

Def/ (slice, slice rank)

$f: A^k \rightarrow \overline{\mathbb{F}}$  is called a slice if

$$f(x_1, \dots, x_k) = h(x_i) \cdot g(x_1, \dots, x_{i-1}, x_{i+1}, \dots, x_k)$$

for some  $i \in [k]$ ,  $h: A \rightarrow \overline{\mathbb{F}}$ ,  $g: A^{k-1} \rightarrow \overline{\mathbb{F}}$ .

For  $f: A^k \rightarrow \overline{\mathbb{F}}$ , the slice rank of  $f$  is

the min.  $m \in \mathbb{Z}$  s.t.  $f$  is a linear combination of  $m$  slices. ( $k=2$ , normal rank of matrices)

Lemma (rank of diagonal tensors)

$k \in \mathbb{Z}$   $k \geq 2$ ;  $A$ : finite set;  $\overline{\mathbb{F}}$ : field;

$f: A^k \rightarrow \overline{\mathbb{F}}$  s.t.  $f(x_1, \dots, x_k) \neq 0 \Rightarrow x_1 = x_2 = \dots = x_k$

$$\Rightarrow \text{sr}(f) = |\{x \in A: f(x, \dots, x) \neq 0\}|$$