c)/2 - \Phi(\lambda, c).$$

- ▶ What matters for our analysis is

$$\Delta\pi(\lambda, c) = m\lambda(u - c)/2 - k.$$

## 2. Middleman Finance and Product Market

*We endogenize the retail price...*

## Downward-sloping demand $D(p)$

- ▶ A continuum of consumers; demand for each product  $D(p)$
- ▶  $c$  is a per-unit cost

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## Direct-selling:

- ▶ A supplier produces only if consumers arrive early
- ▶ In that state, he sets the monopoly price

$$p^*(c) \equiv \arg \max_{p \geq c} (p - c)D(p)$$

Assume the objective is strictly quasi-concave in  $p$  and let the monopoly profit be

$$\pi^*(c) \equiv (p^*(c) - c)D(p^*(c)).$$

# The intermediary

The intermediary can offer  $M$  or  $F$  contracts to suppliers.

$M$  contract:

- ▶ With prob.  $1 - m\lambda$ , match with consumers early.
- ▶ The intermediary sets the monopoly price  $p^*(c)$  for that state and pays to suppliers direct selling value.
- ▶ Supplier of  $(\lambda, c)$  contributes profit of

$$\pi_M(\lambda, c) = (1 - m)\lambda\pi^*(c).$$

Recall that in the benchmark:

$$\pi_M(\lambda, c) = (1 - m)\lambda\frac{u - c}{2}.$$

## $F$ contract:

- ▶ Intermediary advances production cost  $c \cdot D(p)$  to the supplier.
- ▶ The expected profit at retail price  $p$  is

$$\pi_F(\lambda, c, p) = (p - c)D(p) - (1 - \lambda)\pi^*(c) - k.$$

- ▶ The incremental profit is

$$\Delta\pi(\lambda, c, p) \equiv (p - c)D(p) - (1 - m\lambda)\pi^*(c) - k.$$

- ▶ The liquidity contribution from supplier  $(\lambda, c)$ :

$$\theta_F(\lambda, c, p) = (1 - m\lambda)pD(p) - cD(p).$$

## Intermediary's problem

- ▶ The intermediary chooses  $q(\lambda, c) \in [0, 1]$  and  $p(\lambda, c) \in \mathbb{R}_+$ :

$$\begin{aligned} \max_{\{q(\cdot), p(\cdot)\}_{(\lambda, c) \in \Omega}} \int_{\Omega} [q(\cdot) \Delta \pi(\lambda, c, p(\cdot))] dG, \\ \text{s.t. } \int_{\Omega} [q(\cdot) \theta_F(\lambda, c, p(\cdot))] dG + L \geq 0. \end{aligned}$$

- ▶ The corresponding Lagrangian:

$$\mathcal{L} = \int_{\Omega} \left[ q(\lambda, c) \underbrace{\left( \Delta \pi(\lambda, c, p(\lambda, c)) + \mu \theta_F(\lambda, c, p(\lambda, c)) \right)}_{\equiv S(\cdot)} \right] dG.$$



# Optimal pricing for financed products

- The net value of financing supplier  $(\lambda, c)$ :

$$S(\cdot) = (1 + \mu(1 - m\lambda)) (p - \tilde{c}) D(p) - k - (1 - m\lambda)\pi^*(c),$$

with effective cost  $\tilde{c} = \gamma c$ .  $\gamma$  captures liquidity-related costs:

$$\gamma \equiv \frac{1 + \mu}{1 + \mu(1 - m\lambda)} \geq 1.$$

$\gamma = 1$  iff  $\mu = 0$  or  $\lambda = 0$ ;  $\gamma$  increases in  $\mu$  and  $\lambda$ .

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- ▶ The profit-maximizing retail price:

$$p(\lambda, c) = p^*(\tilde{c})$$

$p^*(\tilde{c}) - p^*(c)$ : liquidity-driven double marginalization.

# The new selection rule

- We decompose the net valuation  $S(\lambda, c)$  into a baseline component and a premium derived from pricing flexibility:

$$S(\lambda, c, \mu) = \underbrace{S_{base}(\lambda, c, \mu)}_{\text{Baseline value}} + \underbrace{\mathcal{G}(\lambda, c, \mu)}_{\text{Pricing gain}}.$$

- $S_{base}$  represents the valuation if price is fixed to  $p^*(c)$

$$S_{base}(\lambda, c, \mu) = \underbrace{m\lambda\pi^*(c) - k}_{\text{Baseline Profit}} + \underbrace{\mu [(1 - m\lambda)p^*(c) - c] D(p^*(c))}_{\text{Baseline Liquidity}}.$$

# Price gain and risk resilience

- ▶  $\mathcal{G}(\lambda, c, \mu)$ , captures the gain by setting  $p = p^*(\tilde{c})$ :

$$\mathcal{G}(\lambda, c, \mu) \equiv (1 + \mu(1 - m\lambda)) \left[ \pi^* \left( p^*(\tilde{c}), \tilde{c} \right) - \pi \left( p^*(c), \tilde{c} \right) \right].$$

- ▶  $\mathcal{G}(\cdot)$  is strictly positive, strictly increasing in  $\lambda$  and  $\mu$ .

## Proposition

*The intermediary's selection rule is characterized by a strictly expanded and less risk-sensitive financing boundary:*

$$\begin{aligned} c^*(\lambda) &> c_{base}^*(\lambda), \rightarrow \text{expanded financed set} \\ \partial c^* / \partial \lambda &> \partial c_{base}^* / \partial \lambda, \rightarrow \text{reduced risk sensitivity.} \end{aligned}$$

# Implications on product market surplus

- The change in trade surplus by financing:

$$\Delta W(\lambda, c) \equiv \underbrace{W(p^*(\tilde{c}))}_{\text{F contract surplus}} - \underbrace{(1 - m\lambda) W(p^*(c))}_{\text{M contract surplus}}.$$

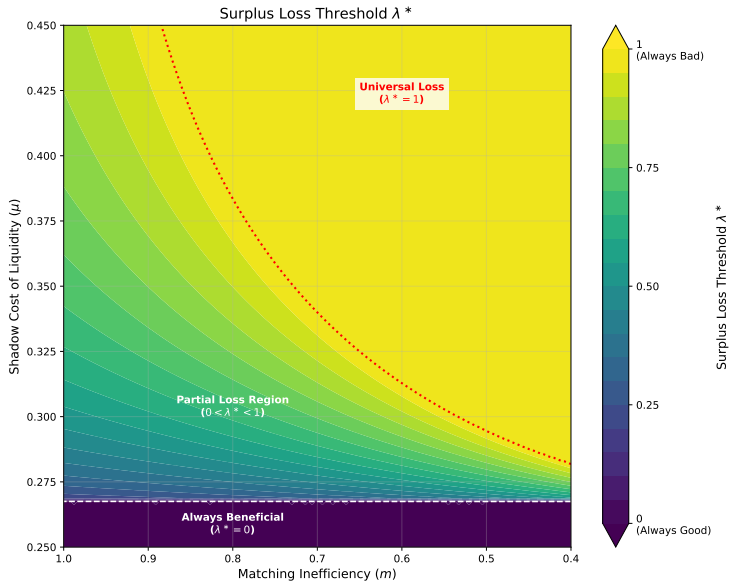
where  $W(p, c) = \int_p^\infty D(t)dt + (p - c)D(p)$ .

## Proposition (Retail trade surplus loss)

Suppose  $\Delta W'_\lambda(0, c) < 0$ . There exists a threshold  $\lambda^* \in (0, 1/m)$  such that **financing suppliers strictly reduces retail trade surplus** for  $\lambda \in (0, \lambda^*)$ .

## Funding cost $\mu$ and matching efficiency $m$

- ▶ **Higher funding costs  $\mu \uparrow \implies$  Loss-range expands  $\lambda^* \uparrow$**
- ▶ Higher  $\mu$  exacerbates the double marginalization problem, requiring a higher risk  $\lambda$  to offset the price distortion.
- ▶ **Better matching  $m \downarrow \implies$  Loss-range expands  $\lambda^* \uparrow$**
- ▶ As  $m \downarrow$ , the M contract becomes a tougher benchmark to beat. The insurance value of financing reduces, but the price distortion remains.



Trade surplus loss threshold  $\lambda^*$  with  $D(p) = p^{-\varepsilon}$

# Implications on consumer surplus

- The change in consumer surplus by financing:

$$\Delta CS(\lambda, c) \equiv CS(p^*(\tilde{c})) - (1 - m\lambda)CS(p^*(c)),$$

where  $CS(p) \equiv \int_p^{\bar{p}} D(z)dz$ .

## Proposition (Consumer surplus loss)

*Fix  $c$  and suppose  $\Delta W(\lambda, c) < 0$  for  $\lambda < \lambda^*$ . Then there exists  $\lambda_{CS}^* > \lambda^*$  such that*

$$\Delta CS(\lambda, c) < 0 < \Delta W(\lambda, c) \text{ for } \lambda \in (\lambda^*, \lambda_{CS}^*).$$

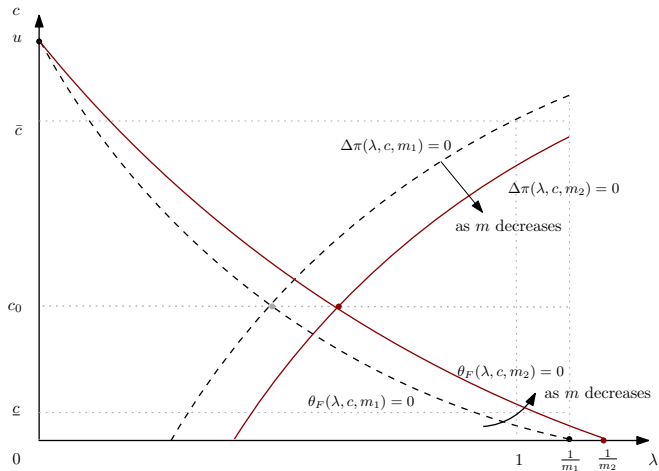


# Summary

- ▶ Middlemen finance features **profit-based liquidity cross-subsidization**.
- ▶ Middlemen finance leads to **liquidity-driven double marginalization** and potentially harms product market trade surplus.

## Supplementary materials

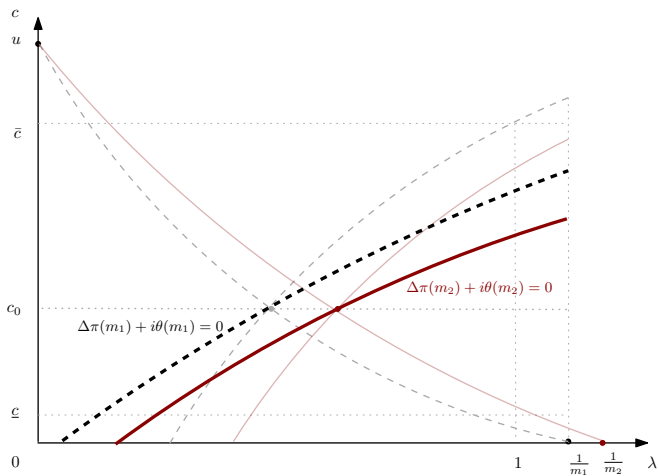
## Matching efficiency and liquidity provision



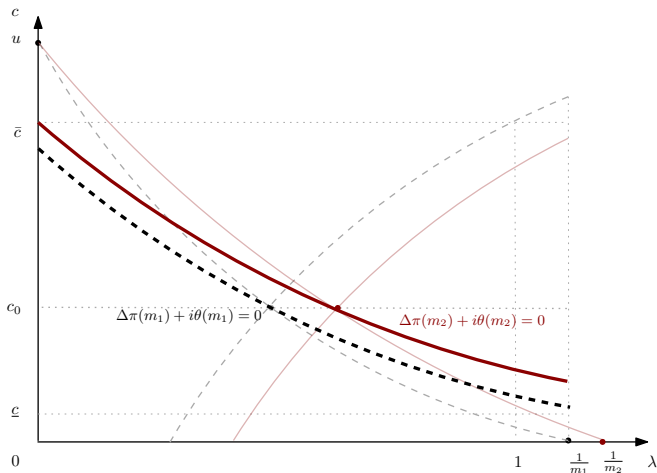
Effects of changes in matching efficiency  $m$ :

$$\Delta\pi(\lambda, c) = m\lambda(u - c)/2 - k$$

$$\theta_F(\lambda, c) = (1 - m\lambda)(u + c)/2 - c$$

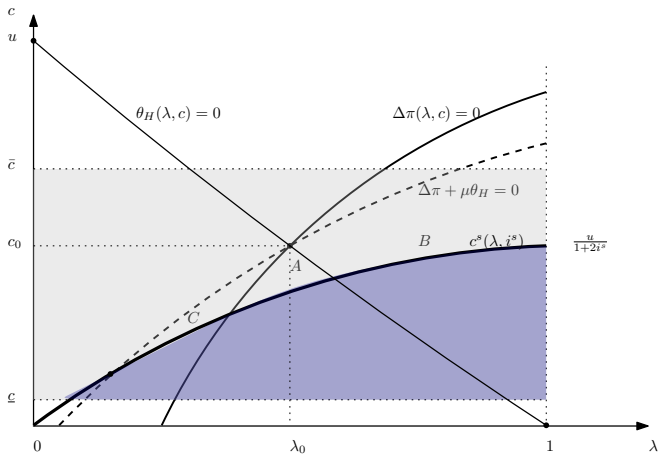


- If the selection curve is upward-sloping, SF shrinks as  $m$  decreases from  $m_1$  to  $m_2$  (matching efficiency improves)



- If the selection curve is downward-sloping, SF expands as  $m$  decreases  $m_1$  to  $m_2$  (matching efficiency improves)

## Suppliers' access to liquidity



**Figure:** Suppliers' money holdings coexist with supplier finance



## Proposition

Suppose  $\lambda_0 < 1$ ,  $\underline{c} > 0$ ,  $i < \frac{k\bar{\lambda}}{\mu u \bar{\lambda} - 2k}$ , and suppliers face money market rate  $i^s$ . There exist thresholds  $i < \underline{i}^s < \bar{i}^s \equiv \frac{(u-\underline{c})\bar{\lambda}}{2\underline{c}}$  such that:

- ▶ If  $i^s \leq \underline{i}^s$ , suppliers with  $c \leq c^s(\lambda, i^s)$  hold money for liquidity, and supplier finance stays inactive.
- ▶ If  $i^s \geq \bar{i}^s$ , no supplier holds money, and supplier finance is activated for some suppliers.
- ▶ If  $i^s \in (\underline{i}^s, \bar{i}^s)$ , suppliers with  $c \leq c^s(\lambda, i^s)$  have money, while supplier finance activates for other suppliers.