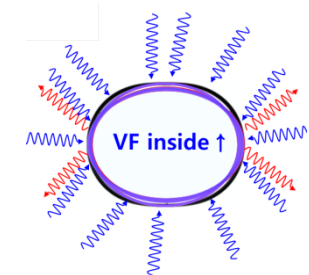
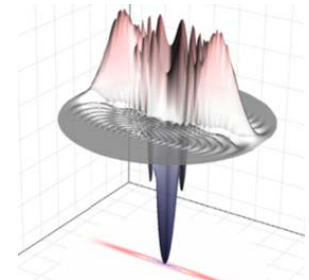
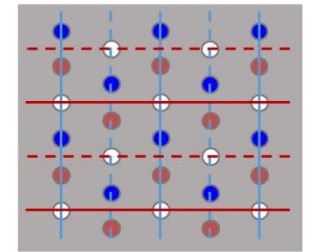
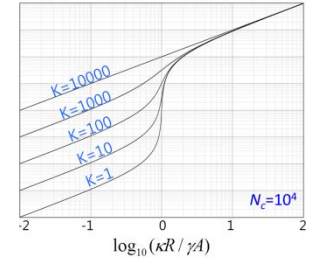


Thresholdless Quantum-Field Lasers  
KW An's Group

# **2015 INTRODUCTION TO RESEARCH PROGRAM**

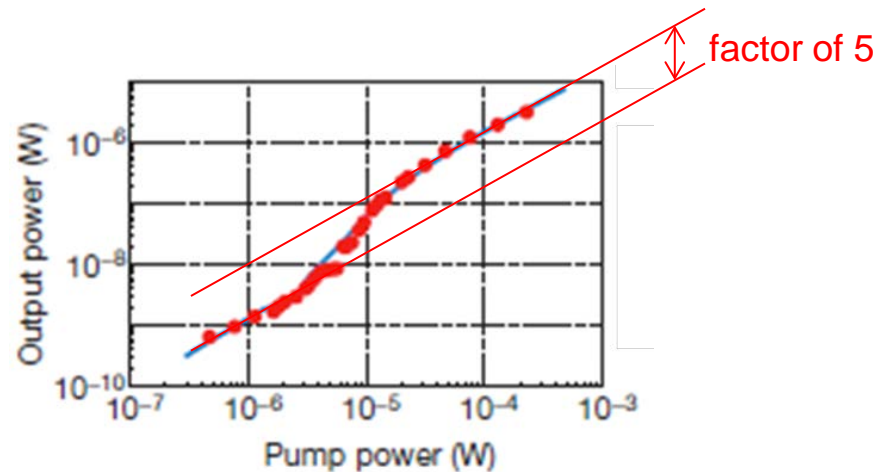
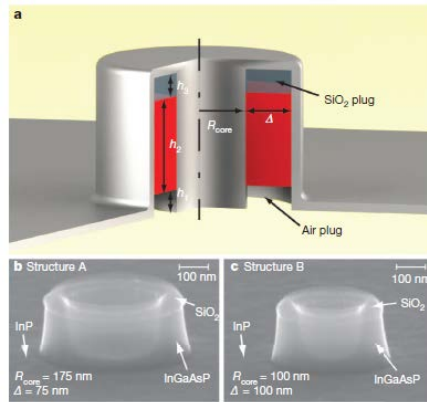
# Thresholdless Quantum-Field Lasers

- Thresholdless lasing
    - Low pumping power for usable output
    - Below the shot noise (Mandel  $Q < 0$ )
  - Multiple phase imprinting
    - More coding capacity than a classical field (of a single phase)
  - Schrödinger-cat-like state generation
    - Quantum information processing
    - Foundation of quantum mechanics
- Our quantum-field laser
- Asymmetric vacuum energy flow
    - Better understanding of vacuum energy and perhaps the dark energy



# Conventional Approach

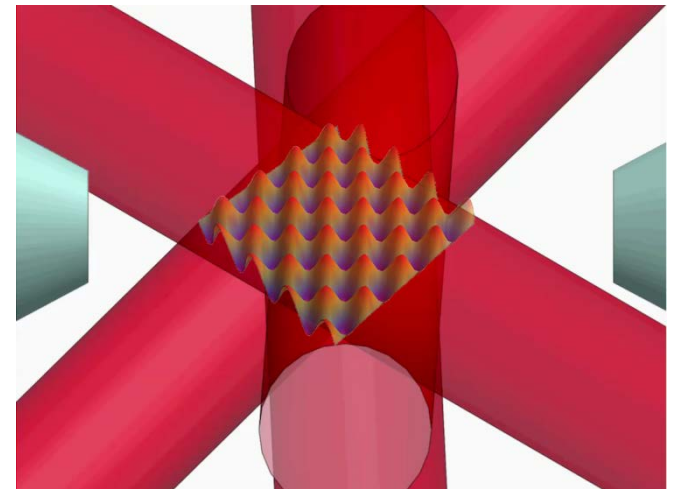
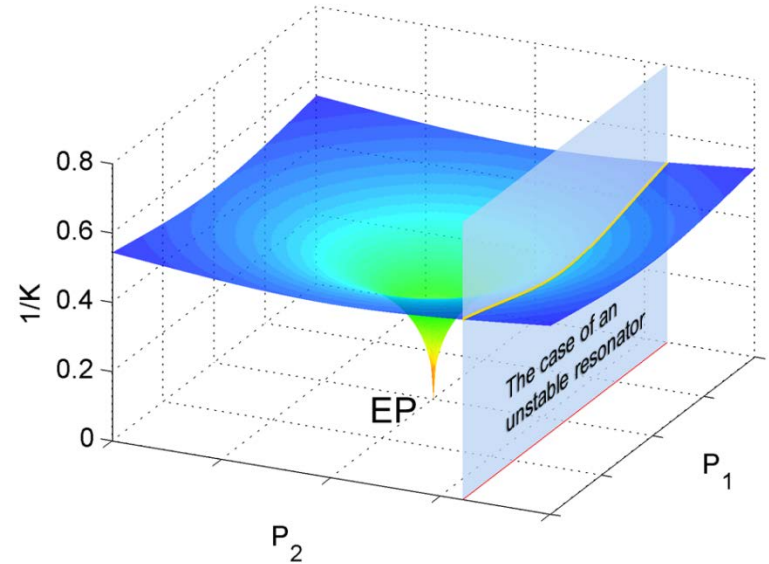
- All thresholdless lasers are based on the Purcell factor: spontaneous emission enhancement due to a small mode volume and a high Q
- To achieve thresholdless lasing, the mode volume  $\rightarrow \lambda^3$
- Relatively low Q  $\rightarrow$  high pump density  $\rightarrow$  heat dissipation problems, short life time, low temp operation



M. Khajavikhan *et al.*, Nature **482**, 204 (2012)

# Our Approaches

- Cavity: diverging Petermann effect at an exceptional point (EP)
- Gain medium: quantum dipole material



# I. Petermann Effect

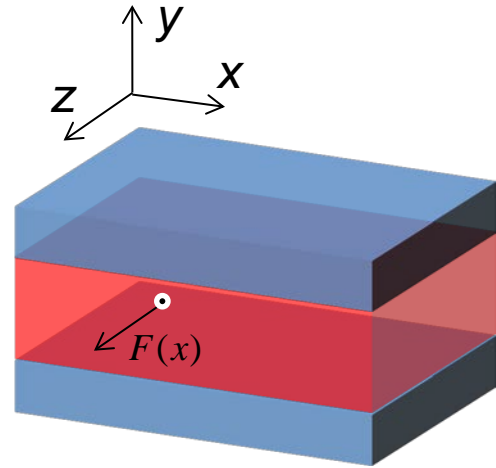
- Klaus Petermann reported that the spontaneous emission into a gain-guided mode is enhanced by a factor  $K$ :



Prof. Klaus Petermann  
Technische Universität Berlin

$$K = \frac{\left(\int |F(x)|^2 dx\right)^2}{\left|\int F^2(x) dx\right|^2}$$

$F(x)$ : the electric field  
amplitude of the lasing  
mode with its *adjoint*  
being  $F^*(x)$



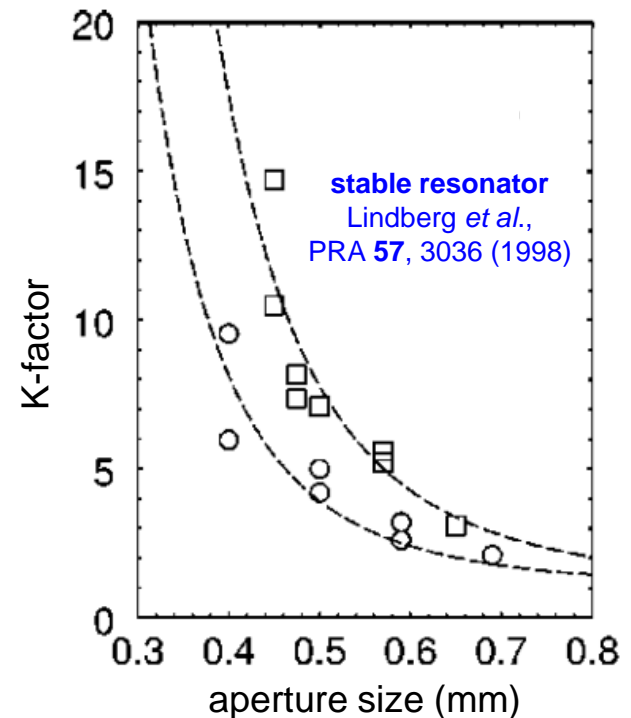
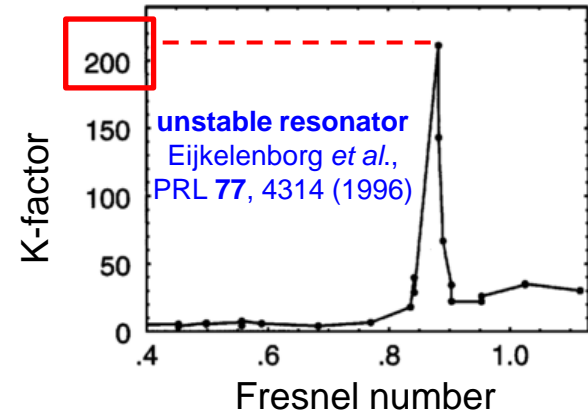
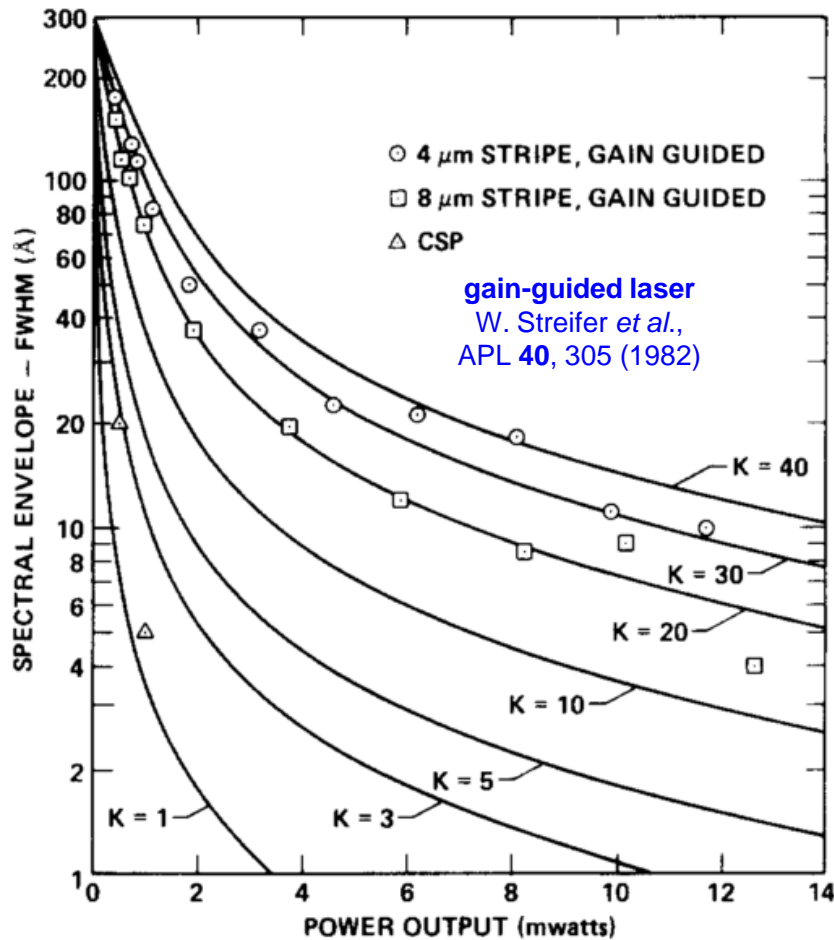
K. Petermann, IEEE J. Quantum  
Electron. **QE-15**, 566 (1979)

*“The spontaneous emission factor not only increases with decreasing volume of the active layer but also increases with increasing astigmatism”. – K. Petermann*

Purcell effect

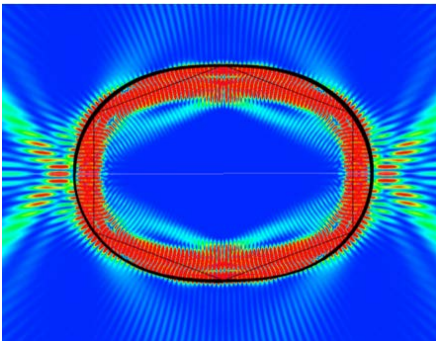
Petermann effect

# Petermann Factor in Experiments

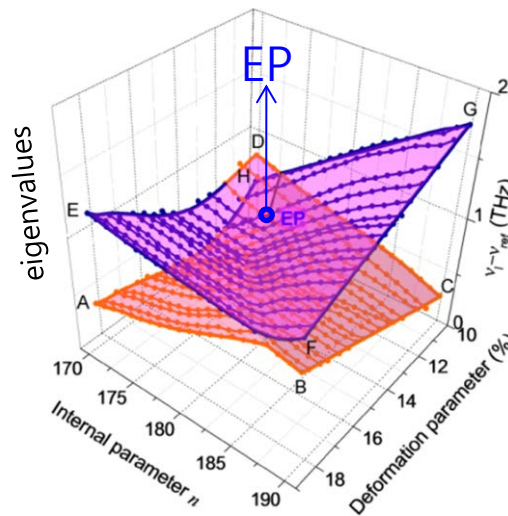


# Exceptional Point (EP)

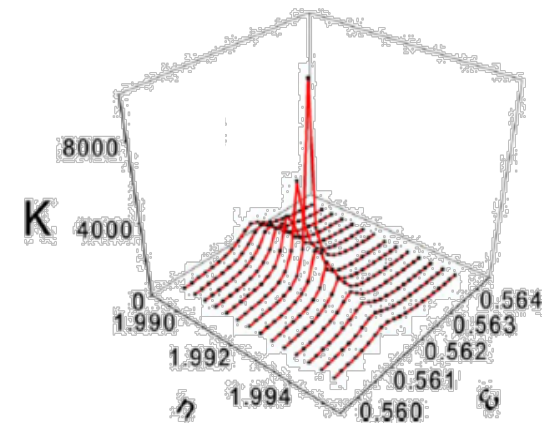
- In a deformed microcavity, two eigenmodes coalesce to a single eigenmode when the intermode coupling equals a combined decay rate.  $\rightarrow$  EP
- Peterman factor  $K$  ( $\propto$  atomic spontaneous emission rate) diverges at an EP.



Deformed microcavity  
S.-B. Lee *et al.*, PRL **88**, 033903  
(2002)



Experimental observation of an EP in a  
deformed microcavity  
S.-B. Lee *et al.*, PRL **103**, 134101 (2009)



Diverging Petermann factor at an EP in  
a deformed microcavity  
S.-Y. Lee *et al.*, PRA **78**, 015805 (2008)

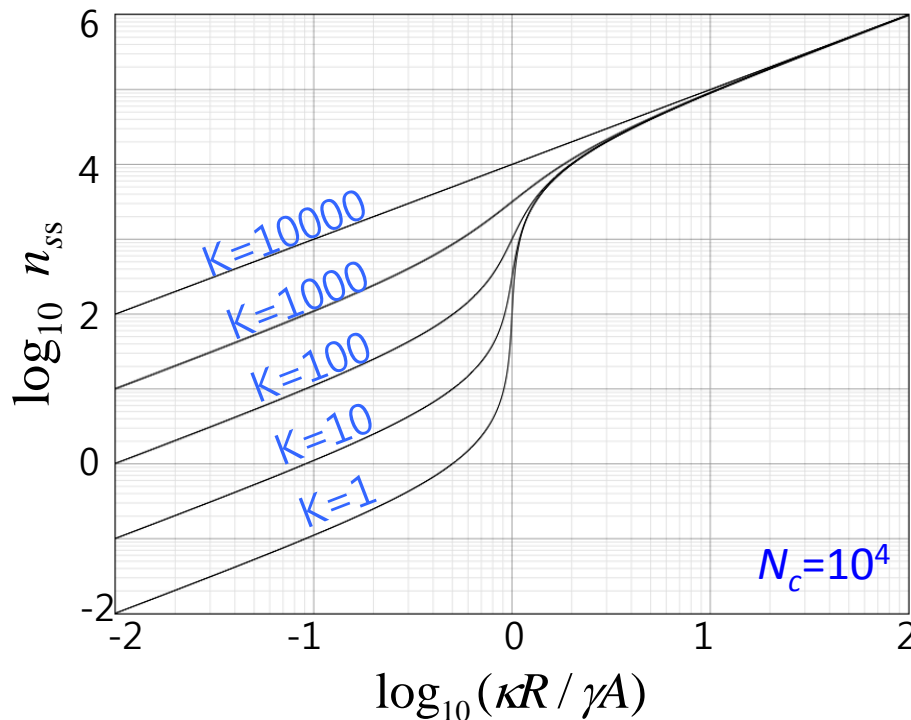
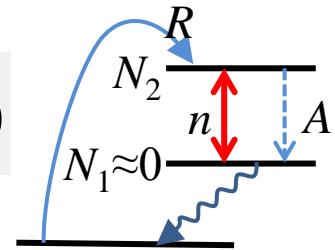


# Thresholdless Lasing

- Steady-state solution of the laser rate equations including  $K$  ( $N_1 \approx 0$  assumed)

Eijkelenborg *et al.*, PRA **57**, 571 (1998)

$$\frac{dn}{dt} \simeq \kappa(n + K)N_2 - \gamma n = 0, \quad \frac{dN_2}{dt} \simeq R - \kappa N_2 n - AN_2 = 0$$

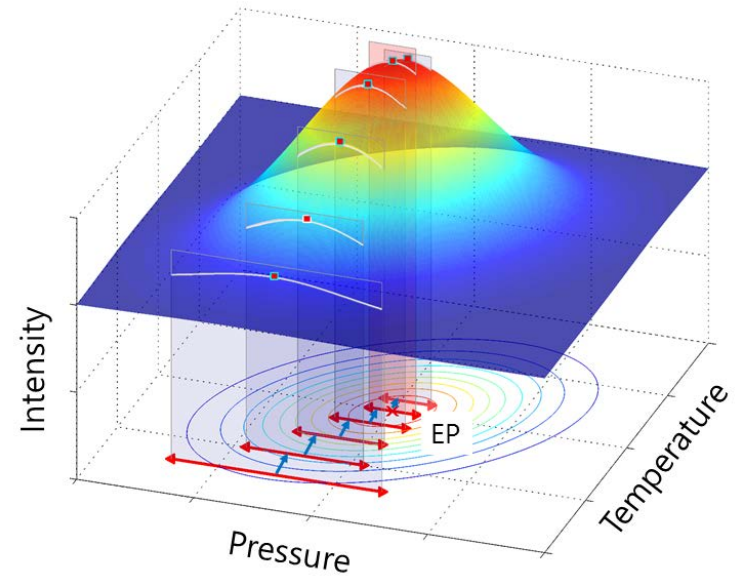
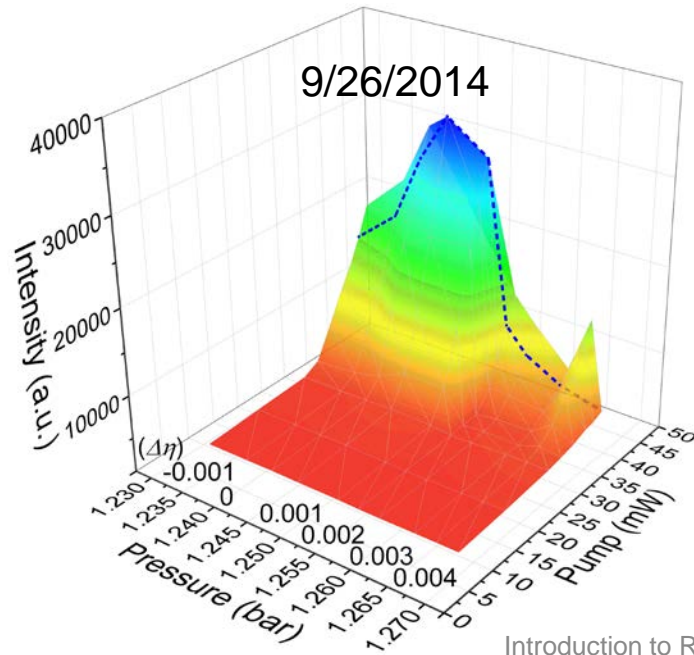
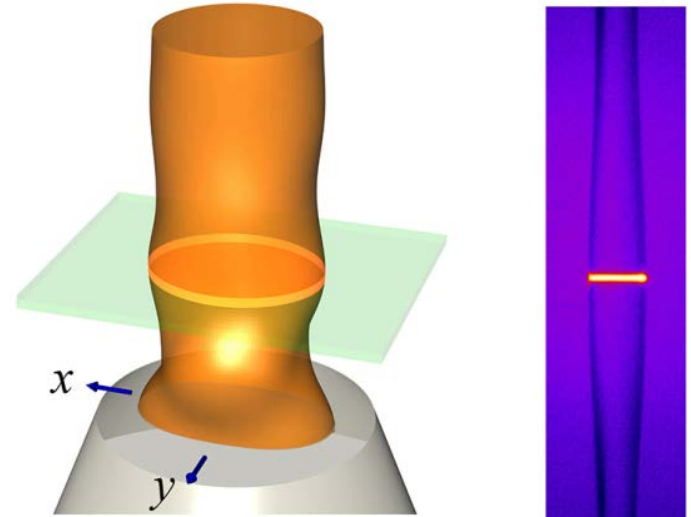
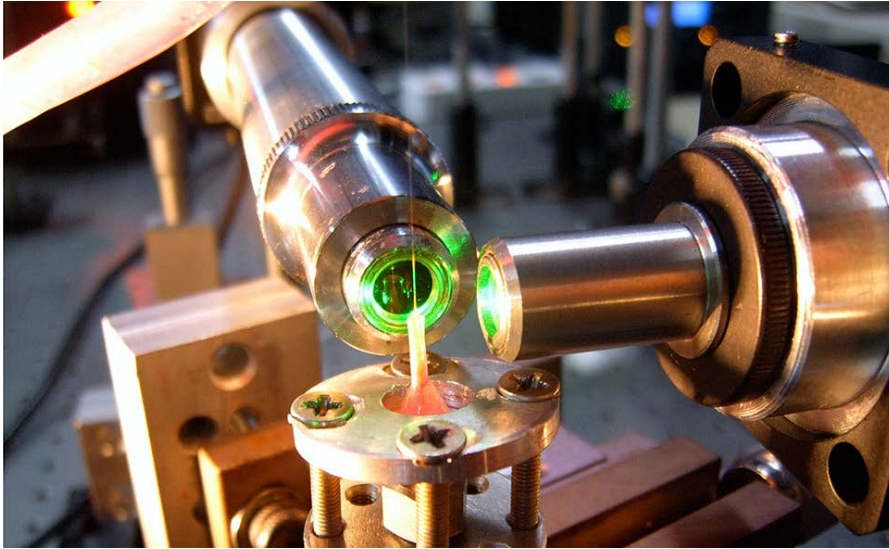


$R$  : pumping power  
 $A$  : decay rate of  $N_2$   
 $\kappa = A/N_c$   
 $N_c$  : # of cavity modes in the gain bandwidth

- The lasing threshold vanishes when  $K = N_c$ , so  $\kappa K = A$ , total spontaneous emission.



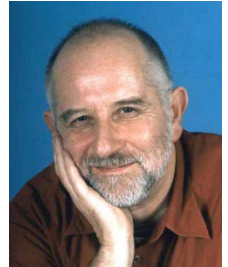
# Preliminary Data



# New Story

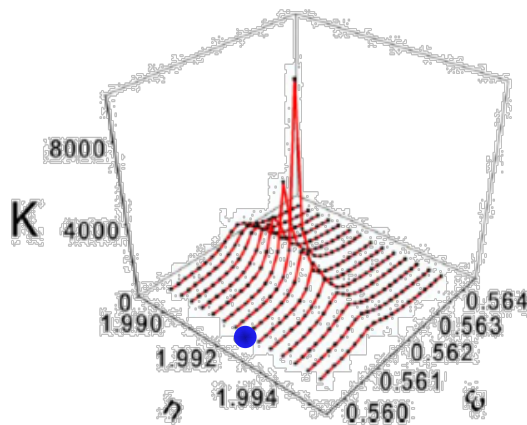
*“New has given an excellent account of the physical meaning and origin of  $K$ .” – M. V. Berry*

M. V. Berry, J. Mod. Opt. **50**, 63 (2003)



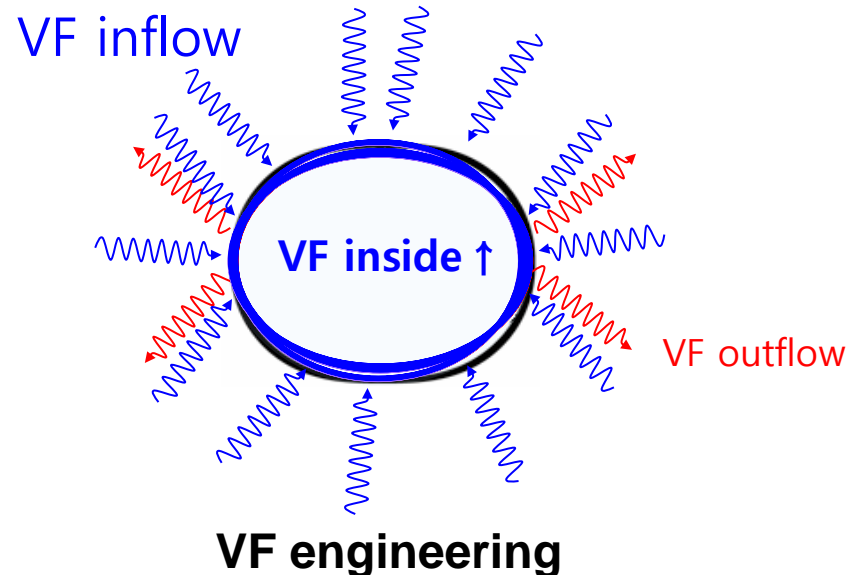
*“Excess noise can be attributed to a combination of spontaneous emission and vacuum fluctuations leaking into a lossy cavity from outside.” – G. H. C. New*

G. H. C. New, J. Mod. Opt. **42**, 799 (1995)



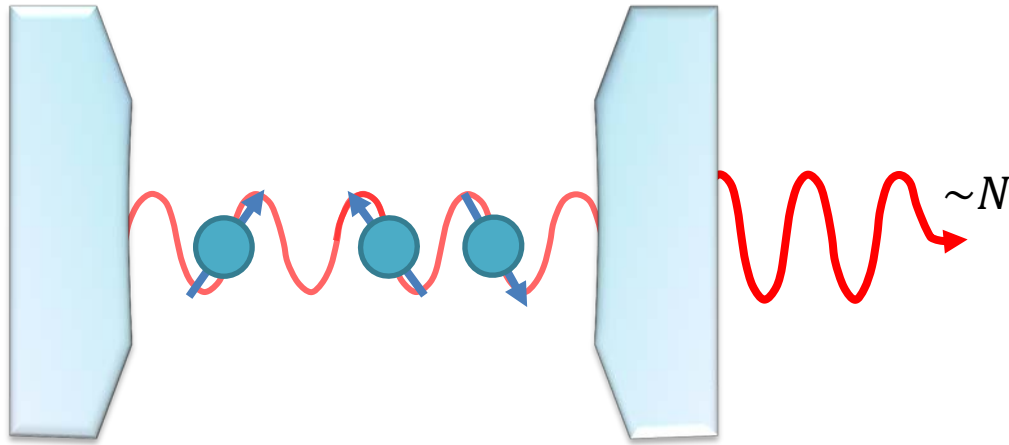
Diverging Petermann factor at an EP in  
a deformed microcavity

S.-Y. Lee *et al.*, PRA **78**, 015805 (2008)



# II. Quantum Dipole Material (QDM)

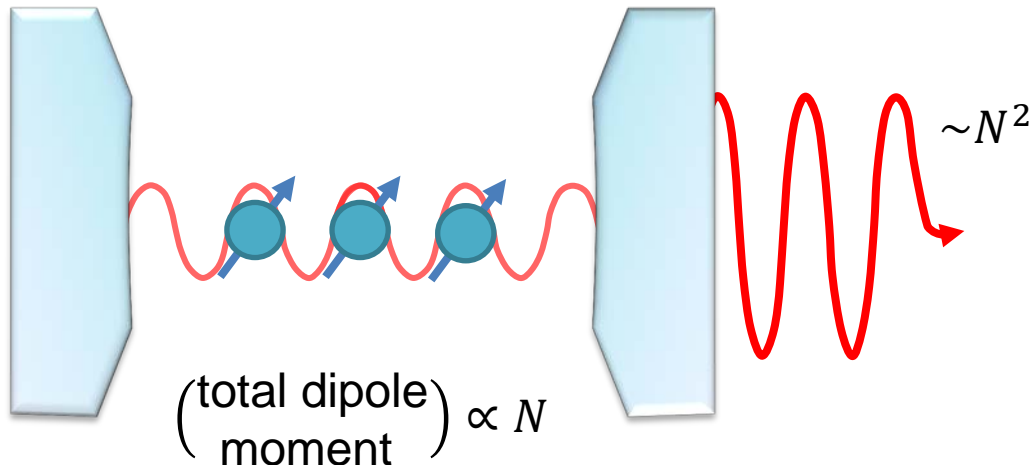
Incoherent quantum dipole



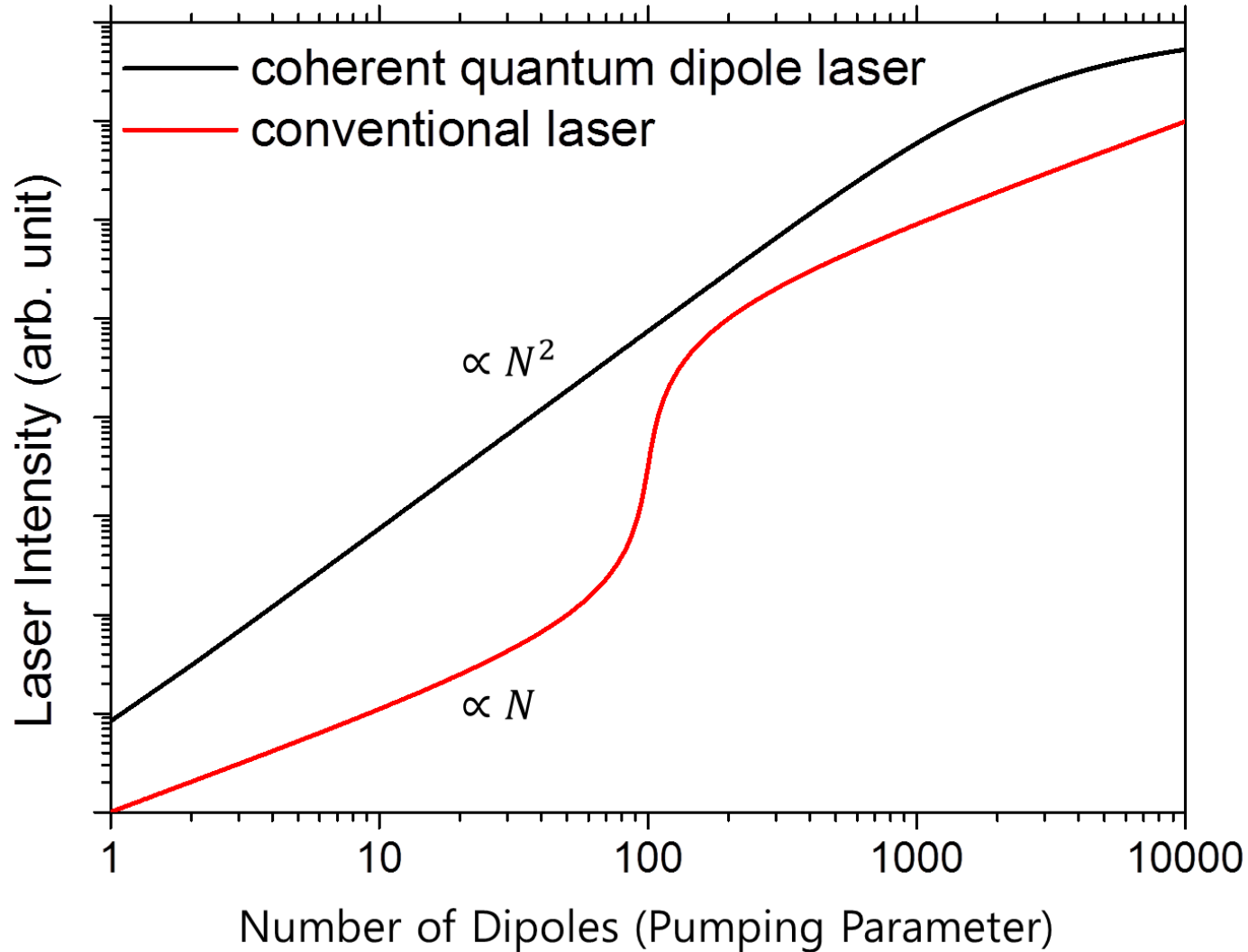
QDM:

A collection of coherent quantum dipoles prepared periodically in space with the same phase

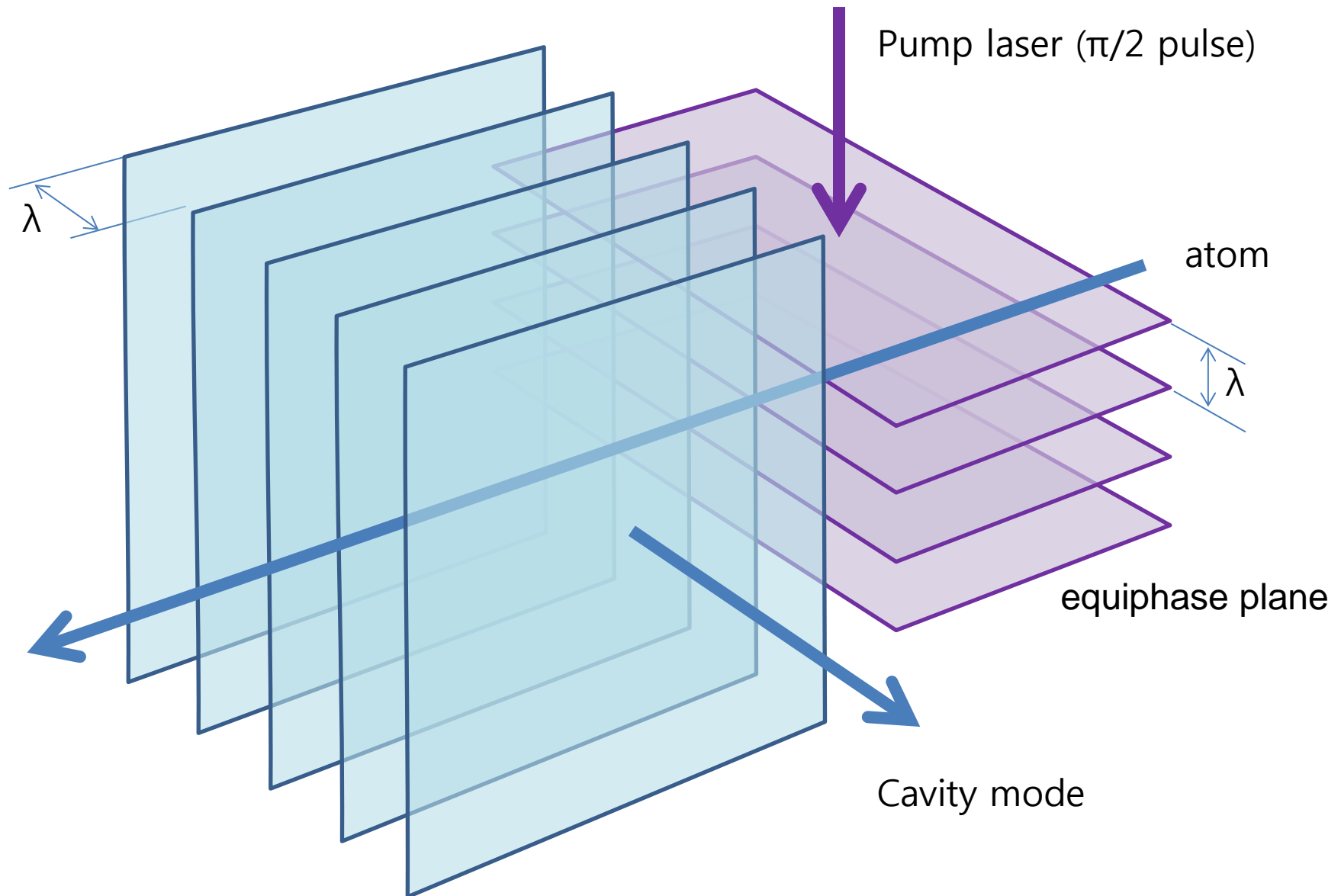
Coherent quantum dipole



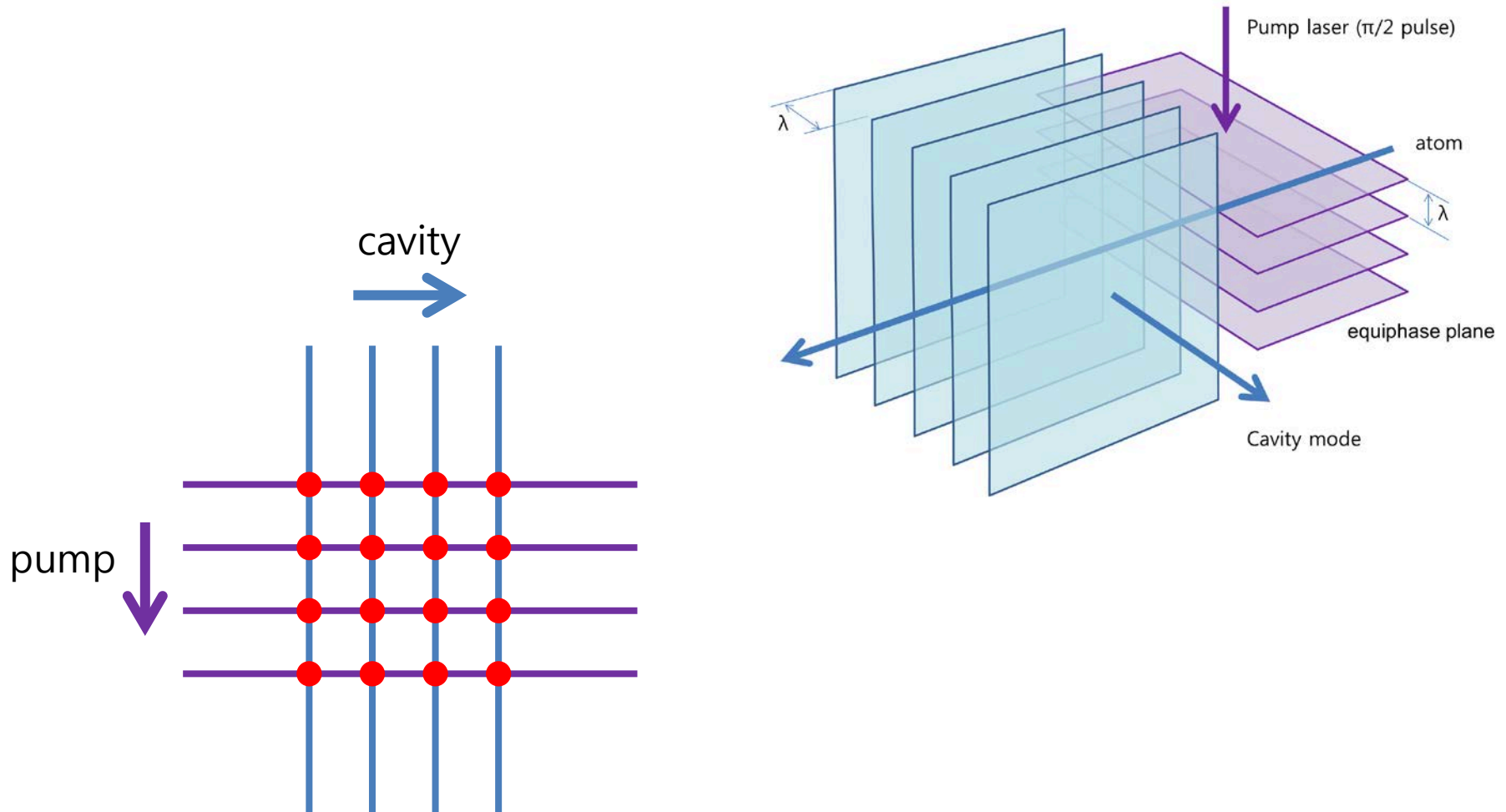
# Thresholdless Lasing with QDM



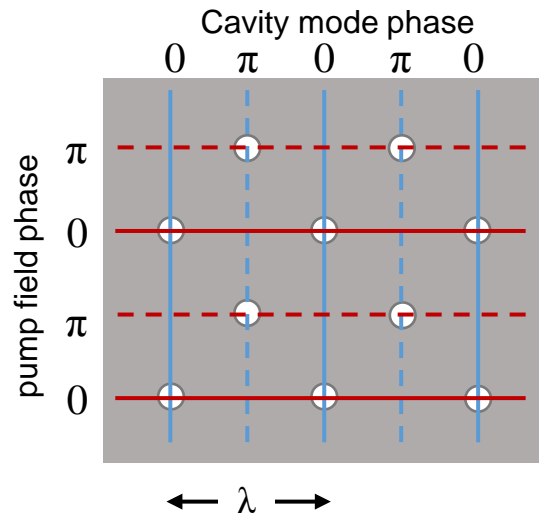
# How to realize the same phase



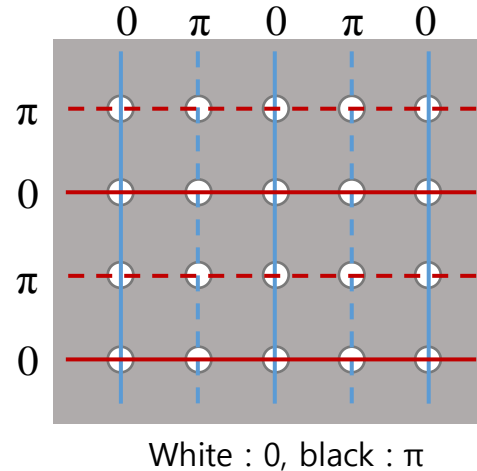
# How to realize the same phase



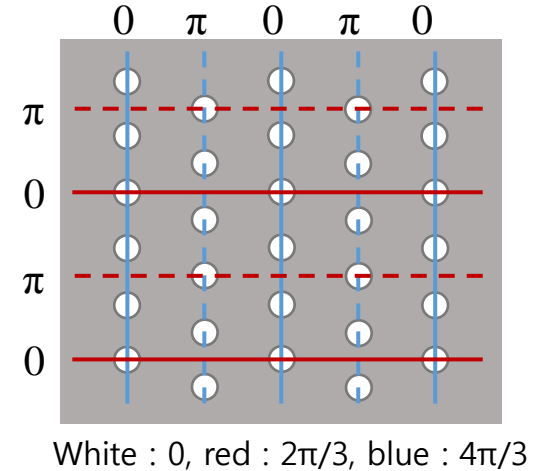
# Multi-Phase Encoding



All the same phase



Two phases



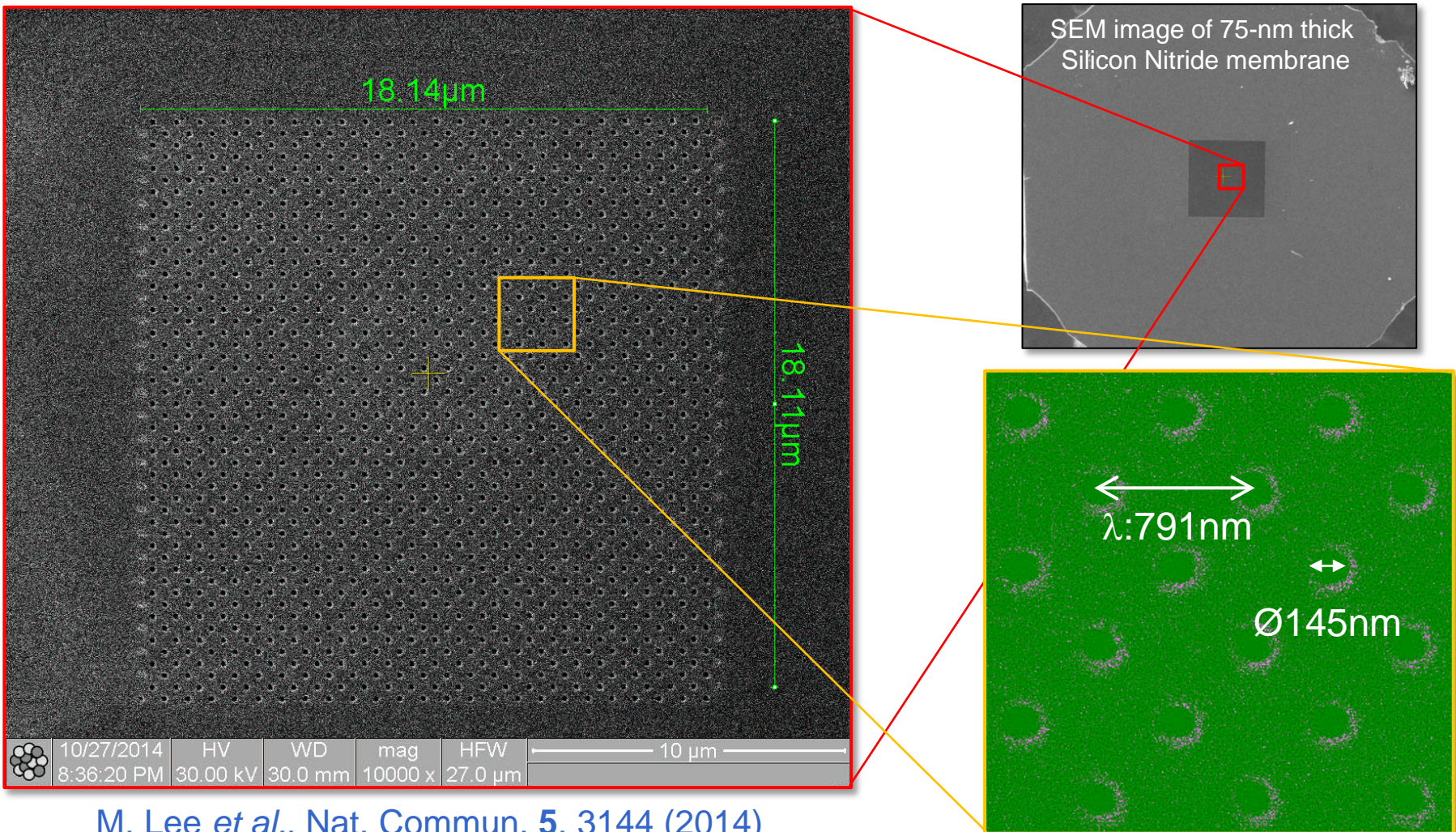
Three phases

- The atom-cavity relative phases are determined by the hole structures.



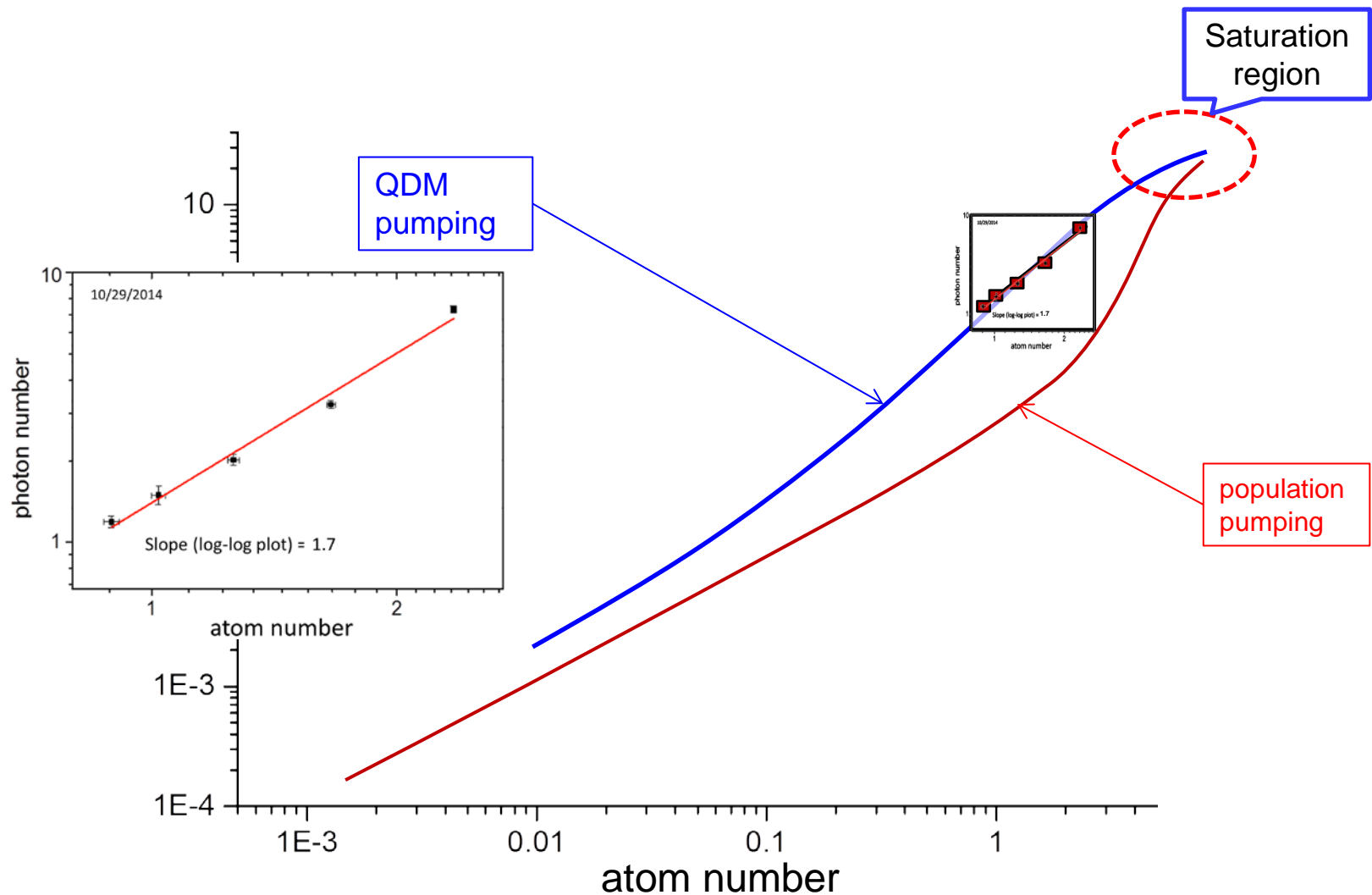
# Nanohole Array

- Machined by focused ion beam (FIB)



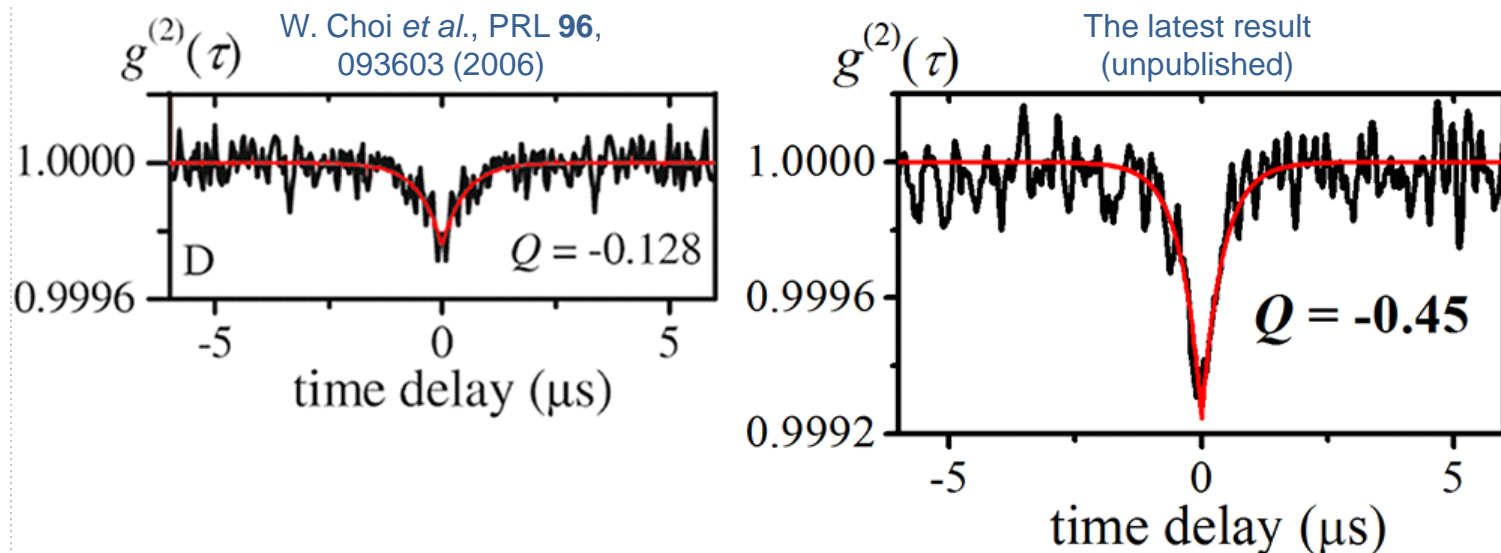
M. Lee *et al.*, Nat. Commun. **5**, 3144 (2014)

# Preliminary Data of $N^2$ Emission



# Sub-Poisson Light Generation

- Photon number stabilization occurs in the saturation region.
- Theoretical prediction, Mandel  $Q \approx -0.7$ 
  - variance  $(\Delta n^2) = 0.3\langle n \rangle$ , only 30% of the shot-noise variance.



$$g^{(2)}(t) = 1 + \frac{Q}{\langle n \rangle} e^{-t/\tau}$$

The second order  
correlation function

$$Q = \frac{\langle n^2 \rangle - \langle n \rangle^2}{\langle n \rangle} - 1$$

Mandel  $Q$

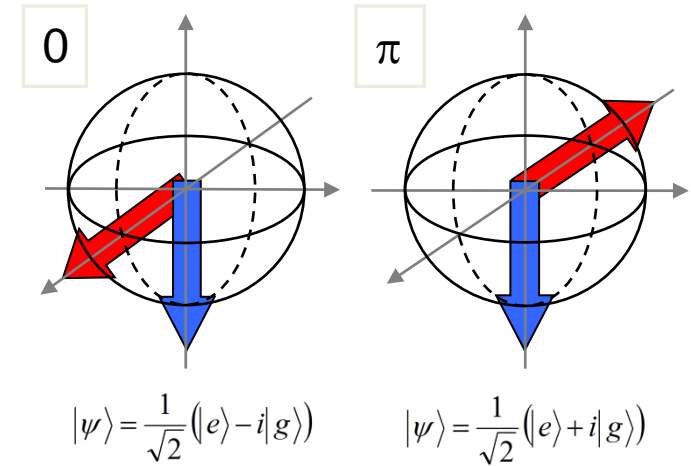
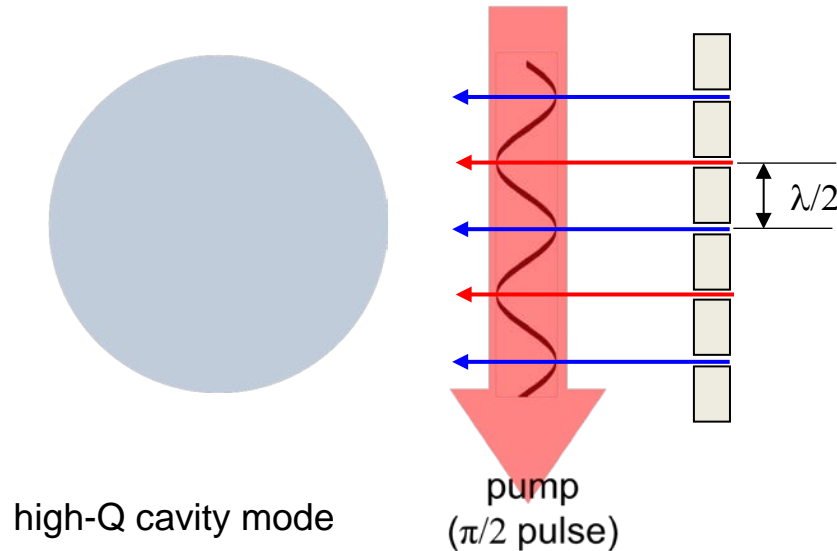
$Q > 0$  super-Poisson  
 $Q = 0$  Poisson  
 $Q < 0$  sub-Poisson

photon statistics



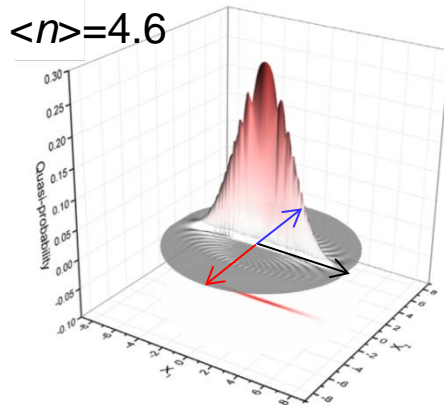
# Opposite-phase Imprinting

The same phase is ensured with a nanohole array.



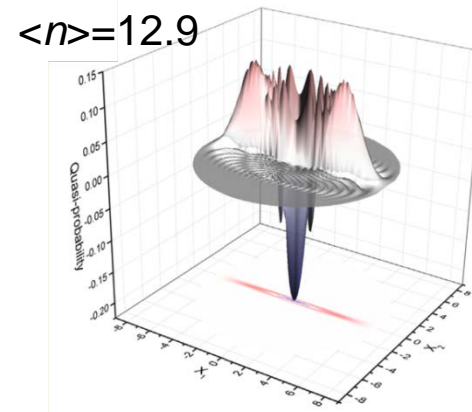
Bloch Sphere

Wigner function of the cavity field



Squeezed vacuum

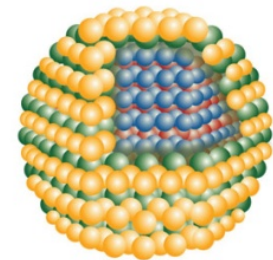
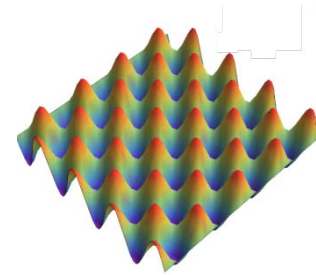
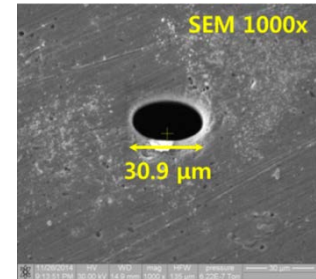
single-photon  
decay (**herald**)



Schrödinger's-cat-like state

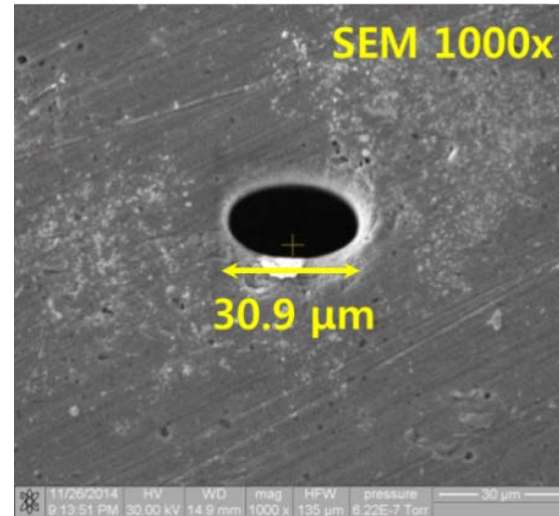
# III. Extension to practical forms

- Develop FIB technique for fabricating various microjet nozzles
- Simulate a stationary QDM by using an optical lattice in a cavity
- Design a thresholdless quantum-field microlaser with artificial atoms (e.g., excitons, polaritons, surface plasmons, etc.)

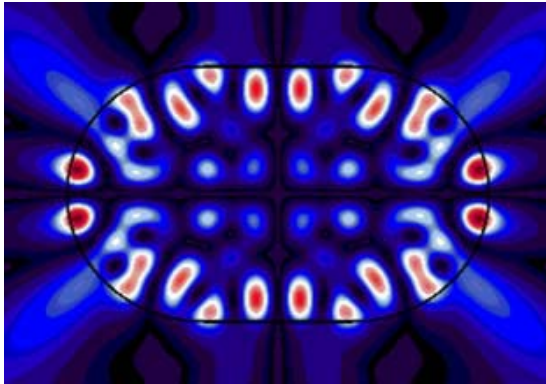
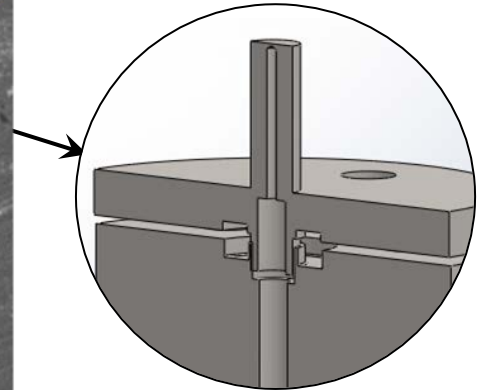


# FIB technique for microjet nozzles

- FIB precision: 10nm
- Simulating various cavity shapes & array of cavities
- Compact optofluidic packaging possible

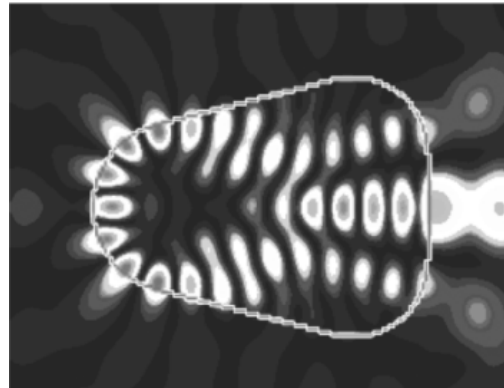


Sectional view



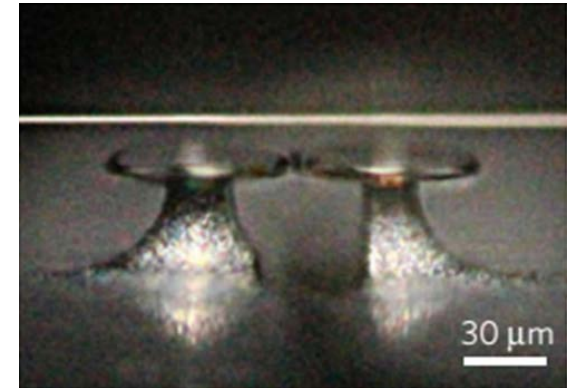
a stadium

Lee *et al.*, Phys. Rev. A **78**, 015805 (2008)



a rounded triangle

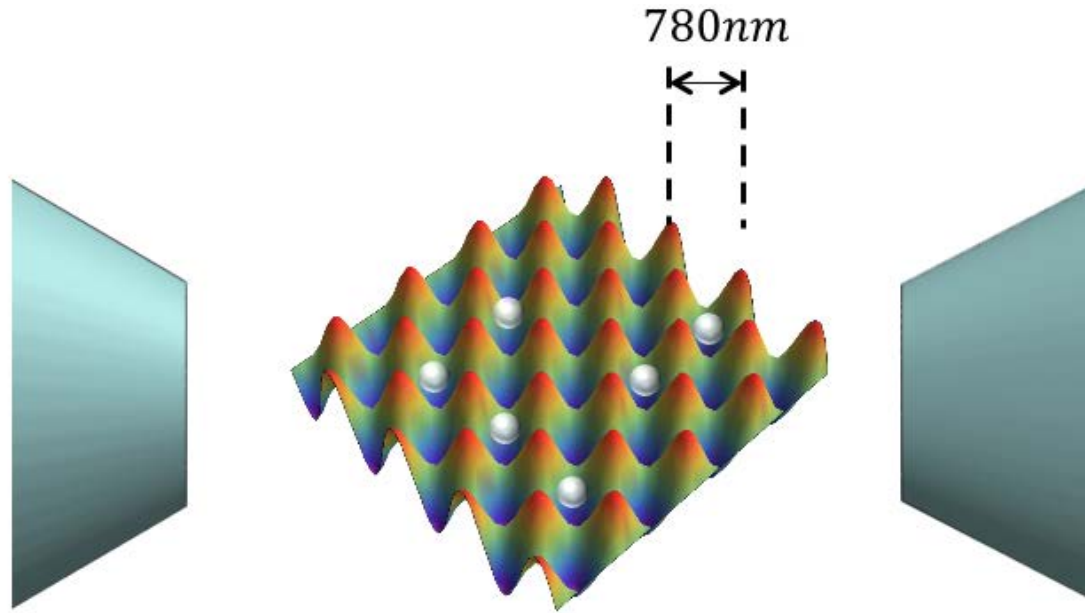
Kurdoglyan *et al.*, Opt. Lett. **29**, 2758 (2004)



coupled disks

Peng *et al.*, Nat. Phys. **10**, 394 (2014)

# Stationary quantum dipole materials



- $^{85}\text{Rb}$  Atoms are confined in a 2D optical lattice (pump in one direction). Along the cavity axis, the lattice spacing equals the Rb wavelength (equiphase to the cavity mode).
- Towards realizing solid-state QDM (e.g. quantum dots)



# Thresholdless Quantum-Field Lasers

- Thresholdless lasing
  - Low pumping power for usable output
  - Below the shot noise (Mandel  $Q < 0$ )
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  - More coding capacity than a classical field (of a single phase)
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- Asymmetric vacuum energy flow
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