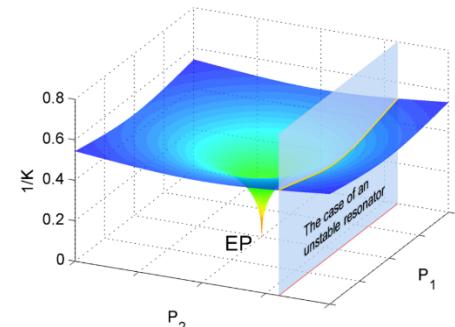
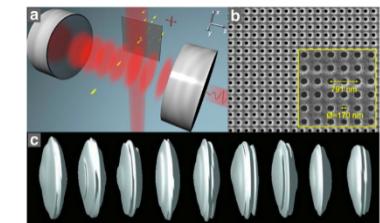
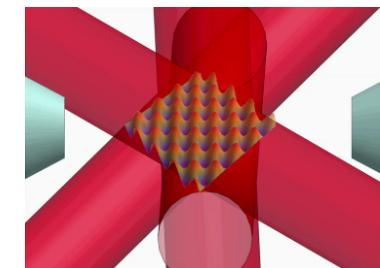
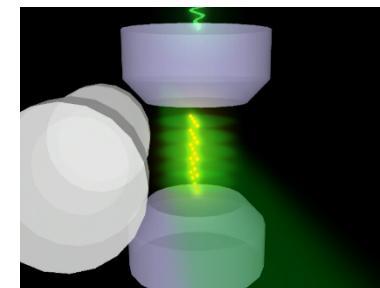


2016 Introduction to Our Research Programs

Quantum-Field Laser Laboratory
KW An's Group

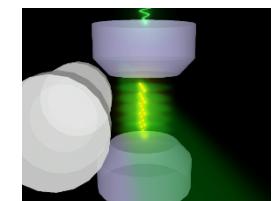
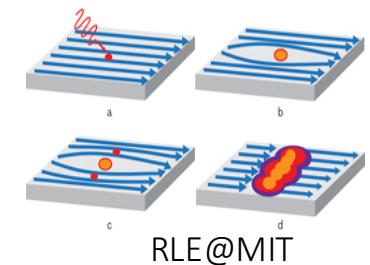
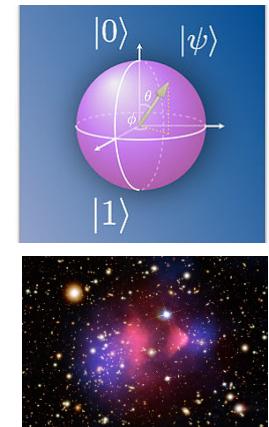
Physics of atom-field interaction

- Quantum information
 - Ideal single-photon sources
 - Ideal single-photon detectors
- Nonclassical light generation
 - Highly sub-Poisson intense light
 - Quantum-dipole lasing
- Manipulation of vacuum fluctuation
 - 3D imaging of vacuum fields
 - Diverging spontaneous emission in a non-Hermitian system
 - Thresholdless lasing

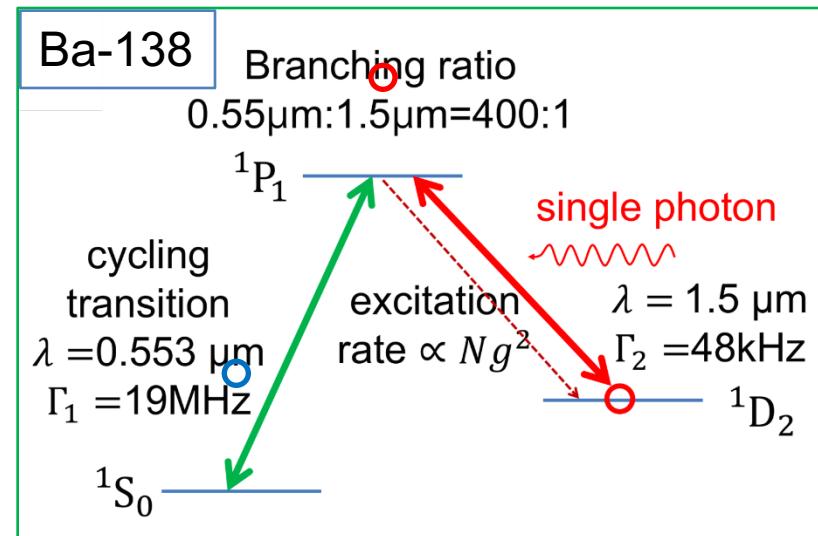
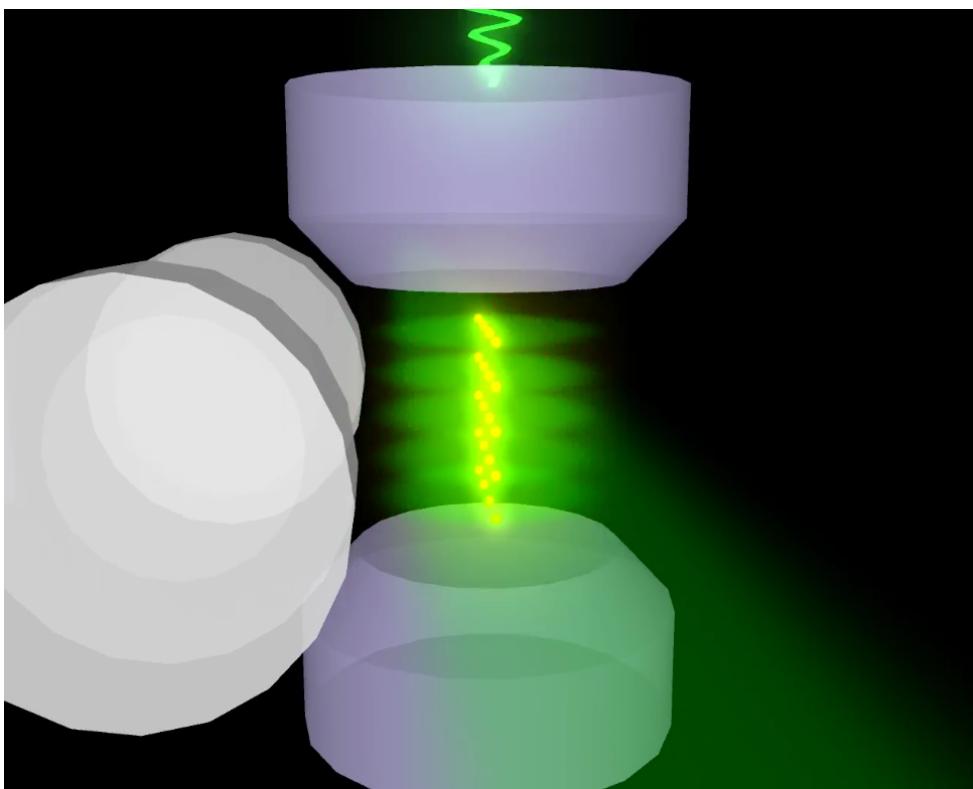


I. Ideal single-photon detectors

- Needs
 - A near ideal single-photon detection efficiency is needed in many photon-qubit-based quantum information processing schemes.
 - Detection of axion dark matter requires a high-efficient microwave photon detector.
- Current technology
 - Superconducting Josephson-junction-based detectors have very high efficiency but do not have single-photon resolution (\because large dark counts).
 - Avalanche photodiode detectors in the optical region have single-photon resolution but have only about 50% single-photon detection efficiency.
- Our goal:
 - to realize an ideal optical/ μ -wave single-photon detector by using
 - quantum dipole material
 - cavity-QED principle

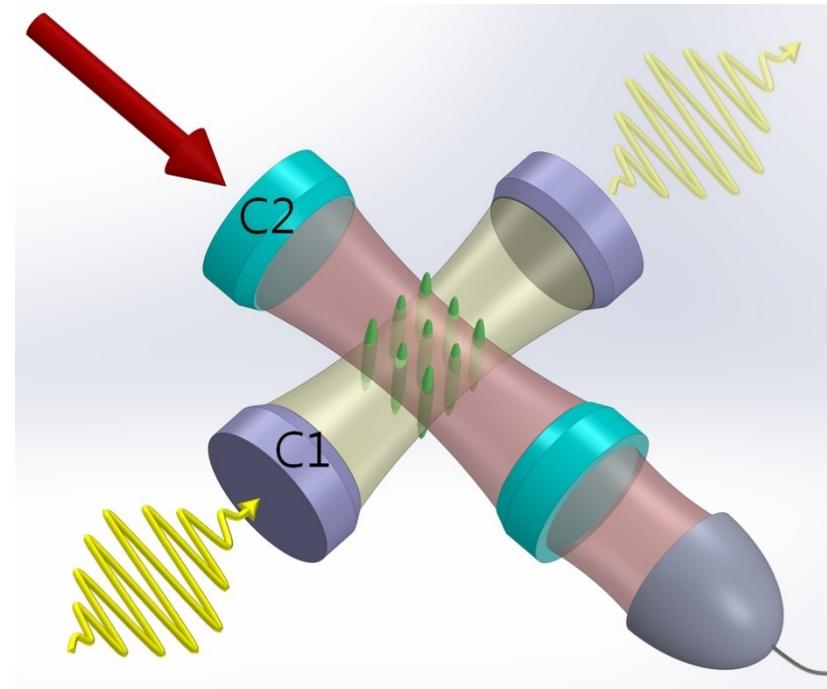
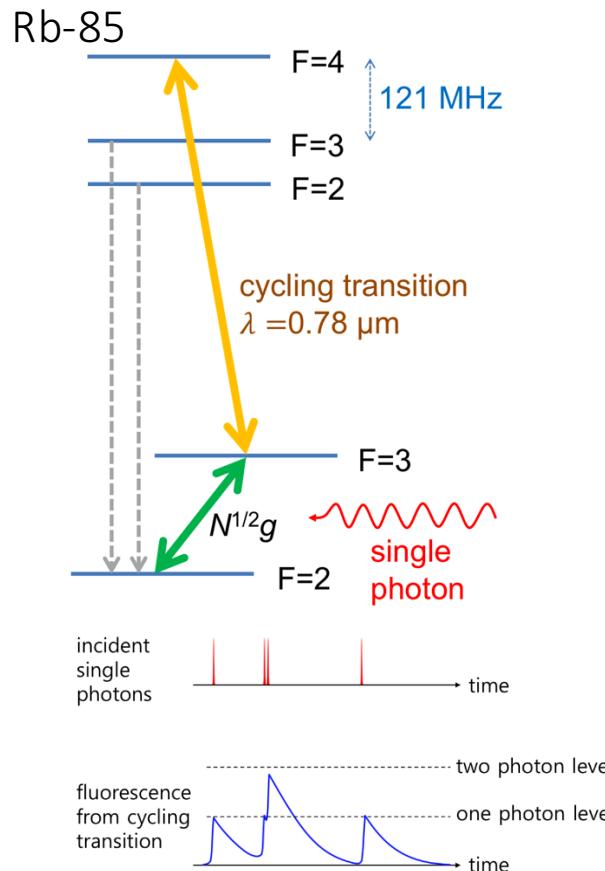


Optical single-photon detector



- Barium atoms in a beam localized by a nanohole array
- 1 input photon will generate about 400 output photons (gain=400).
- With a conventional detector, a near 100% single-photon detection efficiency can be achieved.

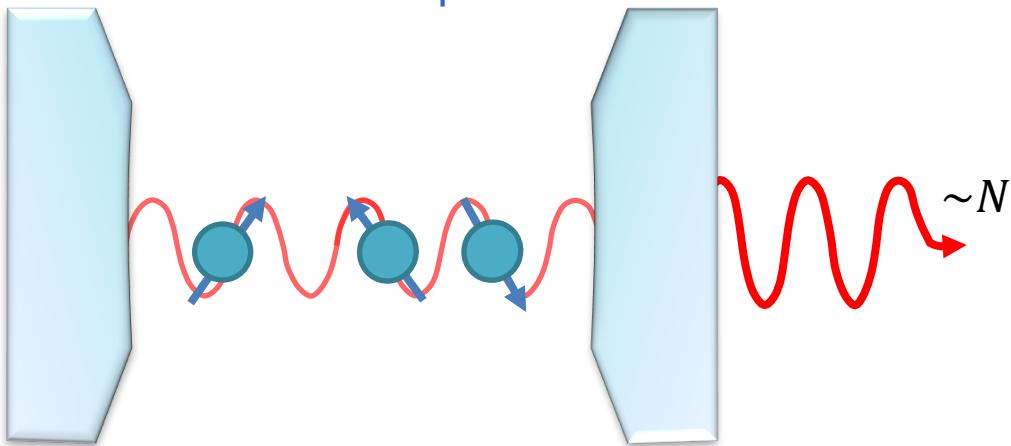
Microwave single-photon detector



- Rubidium atoms localized in an optical lattice
- 1 microwave input photon will generate more than 1000 optical photons (gain>1000).

II. Quantum-dipole laser

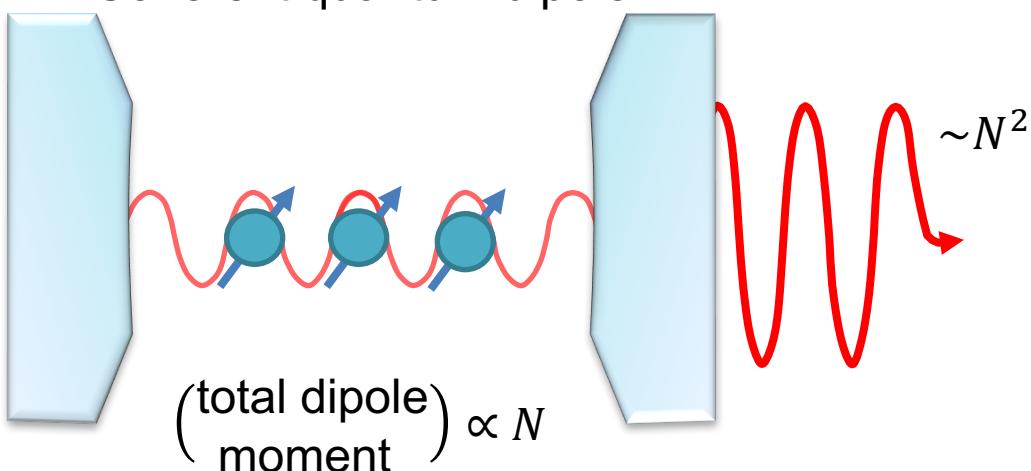
Incoherent dipoles



- What is the quantum-dipole material?

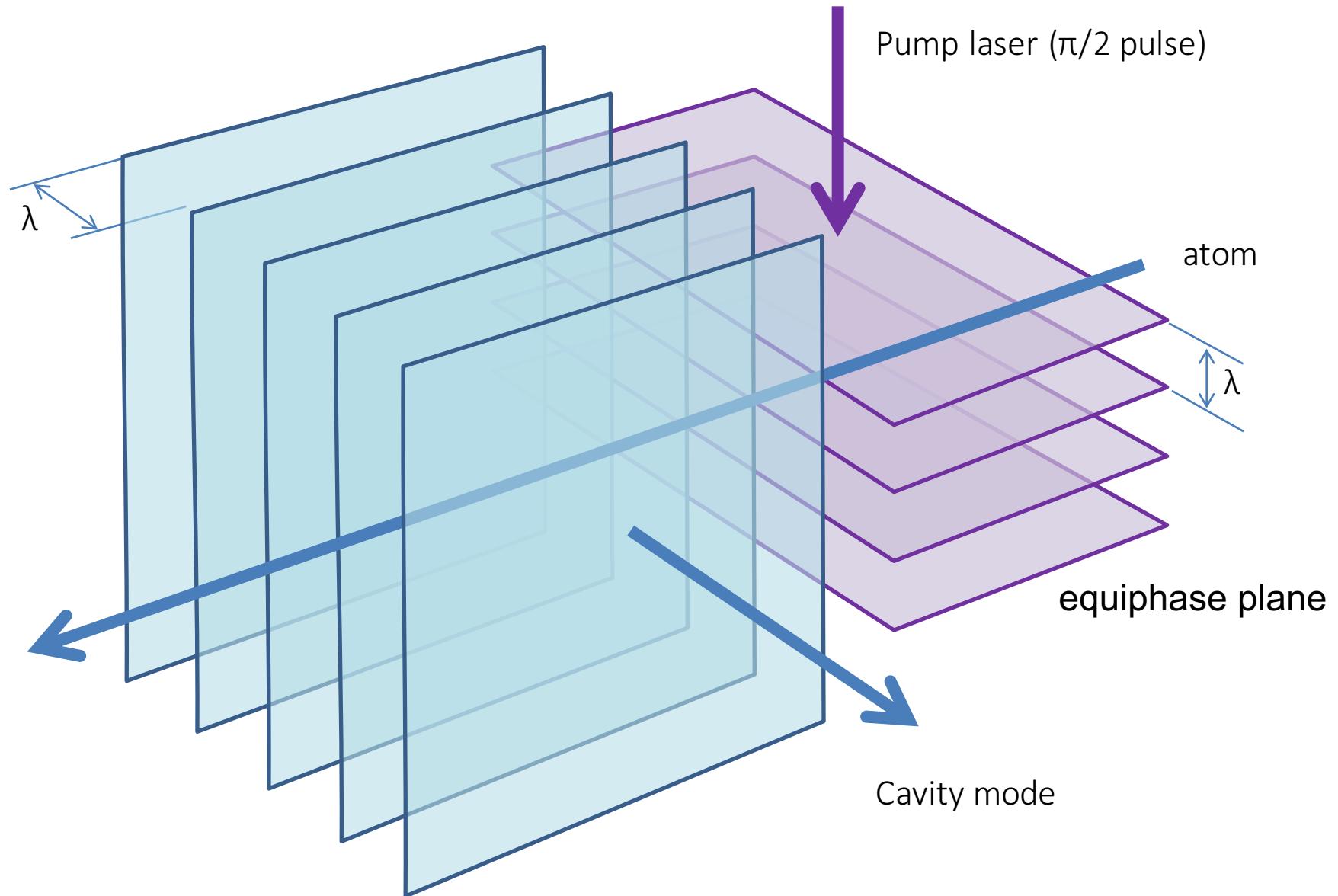
- A collection of identical quantum dipoles* prepared periodically in space with the same phase

Coherent quantum dipole

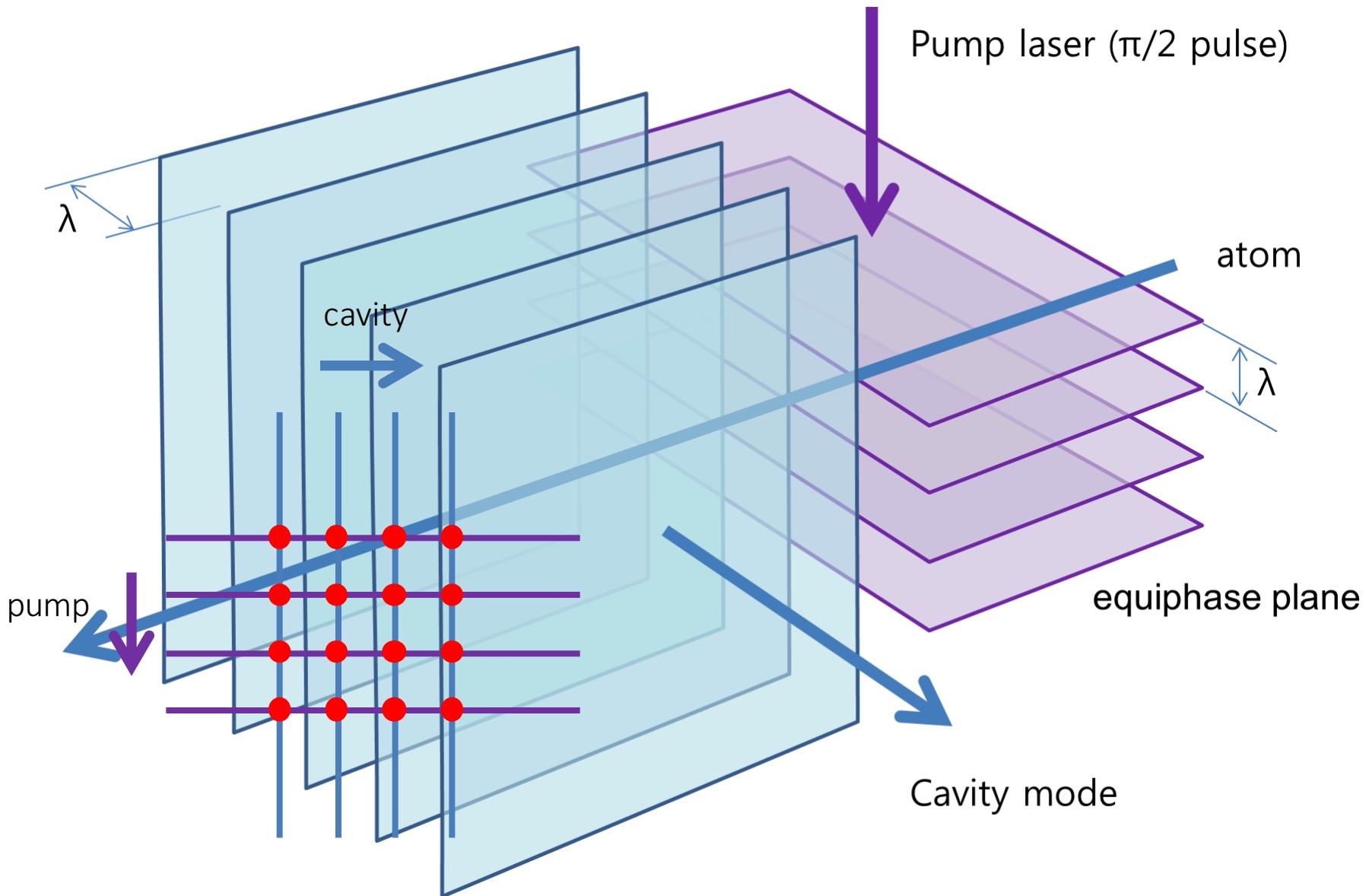


*Quantum dipoles: atoms in the same superposition of ground and excited states with the same phase

How to realize the same phase

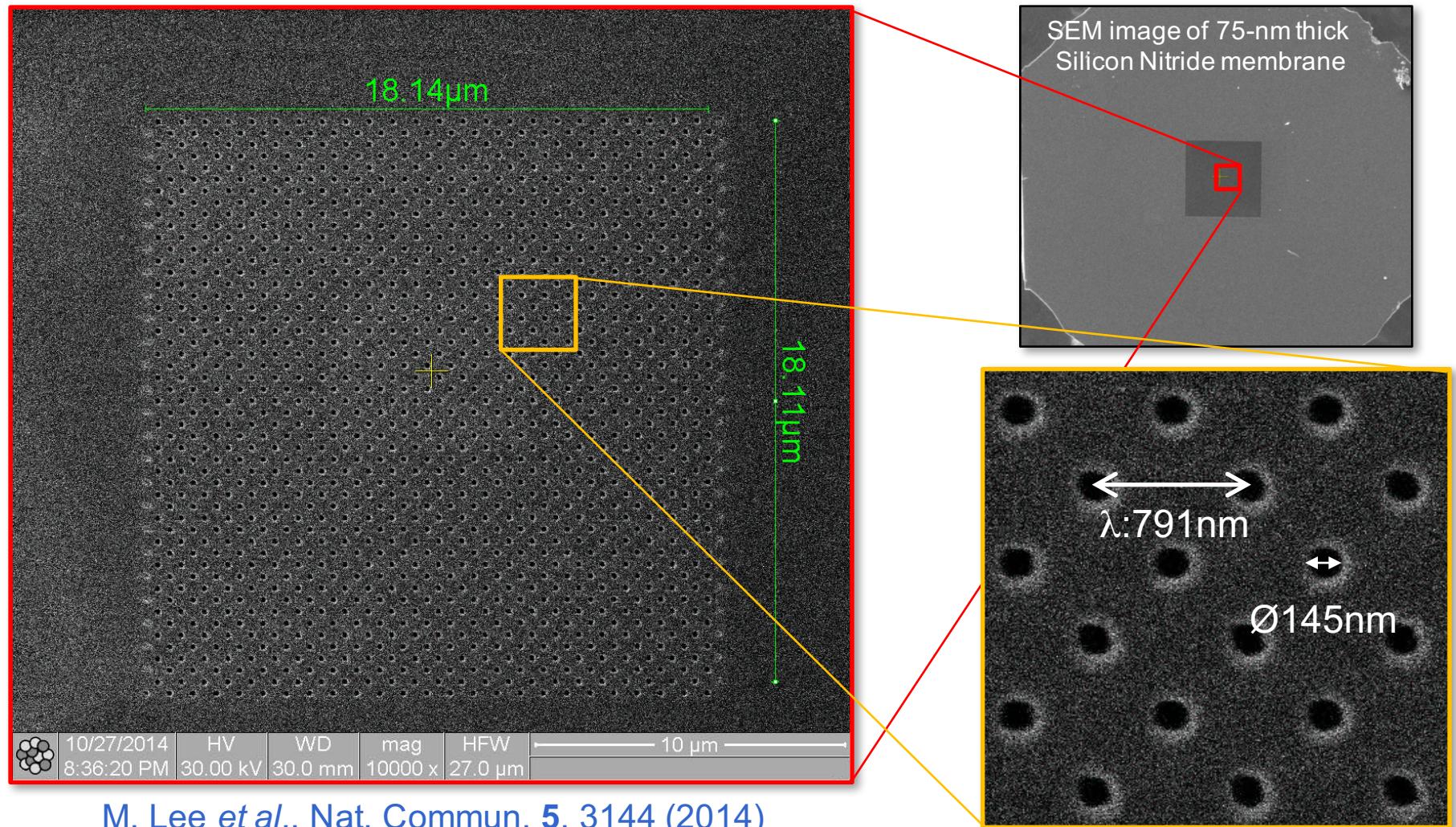


How to realize the same phase



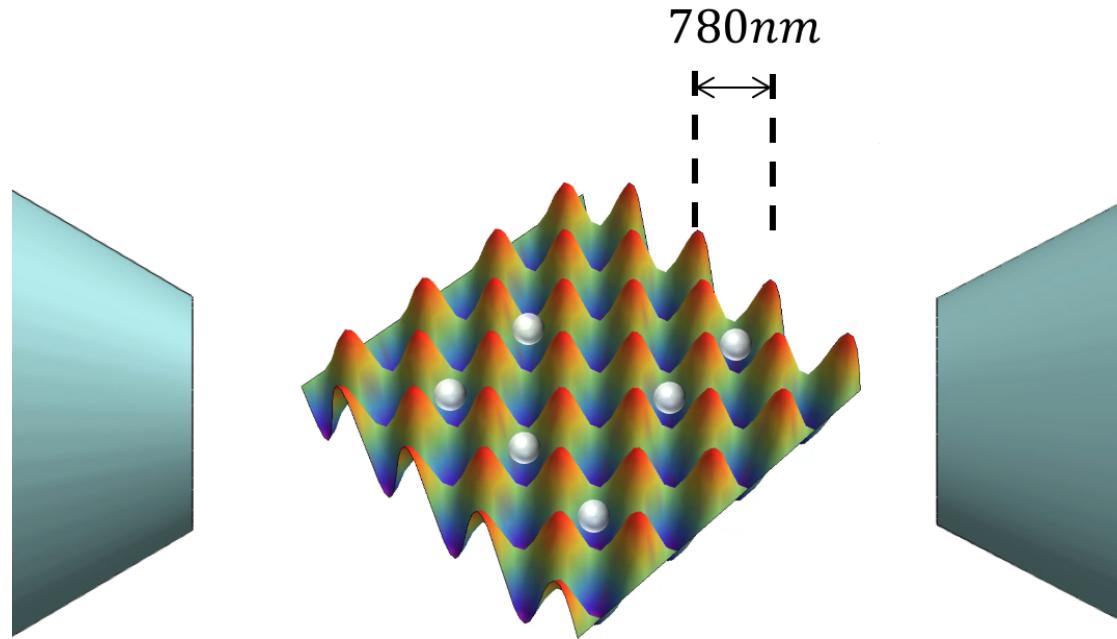
Nanohole array

- Machined by focused ion beam (FIB)



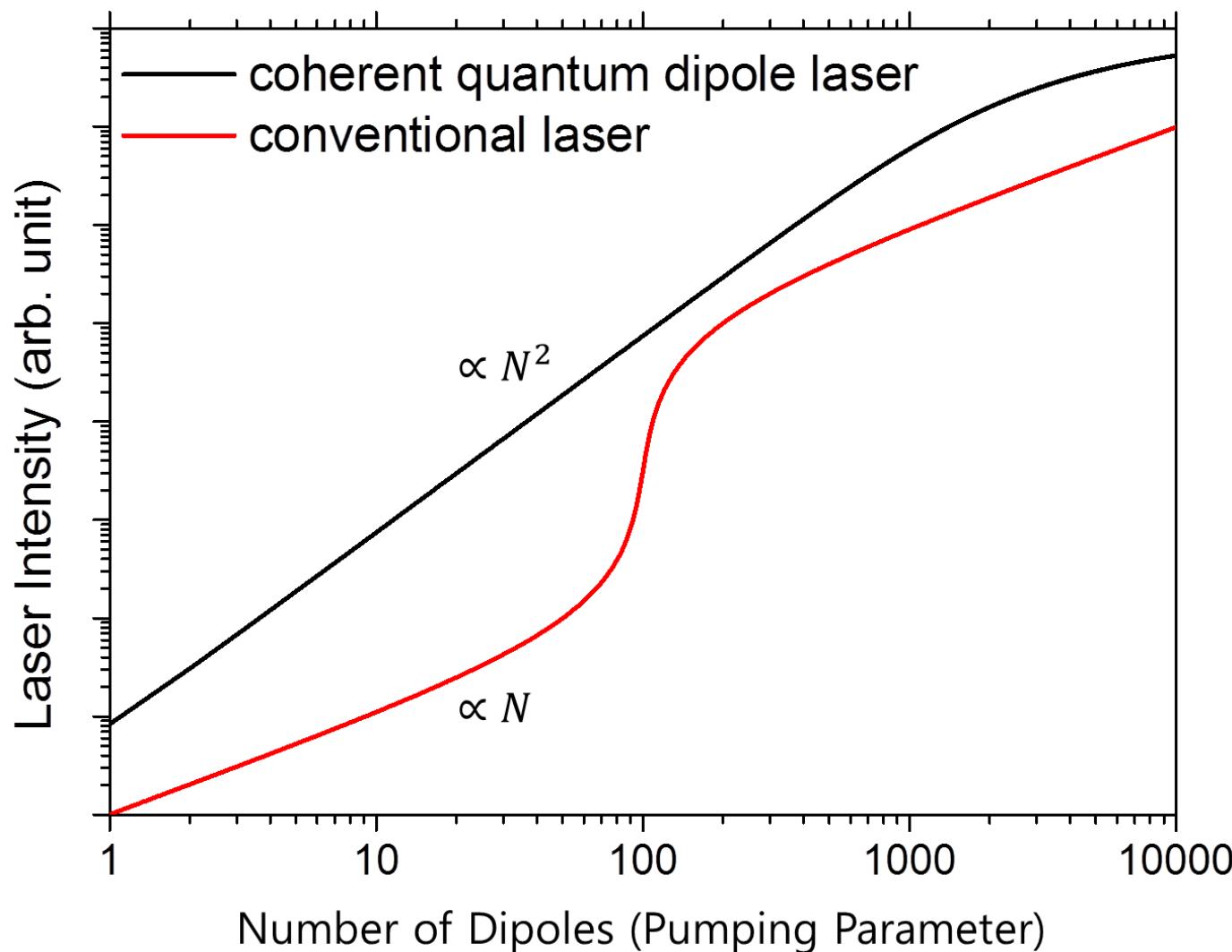
M. Lee et al., Nat. Commun. 5, 3144 (2014)

Stationary quantum dipole materials

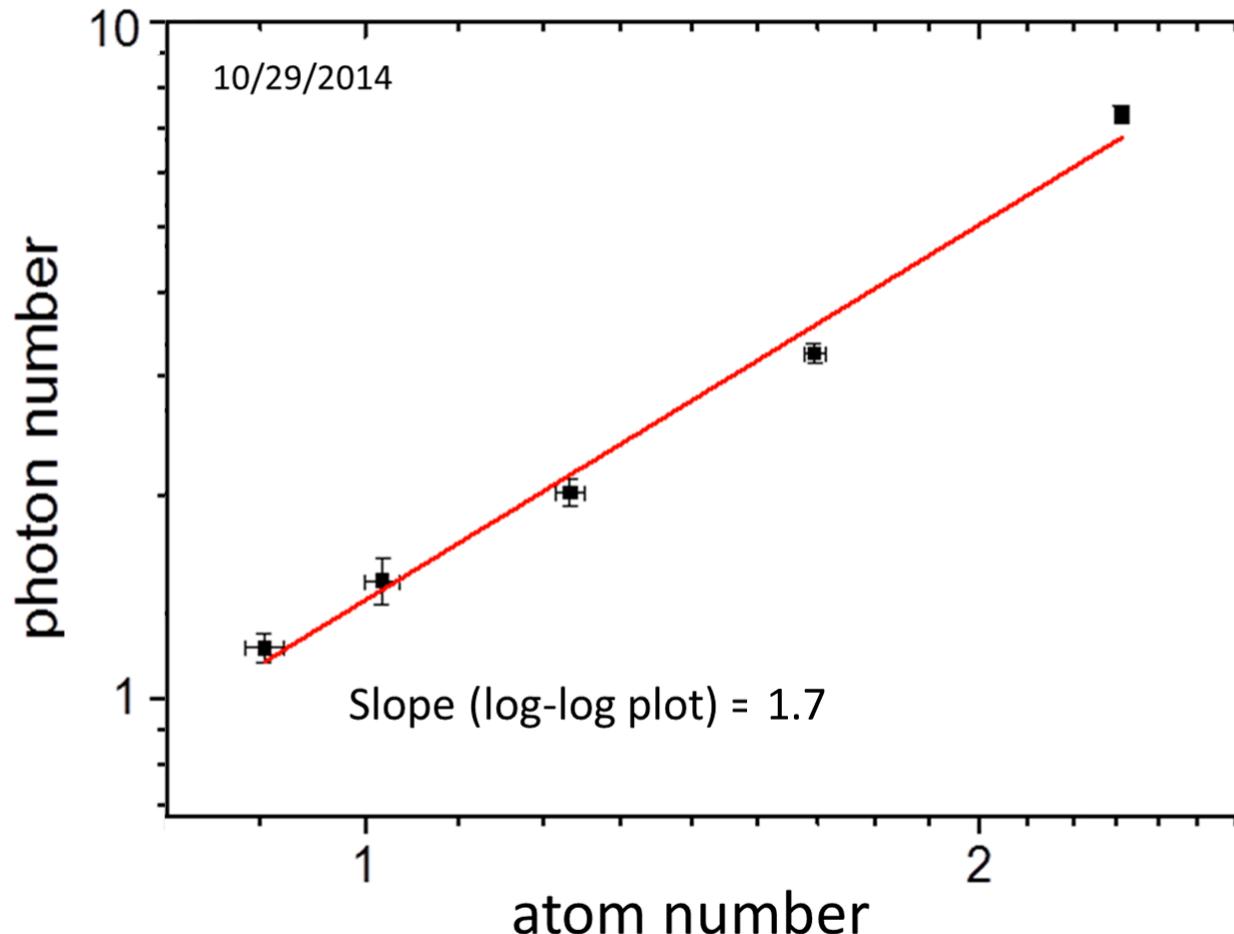


- ^{85}Rb Atoms are confined in a 2D optical lattice (pump in one direction). Along the cavity axis, the lattice spacing equals the Rb wavelength (equiphase to the cavity mode).
- To be used in the microwave single photon detector experiment.

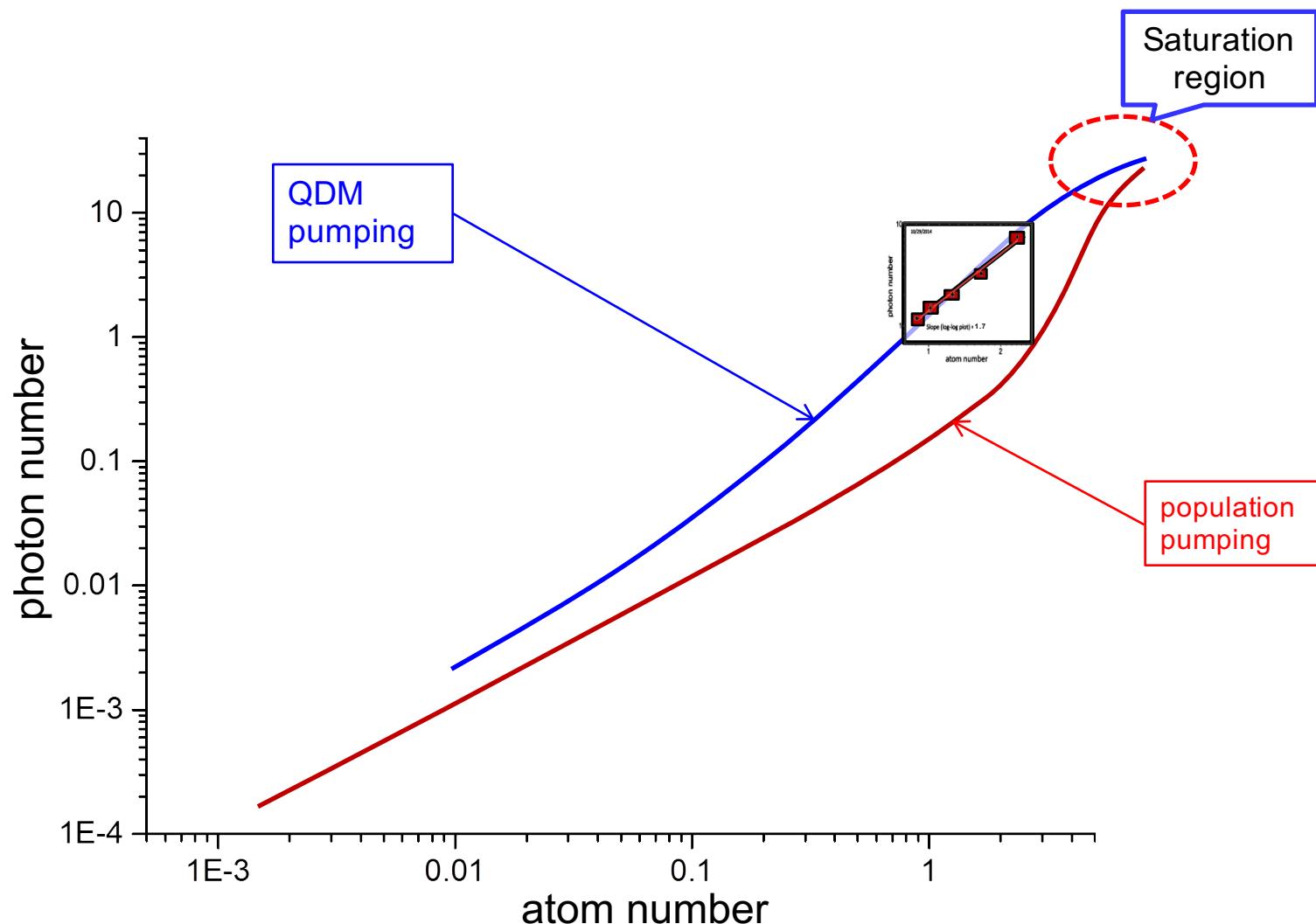
Thresholdless lasing with QDM



Preliminary data of N^2 emission



Preliminary data of N^2 emission



III. Diverging spontaneous emission

- According to our theoretical study, atomic spontaneous emission can *diverge* in a *non-Hermitian* optical system.

- Hermitian Hamiltonian, $H^+ = H$

$$\begin{aligned} 0 &= \langle u_m | H - H | u_n \rangle = \langle u_m | H^+ - H | u_n \rangle \\ &= (E_m - E_n) \langle u_m | u_n \rangle \text{ using } \langle u_m | H^+ = E_m \langle u_m | \end{aligned}$$

$\rightarrow \langle u_m | u_n \rangle = 0$ ($m \neq n$), orthogonality, E_n =real.

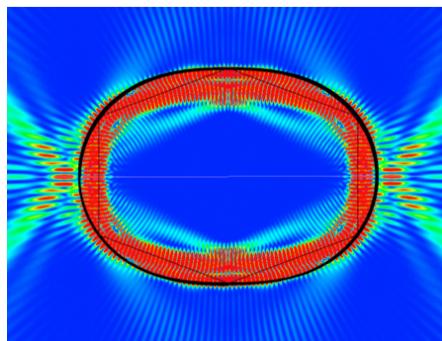
- non-Hermitian, $H^+ \neq H$ (e.g. Energy decays)

$$\begin{aligned} 0 &= \langle \varphi_m | H - H | u_n \rangle \\ &= (E_m - E_n) \langle \varphi_m | u_n \rangle \text{ using } \langle \varphi_m | H = E_m \langle \varphi_m | \text{ adjoint} \\ &\rightarrow \langle \varphi_m | u_n \rangle = 0 \text{ ($m \neq n$)}, \boxed{\text{bi-orthogonality}}, E_n=\text{complex}. \end{aligned}$$

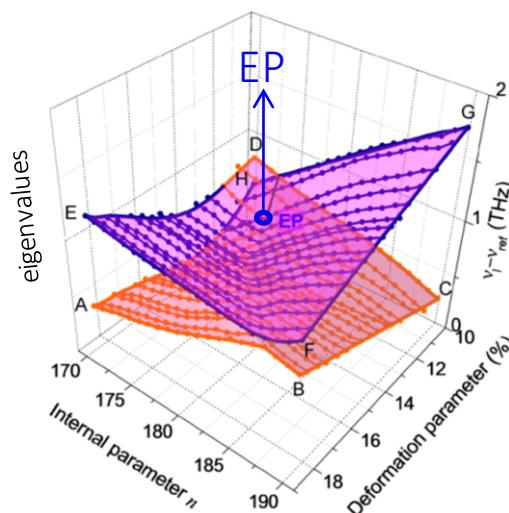
Exceptional Point (EP)

- In a non-Hermitian system (e.g. deformed microcavity), two eigenmodes *coalesce* to a single eigenmode when the intermode coupling equals their differential decay rate ($2g = \gamma_1 - \gamma_2$)
→ exceptional point (EP)

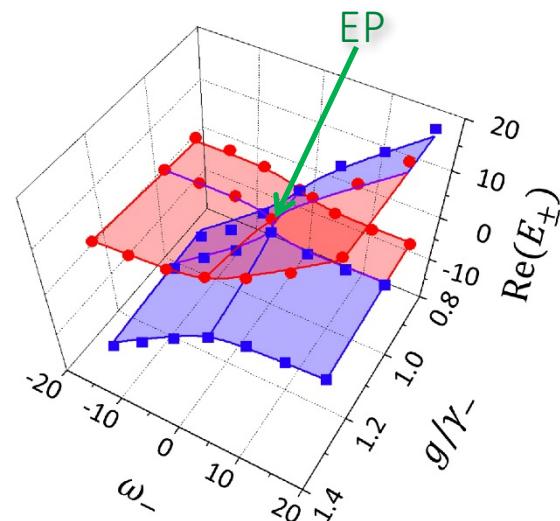
$$H = \begin{bmatrix} \omega - i\gamma_1 & g \\ g & \omega - i\gamma_2 \end{bmatrix}, E_{\pm} = \omega - i\gamma_{+} \pm \sqrt{g^2 - \gamma_{-}^2}, \text{ where } \gamma_{\pm} = |\gamma_1 - \gamma_2|/2$$



Deformed microcavity
S.-B. Lee *et al.*, PRL **88**, 033903 (2002)



Experimental observation of an EP in a deformed microcavity
S.-B. Lee *et al.*, PRL **103**, 134101 (2009)



EP in an atom-cavity quantum composite
Y. Choi *et al.*, PRL **104**, 153601 (2010)

Why Petermann factor diverge at EP

Petermann factor is defined as

$$K_{nn} \equiv \frac{\langle \varphi_n | \varphi_n \rangle \langle u_n | u_n \rangle}{|\langle \varphi_n | u_n \rangle|^2} = \frac{1}{|\langle \varphi_n | u_n \rangle|^2}$$

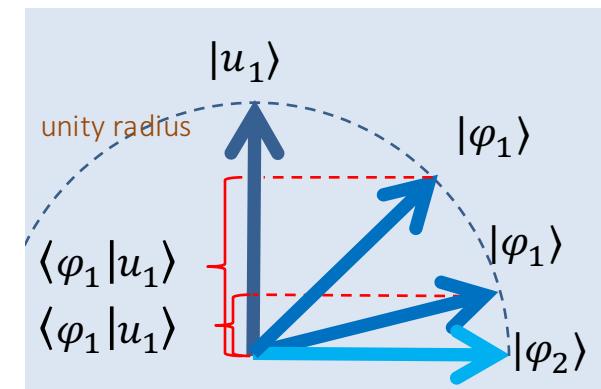
u_n, φ_n normalized

Assume two interacting modes $|u_1\rangle$ and $|u_2\rangle$ coalesce into a single mode $|u_{EP}\rangle$ (at EP):

$$0 = \langle \varphi_1 | u_2 \rangle \rightarrow \langle \varphi_{EP} | u_{EP} \rangle = 0$$

$$\therefore K_{11} = \frac{1}{|\langle \varphi_1 | u_1 \rangle|^2} \rightarrow \frac{1}{|\langle \varphi_{EP} | u_{EP} \rangle|^2} \rightarrow \infty,$$

$$K_{22} = \frac{1}{|\langle \varphi_2 | u_2 \rangle|^2} \rightarrow \frac{1}{|\langle \varphi_{EP} | u_{EP} \rangle|^2} \rightarrow \infty$$



Sum rule of zero-point energy

- Total field energy (with rotating wave approximation)

$$\hat{H} = \int dx \left(\frac{1}{2} \epsilon_0 \hat{E}^2 \times 2 \right)_{\text{time average}} \simeq \sum_{m,n} \hbar \sqrt{\omega_m \omega_n} \left[\hat{a}_m^\dagger \hat{a}_n A_{mn} + \underbrace{\frac{1}{2} K_{nm} A_{mn}}_{\text{zero-point energy}} \right]$$

where $A_{nm} \equiv \langle u_n | u_m \rangle$, $K_{nm} \equiv e^{i(\theta_m - \theta_n)} \sqrt{K_{nn} K_{mm}} A_{mn}$ and $\theta_n = \text{Arg}[\int u_n^2(x) dx]$.

- Zero-point energy is enhanced for diagonal terms, $K_{nn} > 1$
→ can enhance spontaneous emission into n th mode.
- Sum rule $\sum_{n,m} K_{nm} A_{mn} = p$, where p is the total number of cavity modes.
→ total zero point energy is conserved

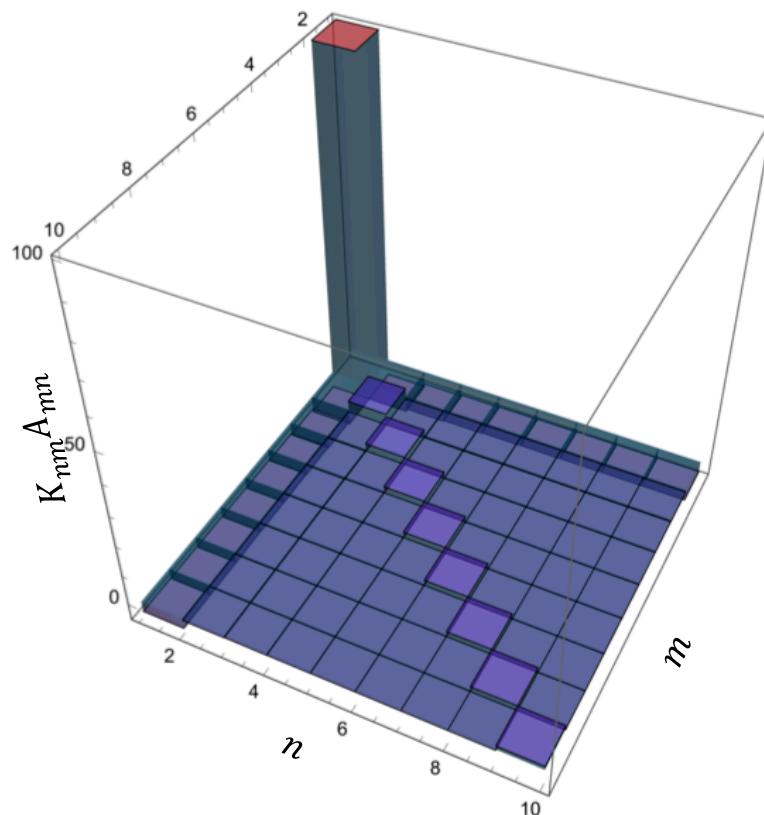
$$\frac{1}{2} \sum_{m,n} \hbar \sqrt{\omega_m \omega_n} K_{nm} A_{mn} \simeq \frac{1}{2} \sum_n \hbar \omega_n$$

→ total spontaneous emission is unchanged.

Simulation

Sum rule: $\sum_{n,m} K_{nm} A_{mn} = p = 10$

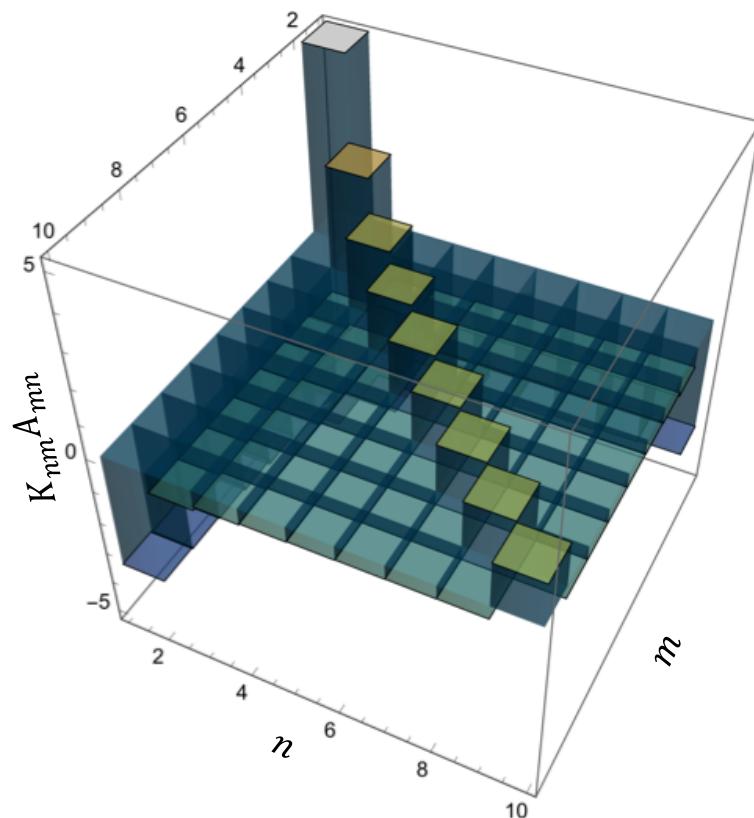
$K_{11} \simeq 100, K_{22} \simeq 3, K_{33} \simeq 2, K_{44} \simeq 2.67, \dots, K_{12}A_{21} \simeq -5.35, K_{13}A_{31} \simeq -0.47$, etc



Simulation

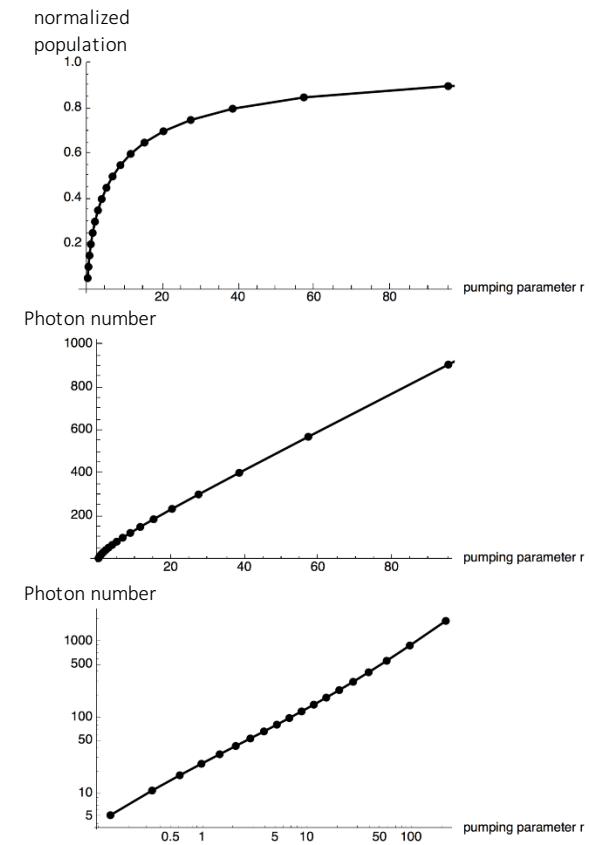
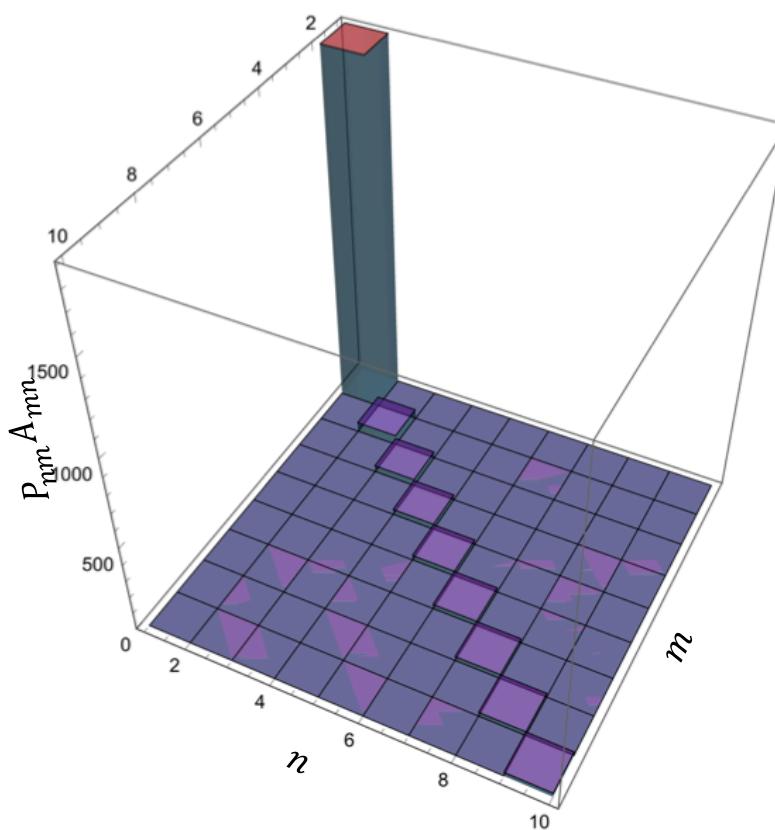
Sum rule: $\sum_{n,m} K_{nm} A_{mn} = p = 10$

$K_{11} \simeq 100, K_{22} \simeq 3, K_{33} \simeq 2, K_{44} \simeq 2.67, \dots, K_{12}A_{21} \simeq -5.35, K_{13}A_{31} \simeq -0.47$, etc



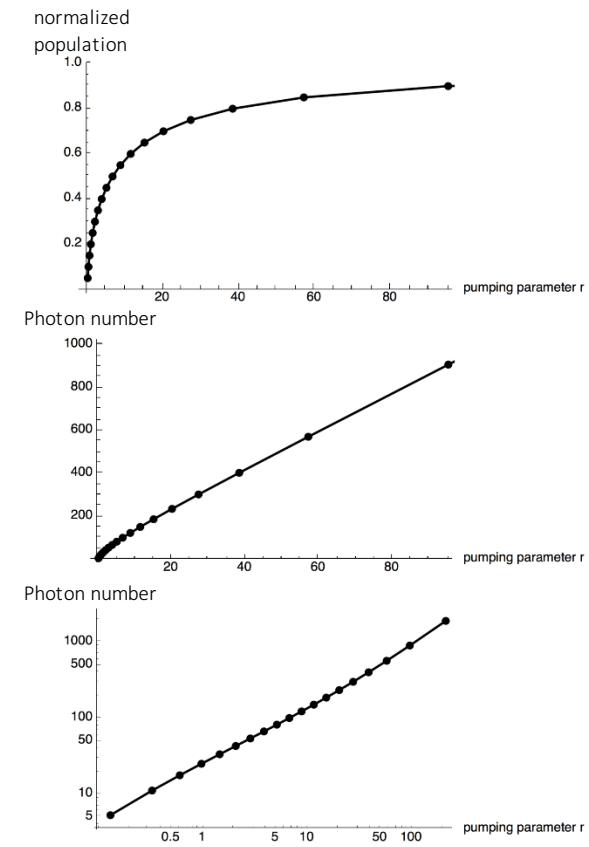
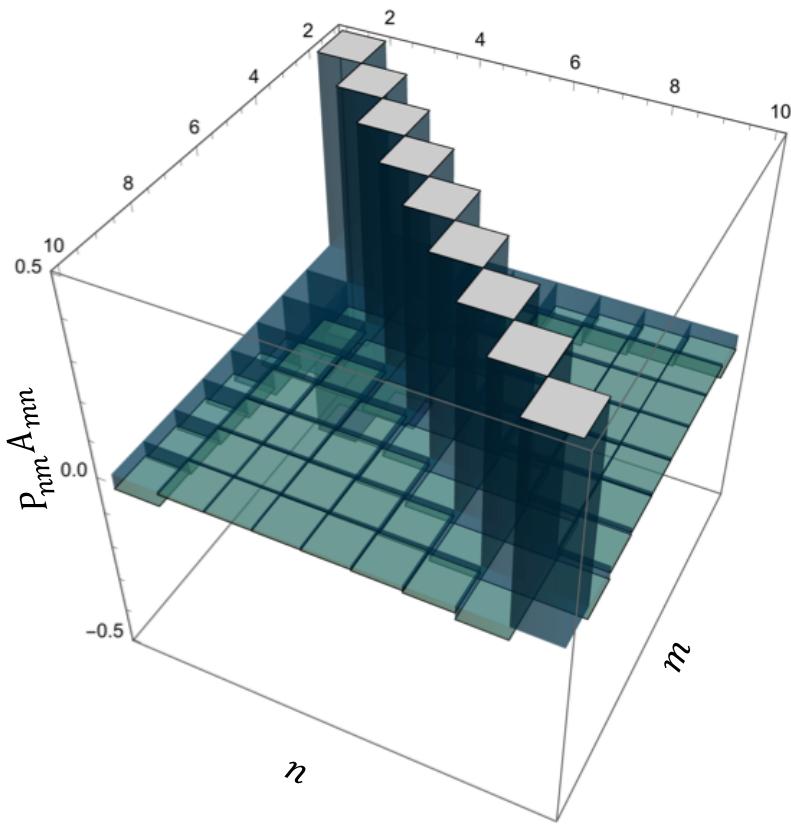
Simulation, near EP lasing

- $P_{11} \simeq 1400$ is the strongest. $P_{12} \simeq -0.5$ because of the large detuning.
- Thresholdless lasing
- Upperbound of $K_{nn} \sim 10^{13}$ (breakdown of dipole approximation)



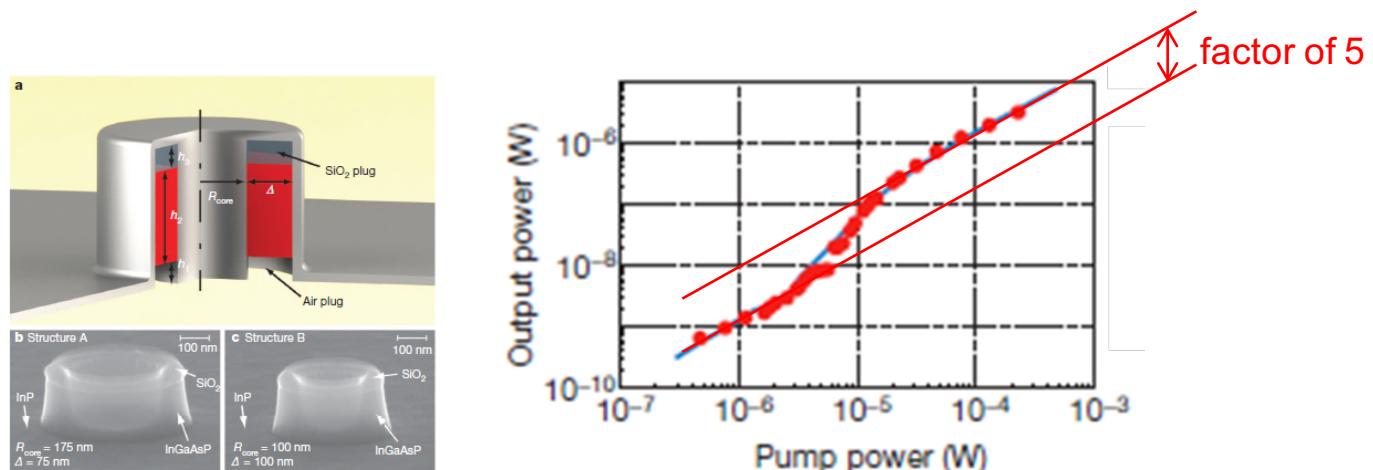
Simulation, near EP lasing

- $P_{11} \simeq 1400$ is the strongest. $P_{12} \simeq -0.5$ because of the large detuning.
- Thresholdless lasing
- Upperbound of $K_{nn} \sim 10^{13}$ (breakdown of dipole approximation)



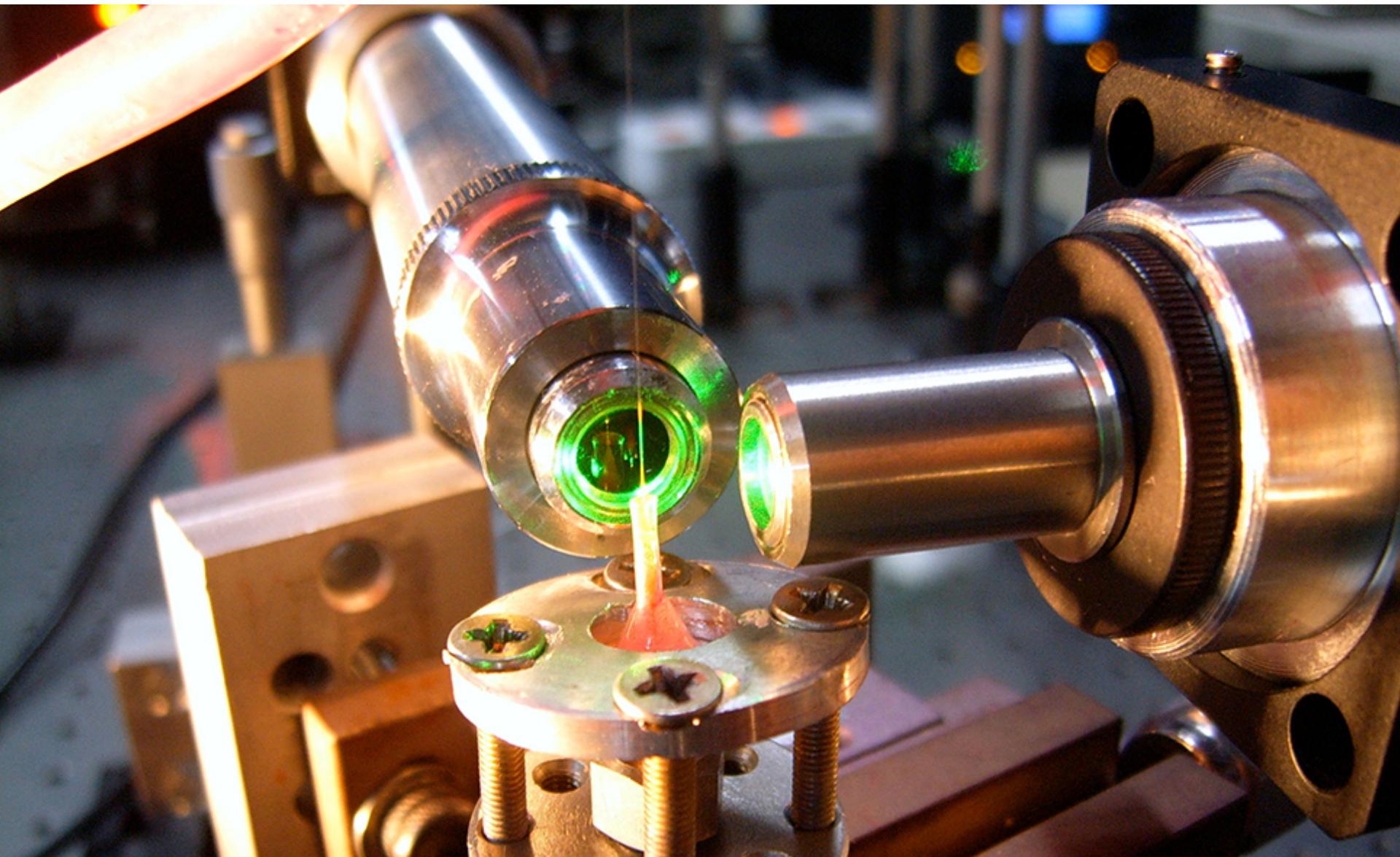
Conventional approach

- All thresholdless lasers are based on the Purcell factor: spontaneous emission enhancement due to a small mode volume and a high Q
- To achieve thresholdless lasing, the mode volume $\rightarrow \lambda^3$
- Relatively low Q \rightarrow high pump density \rightarrow heat dissipation problems, short life time, low temp operation

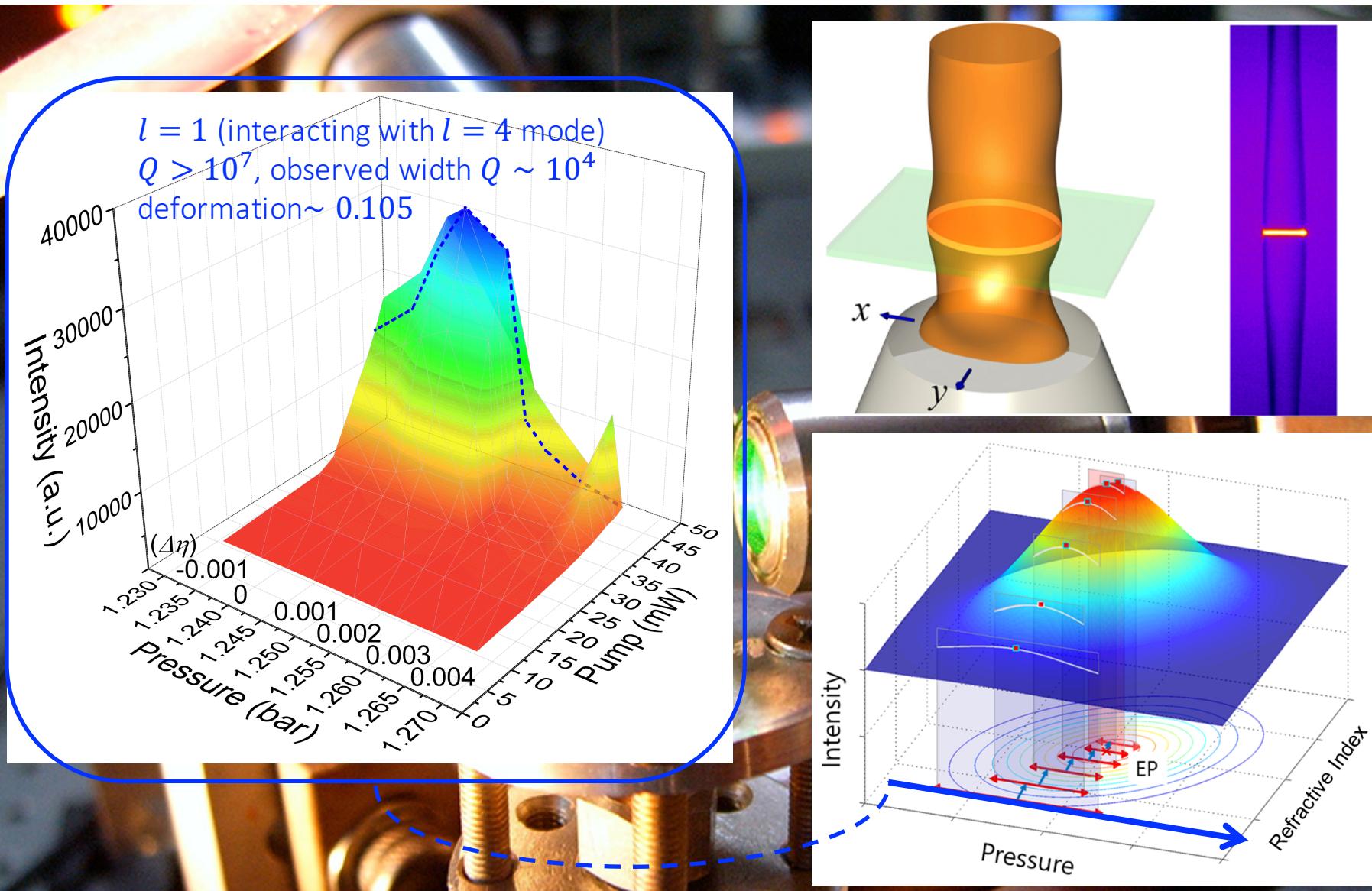


M. Khajavikhan *et al.*, Nature **482**, 204 (2012)

Preliminary experiment

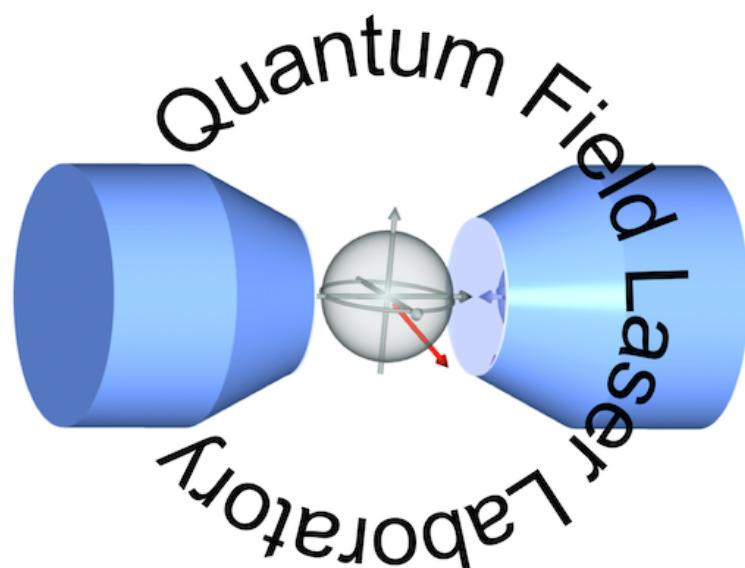


Preliminary experiment



Further information

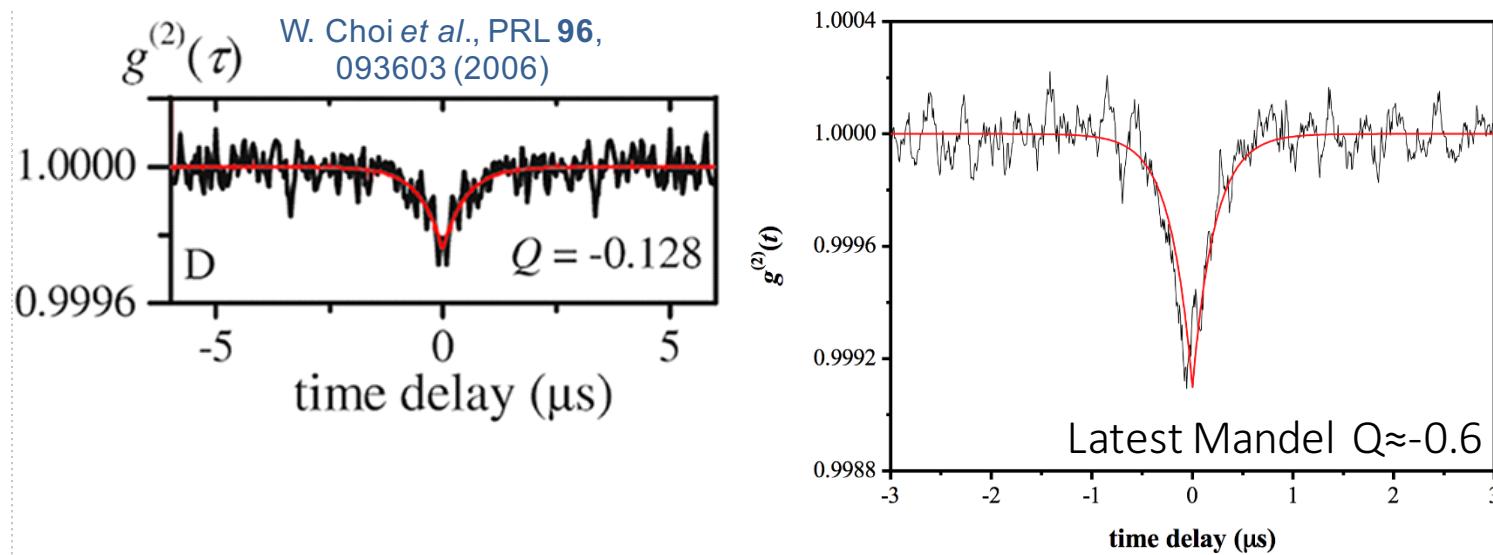
- Visit our homepage, <http://sal.snu.ac.kr>.
- Send e-mail inquiry to kwan@phya.snu.ac.kr or call 8286.
- Drop by my office at 56-324.



SUPPLEMENTARY MATERIALS

Highly sub-Poisson intense light

- Photon number stabilization occurs in the saturation region.
- Theoretical prediction, Mandel $Q \approx -0.7$
 - variance $(\Delta n^2) = 0.3\langle n \rangle$, only 30% of the shot-noise variance.



$$g^{(2)}(t) = 1 + \frac{Q}{\langle n \rangle} e^{-t/\tau}$$

The second order
correlation function

$$Q = \frac{\langle n^2 \rangle - \langle n \rangle^2}{\langle n \rangle} - 1$$

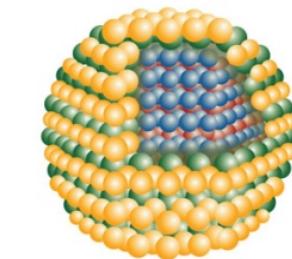
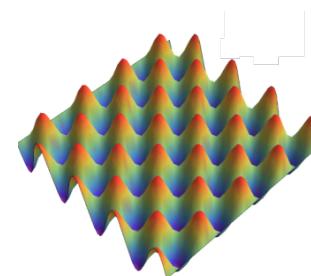
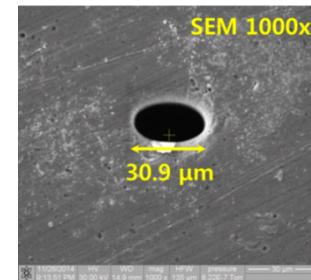
Mandel Q

$Q > 0$ super-Poisson
 $Q = 0$ Poisson
 $Q < 0$ sub-Poisson

photon statistics

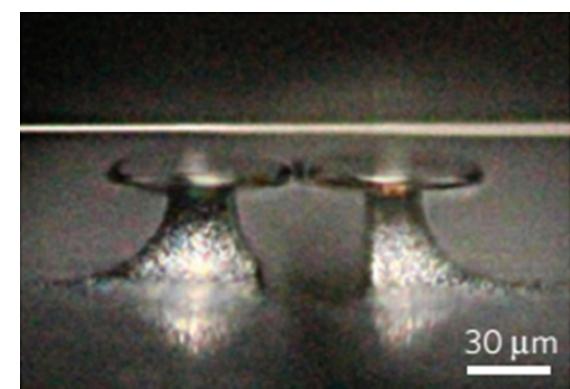
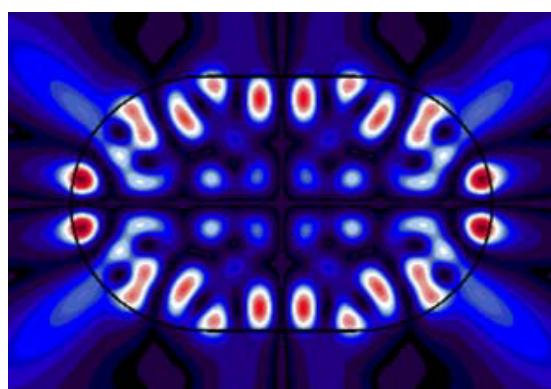
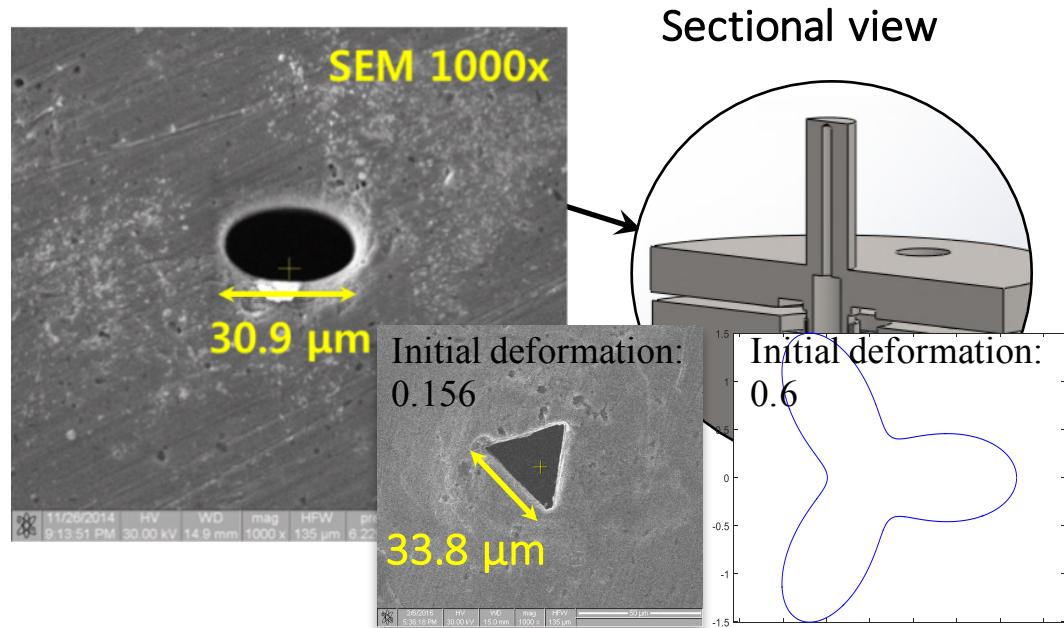
Extension to practical forms

- Develop FIB technique for fabricating various microjet nozzles
- Simulate a stationary QDM by using an optical lattice in a cavity
- Design a thresholdless quantum-field microlaser with artificial atoms (e.g., excitons, polaritons, surface plasmons, etc.)



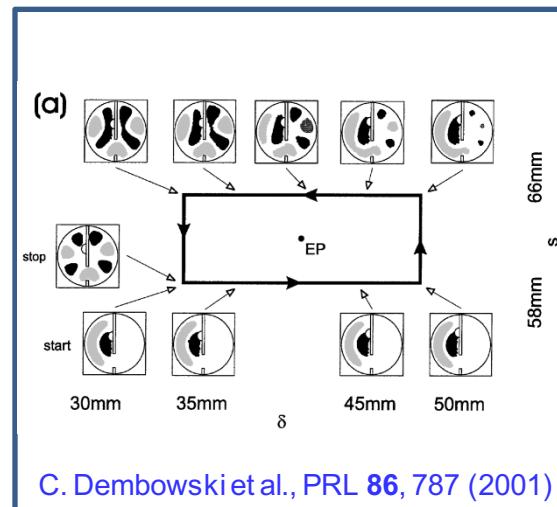
FIB technique for microjet nozzles

- FIB precision: 10nm
- Simulating various cavity shapes & array of cavities
- Compact optofluidic packaging possible

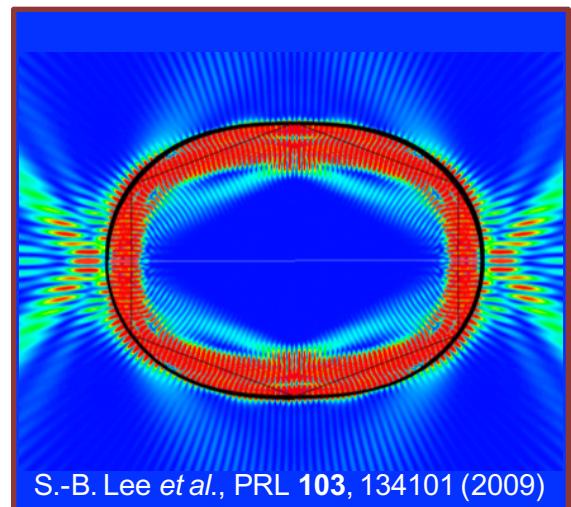


EP in various physical systems

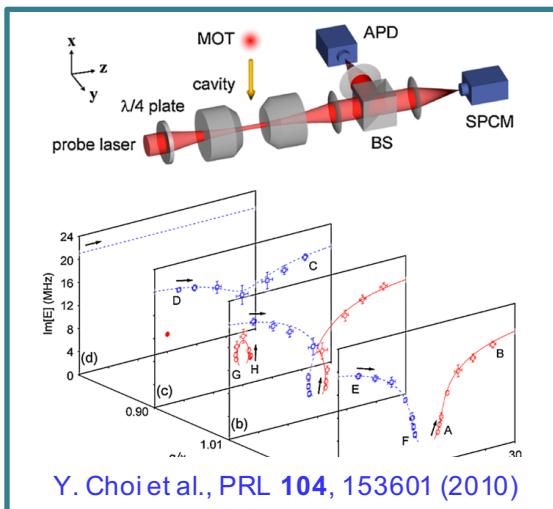
- Various examples of EP
 - ▷ Microwave cavity
 - ▷ Deformed microcavity
 - ▷ Atom-cavity quantum composite (atom-photon)
 - ▷ Coupled disk laser
 - ▷ Exciton-polariton in semiconductor



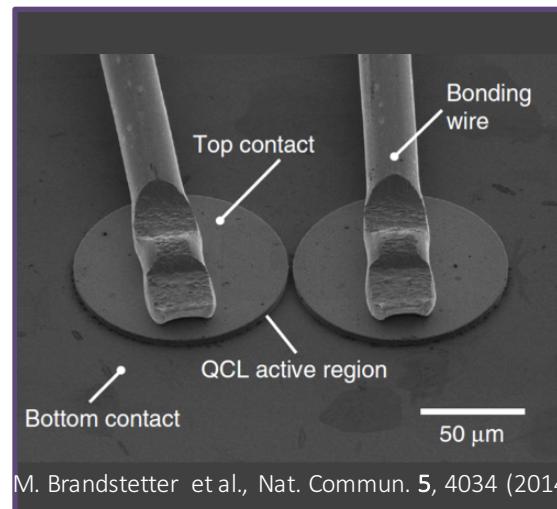
C. Dembowski et al., PRL 86, 787 (2001)



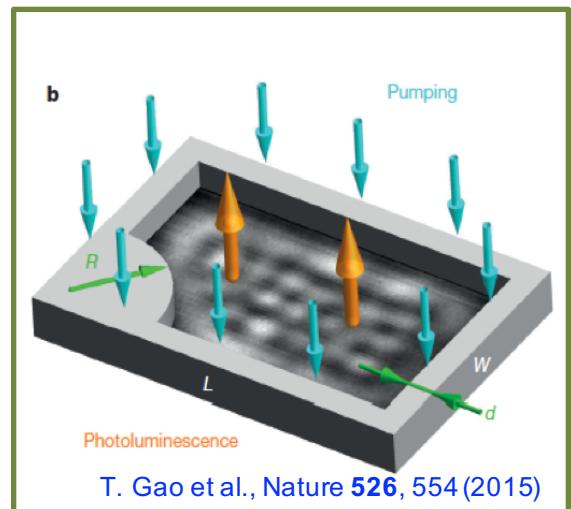
S.-B. Lee et al., PRL 103, 134101 (2009)



Y. Choi et al., PRL 104, 153601 (2010)



M. Brandstetter et al., Nat. Commun. 5, 4034 (2014)



T. Gao et al., Nature 526, 554 (2015)