$$-\sum_{w \in V_{ocab}} y_w | og(\hat{y}_w) = -\left[ 8 \cdot log(\hat{y}_o) + 8 \cdot log(\hat{y}_o) + \dots + 1 \cdot$$

$$\frac{\partial \mathcal{Q}}{\partial \mathcal{V}_c} = -U_0 = -U_y$$

$$\frac{\partial \mathcal{Q}}{\partial \mathcal{V}_c} = \frac{1}{\sum_{w \in Vocab}} \cdot \frac{\partial}{\partial \mathcal{V}_c} \left[ \sum_{w \in Vocab} \exp(U_w \mathcal{V}_c) \right]$$

The gradient is zew when y=y  $\Rightarrow \frac{\partial J_{\text{naive-softmax}}}{\partial V_{\text{c}}} = \coprod (y - y) \quad \text{update } V_{\text{c}} \text{ to } \text{ iet } y \text{ be closert}$  the one-hot vector whose 0 entry is 1. It is equivalent to P(0=0|C=0)

(c)

if 
$$w = 0$$
,

$$\frac{\partial \mathcal{D}}{\partial U_W} = -U_C$$

$$\frac{\partial \mathcal{D}}{\partial U_W} = \frac{1}{\sum_{w \in V_{Ocab}}} \cdot \frac{\partial}{\partial U_w} \left( \frac{\partial \mathcal{D}}{\partial U_w} \right) \cdot \frac{\partial}{\partial U_w} \left( \frac{\partial \mathcal{D}}{\partial U_w}$$

$$e) 6(x) = \frac{1}{1 + e^{-x}} = \frac{e^{x}}{e^{x} + 1}$$

$$6'(x) = \frac{(e^{x} + 1) \cdot e^{x} - e^{x} \cdot e^{x}}{(e^{x} + 1)^{2}} = \frac{e^{x}}{e^{x} + 1} \cdot \frac{1}{e^{x} + 1} = 6(x) \cdot (1 - e^{x} + 1)$$

$$J_{\text{neg-sample}}(v_c, 0, \square) = -\log(\sigma(u_0^T v_c)) - \sum_{k=1}^{K} \log(\sigma(-u_k^T v_c))$$

$$\Rightarrow v_c = -\frac{1}{\sigma(u_0^T v_c)} \cdot \sigma'(u_0^T v_c) \cdot u_0$$

$$= \left[\sigma(u_0^T v_c) - 1\right] u_0$$

$$\Rightarrow \sum_{k=1}^{K} \left[\sigma(-u_k^T v_c)\right] u_k$$

$$= \sum_{k=1}^{K} \left[\sigma(-u_k^T v_c)\right] u_k$$

$$\Rightarrow \frac{\partial J_{\text{neg-sample}}}{\partial v_c} = \left[\sigma(u_0^T v_c) - 1\right] u_0 - \sum_{k=1}^{K} \left[\sigma(-u_k^T v_c) - 1\right] u_k$$

$$\Rightarrow \frac{\partial J_{\text{neg-sample}}}{\partial v_c} = \left[\sigma(u_0^T v_c) - 1\right] u_0 - \sum_{k=1}^{K} \left[\sigma(-u_k^T v_c) - 1\right] u_k$$

$$\Rightarrow \frac{\partial J_{\text{neg-sample}}}{\partial V_{\text{c}}} = \left[ 6(U_{\text{o}}^{\text{T}}V_{\text{c}}) - 1 \right] U_{\text{o}} - \sum_{k=1}^{K} \left[ 6(-U_{\text{k}}V_{\text{c}}) - 1 \right] U_{\text{k}}$$

$$\frac{\partial \mathcal{D}}{\partial U_0} = \left[1 - \mathcal{O}(U_0^T U_c)\right] U_c$$

$$\frac{\partial \Theta}{\partial U_0} = \emptyset$$
 because  $0 \notin \{W_1, W_2, ..., W_K\}$ 

$$\Rightarrow \frac{\partial J_{reg-sample}}{\partial U_0} = \left[ 6(U_0 V_c) - 1 \right] V_c$$

$$\frac{\partial \mathcal{O}}{\partial \mathcal{V}_{R}} = 0$$
 because  $0 \notin \{W_{1}, W_{2}, \dots, W_{K}\}$ 

$$\frac{\partial Q}{\partial U_R} = \frac{-\partial}{\partial U_R} \sum_{k'=1}^{K} \log \left( O(-U_R^T U_C) \right) = \frac{-\partial}{\partial U_R} \log \left( O(-U_R^T U_C) \right)$$

$$= \frac{-1}{O(-U_R^T U_C)} \cdot O(-U_C) = \left[ 1 - O(-U_R^T U_C) \right] U_C$$

$$= \frac{-1}{5(-U_{R}^{T}U_{C})} \cdot 6'(-U_{R}U_{C}) \cdot (-U_{C}) = [1-6(-U_{R}U_{C})]U_{C}$$

$$\Rightarrow \frac{3U_{R}eg-sample}{3U_{R}} = [1-6(-U_{R}U_{C})]U_{C}$$

$$\frac{\partial \mathcal{D}}{\partial U_{R}} = -\frac{\partial}{\partial U_{R}} \left( \sum_{1 \leq k' \leq K} \log \mathcal{D}(-U_{k'} \mathcal{V}_{C}) + \sum_{1 \leq k' \leq K} \log \mathcal{D}(-U_{k'} \mathcal{V}_{C}) \right)$$

$$\frac{\partial \mathcal{D}}{\partial U_{R}} = -\frac{\partial}{\partial U_{R}} \left( \sum_{1 \leq k' \leq K} \log \mathcal{D}(-U_{k'} \mathcal{V}_{C}) + \sum_{1 \leq k' \leq K} \log \mathcal{D}(-U_{k'} \mathcal{V}_{C}) \right)$$

$$\frac{\partial \mathcal{D}}{\partial U_{R}} = -\frac{\partial}{\partial U_{R}} \left( \sum_{1 \leq k' \leq K} \log \mathcal{D}(-U_{k'} \mathcal{V}_{C}) + \sum_{1 \leq k' \leq K} \log \mathcal{D}(-U_{k'} \mathcal{V}_{C}) \right)$$

$$= -\sum_{1 \leq k' \leq k} \frac{1}{\delta(-U_k U_c)} \cdot \delta'(-U_k U_c) \cdot (-U_c)$$

$$W_{k'} = W_k$$

$$= \sum_{1 \leq k' \leq K} \left[ 1 - 6 \left( - U_k V_c \right) \right] V_c$$

$$W_{k'} = W_k$$

$$(ii) \frac{\partial J_{skip-gram}}{\partial V_c} = \sum_{-m \leq j \leq m} \frac{\partial J(V_c, W_{t+j}, U)}{\partial V_c}$$

$$\neq 0$$