Relations between Causality, Fairness, Privacy, Accuracy, Information Flow and Explainability in Machine Learning

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Table of contents depois ou antes do abstract?

Precisa ter tabela de imagens, tabelas e etc.?

OK citar coisas do Arxiv?

Repetição de artigos que cobrem mais de duas áreas? Talvez só mencionar que foi usado na subseção anterior? Coloca "Chapter x of $\subset \{...\}$ " ou " $\subset \{...\}$ "?

O modelo padrão é coluna dupla, mas aparentemente várias pessoas fizeram sem ser coluna dupla sem problemas, e as imagens ficam melhores em coluna simples. Compensa trocar pra coluna dupla???

Abstrac

Do que podemos falar aqui?

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I. Introduction

Recent research [24] [1] [20] [21] indicates numerous tensions and synergies between many concepts that surround the Machine Learning literature, including Fairness, Privacy, Accuracy and Explainability. For instance, there is an inherent tradeoff between Fairness and Accuracy such that, depending on the data distribution, it might be impossible to develop a model that achieves acceptable values for both fairness and accuracy if we consider some reasonable fairness metrics [53]. Also, there has been some work on introducing Causality concepts into the discussion, for instance, to develop better fairness metrics [46]. It has also been suggested to use naturally interpretable models (as explanations for more complex models) for auditing systems and checking if they are fair, although this might lead to problems [76]. This area of research is especially relevant nowadays, given the importance that Machine Learning and Artificial Intelligence systems have: we now have computational systems that are part of processes of making decisions with big impacts on people's lives, for instance, recidivism prediction [8], loan approvals [61], hiring decisions [35], and others.

In this first part of the Undergraduate Thesis, we provide a concise review of the literature on the topics presented. The main goal is to provide a solid basis for future work on these topics and identify the known connections among them. Section IV discusses the already developed theoretical work on these areas; Section V discusses connections between them found in the literature; Section VI provides conclusions and possible future lines of work.

II. METHODOLOGY

The methodology applied to this project consists, in general, of reading as many papers on the subject as possible in order to gather what has been produced recently. Also, for developing the necessary theoretical background, the classical book Causality [51], by Judea Pearl, was of utmost importance.

III. EXPECTED RESULTS

For the first part of the project (POC I), the expected result is an extensive review of the literature on Causality, Fairness, Privacy, Accuracy and Interpretability in Machine Learning, and the relationships between these concepts. For the second part (POC II), the expected results are the reproduction and verification of the viability of applying the theoretical framework of Quantitative Information Flow to these concepts, with the possibility of developing new theoretical results. This document shows the results of the first part, POC I.

IV. THEORETICAL BACKGROUND FOR INDIVIDUAL CONCEPTS

First, we provide a general background on some introductory concepts in the areas of Machine Learning, Causality, Fairness, Privacy, Explainability in Machine Learning, and also Quantitative Information Flow (QIF).

A. Machine Learning and scenario considered

Machine Learning is the field of study that focuses on developing methods of learning general patterns from limited data. In recent years, important advances have been observed in Machine Learning research, and also the popularity and applications of some methods increased significantly. One example is the improvement of Convolutional Neural Network architectures, and the popularity of Generative Models. Also, some recent research is focused on the theory behind such machine learning methods [15] [29], and statistical learning in general [66]. Part of the goal of this formalization is to provide more qualitative guarantees in regard not only to accuracy, but also fairness, privacy, interpretability, and other important qualities. We discuss these different goals in the next four subsections.

Compensa mesmo criar ambiente de definição pra noções gerais tipo supervised nearling, algoritmo de ML, etc.? Eu não defini formalmente o que seria cada uma dessas coisas, deveria?

In general, we consider *supervised learning* problems: in this scenario, a *machine learning algorithm* is an algorithm that receives many data points, which we call *training data*, and outputs a *model*. This model is itself an algorithm that receives a data point with some information omitted, encoded in what we call the *target variable*, and outputs a guess of the omitted information, which we call the *model prediction*. The model is then evaluated with other data points, ideally not the same ones used for training the model. This is called supervised learning because the algorithm has access to the target variable during the training process, which is not the case for unsupervised learning.

Figure 1 shows how the other concepts are related to machine learning in this context: we usually can assume that the training data is generated by some causal process, which can be modeled by a causal model; possible privacy attacks include performing sensitive information inference on the training data and on the model itself; we usually measure how accurate and fair a system is by analyzing its predictions for many data points; we can also obtain local and global explanations for complex models by this type of analysis.

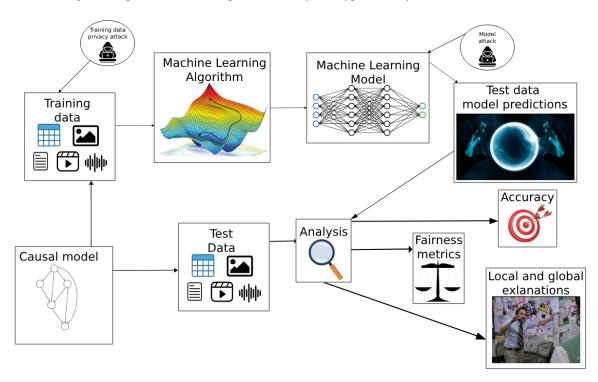


Fig. 1. Figure representing the supervised learning scenario we consider throughout this work.

B. Accuracy

Accuracy is the notion of how close some estimate is to the true value we are estimating. In the context of Machine Learning, it represents how close the predictions of a given model are to the real value of the variable the model aims to predict. For binary classification (the scenario in which the target value has only two possible values), accuracy is defined in machine learning as $\frac{TP+TN}{TP+TN+FP+FN}$, where:

- 1) TP is the number of True Positives: how many predictions were labeled as True and were really True.
- 2) TN is the number of True Positives: how many predictions were labeled as True but were actually False.
- 3) FP is the number of True Positives; how many predictions were labeled as False and were really False.
- 4) FN is the number of True Positives: how many predictions were labeled as False but were actually True.

So, the usual notion of accuracy is the proportion of the predictions from the model that were correct for the available data. This generalizes to multiclass classification problems (in which the target variable has a finite number of possible values) by considering the proportion of times that the model's prediction was the correct class. *Regression* problems are the ones in which the target variable has an infinite number of possible values but can be codified as a vector of numbers: for instance, the value of some building at two different times. We can access how accurate a regression model is in many ways, for instance the square difference between the prediction value and the real value, added through all training data points.

imagem train vs test accuracy

One important point to consider is that it is better to evaluate how accurate the system is with data different from the data used for training. This is because during the training phase the Machine Learning algorithm usually has the goal of providing the model that provides the best possible accuracy in the training data, among the possible models supported. If there is enough freedom among the possible models, then it might be possible to obtain a model that has a very good accuracy, but if we try to use this same model on other data, this same model performs

very badly. For instance, if all functions from the training data to the output are allowed, then a model that simply memorizes the training data and outputs the correct result by looking at the memorized data and outputs a random answer if the input is not in the training data will have one hundred percent accuracy in the training data, but we can obviously provide no guarantee for data points not present. This problem is called **overfitting**, and is usually avoided by limiting how powerfull the model can be, in conjuction with verifying real accuracy values with data other than the training data, and we call this the **testing data**. Also, notice that to evaluate the model, the test data should also have the target value of each data point.

The classical goal of Machine Learning is to provide models with good *test accuracy*, and an Machine Learning algorithm that produces models such that good results on the training data reflet on good results on testing data are said to **generalize** well. However, with the groth of Machine Learning applications in real-life scenarios and the impact on society as a whole, there has been a crescent focus on aspects other than simply maximizing the accuracy, in a similar way that we usually are worried only about how fast a cryptographic algorithm is but also about how safe it is.

Falar aqui pra notar que acurácia nem sempre é o quão acuradamente o modelo cumpre nossos objetivos, uma vez que temos objetivos além de só que o modelo acerte ao máximo, falar de sensitividade e outros concentos, que nem sempre estamos preocupados somente com acurácia, e o impacto da função que estamos otimizando, mencionar regularização

C. Fairness

Dava pra citar Hellman D. Measuring algorithmic fairness pra falar que "Indeed, the general consensus is that the meaning and implication of each approach highly depends on the context and consequential decisions associated with an intelligent system"

Citar Pushing the limits of fairness impossibility: Who's the fairest of them all? De que em geral não dá pra satisfazer as noções principais de fairness ao mesmo tempo, mas dá pra tentar encontrar meio termos e otimizar uma em função da outra. The Possibility of Fairness: Revisiting the Impossibility Theorem in Practice parece melhor porque é mais empírico. The impossibility of "fairness": a generalized impossibility result for decisions fortalece isso um pouco e foi escrito por um cara de harward mas ficou só no arxiv.

Citar Learning Fair Representations como uma forma de balancear group e individual fairness com acurácia boa...

In the context of Machine Learning, fairness refers to the reduction, as much as possible, of **algorithmic bias**. Algorithm Bias is the bias introduced by algorithmic decisions. This bias might have a big social impact, as this can further existing unfair discrimination in society, as machine learning algorithms are being used to make more and more important decisions. One famouse example is the COMPAS recidivism algorithm, that has been used by the United States courts to estimate how likely someone is to reoffend in the future. It was revealed [8] that this tool was heavily biased against black people.

We will say that the result is **positive** for a data point if it benefits the person represented by that data point, and **negative** otherwise. We will say that the **unpriviledged group** is the group of people affected negatively by the bias, and the **priviledged group** is the other group of people.

Such biases can happen because of many factors. The algorithm itself might be introducing bias, or the data might be biased. The data might have been collected in a biased way (in the compass example, this would be the case if reincidivism data was collected more for black reincidivists than for white), or the data might be simply reinforcing some bias of the society.

Also, the bias in society might be such that the data is in disagreement with reality (the unpriviledged group true values for the target variable would affect them in the same way as the priviledged group), or it is in agreement with reality because of structural biases in society. For instance, if the prediction of the algorithm is whether or not someone will have good grades if accepted to some university, people in the unpriviledged group might not have had as good oportunities in life as people in the priviledged group, so the data is correct when it says that those people will have worse grades. Even though, the results might still be considered unfair: this depends on the notion of fairness we consider. All of these unfairness possibilities can be futther divided into other types of unfairness, as was done in [48].

Besides deliberate bias in the algorithm, such that the results of the algorithm do not reflect the data, and biased data, it is also possible to introduce bias because the algorithm might prioritize making correct predictions for the majority of the population, if it can't make correct predictions for both the majority and the minority. Another possibility is that the prediction might depend on past decisions of the algorithm, and we only know the result if the result provided is positive (for instance, we only know if someone will reincide if we release them). In this type

of scenario, according to Learning Theory it's important to take suboptimal decisions to *explore* different options and gather more data [19] (found in arxiv.org), which might be considered unethical as it might have a big cost to society (releasing someone that's probably going to commit more crimes) or to the individual (not giving a life-saving drug to some patients as an experiment to see the survival rates for that specific group).

Many different notions of algorithmic fairness have been developed, and some are not compatible [3]. Initially, the notions of fairness could be grouped into two main types: statistical and individual definitions of fairness [19]. Statistical (group) notions of fairness require some statistical metric to be similar for certain demographic groups, and individual notions enforce constraints on pairs of individuals, for instance requiring similar individuals to be treated similarly. Many problems with statistical notions and why they, in general, don't provide good individual guarantees are presented in [21] [31]. Some of these problems include: satisfying the constraints for two protected attributes individually but not to combinations of these attributes, . One problem with both individual and group notions is *composition*: it is not always the case that satisfying fairness constraints in individual, isolated, components of a system imply that fairness constraints will be satisfied for the whole system [22]. Finally, there are also causal approaches to fairness notions, which we will discuss more in Section V.

The techniques developed to reduce unfairness in algorithmic decision making can be divided into *pre-processing*, *in-processing* and *post-processing*. Pre-processing techniques modify the training data to remove biases present there. In-processing techniques modifies the learning algorithm itself, for instance by changing the objective learning function to include not only accuracy but also adding to it some statistical fairness metric, or including some constraint that it has to satisfy. Post-processing techniques act after the model is trained to reduce the unfairness in the decisions made by such a model.

We summarize below the ways in which unfairness might be introduced:

- 1) Algorithm results does not reflect the data.
 - a) The algorithm might optimize for the majority only, achieving good overall accuracy even though it's mostly wrong for minorities. This can be considered a type of Aggregation Bias.
 - b) Systematic errors in the algorithm, that leads to biased estimation.
- 2) The Data can be biased, not reflecting the reality.
 - a) We can have a structural biases in society, such that people in unpriviledged groups do not have the necessary oportunities, but if they were treated similary to the priviledged group by society, they would have similar results. For instance, an unpriviledged group that doesn't have good education oportunities will have worse scores on exams because of historical discrimination, and although just looking at whether someone is in this group could lead to a good accuracy, it might be only perpetuate current unfair biases in society.
 - b) The bias can also be introduced in a way that people in the unpriviledged group were misclassified before the data was colected, for instance maybe capable people in an unpriviledged group usually don't get a job even though they are actually as capable as the unpriviledged group.
 - c) Data collection doesn't reflect the reality: Measurement bias (for instance, COMPASS used friend/family arrests as a proxy for a risk score present in the dataset), Ommited Variable bias (this violates assumptions of some learning models, for instance linear regression models usually assumes error terms uncorrelated with the parameters considered in the regression), Representation/Sampling Bias (biased sampling lacking the diversity of the population), Simpson's Paradox (if we don't have data on a confounder, correlations might be spurious [51]).
 - d) If the data is collected on a group fundamentally distinct from the one where it will be used, for instance another population (Population Bias) or the same population but at another time (Temporal Bias), unfair bias might be introduced.
 - e) Data that relies on people's opinion is prone to many biases: Social Bias (people do what others are doing), Self-Selection Bias (people think that everyone agrees with them), and many others.
- 3) Data might depend on the algorithm previous output: Presentation Bias (the user is presented to some selected advertisements, for instance), Ranking Bias (search engines ordering results in a biased way), Popularity Bias (more popular itens are shown more). This might strengthen biases through time.
- 4) Finally, the circumstances can change through time, either by influence of the algorithm itself or other factors, which can worsen the quality of algorithms previously considered to provide good results (Emergent Bias).

D. Privacy

Privacy references: https://dl.acm.org/doi/abs/10.1145/3436755 and https://ieeexplore.ieee.org/document/9433648. The second one doesn't add much.

WMLMPASAO: When Machine Learning Meets Privacy: A Survey And Outlook

Membership Inference Attacks Against Machine Learning Models

Privacy-preserving classification of customer data without loss of accuracy

CryptoDL: Deep Neural Networks over Encrypted Data

About dependence between individuals: Dependence Makes You Vulnerable: Differential Privacy Under Dependent Tuples

Falar de DP e LDP também, são importantes: A Comprehensive Survey on Local Differential Privacy Falar de Federated Learning também!

In the context of Machine Learning, a privacy-preserving algorithm is one that doesn't allow information considered private/sensitive to be obtained by unauthorized parties. This has been named *private ML* [38], and the private data to be protected can be the data using to train the model or the model parameters and structure itself. It is also possible to use Machine Learning to enhance privacy, or to serve as an attack tool. We focus on *private ML*.

We call **adversary** the agent that wants to discover the private information, and **secret** the private information itself. There are some possible goals of the adversary, she might wish to recover the model itself (Model Extraction Attack) by trying to approximate the function that represents the model, to recover some feature or statistical property of the dataset (Feature Estimation Attack), to discover whether some individual data point is present in the dataset (Membership Inference Attack), or even recover the exact values of individual samples in the datset (Model Memorization Attack). We distinguish between the **White-Box access** and **Black-Box access** scenarios as the situation in which the adversary has or does not have full access to the trained model and their parameters, respectively.

One approach to improving privacy in Machine Learning is by encrypting the data or the model in a way such that the computations can be done with the encrypted data/model, and just the result is decrypted. Secure Multi-Party Computation is also an option if there are multiple parties responsible for this computation. Other option is to obfuscate the data or the model, by introducing pertubation in a way that protects the private information in a way that (hopefully) doesn't worsen much the results. There is also the aggregation approach, that focuses on multy-party computations such that the data of one party remains private to other parties, and is used by aggregation learning, for instance. Finally, it's possible to develop *back-door* attacks: malicious modifications to the model might allow an adversary to infer private information, if she provides the specific inputs that are designed to trigger that. All of these are listed in more detail in [38].

E. Explainability

Explainability, loosely defined, concerns the ability to assign meaning to why some model took one or more decisions, in a way that can be interpreted by humans. There is currently no consensus for a precise definition of the term, and many papers argue about distinctions between interpretability and explainability. For instance, [27] defines interpretability as the property of being able to describe the internal working of systems to humans and *completeness* as the property of being able to accurately describe the operation of the system, and an explainable system has both properties at an acceptable level. The paper [57] draws this distinction in a different way: they define transparency as the higher-level explanation given by the designers of the system of their choices of architecture, algorithm and hyperparameters, while interpretations are defined as answers to the question "what does the model bases its decision on?", and explanations as the combination of interpretations and contextual information from domain knowledge. In general, it is considered necessary that an explanation both explains the inner workings of a system accurately and is comprehensible enough for humans with the relevant domain knowledge. There is a trade-off between these two goals, as we want not only to reach a balance between simplicity and accuracy, but we also want important biases in the model to be evident in the explanation, as mentioned in [27].

There are some classifications of the existing approaches to explainability, but we focus on the classification defined in [36]. We can divide the approaches based on whether they are **local** or **global**: local explanations focus on explaining individual decisions, and global explanations focus on explaining the overall workings of the model. LIME [55] and SHAP [41] are examples of methods that provide local explanations and can be used to derive global explanations. We can also divide the approaches into **Model Agnostic** and **Model Specific**: the former refers to methods that don't depend on the inner workings of the model (for instance, SHAP [41] and LIME [55]), the latter refer to methods developed to work only for a specific group of models (for instance, Grad-CAM and Shap-CAM are specific for Convolutional Neural Networks). Finally, we can divide explainability approaches on the data types these methods deal with and the purpose of the explanations.

As discussed at [11], explanations may be usefull to data scientists, business owners, model risk analysts, regulators and consummers, each with different goals in mind. The concerns that might be reduced by the use of explainable models include: correctness (only variables relevant should be used in the final decisions and we should not use spurious correlations incorrectly), robustness (the model should not be susceptible to small pertubations), bias (the model should not be biased against specific subgroups), improvement (we might want to improve the model, and explanations can aid in this goal), transferability (the model should be useful in populations other than the one used to train and test the data) and human comprehensibility (this can aid an expert or even a non-expert in using and even trusting the results provided by the model). The paper also mentions some criterias for evaluating explanations, that include how comprehensible the explanation is, how they accurately capture the models they aim to explain, how accurately they can be used to predict other outcomes of the model, how they scale to larger and more complex models, and how restrictive they are on the type of accepted model, some of these notions are further explored in [18]. They also evaluate explanations by example (for instance, counterfactuals [68] that provide examples with small changes to an input that can modify the output), and explanations by simplification (approximating a complex model by a simpler one). These approaches are different from SHAP, for instance, as it is based on game-theoretic based feature importance concepts. LIME can be considered to provide explanations by simplification, by locally approximating the model to a linear model. As mentioned in [57], explanations can also be used to enhance scientific research in natural sciences.

Some models are inheretely interpretable, as their inner working is easier to understand for humans. Some examples mentioned in [11] are: Linear Logistic Regression, Decision Trees, K-Nearest Neighbors (KNN), Rule-based learning, Generalized Additive Models (GAMs) and Bayesian networks. Some researchers criticise this claim for some of these models, for instance, [37] points out that linear models are not necessarily easily interpretable, as they sometimes rely on un-interpretable and heavily-engineered features.

Other criticisms to the current development of explainability approaches were made: for instance, [33] argues that explainability is always a means to an end, and by requiring explanations to our models we may be significaltly restricting the space of possibilities of dealing with the problems we need to face. For instance, there are approaches to verify if a model is fair that do not rely on explanations of the inner workings of the model (and in this case, relying on explanations might lead to other problems, as mentioned in [76]). Another possible problem with explainability is that if we rely on humans opinions we might end up with methods that are *persuasive*, instead of *accurate*, as these two properties might not be fully aligned.

An in-depth survey on machine learning explainability can be found at [14], with some definitions regarding ontology and the philosophical meaning of explanations and knowledge sharing.

Esse paper parece discutir porque black-box pode ser aceitável em ML pra decisões médicas ainda por cima: Artificial Intelligence and Black-Box Medical Decisions: Accuracy versus Explainability

F. Causality

Most of our discussion of causality will be based on the work of Judea Pearl [51]. There are many alternative notions of causality, but most of them are already discussed in [51]. Judea Pearl divides causality into three levels, according to the type of question we want to answer.

The first level of causation deals with questions that can be answered by looking at the data. For instance, questions that can be answered by Bayesian networks, deep neural networks or other machine learning algorithms. According to Pearl, this kind of question can be written in terms of what we see: for instance, given that we see that the floor of an entire street is wet then it probably rained just before. Although the examples usually involve some form of conditional probability, Pearl states that anything that can be computed from the joint distribution belongs to the first level of causation. This includes basically all of the usual machine learning approaches. The notation used by Pearl is the usual probabilistic notation, P(Y = y|X = x), abreviated as P(y|x), this means that we observed X = x and want to know how likely it is for Y to have the value y.

The second level of causation concerns questions of the type: "what's the consequence of some specific action". For instance: "if we make a street wet by throwing water manually into it, what is the probability that it rained?". The difference between seeing and doing is the fundamental distinction between Pearl's first and second levels of causation. Not only is the meaning completely different, it's also impossible to answer questions at the second level of causation by only looking at the data: extra assumptions are necessary. In our example, if we look only at the data what we see is a strong correlation between raining and the floor getting wet, and in principle we have no idea which one causes which. There are also scenarios in which two variables are strongly correlated but neither one causes the other. For instance, in some places the number of ice cream sales is strongly correlated with the

number of deaths by shark attacks, but clearly that's because the times of the year when more people go to the beach are the same of when people buy more ice creams. Pearl proclaims that any method of solving questions at the second level of causation must rely on assumptions beyond the data. One way of structuring many of the relevant assumptions is by using a directed acyclic graph in which each vertex is a variable and each edge represents the causal directions between two variables. There are many other types of assumptions that can be made, Pearl discusses them in detail at [51]. The notation used by Pearl is P(Y = y|do(X = x)), which can be abreviated as P(y|do(x)) or $P(y|\hat{x})$, which can be interpreted as how likely Y is to have value y when we set the value of X to x manually, and when we say "manually", we mean by an external intervention, that is not causally affected by the variables in the system.

The third level of causation regards questions of the type: "what would have happened had something been different?". For instance, "what would be the average temperature of Earth had the Industrial Revolution never happened?". Note that we make an observation about something that happened, then we think what would have happened if we changed something that already happened. This is what Pearl calls a counterfactual question: it requires imagining alternative worlds. To deal with this kind of question, Pearl proposes Structural Causal Models (SCMs), which consider deterministic relationships between variables and adds all the uncertainty to the values of unobserved variables. Also, in the way the Pearl defines counterfactuals, there is a fundamental distinction between counterfactuals and actions with observations: in his notation, when we write the probability of some variable reaching some value given that there was an action and an observation, we interpret this as if the observation came after the action. This is different from the counterfactual notation, in which the observation comes before the action. The notation used by Pearl for the counterfactual notion is $P(Y_{x'} = y | X = x)$, which can be interpreted as how likely it is for Y to have value y in the world that we manually set X to x', given that we observed that the value of X is x. This is different from P(Y = y|do(X = x'), X = x), as this should be interpreted as the probability that Y has a value y when we manually set X to x' and then observe that X has value x, which doesn't make sense if $x \neq x'$ (we shouldn't be able to condition on impossible scenarios). This difference of interpretation can lead to confusion, and was mentioned in the second part of the "question to author" at subsection 11.7.2 of [51].

In general, Judea Pearl's approach to causality assumes an Directed *Acyclic* Graph (DAG) for the relations between variables. This is what is called **recursive models** in [51]. Many results apply only to this type of models, but some generalizations are available and mentioned in [51]. Non-recursive models can be used for representing feedback loops: for instance, price and demand in economic models. This type of model has been widely used in economics in the form of Structural Equations, as presented in subsection 1.4.1 of [51]. Pearl also argues extensively about the possible causal interpretation of such equations, and defines Structural Causal Models as modens in which each variable has an equation that determines its value. This type of model can be used for answering questions of the third level of causation.

Pearl presents many results about Causal Discovery on the second chapter of [51]. Many theoretical results are presented of what can and can not be done regarding the discovery of causal relations when we have access only to data. If two causal structures are capable of generating the same joint distributions, then we will be unable to distinguish between them if we observe only data. Also, sometimes a distribution is unstable for some model, in the sense that although the model can generate this distribution, it can only do so for some very specific configuration of the parameters. For instance, if we have A and B as the outcome of two independent fair coin throws (1 if heads and 0 otherwise, for instance), and C as the XOR between them. In the resulting joint distribution of the three variables, each pair of variables will be marginally independent but dependent if we condition on the third variable. This can be generated by three different causal structures, but only one is stable to small changes in the model (for instance, to small changes in the probability of each coin). With the assumptions that the observed distribution is stable in respect to the underlying causal model, and based on the principle of Occam's Razor, Pearl proceeds to define algorithms to recover as much information as is possible with only the data. In general, it is impossible to distinguish some relations: for instance, $A \to B$ (meaning that A causes B) is indistinguishable from $A \leftarrow B$ or $A \leftarrow U \rightarrow B$ for an unobservable U, as all three of them can generate exactly the same distributions on A, B in a stable way, depending on the model's parameters. Notice that $A \leftarrow U \rightarrow B$ can also generate distributions in which A and B are independent: we can, for instance, set U as the result of a fair four-sided dice with values $\{0,1,2,3\}$, X as an indicator variable of the parity of the result (1 if it is odd and 0 if it is pair) and Y as an indicator of whether the result is bigger than 1 (0 if it is not, 1 if it is), in this case X will be independent of Y even though there is an unobservable confounder U. But this is not stable, in our example if we change slightly the probability distribution of U, for instance by increase the probability of the outcome 0, then X and Y become dependent, $P(X=0|Y=0) \neq P(X=0)$. Pearl provides an extensive analysis of stability and how causal relations are reflected as statistical dependencies between variables in the data.

Causal Inference regards the problem of infering attributes of a causal model given it's structured. In this situation, we have some causal model a priori, and want to estimate quantities such as the P(Y=y|do(X=x)). Pearl introduces the do calculus, which provides a way of deriving expressions for such quantities that do not depend on a do operator, and can thus be estimated from data. The do calculus is based on three basic inference rules, which were shown to be necessary and sufficient, in the sense that a causal effect based on the do operator is identifiable by observing only the data and the assumption of the DAG structure of the underlying model if and only if we can derive an expression without the do operator using only these three rules. Many other quantities can be defined with Pearl's framework, for instance there are also definitions for the identifying the results of dynamic plans, in which one action comes after others and might depend on the results of previous actions. This is further discussed in section 4.4 of [51]. In section 4.5, Pearl dives into two other causal concepts: Direct and Indirect **Effects**, which regard the effects that some variable X have on other variable Y that do or do not depend on other variables. For instance, smoking causes tar deposits in the lungs and also cancer, but we can think of how much of the effect of smoking on the probability of cancer is due to tar deposits, and how much is due to other more direc factors. Natural Direct Effects are "average" estimations of direct effects for the different values the variables can assume, as the way that Pearl defines Direct and Indirect Effects is dependent of the exact values of the variables in question.

Another contribution of the causality framework presented in [51] is the causal approach to **confounding**. In some situations, it is necessary to condition on some variables to account for possible spurious correlations that might arrise due to confounding, but in other situations controling for some variables would actually create new spurious correlations. This also depends on what we want to compute, but if the goal is computing the effect of some intervention, then the do-calculus can be used. Pearl argues in chapter 6 of [51] in favor of the causal approaches to confounding.

Counterfactual statements are defined in terms of simpler axioms, [51, Chapter 7] further discusses many results about counterfactuals. These results include how to use an Structural Causal Model to estimate the value counterfactual statements, or how to check if this is even possible to estimate only with the SCM and data. Chapter 8 delves into the problem of bounding values of expressions that can not be computed directly. Pearl also discusses how some extra assumptions and tools can help in the estimation of expressions with the *do* operator and counterfactual expressions, for instance, if we can experimentally change the value of some variables via external interventions then some effects are easier to estimate.

Finally, there are some subtleties to the meaning of causation in different settings. Pearl discusses many notions of causation, including the probability of necessity, the probability of sufficiency, the natural direct effect (which we already mentined), the actual cause, and others. We say that X=1 was a sufficient cause of Y=1 if when we are in a situation in which X=0 and Y=0 we expect that manipulating the value of X so it becames 1 is likely to change the value of Y to 1, in Pearl's notation $P(Y_{X=1}=1|X=0,Y=0)\approx 1$, and $P(Y_{X=1}=1|X=0,Y=0)$ is called the **Probability of Sufficiency**. We say that X=1 was a necessary cause of Y=1 if when we are in a situation in which X=1 and Y=1 we expect that manipulating the value of X so it becomes 0 is likely to change the value of Y to 0, in Pearl's notation $P(Y_{X=0}=0|X=1,Y=1)\approx 1$, and $P(Y_{X=0}=0|X=1,Y=1)$ is called the **Probability of Necessity**. There is also the **Probability of Necessity and Sufficiency**, defined as the chance that manipulating the value of X so it becomes 1 will set Y to 1 and manipulating X so it becomes 0 will set Y to 0, written as $P(Y_{X=1}=1,Y_{X=0}=0)$. Pearl also defines the **Probability of Disablement** as $P(Y_{X=0}=0|Y=1)$ and the **Probability of Enablement** as $P(Y_{X=1}=1|Y=0)$. Many relations between these values, bounds and conditions for identification are presented in [51, Chapter 9].

The notion of Actual Cause is defined as an alternative to the sufficient and necessary notions of causation. Pearl mentions that necessary causation is closer to **token-level**, more individual than generic, as it conditions on events that really happenned, while sufficient causation is closer to **type-level**, more generic than individual, as the events we condition on are less specific and related to an alternative imaginary scenario. The Actual Cause is intended to be token-level, to define what actually caused something. It is defined in terms of Causal Beams and Sustenance.

We say that X=x causally sustains Y=y in U=u (representing the uncertainty, the unobservable factors) relative to contingencies in W if and only if we have: X=x and Y=y under U=u, for any w we get Y=y under U=u and interventions that set X=x and W=w, and we get $Y=y'\neq y$ under U=u and interventions that set X=x', W=w' for some $x'\neq x$ and some w'. In other words, X=x causally sustains Y=y in the circumstances Y=x0 in the value of Y=x1 in the value of Y=x2 in the value of Y=x3 in the value of Y=x4 in the value of Y=x5 in t

of X and Y, keeping everyting else as it is with U=u. This means that in the situation that actually happenned U=u, then X=x is enough to sustain Y=y under inverventions on W, but if we intervene to change X there will be a scenario in which intervening in W changes Y. If $W=\emptyset$, then X=x causally sustains Y=y in U=u relative to W if in U=u we have X=x and Y=y, but it is possible to change Y by changing X.

A Causal Beam is a causal model defined in terms of circunstances U=u and another causal model, such that the parents of each node in the new model are sufficient to entain the value of the node regardless of the value of changes on the other parent's values, and that it is possible to change the value of other parents and the new parents to change the value of the node. If changing the value of only the new parents is enough to change the value of the node for every node, then the Causal Beam is considered a Natural Beam. Natural Beams represent the simplified version of the model that represents the actual scenario U=u, such that the parents of each node are enough to sustain the value of the node regardless of changes in other variables, and are also capable of changing the value of the node by themselves. Pearl notes that in the definition of Causal Models provided, the parents of a node are defined in a way that makes the functions of the model non-trivial regarding all their arguments and all possible circunstances u, but when we consider a specific value of u0 we can simplify the model further. The example introduced by Pearl considers u1 when u2 as the function that defines the value of variable u3 in the original model: in this scenario when u3 becomes irrelevant, so we can simplify the model by defining u4.

Finally, we say that X=x is an **Actual Cause** of Y=y in the state U=u if and only if there is a natural beam under circumstances U=u such that if intervene with X=x then Y=y and if we intervene with X=x' for some $x'\neq x$ we get $Y\neq y$. This represents a token-level causation, whether or not X=x actually caused Y=y in the real scenario U=u. As with many of the results presented, these definitions assume we have a full description of the causal model. The notion of Actual Cause is further discussed in Chapter 10 of [51].

G. Quantitative Information Flow

The area of Quantitative Information Flow deals with methods of measuring information leak from systems. This estimation is important to consider when developing real systems, as some information leaks are acceptable. For instance, whenever someone tries to authenticate with an username and password, but incorrectly guesses the password, some information leaked about the real value of the password: we now at least know that it's not the one that was tried. But intuitively, this is acceptable, while revealing the real password whenever someone makes an incorrect guess is unacceptable. How to adequately quantify the ammount of information leak from a system might depend on the goals of the people involved and on the information they have before the system executes.

We define an **adversary** as an agent that tries to gain something with the information that leaks from the system, the **secret** as the data that the system processes, the **prior** as the distribution on secrets that represents the knowledge of the adversary before the system is run, and the **posterior** as the hyper-distribution (a distribution on distributions) on secrets that represents the knowledge of the adversary after the system is run. We use an information-theoretic **channel** to represent the distributions of observable values outputed from the system, which might depend on the secret value. The set \mathcal{X} represents the set of possible values of the secrets, the set \mathcal{Y} represents the possible values of observable outputs of the system, and the set \mathcal{W} represents the possible values of actions the adversary might take.

We consider the g-vulnerability framweork, introduced in [6]. We define a gain function $g: \mathcal{W} \times \mathcal{X} \to \mathbb{R}$, such that g(w,x) defines the gain of the adversary if she takes the action w when the actual secret value is x. We consider a zero-sum game: the gain of the adversary is exactly the loss of the people responsible for the system. The **prior vulnerability** of the system is defined as the average gain of the adversary if she takes the action that maximizes her gain, according to the prior distribution on secrets that represents her knowledge of the secret. The **posterior vulnerability** of the system is defined in the same way, but considering the hyper-distribution that represents the posterior knowledge. Notice that each distribution in the posterior hyper-distribution represents the knowledge of the adversary after some of the possible observations after the system is run, so it represents what we, before the system runs, estimate will be the future values of the adversarial knowledge after the system runs. The **additive leakage** can be defined as the difference between posterior and prior vulnerability, and the **multiplicative leakage** as the result of dividing of the posterior vulnerability by the prior vulnerability values. As teorema leak $\zeta = 1$ $\zeta = 0$

There are some valuable theoretical results about channels regarding the relationships between prior and posterior g-vulnerabilities. Chapter 7 of [6] shows results about the *capacity* of a channel, which is the maximum possible (aditive or multiplicative) leakage that can happen through a channel if we fix either the prior, the gain function or neither. Chapter 9 discusses results about *refinement* of channels: in short, a channel is strictly better (for all

priors and gain functions) to another channel in respect to the posterior vulnerability if and only if it can be written as a post-processing of this other channel. Chapter 10 discusses the notion of *Dalenious vulnerability*: it might be the case that the adversary is interested in a secret other than the one considered in the system, and can obtain information about this other system via a known joint distribution between this other secret and the secret that the system considers. In this case, a channel is also strictly better than another in respect to Dalenious leakage, for any such joint distribution and gain function, if and only it can be written as a post-processing of this other channel. Chapter 11 [6] discusses the axiomatic characterization of the notion of vulnerability, and even how some results can be obtained by different axioms that consider the worst-case scenario instead of the average gains of the adversary.

V. CONTRIBUTIONS: A REVIEW OF THE RELATIONS BETWEEN THE CONCEPTS

In this section we mention comparisons found in the literature between these areas of research, and comment some ideas for unexplored relations in the literature.

A. $Accuracy \times Fairness$

There are results that indicate an inherent trade-off between fairness and accuracy in machine learning:

- 1) [53] shows that there are trade-offs between Equal Oportunity Difference and accuracy such that, depending on the data distribution, it might impossible to achieve both perfect Equal Oportunity Difference and non-trivial accuracy. It also shows some other theoretical results that associate EOD and accuracy, such as sufficient conditions for the existance of non-trivially accurate predictors that lead to zero Equal Opportunity Difference and non-trivial accuracy and algebraic and geometric properties of the feasible values of Equal Opportunity Difference and accuracy.
- 2) [1] provides methods for computing the best possible accuracy given some level of fairness, for a general notion of fairness that encompasses many common metrics. They devise an algorithm for solving a constrained linear optimization problem that minimizes the error subject to fairness constraints, and provide experimental results for some datasets, including the COMPAS [8] dataset. One interesting results is that for some datasets (such as the Compas dataset), it is possible to reduce Equal Opportunity Difference without changing much the accuracy, but for some datasets (such as the Dutch Census Dataset [49] with gender as the protected attribute and the goal is if someone has a prestigious occupation) precisava citar o dataset assim?
- 3) [32] shows that it is always possible for an adversary to corrupt the data available for a learning algorithm in a way that the algorithm is unfair, and sometimes it is possible to do so without changing the accuracy.
- 4) [65] Provides a method of finding the full Paretto front of accuracy versus fairness. Their approach is based on a genetic algorithm, and the notion of fairness that they consider is False-Positive Rate for avoiding disparate mistreatment, but it is possible to use most metrics available in the literature.
- 5) [26] provides empirical analysis of some of the existing fairness-enhancing methods for machine learning, showing that the results are influenced a lot by the fairness notion used and also by the dataset.

B. $Accuracy \times Privacy$

If we consider obfuscation methods for privacy (such as Differential-Privacy and Local Differential Privacy mechanisms), in general bigger privacy constraints imply in a smaller accuracy when training Machine Learning Models. There are also homomorphic encryption and secure multi-party computation approaches, which have computational complexity as a major challenge instead of the accuracy. In fact, some predictions can be made without any loss of accuracy at all, as shown in [72] for the naive Bayes classifier. Notice that in the Local Differential Privacy context, we know exactly how the noise is applied an thus might be able to reverse some the effect of the noise when training the model, and in general the effectiveness of this reversion determines how much the accuracy of the model will be affected.

- 1) [71] provides an overview of the use of Local Differential Privacy in general, but also further discusses machine learning in the local different privacy scenario, both for unsupervised and supervised learning.
- 2) [75] compares Local Differential Privacy and Federated Learning approaches empirically, concluding that LDP approaches consume less computational resources on the client-side, benefits from a large user population and can be reused for other tasks, while the data transferred to the server for the Federated Learning approach is specific for one inference task.
- 3) [54] proposes a method for applying Local Differential Privacy to high-dimensional data, and evaluates it empirically, showing that in general stronger privacy also implies smaller accuracy.

- 4) [39] explores differential privacy in the setting in which the individual data points are correlated in a way that can be explored by the adversary, and investigates how to provide better privacy guarantees in this scenarios. This might be important to consider in the machine learning scenario as well in the future, as the advesary might take advantage of such correlations in this type of situation as well.
- 5) [72] discusses how to use homomorphic encryption to preserve privacy without loss of accuracy. The classification algorithm used as an example is the naive bayes classifier,

C. Accuracy \times Explainability

If the Machine Learning model is inherentely interpretable by humans, then usually it is less accurate than more complex models (the most common example are the deep convolutional neural networks). Also, explainability methods might help the model developer in identifying problems and improving the model quality, which might include improving the accuracy [14]. Also, for simpler models it might be possible to keep good accuracy and explainability levels.

- 1) [52] discusses some arguments for and against this dilemma, and points out some options of where the focus should be when developing and implementing Machine Learning systems.
- 2) [40] argues that in some situations it might be better to accept results without an explanation when these results can be empirically verified to lead to better results than well-explained results. Two important points raised by the paper are: "The opacity, independence from an explicit domain model, and lack of causal insight associated with some powerful machine learning approaches are not radically different from routine aspects of medical decision-making" and "In medicine, the ability to intervene effectively in the world by exploiting causal relationships often derives from experience and precedes clinicians' ability to understand why interventions work."
- 3) [7] discusses the known trade-offs between accuracy and explainability for some distinct scenarios and models, the areas that can benefit the most from explainable ML and a general review of explainability.
- 4) [10] and [2] provide an empirical study on whether explanations for AI predictions do or do not improve the accuracy of human decision-making, and the results indicate that this might not be the case.
- 5) [67] provides an empirical study to evaluate the opinion of the general public on whether it is worth trading explainability for accuracy in healthcare and non-healthcare scenarios. The conclusion is that in healthcare accuracy is favored, and in other scenarios explainability is valued equally to or more than accuracy.

D. $Accuracy \times Causality$

Accuracy is about how much a machine learning model makes correct guesses, Causality is about studying the causal relationships between variables. We can say that the problem of getting good accuracy lies on the first level of causation, as we are concerned about the data, although we could, for instance, use causality concepts to transfer what was learned with the data of one population to another. In some situations, algorithms based on causal notions can be even more accurate than purely associative algorithm.

- 1) [56] presents a counterfactual-based algorithm for medical diagnosis when there are many possible causes for a patient's symptoms. Their algorithm results in better accuracy than some classical Machine Learning algorithms not based on causal notions.
- 2) [60] discusses many relations between causal learning and machine learning, including references to works that discuss the idea of transfering results to different populations without losing too much accuracy.
- 3) [74] present a method of selecting features with causal analysis before training a machine learning model based on causal concepts, and show that this approach can improve accuracy of network intrusion detection when compared to classical machine learning methods.

E. Accuracy \times QIF

Acuracy can be viewed as a form of utility, which represents how useful a system is, which might be affected by how vulnerable it is. It is trivial to develop a system without any vulnerability, for instance, a system that always outputs 0 no matter what is the input. But it's not useful, so we can consider that QIF is related to accuracy when we consider the former as the study of information leakage from a system and the latter as a form of measuring utility.

F. Fairness × Privacy

There are some impossibility results in the literature that argue why it is impossible to achieve both pricacy and group fairness constraints under non-trivial accuracy [20]. We also have positive results that show how stasifying privacy constraints can help mitigating group unfairness [44] [43] [9], and we also have similar positive results results for individual fairness notions [21].

- 1) [44] aims to provide theoretical results that relate how training a machine learning model on a dataset in which local differential privacy mechanisms were applied can impact the fairness of this model, if the data-gatherer does not try to reverse the applied noise. The results are provided for a simplified machine learning model, from a theoretical persepctive.
- 2) [43] aims to evaluate experimentally how training a machine learning model on a multi-dimensional data set in which local differential privacy mechanisms were applied can impact the fairness of the model, again if the data-gatherer does not try to reverse the noise.
- 3) [9] executes an empirical evaluation of the impact of many Local Differential Privacy mechanisms on fairness when we do not try to reverse the applied noise, including a new privacy budget allocation scheme based on the domain size of sensitive attributes.
- 4) [21] introduces a notion of individual fairness that is a generalization of differential privacy, and explores the relationship between this notion of fairness, differential privacy and statistical disparity.
- 5) [20] present theoretical results that show the impossibility of having a classifier that is not trivially accurate and at the same time satisfies $(\epsilon, 0)$ -differential privacy and equality of opportunity constraints. The paper also shows a PAC learner for an approximate fairness definition they provide.
- 6) [30] compiles results that relate the concetps of privacy and fairness, and also causal discovery.
- 7) [25] discusses the use of Homomorphic Encryption in combination with fair representation learning [73] to provide both privacy and fairness guarantees, respectively, when training machine learning models. Then the paper discusses how to provide local and global explanations for the model.

G. Fairness × Explainability

Fairness evaluation is a goal usually mentioned when the utility of explainability studies is discussed in the literature [58]. There are also some negative results in this respect, that indicate that in some situations, it is possible to provide convincingly fair explanations for decisions that were actually made in an unfair way [76].

- 1) [58] discusses how not providing explanations for decision can threaten accountability, bias avoidance and transparency when evaluating and mitigating unfairness in ML-based decisions.
- 2) [76] shows empirical results of training a baseline, a fair, an unfair and a random model on the COMPAS [8] dataset and then finding possible explanations for the results provided by the model. The paper explores a space of explanations that are simple, verifiable and relevant according to definitions they provide for these terms, and show that it's possible to provide valid justifications for the decisions for the majority of the models. They also explore the situation in which explanations are provided for many data points and then analysed to verify for consistency, sufficiency and uniqueness (which they define formally in the paper), and achieve similar results: it can be possible to provide justifications for almost any decision that seem valid, even if the justification does not reflect how the model really decides.
- 3) [25] discusses the use of Homomorphic Encryption in combination with fair representation learning [73] to provide both privacy and fairness guarantees, respectively, when training machine learning models. Then the paper discusses how to provide local and global explanations for the model.

H. Fairness × Causality

Fairness might be considered a causal concept: we want to know whether the outcome was or was not caused by an unfair process. The causal distinction might be important because, for instance, we might consider some causes fair and others unfair for the decision of not hiring someone. If the cause of the decision was the educational background and work experience of the person, it is usually considered fair, but if it is the skin color of the person it is usually considered unfair. There are many different definitions of causal notions of fairness, each of it's own specific meaning, as with causal notions in general.

- 1) [51] mentions notions of sex discrimination in college admissions and discrimination in hiring. Pearl also argues why the causal interpretation should be used instead of purely statistical notions.
- 2) [47] and [62] survey many of the causal definitions of fairness present in the literature, [47] also classifies them according to Pearl's levels of causation and guidelines for which situations best suit each notion.

- 3) [59] shows a causal interpretation of notions of fairness and approaches the conflict between different fairness notions from this perpective. One important note is that this paper does not use the correct notion of equalized odds, it reverses Y and \hat{Y} : the correct notion is that the prediction is independent of the sensitive attriute given the ground-truth, but they consider the definition of the output being independent of the sensitive attribute given the prediction. The correct notion of equalized odds is what they call predictive parity. This paper was found in arxiv.org.
- 4) [45] compiles major identifiability results from the causality literature and also discusses how they can be used in practice to obtain causal knowledge from data.

I. Fairness × OIF

One possibility of measuring fairness with Quantitative Information Flow notions is to measure the *reverse flow*: instead of looking at how much observing the output of a model helps in estimating input values (this would be a privacy concern), we measure how much observing the sensitive attribute helps in estimating output values. This idea is explored in [5] and [50].

J. $Privacy \times Explainability$

One of the main questions of the relation between Privacy and Explainability is whether explainability is affected when privacy-preserving mechanisms are applied. Some results indicate that this is not always the case, but the conceptual differences are discussed times in more detail througout the literature.

- 1) [13] evaluates the effect of applying privacy protection mechanisms on Shapley values, which can be used for explanation purposes, both local and global. The conclusion is that applying privacy-protection mechanisms does not affect much explanations based on Shapley values.
- 2) [28] discusses the legislation of privacy and explainability, arguing that we should not have both in the law, as they claim that demanding explanations can inevitably lead to demands on the visualization of the training data itself.
- 3) [24] points some conflicts and synergies that involve the two concepts: the conflicts include the conceptual difference between demanding more transparency in respect to the process and demanding secrecy in respect to the training data, which is part of the training process of the model, the possibility of using data obtained from explainability methods to infer sensitive inforantion. The synnergies involve the possibility of using inforantion obtained from explainability methods to improve the privacy of the model, and the fact that some results in the literature claim to have achieved good explainability for some models while keeping acceptable privacy constraints.
- 4) [25] discusses the use of Homomorphic Encryption in combination with fair representation learning [73] to provide both privacy and fairness guarantees, respectively, when training machine learning models. Then the paper discusses how to provide local and global explanations for the model.

K. Privacy \times Causality

In regard to the relationship between privacy and causality, one approach in the literature is to try to provide privacy for sensitive data by the addition of noise, and at the same time allow causal discovery and causal inference based on the noisy data. Another relation noted in the literature is that models based on causal relationships between variables are more resilient to privacy attacks, such that privacy-protection mechanisms are more effective for this type of model. Another possibility is modeling differential privacy as a causal, instead of purely statistical, property.

- 1) [12] discusses local differential privacy in the context of causal discovery: how local differential privacy mechanisms affect the task of causal discovery. The conclusion is that the geometric mechanism has a smaller effect than the methods based on generalizations of the Randomized Response mechanism, as they tend to degrade less the original correlations present in the data. It seems that this paper also doesn't try to recover the original distribution from the noisy one before trying causal discovery...
- 2) [63] shows that models that use only the parents of the target variable, which they call causal models, provide stronger ϵ -differential privacy guarantees, are provably more robust to Membership Inference Attacks, generalize better to other distributions based on the same causal structure.
- 3) [64] discusses how differential privacy can be interpreted as a causal notion and what are the benefits of this interpretation. They analyse some possible causal and associational interpretations of the intuitive idea of Differential Privacy. The causal interpretations consist of interventions on all data points or one data point, and they distinguish between an individual's data point and the real value of the individual. They show the

equivalence between many of the definitions they present and the unidirectional implications of two of them. In summary:

- a) Differential privacy constraints on an algorithm that takes many data points as input can be interpreted as requiring that the output value of this algorithm does not change if we change only one data point. This will be considered the definition of Differential Privacy.
- b) This is equivalent to requiring that for any input distributions the probability of any outcome of the algorithm is the similar if one data point was observed to be different and the rest equal.
- c) This is equivalent to requiring that for any distribution with independent data points such that any individual data point value is possible, the probability of any outcome of the algorithm is the same if one data point was observed to be different.
- d) Requiring the same as above without the assumption of independent data points is a stronger requirement than differential privacy (it implies DP, but not the opposite).
- e) This is also equivalent to causal notions that require that intervening to change one value and *intervening* to keep the others constant do not change much the probability of any outcome. This holds regardless of whether we consider that for an algorithm to satisfy differential privacy this must hold for all distributions or for only one (as the interventions are done on *all* variables).
- f) This is also equivalent to the causal notion that interevening on one variable should not change much the probability of each output, if we consider this must hold for all probability distributions.
- g) If we consider the previous definition but without requiring to hold for all distributions, then for technical reasons of specific zero probability distributions, this is weaker than differential privacy (DP implies this definition, but not the opposite).
- 4) [70] discusses new methods to pursue causal discovery and at the same time mantain differential privacy guarantees. The core of the idea considered is to obtain some independence information from the original data in order to reduce the privacy budget necessary for differential privacy. The focus of this paper is classical differential privacy instead of local differential privacy.
- 5) [34] discusses causal inference instead of causal discovery under differential privacy guarantees, for the causal discovery framework of Additive Noise Model.

L. Privacy × QIF

As QIF aims to quantify the flow of information, we can naturally consider applying it to the privacy scenario, by measuring how much information leaks about an arbitrary individual. One general idea is that differential privacy is a worst-case notion and g-vulnerability is an average-case notion, and there are results [6] showing that differential privacy implies bounds on leakage under arbitrary gain functions and prior distributions, but not the opposite.

- 1) [4] discusses the relations between differential privacy and g-vulnerability, including bounds on g-leakage as a function of the ϵ parameter of differential privacy, and the fact that there is no bound on differential privacy as a function of the g-vulnerability.
- 2) [23] discusses how the ϵ parater of Differential Privacy is related to max-case g-vulnerability: e^{ϵ} is exactly the multiplicative max-case channel capacity under a fixed prior. This work also discusses many other theoretical results relating g-vulnerability notions with differential privacy. *Found in arxiv.org*.

M. Explainability \times Causality

Causal models are considered inheretly interpretable, as the causal relationships between variables are explicitly represented in the model. Many machine learning explanation methods are based only on the data and thus based on the correlations between variables, so they usually lack a causal basis, which is a recurrent critic to such methods. So, another possible relation between the two concepts is to apply causal tools and measures to improve the quality of the machine learning explanations.

- 1) [69] discusses how machine learning models in combination with explainability methods may not capture all the relevant correlations between the variables. As mentioned in the paper these explanations are *local to the model*, and the paper shows that they important correlations in the data might not be captured by ML models trained with the data. *This paper was found in arxiv.org*.
- 2) [42] discusses a method of providing causal-based explanations for some types of user queries. The idea is to estimate a causal graph from the data and answer queries of why some effect is observed by estimating the causal effect of each variable. The causal notion used is Database Causality, an extension of Pearl's Actual Causality.

- 3) [17] provides a broad literature review of the relations between causality and explainability. They identify three main connections between the two concepts present in the literature:
 - a) Some works present critics to Explainable AI through a causal perspective, which involve mainly the fact that many explainability approaches lack a causal interpretation, others discuss problems with non-causal explanations in general, and others discuss the adequate form of presenting explanations.
 - b) Some works support explainability as a basis for further causal investigation, which might be done empirically.
 - c) Finally, some works adhere to the idea of using causal tools to support machine learning model explanations, for instance the use of the *do* operator, the estimation of the probability of necessity and the probability of sufficiency etc.. Causal counterfactual explanations are also considered, and some works consider simply providing a coherent causal model of a system to be a form of explaining the system itself.

N. Explainability \times QIF

It might be possible to create an explanation method based on how much information flows through each input to the outputs of a machine learning model. The relation between these two concepts remain largely unexplored. There is, though, an approach by [16, Part III] that uses an alternative definition of information based on sigma algebras and brings concepts from measure theory to provide some theoretical results involving deep learning.

O. Causality \times QIF

Some unpublished preliminary work indicate that there might be a relation between causal discovery and Quantitative Information Flow metrics. But the relation between these two concepts still remains largely unexplored. Faz sentido mencionar isso?

VI. CONCLUSIONS AND FUTURE WORK

We can summarize our findings in the following way:

- 1) **Accuracy** × **Fairness:** There is an inherent trade-off between accuracy and some notions of fairness such as Equal Opportunity Difference and Statistical Parity.
- 2) **Accuracy** × **Privacy**: Privacy by addition of noise usually reduces accuracy. Privacy by homomorphic encryption does *not* affect accuracy at the cost of greater computational complexity.
- 3) **Accuracy** × **Explainability:** In many situations, more interpretability implies less accuracy (as more compex models are harder to explain/interpret).
- 4) **Accuracy** × **Causality:** Causality might help in the transference of machine learning model results between distinct populations, and the development with causal basis can reduce how sensible it is to small changes in the data used to train the model.
- 5) **Accuracy** × **QIF:** accuracy can be seem as a form of utility, which usually has a trade-off with information leakage, measured by QIF.
- 6) **Fairness** × **Privacy:** If the privacy-preserving mechanism is based on noise, then it might help in reducing unfairness according to some measures. Most results use the noisy distribution directly, without first trying to recover the original distribution.
- 7) **Fairness** × **Explainability:** One possibility for checking wheter a system is fair is to demand explanations for the system's working, but sometimes it is possible to deceive this verification.
- 8) Fairness \times Causality: there are many distinct causal fairness notions, each with their own meaning and class of applicable situations.
- 9) **Fairness** × **QIF:** Fairness might be measured by *reverse* information flow, how much one can infer from the output by observing the sensitive values of the input instead of how much can be inferred from the input from observing the output.
- 10) **Privacy** × **Explainability:** Conceptually, more privacy implies less explaination power as the data points can not be used in explanations. In practice, however, privacy constraints do not seem to have an impact on some of the classical XAI methods.
- 11) **Privacy** × **Causality:** Causal interpretations were used to disentangle confusions about Differential Privacy assumptions, we can use causal notions to improve the use of differential privacy budget and some methods make causal discovery/inference harder.
- 12) **Privacy** \times **QIF:** It is possible to use the Quantitative Information Flow *g*-vulnerability framework to model private information leakage, and there are theoretical results that show relations with differential privacy, with equality for max-vulnerability.

- 13) **Explainability** × **Causality:** In many situations, causal explanations the final goal and although classical explainability methods are based only on the data, it might be possible to use them as basis for further empirical explanation.
- 14) **Explainability** × **QIF:** The relationship between these two is largely unexplored. Maybe it's possible to provide explanations based on how much information flows from each feature to the output?
- 15) Causality × QIF: The releationship between these two ins largely unexplored too. There is some preliminary unpublished work relating QIF and causal discovery, though. Faz sentido falar isso?

There are some possibles avenues for future works:

- 1) Using Quantitative Information Flow notions to develop explainability methods.
- 2) Using Quantitative Information Flow notions to quantify the flow of information for all types of machine learning attacks.
- 3) Explore what happens with the Privacy × Fairness and Privacy × Accuracy trade-offs under noisy distributions if we first try to recover the original distribution.
- 4) Exploring the relationship between Quantitative Information and causality, maybe by measuring the information flow between variables to see which variable should be observed to increase the expected information gain on other variables, or other relations.
- 5) Discover to which variables to add noise in order to hinder individual sensitive attribute inference under the least possible privacy budget expense.
- 6) Using Quantitative Information Flow to develop privacy results similar to the ones obtained with Differential Privacy, maybe by developing new and useful gain functions.
- 7) Combining existing results to modern Learning Theory, especially by using theoretical results related to Deep Learning.

REFERENCES

- [1] Agarwal, A., Beygelzimer, A., Dudik, M., Langford, J., Wallach, H.: A reductions approach to fair classification. In: Dy, J., Krause, A. (eds.) Proceedings of the 35th International Conference on Machine Learning. Proceedings of Machine Learning Research, vol. 80, pp. 60–69. PMLR (10–15 Jul 2018), https://proceedings.mlr.press/v80/agarwal18a.html
- [2] Alufaisan, Y., Marusich, L.R., Bakdash, J.Z., Zhou, Y., Kantarcioglu, M.: Does explainable artificial intelligence improve human decision-making? In: Proceedings of the AAAI Conference on Artificial Intelligence. vol. 35, pp. 6618–6626 (2021)
- [3] Alves, G., Bernier, F., Couceiro, M., Makhlouf, K., Palamidessi, C., Zhioua, S.: Survey on fairness notions and related tensions. EURO journal on decision processes 11, 100033 (2023)
- [4] Alvim, M.S., Andrés, M.E., Chatzikokolakis, K., Degano, P., Palamidessi, C.: On the information leakage of differentially-private mechanisms. Journal of Computer Security 23(4), 427–469 (2015)
- [5] Alvim, M., Fernandes, N., Nogueira, B., Palamidessi, C., Silva, T.: On the duality of privacy and fairness (extended abstract). In: International Conference on AI and the Digital Economy (CADE 2023). Institution of Engineering and Technology, United Kingdom (2023). https://doi.org/10.1049/icp.2023.2563, 9th International Conference on AI and the Digital Economy, CADE 2023; Conference date: 26-06-2023 Through 28-06-2023
- [6] Alvim, M., Chatzikokolakis, K., McIver, A., Morgan, C., Palamidessi, C., Smith, G.: The Science of Quantitative Information Flow. Information Security and Cryptography, Springer International Publishing (2020), https://books.google.com.br/books?id=jJH-DwAAQBAJ
- [7] Angelov, P.P., Soares, E.A., Jiang, R., Arnold, N.I., Atkinson, P.M.: Explainable artificial intelligence: an analytical review. Wiley Interdisciplinary Reviews: Data Mining and Knowledge Discovery 11(5), e1424 (2021)
- [8] Angwin, J., Larson, J., Mattu, S., Kirchner, L.: Machine bias: There's software used across the country to predict future criminals. and it's biased against blacks. URL https://www.propublica.org/article/machine-bias-risk-assessments-in-criminal-sentencing (2019)
- [9] Arcolezi, H.H., Makhlouf, K., Palamidessi, C.: (local) differential privacy has no disparate impact on fairness. In: IFIP Annual Conference on Data and Applications Security and Privacy. pp. 3–21. Springer (2023)
- [10] Bell, A., Solano-Kamaiko, I., Nov, O., Stoyanovich, J.: It's just not that simple: an empirical study of the accuracy-explainability trade-off in machine learning for public policy. In: Proceedings of the 2022 ACM conference on fairness, accountability, and transparency. pp. 248–266 (2022)
- [11] Belle, V., Papantonis, I.: Principles and practice of explainable machine learning. Frontiers in big Data 4, 688969 (2021)
- [12] Binkyte, R., Pinzón, C.A., Lestyán, S., Jung, K., Arcolezi, H.H., Palamidessi, C.: Causal discovery under local privacy. In: Causal Learning and Reasoning. pp. 325–383. PMLR (2024)
- [13] Bozorgpanah, A., Torra, V., Aliahmadipour, L.: Privacy and explainability: The effects of data protection on shapley values. Technologies 10(6), 125 (2022)
- [14] Burkart, N., Huber, M.F.: A survey on the explainability of supervised machine learning. Journal of Artificial Intelligence Research 70, 245–317 (2021)
- [15] Calin, O.: Deep learning architectures. Springer (2020)
- [16] Calin, O.: Deep learning architectures. Springer (2020)
- [17] Carloni, G., Berti, A., Colantonio, S.: The role of causality in explainable artificial intelligence. arXiv preprint arXiv:2309.09901 (2023)
- [18] Carvalho, D.V., Pereira, E.M., Cardoso, J.S.: Machine learning interpretability: A survey on methods and metrics. Electronics 8(8), 832 (2019)
- [19] Chouldechova, A., Roth, A.: The frontiers of fairness in machine learning. arXiv preprint arXiv:1810.08810 (2018)
- [20] Cummings, R., Gupta, V., Kimpara, D., Morgenstern, J.: On the compatibility of privacy and fairness. In: Adjunct Publication of the 27th Conference on User Modeling, Adaptation and Personalization. p. 309–315. UMAP'19 Adjunct, Association for Computing Machinery, New York, NY, USA (2019). https://doi.org/10.1145/3314183.3323847, https://doi.org/10.1145/3314183.3323847

- [21] Dwork, C., Hardt, M., Pitassi, T., Reingold, O., Zemel, R.: Fairness through awareness. In: Proceedings of the 3rd Innovations in Theoretical Computer Science Conference. p. 214–226. ITCS '12, Association for Computing Machinery, New York, NY, USA (2012). https://doi.org/10.1145/2090236.2090255, https://doi.org/10.1145/2090236.2090255
- [22] Dwork, C., Ilvento, C.: Fairness under composition. arXiv preprint arXiv:1806.06122 (2018)
- [23] Fernandes, N., McIver, A., Sadeghi, P.: Explaining epsilon in local differential privacy through the lens of quantitative information flow. arXiv preprint arXiv:2210.12916 (2022)
- [24] Ferry, J., Aïvodji, U., Gambs, S., Huguet, M.J., Siala, M.: Sok: Taming the triangle on the interplays between fairness, interpretability and privacy in machine learning. ArXiv abs/2312.16191 (2023), https://api.semanticscholar.org/CorpusID:266573131
- [25] Franco, D., Oneto, L., Navarin, N., Anguita, D.: Toward learning trustworthily from data combining privacy, fairness, and explainability: an application to face recognition. Entropy 23(8), 1047 (2021)
- [26] Friedler, S.A., Scheidegger, C., Venkatasubramanian, S., Choudhary, S., Hamilton, E.P., Roth, D.: A comparative study of fairness-enhancing interventions in machine learning. In: Proceedings of the conference on fairness, accountability, and transparency. pp. 329–338 (2019)
- [27] Gilpin, L.H., Bau, D., Yuan, B.Z., Bajwa, A., Specter, M., Kagal, L.: Explaining explanations: An overview of interpretability of machine learning. In: 2018 IEEE 5th International Conference on data science and advanced analytics (DSAA). pp. 80–89. IEEE (2018)
- [28] Grant, T.D., Wischik, D.J.: Show us the data: Privacy, explainability, and why the law can't have both. Geo. Wash. L. Rev. 88, 1350 (2020)
- [29] Grohs, P., Kutyniok, G.: Mathematical aspects of deep learning. Cambridge University Press (2022)
- [30] Henao, C.P.: Exploring fairness and privacy in machine learning. Ph.D. thesis, Institut Polytechnique de Paris (2023)
- [31] Kearns, M., Neel, S., Roth, A., Wu, Z.S.: Preventing fairness gerrymandering: Auditing and learning for subgroup fairness. In: International conference on machine learning. pp. 2564–2572. PMLR (2018)
- [32] Konstantinov, N., Lampert, C.H.: On the impossibility of fairness-aware learning from corrupted data. In: Algorithmic Fairness through the Lens of Causality and Robustness workshop. pp. 59–83. PMLR (2022)
- [33] Krishnan, M.: Against interpretability: a critical examination of the interpretability problem in machine learning. Philosophy & Technology 33(3), 487–502 (2020)
- [34] Kusner, M.J., Sun, Y., Sridharan, K., Weinberger, K.Q.: Private causal inference. In: Artificial Intelligence and Statistics. pp. 1308–1317. PMLR (2016)
- [35] Li, L., Lassiter, T., Oh, J., Lee, M.K.: Algorithmic hiring in practice: Recruiter and hr professional's perspectives on ai use in hiring. In: Proceedings of the 2021 AAAI/ACM Conference on AI, Ethics, and Society. pp. 166–176 (2021)
- [36] Linardatos, P., Papastefanopoulos, V., Kotsiantis, S.: Explainable ai: A review of machine learning interpretability methods. Entropy 23(1), 18 (2020)
- [37] Lipton, Z.C.: The mythos of model interpretability: In machine learning, the concept of interpretability is both important and slippery. Queue 16(3), 31–57 (2018)
- [38] Liu, B., Ding, M., Shaham, S., Rahayu, W., Farokhi, F., Lin, Z.: When machine learning meets privacy: A survey and outlook. ACM Computing Surveys (CSUR) 54(2), 1–36 (2021)
- [39] Liu, C., Chakraborty, S., Mittal, P.: Dependence makes you vulnberable: Differential privacy under dependent tuples. In: NDSS. vol. 16, pp. 21–24 (2016)
- [40] London, A.J.: Artificial intelligence and black-box medical decisions: accuracy versus explainability. Hastings Center Report 49(1), 15–21 (2019)
- [41] Lundberg, S.M., Lee, S.I.: A unified approach to interpreting model predictions. Advances in neural information processing systems 30 (2017)
- [42] Ma, P., Ding, R., Wang, S., Han, S., Zhang, D.: Xinsight: explainable data analysis through the lens of causality. Proceedings of the ACM on Management of Data 1(2), 1–27 (2023)
- [43] Makhlouf, K., Arcolezi, H.H., Zhioua, S., Brahim, G.B., Palamidessi, C.: On the impact of multi-dimensional local differential privacy on fairness. Data Mining and Knowledge Discovery pp. 1–24 (2024)
- [44] Makhlouf, K., Stefanovic, T., Arcolezi, H.H., Palamidessi, C.: A systematic and formal study of the impact of local differential privacy on fairness: Preliminary results (2024), https://arxiv.org/abs/2405.14725
- [45] Makhlouf, K., Zhioua, S., Palamidessi, C.: Identifiability of causal-based ml fairness notions. In: 2022 14th international conference on computational intelligence and communication networks (CICN). pp. 1–8. IEEE (2022)
- [46] Makhlouf, K., Zhioua, S., Palamidessi, C.: Survey on causal-based machine learning fairness notions (2022)
- [47] Makhlouf, K., Zhioua, S., Palamidessi, C.: When causality meets fairness: A survey. Journal of Logical and Algebraic Methods in Programming p. 101000 (2024)
- [48] Mehrabi, N., Morstatter, F., Saxena, N., Lerman, K., Galstyan, A.: A survey on bias and fairness in machine learning. ACM computing surveys (CSUR) 54(6), 1–35 (2021)
- [49] Meroño-Peñuela, A., Ashkpour, A., Guéret, C., Schlobach, S.: Cedar: the dutch historical censuses as linked open data. Semantic Web 8(2), 297–310 (2017)
- [50] Nogueira, B.D., et al.: On the relation of privacy and fairness through the lenses of quantitative information flow (2023)
- [51] Pearl, J.: Causality: Models, Reasoning and Inference. Cambridge University Press, USA, 2nd edn. (2009)
- [52] Petkovic, D.: It is not "accuracy vs. explainability"—we need both for trustworthy ai systems. IEEE Transactions on Technology and Society 4(1), 46–53 (2023)
- [53] Pinzón, C., Palamidessi, C., Piantanida, P., Valencia, F.: On the incompatibility of accuracy and equal opportunity. Machine Learning (May 2023). https://doi.org/10.1007/s10994-023-06331-y
- [54] Ren, X., Yu, C.M., Yu, W., Yang, S., Yang, X., McCann, J.A., Philip, S.Y.: Lopub: high-dimensional crowdsourced data publication with local differential privacy. IEEE Transactions on Information Forensics and Security 13(9), 2151–2166 (2018)
- [55] Ribeiro, M.T., Singh, S., Guestrin, C.: "why should i trust you?" explaining the predictions of any classifier. In: Proceedings of the 22nd ACM SIGKDD international conference on knowledge discovery and data mining. pp. 1135–1144 (2016)
- [56] Richens, J.G., Lee, C.M., Johri, S.: Improving the accuracy of medical diagnosis with causal machine learning. Nature communications 11(1), 3923 (2020)
- [57] Roscher, R., Bohn, B., Duarte, M.F., Garcke, J.: Explainable machine learning for scientific insights and discoveries. Ieee Access 8, 42200–42216 (2020)
- [58] Rueda, J., Rodríguez, J.D., Jounou, I.P., Hortal-Carmona, J., Ausín, T., Rodríguez-Arias, D.: "just" accuracy? procedural fairness demands explainability in ai-based medical resource allocations. AI & society pp. 1–12 (2022)

- [59] Saravanakumar, K.K.: The impossibility theorem of machine fairness-a causal perspective. arXiv preprint arXiv:2007.06024 (2020)
- [60] Schölkopf, B.: Causality for machine learning. In: Probabilistic and causal inference: The works of Judea Pearl, pp. 765-804 (2022)
- [61] Sheikh, M.A., Goel, A.K., Kumar, T.: An approach for prediction of loan approval using machine learning algorithm. In: 2020 international conference on electronics and sustainable communication systems (ICESC). pp. 490–494. IEEE (2020)
- [62] Su, C., Yu, G., Wang, J., Yan, Z., Cui, L.: A review of causality-based fairness machine learning. Intelligence & Robotics 2(3), 244–274 (2022)
- [63] Tople, S., Sharma, A., Nori, A.: Alleviating privacy attacks via causal learning. In: International Conference on Machine Learning. pp. 9537–9547. PMLR (2020)
- [64] Tschantz, M.C., Sen, S., Datta, A.: Sok: Differential privacy as a causal property. In: 2020 IEEE Symposium on Security and Privacy (SP). pp. 354–371. IEEE (2020)
- [65] Valdivia, A., Sánchez-Monedero, J., Casillas, J.: How fair can we go in machine learning? assessing the boundaries of accuracy and fairness. International Journal of Intelligent Systems 36(4), 1619–1643 (2021)
- [66] Vapnik, V.N.: An overview of statistical learning theory. IEEE transactions on neural networks 10(5), 988–999 (1999)
- [67] van der Veer, S.N., Riste, L., Cheraghi-Sohi, S., Phipps, D.L., Tully, M.P., Bozentko, K., Atwood, S., Hubbard, A., Wiper, C., Oswald, M., et al.: Trading off accuracy and explainability in ai decision-making: findings from 2 citizens' juries. Journal of the American Medical Informatics Association 28(10), 2128–2138 (2021)
- [68] Verma, S., Dickerson, J., Hines, K.: Counterfactual explanations for machine learning: A review arXiv preprint arXiv:2010.10596 2, 1 (2020)
- [69] Vowels, M.J.: Trying to outrun causality with machine learning: Limitations of model explainability techniques for identifying predictive variables. stat 1050, 22 (2022)
- [70] Xu, D., Yuan, S., Wu, X.: Differential privacy preserving causal graph discovery. In: 2017 IEEE Symposium on Privacy-Aware Computing (PAC). pp. 60–71. IEEE (2017)
- [71] Yang, M., Guo, T., Zhu, T., Tjuawinata, I., Zhao, J., Lam, K.Y.: Local differential privacy and its applications: A comprehensive survey. Computer Standards & Interfaces p. 103827 (2023)
- [72] Yang, Z., Zhong, S., Wright, R.N.: Privacy-preserving classification of customer data without loss of accuracy. In: Proceedings of the 2005 SIAM International Conference on Data Mining. pp. 92–102. SIAM (2005)
- [73] Zemel, R., Wu, Y., Swersky, K., Pitassi, T., Dwork, C.: Learning fair representations. In: International conference on machine learning. pp. 325–333. PMLR (2013)
- [74] Zeng, Z., Peng, W., Zhao, B.: Improving the accuracy of network intrusion detection with causal machine learning. Security and Communication Networks 2021(1), 8986243 (2021)
- [75] Zheng, H., Hu, H., Han, Z.: Preserving user privacy for machine learning: Local differential privacy or federated machine learning? IEEE Intelligent Systems 35(4), 5–14 (2020)
- [76] Zhou, J., Joachims, T.: How to explain and justify almost any decision: Potential pitfalls for accountability in ai decision-making. In: Proceedings of the 2023 ACM Conference on Fairness, Accountability, and Transparency. p. 12–21. FAccT '23, Association for Computing Machinery, New York, NY, USA (2023). https://doi.org/10.1145/3593013.3593972, https://doi.org/10.1145/3593013.3593972