R Handout: Simulation

This handout will introduce a basic method of simulation. This pdf file and the R program are provided on Blackboard.

- 1. Simulate data from a standard normal distribution
 - (a) Direct simulation
 - R code

```
# Set a seed to make this process repeatable
set.seed(12345)

# Set the number of simulations
n <- 100000

# Simulate data from a standard normal distribution
X <- rnorm(n)</pre>
```

```
# Use histogram to graph the distribution
hist(X, freq = F)
```

2. Simulate data from a contaminated normal distribution. Suppose we have a contaminated normal distribution as section 3.4.1 in the 7th edition. Because $W = ZI_{1-\epsilon} + \sigma_c Z(1-I_{1-\epsilon})$, we have this definition

$$W = XI_{1-\epsilon} + Y(1 - I_{1-\epsilon})$$

where $X \sim N(0,1), Y \sim N(0,\sigma_c^2)$ and $I \sim Bernoulli(1-eps)$

• R code

```
# Set a seed to make this process repeatable
set.seed(12345)
```

```
# Set the number of simulations
n < -100000
# Build a function to simulate a contaminated normal distribution
rctnorm \leftarrow function(n, eps = 0.5, mu = c(0, 0),
sigma = c(1, 1)) {
# Simulate I
I \leftarrow rbinom(n, 1, 1 - eps)
# Simulate X
X \leftarrow rnorm(n, mu[1], sigma[1])
# Simulate Y
Y <- rnorm(n, mu[2], sigma[2])
# Simulate W
W \leftarrow rep(NA, n)
for (i in 1:n) {
W[i] \leftarrow ifelse(I[i] == 1, X[i], Y[i])
}
W
}
# the p.d.f of contaminated normal distribution
dctnorm <- function(x, eps = 0.5, mu = c(0, 0),
sigma = c(1, 1)){
dnorm(x, mu[1], sigma[1]) * (1 - eps) +
dnorm(x, mu[2], sigma[2]) * eps
}
# get a sequence from -100 to 100 having step 0.01
# as the points in x-aixs
x \leftarrow seq(-100, 100, 0.01)
```

```
\# 3.4.26 part b, eps = 0.15, mu1 = mu2 = 0,
\# sigma1 = 1, sigma2 = sigma.c = 10
X1 < - retnorm(n, 0.15, mu = c(0, 0), sigma = c(1, 10))
# Use histogram to graph the distribution
hist (X1, freq = F, main = 'eps = 0.15 and sigma.c = 10'
, ylim = c(0, 0.45))
# graph the p.d.f. of standard normal distribution
# in a red curve
points(x, dnorm(x, 0, 1), type = 'l', col = 'red')
# graph the p.d.f. of normal distribution with mu=0
# and sigma=10 in a blue curve
points(x, dnorm(x, 0, 10), type = 'l', col = 'blue')
# graph the p.d.f. of contanminated normal distribution
\# with eps = 0.15, mu1 = mu2 = 0, sigma1 = 1, sigma 2 = 10
# in a black curve
points(x, dctnorm(x, 0.15, c(0, 0), c(1, 10)), type = '1'
, col = 'black')
# An example when we have 2 normal distribution
# with different locations. eps = 0.5, mu1 = 0,
\# \text{ mu2} = 5, \text{sigma1} = \text{sigma2} = 1
X4 \leftarrow rctnorm(n, 0.5, mu = c(0, 5), sigma = c(1, 1))
hist (X4, freq = F, main = 'eps = 0.5 with different locations
and same sigmas', ylim = c(0, 0.45))
# graph the p.d.f. of standard normal distribution
# in a red curve
points(x, dnorm(x, 0, 1), type = 'l', col = 'red')
# graph the p.d.f. of normal distribution
# with mu = 5 and sigma = 1 in a blue curve
```

```
points(x, dnorm(x, 5, 1), type = 'l', col = 'blue')

# graph the p.d.f. of contaminated normal distribution
# with eps = 0.5, mu1 = 0, mu2 = 5, sigmal = 1
# and sigma2 = 2 in a black curve
points(x, dctnorm(x, 0.5, c(0, 5), c(1, 1)), type = 'l', col = 'black')
15
```

3. Practice: Simulate data from a gamma distribution with $\alpha=2$ and $\beta=5$. (You will need to use rgamma and help(rgamma) in R)