

# Solving the Dial-a-Ride Problem with the Firefly Metaheuristic

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# Introduction & Motivation

- The DARP: A vehicle routing problem characterized by
  - User-orientation
  - Small vehicles, like vans, shared by users
  - Flexible routes and schedules
- In Germany: (An-)Rufbus or Taxibus. In Switzerland: Publicar
- Example of application: Patients of hemodialysis
- Their need: Door-to-door transport from home to the hospital

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- Example of application: Patients of hemodialysis
- Their need: Door-to-door transport from home to the hospital
- **Motivations:**
  - Improvement of urban mobility and public transportation
  - Reduction of costs for people who need this kind of transport

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# Approach & Contribution

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- Subject to a set of constraints that guarantee comfort
- We proceed with 2 approaches:
  - Exact approach with a generic solver
  - Near-optimal approach with the implementation of a metaheuristic
- Our contribution:
  - Comparison of the generic solver with the metaheuristic
  - Application of swarm intelligence to the DARP
  - New way to represent the solution

# The Dial-a-Ride Problem (DARP)

- The DARP is a vehicle routing problem, proven to be  $\mathcal{NP}$ -hard
- It “extends” the *Pickup and Deliver Vehicle Routing Problem* and the *Vehicle Routing Problem with Time Windows*



# The Dial-a-Ride Problem (DARP)

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- It “extends” the *Pickup and Deliver Vehicle Routing Problem* and the *Vehicle Routing Problem with Time Windows*
- There is a fleet of **homogeneous vehicles** with a **unique depot**
- Set of transport requests from passengers, known beforehand (**static** version)
- Maximal vehicle route duration and vehicle capacity
- Maximal user ride time

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- The costs and time are assumed to be the *Cartesian distance* between the locations

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**Optimal Solution:** Feasible solution whose total duration time is less than or equal to any other feasible solution's total duration time

# Exact Approach

- **Integer Linear Programming**
- Method commonly used in mathematics and operations research
- Represent the problem in a mathematical language (e.g. *AMPL*)
- Solve via generic solver (e.g. *GNU Linear Programming Kit*)
- Algorithms behind it: *Simplex, branch and bound, cutting plane*



# Near-optimal Approach

- Implement a metaheuristic named **Firefly Algorithm (FA)**
- Other examples: *Simulated annealing, genetic algorithms*
- The FA is nature-inspired and applies the concept of swarm intelligence
- Similar to: *Ant colony, particle swarm optimization*

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- Other examples: *Simulated annealing, genetic algorithms*
- The FA is nature-inspired and applies the concept of swarm intelligence
- Similar to: *Ant colony, particle swarm optimization*
- Represent the position of a firefly as a vector
- Represent a solution as a firefly (i.e. the vector of its position)

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- The attractiveness of a firefly  $\mathbf{x}$  to another one  $\mathbf{y}$  is directly proportional to the brightness of  $\mathbf{y}$  and inversely proportional to the distance between them
- **Result:** Ideally, there will be a convergence of fireflies to the optimum

# Solution Representation

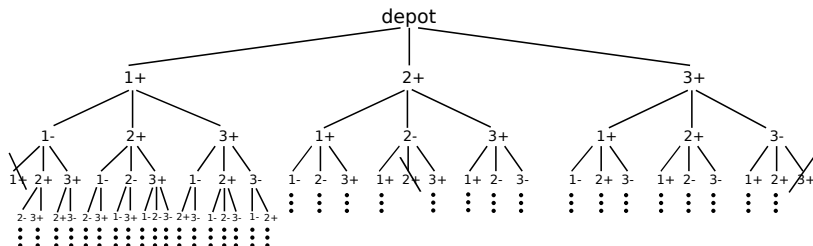
- $\mathbf{v} = (v_1, v_2, \dots, v_{k+1})$ , where  $v_1, v_2, \dots, v_{k+1} \in \mathbb{N}_{\geq 0}$  and  $k$  is the number of vehicles
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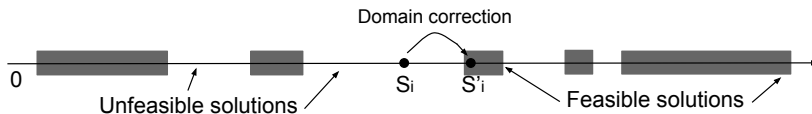
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- Initial solution easily generated, simply random numbers in an interval
- A value in  $v_1$  represents a unique assignment from requests to vehicles, it may vary between 0 and  $k^n$ , where  $n$  is the number of requests

- The values in  $v_2, \dots, v_{k+1}$  represent each vehicle's routes, analogously to  $v_1$
- The possible arrangement of the requests can be seen as a tree



# Correction of Unfeasibility

- Time constraints cause unfeasibility of solutions
- Fireflies in these unfeasible regions should be moved into a feasible one
- Constraint satisfaction problem + Arc Consistency #3



# Generic Solver vs. Metaheuristic

- CPU: Intel Xeon 2.3 GHz 64bits, 15GB of RAM, Linux OS
- Generic solver: GNU Linear Programming Kit.
- Metaheuristic implemented in Python with SciPy
- Instances created from an instance of the literature

# Generic Solver vs. Metaheuristic

- Solution through GLPK is impracticable. Exponential growth of time
- Firefly implementation shows a steady growth of CPU time

**Table:** Results of the first evaluation

Inst.	Req.	Opt.	CPU-GLPK	Firefly Sol.	% Opt.	CPU-Firefly
Test-1	2	58.05	0.1	69.75	83.2%	7.4
Test-2	4	68.10	0.9	98.51	69.1%	11.7
Test-3	5	76.27	2.0	134.29	56.8%	2.5
Test-4	6	96.54	45.0	149.32	64.6%	3.3
Test-5	8	-	-	158.67	-	5.7

# Metaheuristic with Literature Instances

- 24 instance from the literature
- Smaller instances: 90% of optimality in average
- Deviation to the initial solution varies considerably

**Table:** Results of the second evaluation — Quality and progress

Instance	Optimum	Final Sol.	Optimality	Initial Sol.	Dev. to Initial Sol.
a2-16	294.25	312.96	94.02%	335.85	6.81%
a2-20	344.83	373.89	92.23%	427.48	12.54%
a2-24	431.12	442.85	97.35%	496.92	10.88%
a3-18	300.48	347.10	86.57%	374.20	7.24%
a3-24	344.83	409.73	84.16%	456.86	10.32%
a3-30	494.85	614.13	80.58%	615.99	0.30%
a3-36	583.19	-	-	-	-
a4-16	282.68	310.84	90.94%	354.54	12.33%

# Metaheuristic with Literature Instances

## ■ Optimality sinks as instance sizes rise

**Table:** Results of the second evaluation – Quality and progress

Instance	Optimum	Final Sol.	Optimality	Initial Sol.	Dev. to Initial Sol.
a4-24	375.02	481.16	77.94%	567.63	15.23%
a4-32	485.50	639.73	75.89%	665.27	3.84%
a4-40	557.69	780.13	71.49%	841.92	7.34%
a4-48	668.82	956.90	69.89%	1032.38	7.31%
a5-40	498.41	779.32	63.95%	818.14	4.74%
a5-50	686.62	926.23	74.13%	1018.84	9.09%
a5-60	808.42	1195.94	67.60%	1257.38	4.89%
a6-48	604.12	993.08	60.83%	1025.55	3.17%

# Metaheuristic with Literature Instances

- Comparison of CPU times to another two approaches
- $CPU^1$ : Parragh (2011).  $CPU^2$ : Parragh and Schmid (2013).

Table: Results of the second evaluation – Running time

Instance	$CPU^1$	$CPU^2$	CPU-Firefly
a2-16	68.2	0.12	<b>63.3</b>
a2-20	133.8	0.28	160.5
a2-24	187.8	0.35	419.3
a3-18	45.4	-	<b>29.5</b>
a3-24	86.8	0.29	<b>77.4</b>
a3-30	105.6	0.50	151.2
a3-36	162.6	0.83	370.6
a4-16	26.0	-	<b>14.5</b>
a4-24	50.8	-	<b>37.0</b>
a4-32	86.0	0.55	129.4
a4-40	130.6	0.78	233.5
a4-48	253.8	1.62	<b>222.3</b>



# Conclusion

- Solution via generic solver is impracticable
- Solution via FA can solve much larger instances, though not the largest ones
- Main issue: The time constraints (time windows and ride time)
- How to overcome: Rethink solution representation, for example
- Improve efficiency: Reduce domain corrections and improve transformation functions

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Thank you for your attention  
Questions...