

i, j
 nat, k
 $floating_number, n$
 $label, \alpha$
 $expression, e \quad ::=$
 $\quad | \quad k$
 $\quad | \quad n$
 $\quad | \quad \phi$
 $\quad | \quad e :: e'$
 $\quad | \quad e + e'$
 $\quad | \quad \mathbf{reshape} \ e \ \sigma$

$type, \tau \quad ::=$
 $\quad | \quad \mathbf{tensor} \ \sigma$
 $\quad | \quad \mathbf{float}$
 $\quad | \quad \mathbf{int}$

$dimension, \delta \quad ::=$
 $\quad | \quad \alpha$
 $\quad | \quad k$

$shape, \sigma \quad ::=$
 $\quad | \quad \cdot$
 $\quad | \quad \delta, \sigma$

$\tau \sqsubseteq \tau'$

$\overline{\mathbf{int} \sqsubseteq \mathbf{float}} \quad \text{T_SUB_INT}$

$\overline{\mathbf{float} \sqsubseteq \mathbf{tensor} \cdot} \quad \text{T_SUB_NUM}$

$\overline{\mathbf{tensor} \ \sigma \sqsubseteq \mathbf{tensor} \ (1, \sigma)} \quad \text{T_BROADCAST1}$

$\overline{\mathbf{tensor} \ (\sigma, 1, \sigma') \sqsubseteq \mathbf{tensor} \ (\sigma, k, \sigma)} \quad \text{T_BROADCAST2}$

$e : \tau$

$\overline{k : \mathbf{int}} \quad \text{T_NUM}$

$\overline{n : \mathbf{float}} \quad \text{T_FLOAT}$

$\overline{\phi : \mathbf{tensor} \ 0} \quad \text{T_EMPTY}$

$\frac{e : \mathbf{tensor} \ \sigma \quad e' : \mathbf{tensor} \ (\delta, \sigma)}{e :: e' : \mathbf{tensor} \ (\delta + 1, \sigma)} \quad \text{T_CONS}$

$\frac{e : \tau \quad e' : \tau}{e + e' : \tau} \quad \text{T_ADD}$

$$\begin{array}{c}
e : \mathbf{tensor} \overline{\delta_j}^j \\
\prod_i \delta_i = \prod_j \delta_j' \\
\hline
\mathbf{reshape} \, e \, \overline{\delta_i}^i : \mathbf{tensor} \overline{\delta_i}^i \quad \text{T_RESHAPE}
\end{array}$$

$$\begin{array}{c}
e : \tau \\
\tau \sqsubseteq \tau' \\
\hline
e : \tau' \quad \text{T_SUB}
\end{array}$$

Definition rules: 11 good 0 bad
Definition rule clauses: 19 good 0 bad