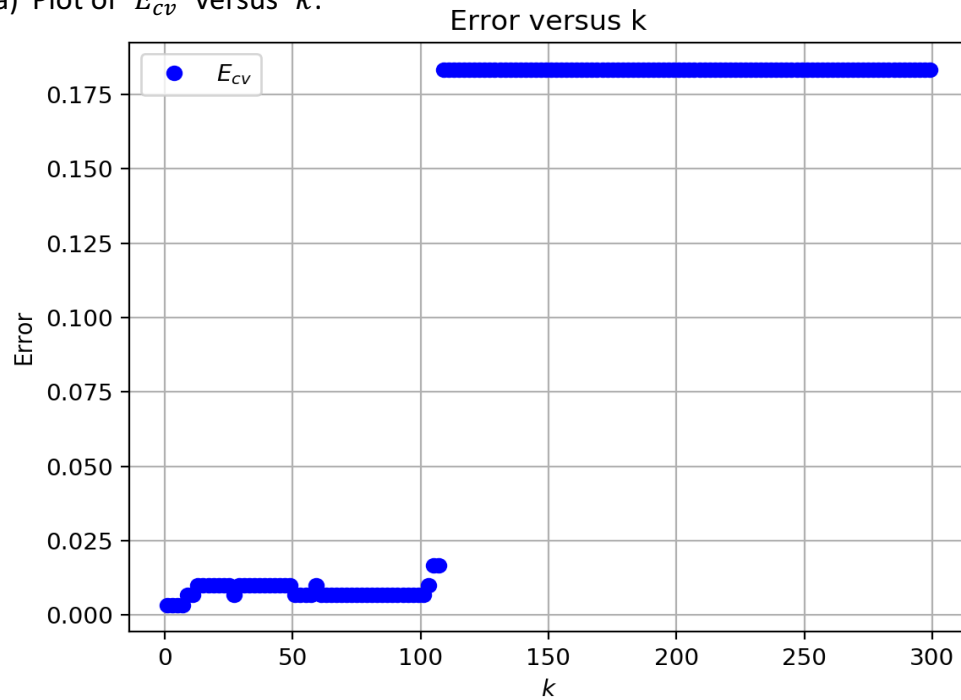
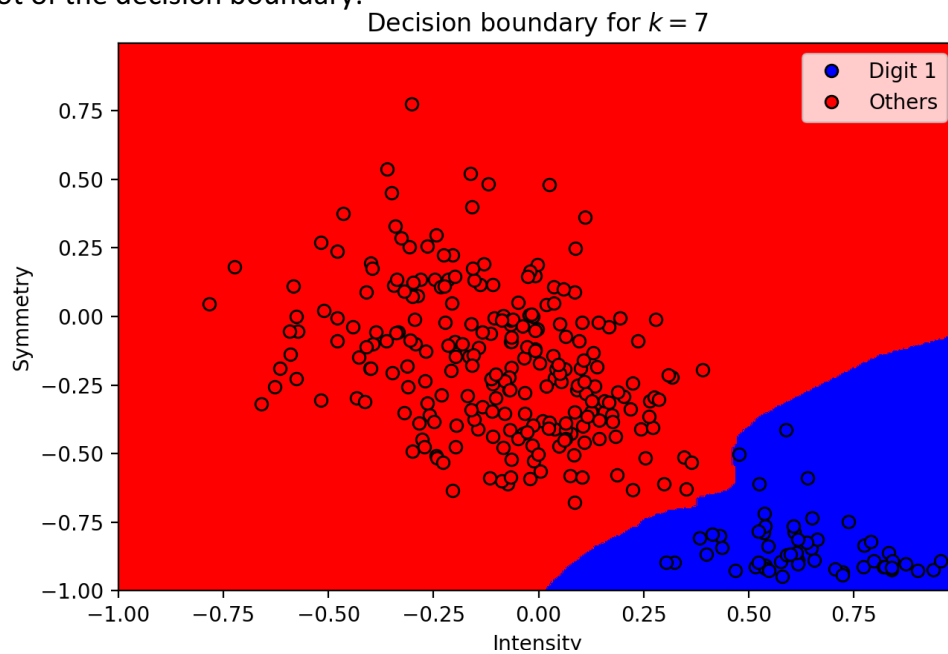


## 1. k-NN Rule

(a) Plot of  $E_{cv}$  versus  $k$ :

I choose  $k = 7$  because when  $k = 7$ ,  $E_{cv} = 0.003335$  is smallest.

(b) Plot of the decision boundary:

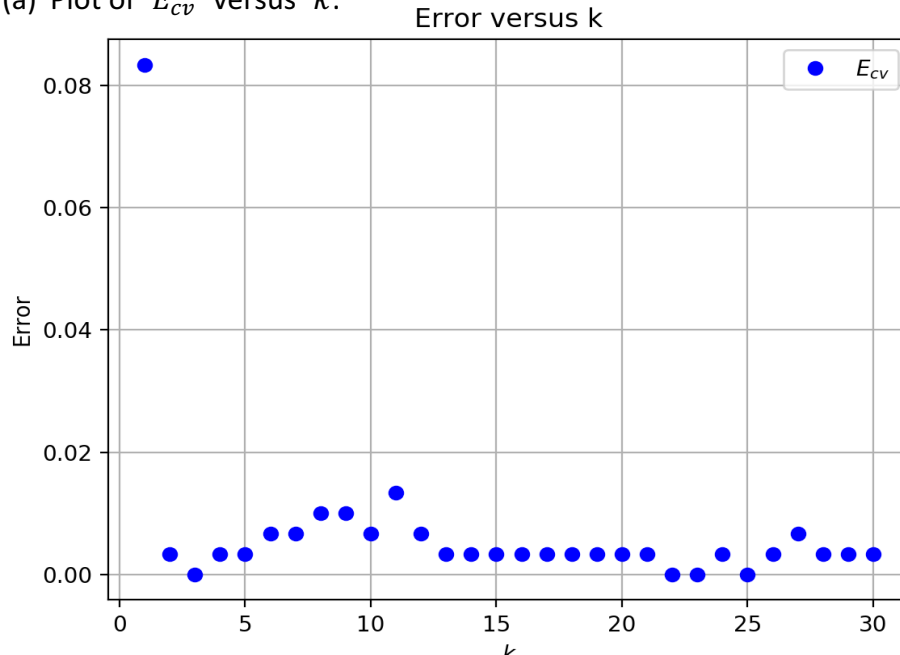


The in-sample error is  $E_{in} = 0.0$ , the cross validation error is  $E_{cv} = 0.003335$ .

(c) The test error  $E_{test} = 0.009441$ .

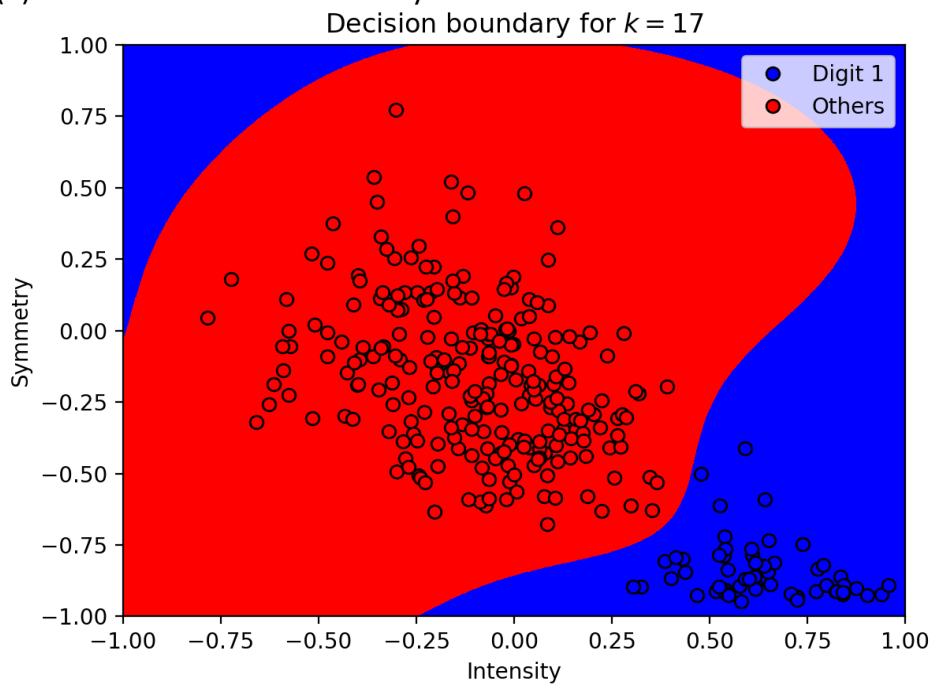
## 2. RBF-network

(a) Plot of  $E_{cv}$  versus  $k$ :



I choose  $k = 17$  because when  $k = 17$ ,  $E_{cv} = 0.008869$  is smallest.

(b) Plot of the decision boundary:



The in-sample error is  $E_{in} = 0.0$ , the cross validation error is  $E_{cv} = 0.008869$ .

(c) The test error  $E_{test} = 0.009726$ .

### 3. Compare Linear, k-NN, RBF-network

The final test error from my three attempts are: for Linear model with 8<sup>th</sup> order polynomial transform,  $E_{test} = 0.057199$ ; for k-NN rule,  $E_{test} = 0.009441$ ; for RBF-network,  $E_{test} = 0.009726$ . We can see that k-NN rule gives us the smallest test error, followed by RBF-network, and then the Linear model.

However, k-NN is the slowest among these three algorithms and requires the largest memory space. Thus, k-NN is not a good choice.

The Linear model with 8<sup>th</sup> order polynomial transform is not a good choice as well. Not only it has the largest test error, but it also has a higher order polynomial transform which results in an increase in complexity.

For RBF-network, the running time is fast and it has a small test error without requiring large memory. Therefore, RBF is the best among these three.