Optimizing smallpt

020-11-02

Optimizing smallpt
Davens Scies, Siddharth Bhar
Madel Statungs
November 4th, 2020

Optimizing smallpt

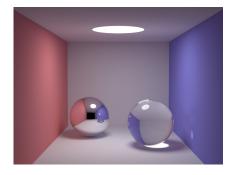
Davean Scies, Siddharth Bhat

Haskell Exchange

November 4th, 2020

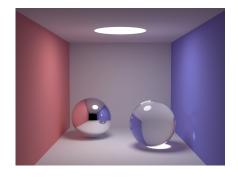






▶ 100 LoC C demo of a raytracer





- ▶ 100 LoC C demo of a raytracer
- Perfect for an optimization case study

Optimizing smallpt

20-11-02

☐What is smallpt anyway?



What is smallpt anyway?

Note for first slide: what is smallpt anyway?

```
#include <math.h>
#include <stdlib.h>
#include <stdio.h>
struct Vec {
 double x, y, z; // position, also color (r,g,b)
  ... methods...
struct Ray { Vec o, d; Ray(Vec o_, Vec d_) : o(o_), d(d_) {} };
enum Refl_t { DIFF, SPEC, REFR }; // material types, used in radiance()
struct Sphere {
 double rad; // radius
 Vec p, e, c; // position, emission, color
 Refl_t refl; // reflection type (DIFFuse, SPECular, REFRactive)
  ... methods ...
 double intersect(const Ray &r) const // returns distance, 0 if nohit
Sphere spheres[] = {//Scene: radius, position, emission, color, material
 Sphere(1e5, Vec( 1e5+1,40.8,81.6), Vec(), Vec(.75,.25,.25), DIFF), //Left
  ... initialization ...
inline bool intersect(const Ray &r, double &t, int &id)
```

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─What is smallpt anyway?

What is smallpt anyway?

Findleds Couth.h> Findleds Cotdishb Findleds Cotdishb struct Wes {

 \mathbf{z}_{j} // position, also color (r,g,b) ...

); artuct key { Yes u, d; key(Yes u, Yes u,): e(u,), d(u,) {}; }; sum bell; (2079, 2002, 8002,); // material types, used to redisses sumbles. We p, u, u, // rediss. Yes p, u, u, // yestitus, measure, soler Rell; xeelj. // reflection type (1971as, 2002); 2002, 2002, 2002, 2002.

Tem p. m. i. // partiess, marches, course for the Refl. vedi; // reflection type (EFFace, FECular, AFFactive) ... methods ... double intersect(count Ray Nr) count // returns distance, 0 if making the following for the returns of the same of the s

);

Sphere spheres[= {//Scene; radius, position, emission, color, natural Sphere(tol., Vec(tol-1,00,011.0), Vec(),Vec(.75,.25,.25),DIFP),//Left tol-1,00,011.0);

isline bool intersect(count kay is, double it, int iid)

```
Vec radiance(const Ray &r. int depth, unsigned short *Xi){
 double t;
                                         // distance to intersection
 int id=0:
                                         // id of intersected object
 if (!intersect(r, t, id)) return Vec(); // if miss, return black
 const Sphere &obj = spheres[id];
                                        // the hit object
 Vec x=r.o+r.d*t, n=(x-obj.p).norm(), nl=n.dot(r.d)<0?n:n*-1, f=obj.c;
 double p = f.x > f.y && f.x > f.z ? f.x : f.y > f.z ? f.y : f.z; // max refl
 if (++depth>5) if (erand48(Xi)<p) f=f*(1/p); else return obj.e; //R.R.
 if (obj.refl == DIFF){
                                        // Ideal DIFFUSE reflection
   double r1=2*M PI*erand48(Xi), r2=erand48(Xi), r2s=sqrt(r2);
   Vec w=n1, u=((fabs(w.x)>.1?Vec(0,1):Vec(1))\%w).norm(), v=w\%u;
   Vec d = (u*cos(r1)*r2s + v*sin(r1)*r2s + w*sart(1-r2)).norm():
   return obj.e + f.mult(radiance(Ray(x,d),depth,Xi));
 } else if (obi.refl == SPEC)
                                 // Ideal SPECULAR reflection
   return obj.e + f.mult(radiance(Ray(x,r.d-n*2*n.dot(r.d)),depth,Xi));
 Ray reflRay(x, r,d-n*2*n,dot(r,d)): // Ideal dielectric REFRACTION
 bool into = n.dot(n1)>0;
                                        // Ray from outside going in?
 double nc=1, nt=1.5, nnt=into?nc/nt:nt/nc, ddn=r.d.dot(nl), cos2t;
 if ((cos2t=1-nnt*nnt*(1-ddn*ddn))<0) // Total internal reflection
   return obj.e + f.mult(radiance(reflRay,depth,Xi));
 Vec tdir = (r.d*nnt - n*((into?1:-1)*(ddn*nnt+sqrt(cos2t)))).norm();
 double a=nt-nc, b=nt+nc, R0=a*a/(b*b), c = 1-(into?-ddn:tdir.dot(n));
 double Re=R0+(1-R0)*c*c*c*c*c,Tr=1-Re,P=,25+,5*Re,RP=Re/P,TP=Tr/(1-P);
 return obj.e + f.mult(depth>2 ? (erand48(Xi)<P ? // Russian roulette
   radiance(reflRay.depth.Xi)*RP:radiance(Ray(x,tdir),depth.Xi)*TP) :
   radiance(reflRay,depth,Xi)*Re+radiance(Ray(x,tdir),depth,Xi)*Tr);
```



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-What is smallpt anyway?

What is smallpt anyway?

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that late's a many activity of the production of

Establishing baselines



Establishing baselines

```
main :: IO ()
main = smallptM 200 200 256

smallptM :: Int -> Int -> Int -> IO ()
smallptM !w !h !nsamps = do
    -- ... processing
withFile "image.ppm" WriteMode $ \hdl -> do
    hPrintf hdl "P3\n%d %d\n%d\n" w h (255::Int)
flip mapM_ [0..w*h-1] $ \i -> do
    Vec r g b <- VM.unsafeRead c i
    hPrintf hdl "%d %d %d " (toInt r) (toInt g) (toInt b)</pre>
```

▶ Sha256 hash of the output image — 4dac691082bb

Optimizing smallpt

2020-11-02

Establishing baselines

AMAZIN IGEN OF OR GREAT STAGE — COMMENTERS OF

Establishing baselines

```
Haskell: the first stab (1\times)
       radiance :: Ray -> CInt -> Ptr CUShort -> IO Vec
       radiance ray@(Ray o d) depth xi = case intersects ray of
         (Nothing,_) -> return zerov
         (Just t, Sphere _r p e c refl) -> do
           let x = o 'addv' (d 'mulvs' t)
               n = norm $ x `subv` p
               nl = if n 'dot' d < 0 then n else n 'mulvs' (-1)
               pr = maxv c
               depth' = depth + 1
               continue f = case refl of
                 DIFF -> do
                   r1 <- ((2*pi)*) `fmap` erand48 xi
                   r2 <- erand48 xi
                  let r2s = sart r2
                       w@(Vec wx _ _) = n1
                       u = norm $ (if abs wx > 0.1 then (Vec 0 1 0) else (Vec 1 0 0)) `cross` w
                       v = w 'cross' u
                       d' = norm $ (u`mulvs`(cos r1*r2s)) `addv` (v`mulvs`(sin r1*r2s)) `addv` (w`mulvs`sqrt (1-r2))
                   rad <- radiance (Ray x d') depth' xi
                  return $ e 'addv' (f 'mulv' rad)
                 SPEC -> do
                  let d' = d `subv` (n `mulvs` (2 * (n`dot'd)))
                   rad <- radiance (Ray x d') depth' xi
                   return $ e 'addy' (f 'mulv' rad)
                 REFR -> do
                  let reflRay = Ray x (d 'subv' (n 'mulvs' (2* n'dot'd))) -- Ideal dielectric REFRACTION
                       into = n'dot'nl > 0
                                                         -- Ray from outside going in?
                       nc = 1
                       nt = 1.5
                       nnt = if into then nc/nt else nt/nc
                       ddn= d'dot'nl
                       cos2t = 1-nnt*nnt*(1-ddn*ddn)
                   if cos2t<0 -- Total internal reflection
                     then do
                       rad <- radiance reflRay depth' xi
                       return $ e 'addy' (f 'mulv' rad)
                     else do
                       let tdir = norm $ (d'mulvs'nnt 'subv' (n'mulvs'((if into then 1 else -1)*(ddn*nnt+sqrt cos2t))))
```

a=nt-nc b=nt+nc

r0=a*a/(b*b)

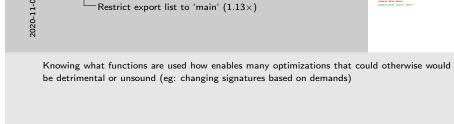
Optimizing smallpt Haskell: the first stab (1×) Haskell: the first stab (1×)

11-02

4 D > 4 A > 4 B > 4 B > B 9 Q (>

```
Restrict export list to 'main' (1.13\times)
```

```
-module Main where
+module Main (main) where
```



Optimizing smallpt

Restrict export list to 'main' (1.13×)

-module Main where -module Main (main) where

Mark entries of Ray and Sphere as UNPACK and Strict $(1.07 \times)$



Optimizing smallpt

20-11-03

Mark entries of Ray and Sphere as UNPACK and Strict $(1.07\times)$

Mark entries of Ray and Sphere as UNPACK and Strict (1.07×)

This optimization removes indirection and laziness.

Use a pattern synonym to unpack Refl in Sphere $(1.07\times)$



Optimizing smallpt

Use a pattern synonym to unpack Refl in Sphere (1.07 imes)



Use a pattern synonym to unpack Refl in Sphere (1.07×)

While we weren't able to unpack Refl in the last step because it is a sum type, we can if we use a trick modeled after an C Enum. The use of COMPLETE is unsafe here because other values could be constructed. For this small example though we rely on the fact that we create values of Refl via the patterns.

Change from maximum on a list to max $(1.08\times)$

```
-maxv (Vec a b c) = maximum [a,b,c]
+\max v (Vec \ a \ b \ c) = \max a (\max b \ c)
@@ -84,7 +85,6 @@ radiance ray@(Ray o d) depth xi = case intersects ray of
     let x = o `addv` (d `mulvs` t)
         n = norm $ x `subv` p
         nl = if n `dot` d < 0 then n else n `mulvs` (-1)
         pr = maxv c
         depth' = depth + 1
         continue f = case refl of
           DIFF -> do
@@ -140,6 +140,7 @@ radiance ray@(Ray o d) depth xi = case intersects ray of
     if depth'>5
       then do
         er <- erand48 xi
         let !pr = maxv c
```



This is a finicky optimization. At first it actually benched worse than the maximum version. The strictness on the binding is required for reliable performance, but it seemed sensible to only do that where it was actually used since its in a single branch and no longer lazy.

Convert erand48 to pure Haskell $(1.09\times)$

```
-radiance :: Ray -> CInt -> Ptr CUShort -> IO Vec
+radiance :: Ray -> Int -> IORef Word64 -> IO Vec
 radiance ray@(Ray o d) depth xi = case intersects ray of
   (Nothing,_) -> return zerov
   (Just t,Sphere _r p e c refl) -> do
00 - 153,9 + 153,8 00 \text{ smallpt w h nsamps} = do
       cx = Vec (fromIntegral w * 0.5135 / fromIntegral h) 0 0
       cy = norm (cx `cross` dir) `mulvs` 0.5135
   c <- VM.replicate (w * h) zerov
- allocaArray 3 $ \xi ->
       flip mapM_ [0..h-1] $ \y -> do
+ xi <- newIORef 0
+ flip mapM_ [0..h-1] $ \y -> do
       writeXi xi v
```

TODO: add better version of erand48 into this commit

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Optimizing smallpt

2020-11-02

Convert erand48 to pure Haskell $(1.09 \times)$

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Convert erand48 to pure Haskell (1.09×)

* flip map([1..h-1] I by -> do writeEi mi y 7000: add better version of erandeR into this counit

Change erand48 to IORefU $(1.13\times)$

```
-radiance :: Rav -> Int -> IORef Word64 -> IO Vec
+radiance :: Rav -> Int -> IORefU Word64 -> IO Vec
 radiance ray@(Ray o d) depth xi = case intersects ray of
   (Nothing,_) -> return zerov
   (Just t, Sphere _r p e c refl) -> do
00 - 153,7 + 154,7 00 \text{ smallpt w h nsamps} = do
       cx = Vec (fromIntegral w * 0.5135 / fromIntegral h) 0 0
       cy = norm (cx `cross` dir) `mulvs` 0.5135
   c <- VM.replicate (w * h) zerov
- xi <- newIORef 0
+ xi <- newIORefU 0
   flip mapM_ [0..h-1] $ \y -> do
       writeXi xi y
       flip mapM_ [0..w-1] $ \x -> do
00 - 181,8 + 182,8 00 \text{ smallpt w h nsamps} = do
           Vec r g b <- VM.unsafeRead c i
           hPrintf hdl "%d %d %d " (toInt r) (toInt g) (toInt b)
-writeXi :: IORef Word64 -> Int -> IO ()
-writeXi !xi !v = writeIORef xi (mkErand48Seed' v)
+writeXi :: IORefU Word64 -> Int -> IO ()
+writeXi !xi !y = writeIORefU xi (mkErand48Seed' y)
TODO: change to new shorter erand48
```

```
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```

```
Change erand48 to IORefU (1.13×)
Optimizing smallpt
                                                                                                                                                                                                                                      -radiance :: Ray -> Int -> 108ef Word64 -> 10 Yes
                                                                                                                                                                                                                                       undiance suyt(Kay o d) depth xi - case intersects suy of
                                                                                                                                                                                                                                         Olothing. ) -> return peruy
                                                                                                                                                                                                                                         (Just t,Sphere _r p = c refl) -> do
                                                                                                                                                                                                                                    cc - Sec (from integral u + 0.5155 / from integral h) 0 0
                                                                                                                                                                                                                                             cy - norm (cg 'cross' diy) 'mulve' 0.5135
                                                                                                                                                                                                                                       c <- WM.replicate (u * h) zerov
                                                                                                                                                                                                                                      - xi <- megDShef 0
- xi <- megDShefU 0
                                  Change erand48 to IORefU (1.13\times)
                                                                                                                                                                                                                                         flip mapH, [0..h-1] # \forall y \rightarrow do
                                                                                                                                                                                                                                           uvited1 x1 y
flip maght, [0..u-1] $ \x -> do
                                                                                                                                                                                                                                               Vec v g b <- Wi.unafeRead c i
hPrintf hdi "5d Nd Td " (tolat v) (tolat s) (tolat b)
                                                                                                                                                                                                                                     -writed: :: DOMed Words4 -> Dat -> DD ()
-writed: tx: ty = writedDMed x: (akkyanddMdeed* y)
                                                                                                                                                                                                                                      1000; change to new shorter expanded
```

This just removes yet one more layer of indirection, but on a fairly hot function this time.

Rewrite the remaining IORef into a foldM $(1.17\times)$

```
@@ -161,8 +161,7 @@ smallpt w h nsamps = do
    let i = (h-y-1) * w + x
    flip mapM_ [0..1] $ \sy -> do
        flip mapM_ [0..1] $ \sx -> do
        r <- newIORef zerov
- flip mapM_ [0.samps-1] $ \_s -> do
+ Vec rr rg rb <- (\f -> foldM f zerov [0..samps-1]) $ \ !r _s -> do
        r1 <- (2*) `fmap` erand48 xi
        let dx = if r1<1 then sqrt r1-1 else 1-sqrt(2-r1)
        r2 <- (2*) `fmap` erand48 xi
@@ -171,9 +170,8 @@ smallpt w h nsamps = do
        modifyIORef r (`addv` (rad `mulvs` (1 / fromIntegral samps)))
+ pure (r `addv` (rad `mulvs` (1 / fromIntegral samps)))
        ci <- VM.unsafeRead c i
- Vec rr rg rb <- readIORef r</pre>
```



Optimizing smallpt Rewrite the remaining IORef into a foldM (1.17×) Rewrite the remaining IORef into a foldM (1.17×)

This removes another source of mutability, and potentially indirection. This use of an IORef wasn't very Haskelly, so unlike erand48 where the IORef was in a way appropriate, it made more sense to just remove this one.

```
Remove the Data. Vector. Mutable by being purer (1.17\times)
    -radiance :: Ray -> Int -> IORefU Word64 -> IO Vec
    +radiance :: Ray -> Int -> STRefU s Word64 -> ST s Vec
     radiance ray@(Ray o d) depth xi = case intersects ray of
       (Nothing,_) -> return zerov
       (Just t, Sphere _r p e c refl) -> do
    00 - 153, 14 + 154, 10 00 \text{ smallpt w h nsamps} = do
           dir = norm \$ Vec 0 (-0.042612) (-1)
           cx = Vec (fromIntegral w * 0.5135 / fromIntegral h) 0 0
           cy = norm (cx `cross` dir) `mulvs` 0.5135
    - c <- VM.replicate (w * h) zerov
    - xi <- newTORefU 0</p>
    - flip mapM_ [0..h-1] $ \y -> do
           writeXi xi v
           flip mapM_ [0..w-1] $ \x -> do
            let i = (h-y-1) * w + x
            flip mapM_ [0..1] $ \sy -> do
              flip mapM_ [0..1] $ \sx -> do
           img = (`concatMap` [(h-1), (h-2)..0]) $ \y -> runST $ do
             xi <- newSTRefU (mkErand48Seed' y)
            forM [0..w-1] $ \x -> do
               (\pf -> foldM pf zerov [(sy, sx) | sy <- [0,1], sx <- [0,1]) $ \ci
                ci <- VM.unsafeRead c i
                VM.unsafeWrite c i $ ci `addv` (Vec (clamp rr) (clamp rg) (clamp r
                pure $ ci `addv` (Vec (clamp rr) (clamp rg) (clamp rb) `mulvs` 0.2
```

flip mapH, [0..1] \$ \ax -> do ing = ('concattap' [(b.1), (b-2)..0]) \$ \y -> rundT \$ do Theres a few things going on here. First we stop being in IO and create a new STRefU for each Y row. This is slightly more allocation but breaks the dependency between y rows which would be useful if parallel. Second remove the vector, and instead directly accumulate into the result.

Remove the Data. Vector. Mutable by being purer (1.17×)

radiance ray@(Ray o d) depth xi = case intersects ray of (Nothing,_) -> return mesus (Just t,Sphere _r p = c refl) -> do 00 -153,14 +154,10 00 smallpt u h manaps = 4 dir = norm \$ Vec 0 (-0.042612) (-1) cs - Wes (from[ategral w * 0.5125 / from[ategral h) 0 0

-radiance :: Ray -> Int -> 10kefU Word64 -> 10 Vec

flip mapH_ [0..h-1] # \y -> do

uviteEi xi y flip mapH, [0..u-1] # \x -> do let 1 = (h-y-1) * u * x flip mask [0..1] # \sv -> do

Third, since we're generating results directly, we just produce a list, and don't bother with the 'i' variable placement, which means we want to reorder which y rows we generate first. So we generate them in the reverse order (but this does potentially change edge cases and parameter validation should be added to cover). This notably removes a decent number of lines of code and might even be clearer.

Remove the Data. Vector. Mutable by being purer $(1.17\times)$

Optimizing smallpt

Set everything in smallpt to be strict $(1.17\times)$

```
- let samps = nsamps 'div' 4
       org = Vec 50 52 295.6
       dir = norm \$ Vec 0 (-0.042612) (-1)
       cx = Vec (fromIntegral w * 0.5135 / fromIntegral h) 0 0
       cy = norm (cx 'cross' dir) 'mulvs' 0.5135
+ let !samps = nsamps 'div' 4
       !org = Vec 50 52 295.6
       !dir = norm $ Vec 0 (-0.042612) (-1)
       !cx = Vec (fromIntegral w * 0.5135 / fromIntegral h) 0 0
       !cv = norm (cx 'cross' dir) 'mulvs' 0.5135
               r1 <- (2*) 'fmap' erand48 xi
               let dx = if r1<1 then sqrt r1-1 else 1-sqrt(2-r1)
               r2 <- (2*) 'fmap' erand48 xi
               let dy = if r2<1 then sqrt r2-1 else 1-sqrt(2-r2)
                  d = (cx \text{ `mulvs'} (((sx + 0.5 + dx)/2 + fromIntegral x)/fromIntegral w - 0.5)) `addv`
                       (cy 'mulvs' (((sy + 0.5 + dy)/2 + fromIntegral y)/fromIntegral h - 0.5)) 'addv' dir
               rad <- radiance (Ray (org'addv'(d'mulvs'140)) (norm d)) 0 xi
               !r1 <- (2*) 'fmap' erand48 xi
               let !dx = if r1<1 then sqrt r1-1 else 1-sqrt(2-r1)
               !r2 <- (2*) `fmap` erand48 xi
               let !dy = if r2<1 then sqrt r2-1 else 1-sqrt(2-r2)
                  !d = (cx `mulvs` (((sx + 0.5 + dx)/2 + fromIntegral x)/fromIntegral w - 0.5)) `addv`
                        (cy `mulvs` (((sy + 0.5 + dy)/2 + fromIntegral y)/fromIntegral h - 0.5)) `addv` dir
               !rad <- radiance (Ray (org'addv'(d'mulvs'140)) (norm d)) 0 xi
               pure (r 'addv' (rad 'mulvs' (1 / fromIntegral samps)))
             pure $ ci 'addv' (Vec (clamp rr) (clamp rg) (clamp rb) 'mulvs' 0.25)
              pure $! (r `addv` (rad `mulvs` (1 / fromIntegral samps)))
             pure $! ci 'addv' (Vec (clamp rr) (clamp rg) (clamp rb) 'mulvs' 0.25)
```



Optimizing smallpt

11-02

—Set everything in smallpt to be strict (1.17imes)



This does make a difference but a small one. The question is which ones matter.

Reduce to only effectful strictnesses $(1.17\times)$

```
- let !samps = nsamps `div` 4
       !org = Vec 50 52 295.6
       !dir = norm \$ Vec 0 (-0.042612) (-1)
       !cx = Vec (fromIntegral w * 0.5135 / fromIntegral h) 0 0
       !cy = norm (cx `cross` dir) `mulvs` 0.5135
+ let samps = nsamps `div` 4
      org = Vec 50 52 295.6
      dir = norm \$ Vec 0 (-0.042612) (-1)
       cx = Vec (fromIntegral w * 0.5135 / fromIntegral h) 0 0
      cy = norm (cx `cross` dir) `mulvs` 0.5135
               !r1 <- (2*) `fmap` erand48 xi
              r1 <- (2*) `fmap` erand48 xi
               !r2 <- (2*) `fmap` erand48 xi
              r2 <- (2*) `fmap` erand48 xi
               !rad <- radiance (Ray (org'addv'(d'mulvs'140)) (norm d)) 0 xi
              rad <- radiance (Ray (org'addv'(d'mulvs'140)) (norm d)) 0 xi
               pure $! (r `addv` (rad `mulvs` (1 / fromIntegral samps)))
             pure $! ci `addv` (Vec (clamp rr) (clamp rg) (clamp rb) `mulvs` 0.25)
              pure $ (r `addv` (rad `mulvs` (1 / fromIntegral samps)))
             pure $ ci `addv` (Vec (clamp rr) (clamp rg) (clamp rb) `mulvs` 0.25)
```



Optimizing smallpt

20-11-0

Reduce to only effectful strictnesses (1.17imes)

```
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```

Reduce to only effectful strictnesses (1.17×)

Some inspection shows us which bang patters are actually carrying the weight. Most are unnecessary.

```
Remove Maybe from intersect(s) (1.32\times)
     -intersect :: Ray -> Sphere -> Maybe Double
     +intersect :: Ray -> Sphere -> Double
     intersect (Rav o d) (Sphere r p e c refl) =
     - if det<0 then Nothing else f (b-sdet) (b+sdet)
     + if det<0 then (1/0.0) else f (b-sdet) (b+sdet)
        where op = p `subv` o
             eps = 1e-4
              b = op 'dot' d
              det = b*b - (op `dot` op) + r*r
              sdet = sart det
              f a s = if a>eps then Just a else if s>eps then Just s else Nothing
              f a s = if a>eps then a else if s>eps then s else (1/0.0)
     -intersects :: Ray -> (Maybe Double, Sphere)
     +intersects :: Ray -> (Double, Sphere)
      intersects ray = (k, s)
     - where (k,s) = foldl' f (Nothing, undefined) spheres
              f (k',sp) s' = case (k',intersect ray s') of
                        (Nothing, Just x) -> (Just x,s')
                        (Just y, Just x) \mid x < y \rightarrow (Just x,s')
                        -> (k'.sp)
     + where (k,s) = foldl' f (1/0.0,undefined) spheres
              f (k', sp) s' = let !x = intersect ray s' in if x < k' then (x, s') else (k', sp)
      radiance :: Ray -> Int -> STRefU s Word64 -> ST s Vec
      radiance ray@(Ray o d) depth xi = case intersects ray of
     - (Nothing,_) -> return zerov
     - (Just t,Sphere _r p e c refl) -> do
     + (t,_) | t == (1/0.0) -> return zerov
     + (t.Sphere r p e c refl) -> do
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```

```
Optimizing smallpt

Remove Maybe from intersect(s) (1.32×)

Remove Maybe from intersect(s) (1.32×)
```

redinant exp(0) by e(d) depth at e can intersects ray of $(0.04 \log_2 e) > e$ even ever $(0.04 + 0.04 \log_2 e) > e$ or e(d) > de $(d_2) + 0.04 \log_2 e > e$ (1/2, d) > e return ever

Our innermost functions are of critical importance. Here we remove a Maybe which significantly reduces the boxing (which could have been mitigated with a StrictMaybe) and the cases. Since a Ray that fails to intersect something can be said to intersect at infinity, Double already actually covers the structure at play.

This also reduces allocation

Hand unroll the fold in intersects $(1.35\times)$

```
intersects :: Ray -> (Double, Sphere)
-intersects ray = (k, s)
- where (k,s) = foldl' f (1/0.0,undefined) spheres
      f (k', sp) s' = let !x = intersect ray s' in if x < k' then (x, s') else (k', sp)
+intersects ray =
+ f (f (f (f (f (f (f (f (intersect ray sphLeft, sphLeft) sphRight) sphBack) sphFrnt) sphBotm) sphTop) sphMirr) sphGlas) sph
+ where
+ f (k', sp) s' = let !x = intersect ray s' in if x < k' then (x, s') else (k', sp)
-spheres :: [Sphere]
-spheres = let s = Sphere ; z = zerov ; (.*) = mulvs ; v = Vec in
- [ s 1e5 (v (1e5+1) 40.8 81.6) z (v 0.75 0.25 0.25) DIFF --Left
    s 1e5 (v (-1e5+99) 40.8 81.6) z (v 0.25 0.25 0.75) DIFF --Rght
    s 1e5 (v 50 40.8 1e5)
                                     z (v 0.75 0.75 0.75) DIFF --Back
- , s 1e5 (v 50 40.8 (-1e5+170)) z z
                                                            DIFF --Frnt
- , s 1e5 (v 50 1e5 81.6)
                                     z (v 0.75 0.75 0.75) DIFF --Botm
- , s 1e5 (v 50 (-1e5+81.6) 81.6) z (v 0.75 0.75 0.75) DIFF --Top
- , s 16.5(v 27 16.5 47)
                                     z ((v 1 1 1).* 0.999) SPEC --Mirr
- , s 16.5(v 73 16.5 78)
                                     z ((v 1 1 1).* 0.999) REFR --Glas
- , s 600 (v 50 (681.6-0.27) 81.6) (v 12 12 12)
                                                         z DIFF]--Lite
+sphLeft, sphRight, sphBack, sphFrnt, sphBotm, sphTop, sphMirr, sphGlas, sphLite :: Sphere
+sphLeft = Sphere 1e5 (Vec (1e5+1) 40.8 81.6)
                                                     zerov (Vec 0.75 0.25 0.25) DIFF --Left
+sphRight = Sphere 1e5 (Vec (-1e5+99) 40.8 81.6) zerov (Vec 0.25 0.25 0.75) DIFF --Rght
+sphBack = Sphere 1e5 (Vec 50 40.8 1e5)
                                                     zerov (Vec 0.75 0.75 0.75) DIFF --Back
+sphFrnt
          = Sphere 1e5 (Vec 50 40.8 (-1e5+170))
                                                                                DIFF --Frnt
                                                     zerov zerov
+sphBotm = Sphere 1e5 (Vec 50 1e5 81.6)
                                                     zerov (Vec 0.75 0.75 0.75) DIFF --Botm
+sphTop
          = Sphere 1e5 (Vec 50 (-1e5+81.6) 81.6)
                                                     zerov (Vec 0.75 0.75 0.75) DIFF --Top
+sphMirr = Sphere 16.5 (Vec 27 16.5 47)
                                                     zerov (Vec 0.999 0.999 0.999) SPEC --Min
+sphGlas = Sphere 16.5 (Vec 73 16.5 78)
                                                     zerov (Vec 0.999 0.999 0.999) REFR --Gla
+sphLite = Sphere 600 (Vec 50 (681.6-0.27) 81.6) (Vec 12 12 12)
                                                                            zerov DIFF --Lite
```



Optimizing smallpt

Hand unroll the fold in intersects (1.35 imes)

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This removes the list and this a potential level of indirections and branches. Sadly GHC did not do this for us even though the list was static.

```
intersects ray = ...
   where
-     f (k', sp) s' = let !x = intersect ray s' in if x < k' then (x, s') else (k', sp)
+     f !(!k', !sp) !s' = let !x = intersect ray s' in if x < k' then (x, s') else (k', sp)</pre>
```



Marking interesects' f parameters strict. Again, its clear these will get used.

Strategic application of strictness $(1.49\times)$

```
TODO: This diff looks very bad
- if det<0 then (1/0.0) else f (b-sdet) (b+sdet)
- where op = p `subv` o
         eps = 1e-4
        b = op 'dot' d
        det = b*b - (op 'dot' op) + r*r
        sdet = sqrt det
        f a s = if a>eps then a else if s>eps then s else (1/0.0)
+ if det<0
+ then (1/0.0)
+ else
    let !eps = 1e-4
         !sdet = sqrt det
         !a = b-sdet
        !s = b+sdet
    in if a>eps then a else if s>eps then s else (1/0.0)
+ where
    !det = b*b - (op 'dot' op) + r*r
     !b = op 'dot' d
    !op = p `subv` o
- (t, ) | t == (1/0.0) -> return zerov
- (t,Sphere _r p e c refl) -> do
    let x = o 'addy' (d 'mulvs' t)
        n = norm $ x `subv` p
        nl = if n 'dot' d < 0 then n else n 'mulvs' (-1)
        depth' = depth + 1
+ (!t. ) | t == (1/0.0) -> return zerov
+ (!t,!Sphere _r p e c refl) -> do
    let !x = o `addv` (d `mulvs` t)
        !n = norm $ x `subv` p
        !nl = if n 'dot' d < 0 then n else n 'mulvs' (-1)
        !depth' = depth + 1
                    a=nt-nc
                    b=nt+nc
                    r0=a*a/(b*b)
                    c' = 1-(if into then -ddn else tdir'dot'n)
                    re=r0+(1-r0)*c'*c'*c'*c'*c'
                    tr=1-re
                    pp=0.25+0.5*re
                    rp=re/pp
```



11-02

4 D > 4 A > 4 B > 4 B > B 9 Q (>

Strategic application of strictness $(1.49\times)$



Here we go through the program and apply some considered strictness to it. Forcing computation we don't need to do, or often forcing it to far before we need it is a loss. When we put a bang pattern in, GHC doesn't move it so we have to hand float it to an appropriate location.

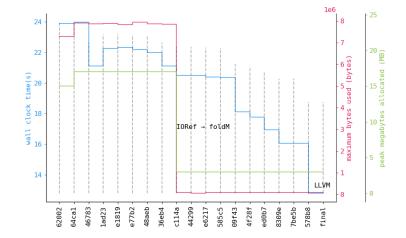
Use LLVM backend $(1.87\times)$

```
+packages: .
+
+package smallpt-opt
+ ghc-options: -fllvm
```



The LLVM backend can pick up assembly level optimizations that GHC has missed.

The view from the mountaintop





Takeaways

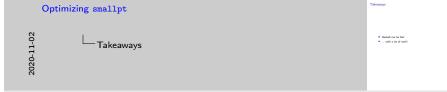
Optimizing smallpt



└─ Takeaways

► Haskell can be fast

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- ... with a lot of work!



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