# Solving the Dial-a-Ride Problem with the Firefly Metaheuristic

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#### Contents

- 1 Introduction
  - Overview
  - Definition
- 2 Development
  - Theoretical Framework
  - Designing the Firefly Metaheuristic
- 3 Conclusion
  - Evaluation
  - Conclusion

#### Introduction & Motivation

- The DARP: A vehicle routing problem characterized by
  - User-orientation
  - Small vehicles, like vans, shared by users
  - Flexible routes and schedules
- In Germany: (An-)Rufbus or Taxibus. In Switzerland: Publicar
- Example of application: Patients of hemodialysis
- Their need: Door-to-door transport from home to the hospital

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- Example of application: Patients of hemodialysis
- Their need: Door-to-door transport from home to the hospital
- Motivations:
  - Improvement of urban mobility and public transportation
  - Reduction of costs for people who need this kind of transport

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# Approach & Contribution

- Problem of optimization of the operation costs
- Subject to a set of constraints that guarantee comfort
- We proceed with 2 approaches:
  - Exact approach with a generic solver
  - Near-optimal approach with the implementation of a metaheuristic
- Our contribution:
  - Comparison of the generic solver with the metaheuristic
  - Application of swarm intelligence to the DARP
  - New way to represent the solution

# The Dial-a-Ride Problem (DARP)

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- It "extends" the Pickup and Deliver Vehicle Routing Problem and the Vehicle Routing Problem with Time Windows

### The Dial-a-Ride Problem (DARP)

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- It "extends" the Pickup and Deliver Vehicle Routing Problem and the Vehicle Routing Problem with Time Windows
- There is a fleet of homogeneous vehicles with a unique depot
- Set of transport requests from passengers, known beforehand (static version)
- Maximal vehicle route duration and vehicle capacity
- Maximal user ride time

- Pick-up and drop-off locations (ordered pairs)
- Time windows for the pick-up and for the drop-off
- Time necessary for boarding or alighting
- Quantity of passengers

### Request Characteristics

- Pick-up and drop-off locations (ordered pairs)
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  - V is the set with every location of every request
  - A is the set of edges that tell the travel costs and travel times between any pair of locations
- The costs and time are assumed to be the Euclidean distance between the locations

Definition

# Definition (Route)

The order of the locations through which a vehicle travels. It always starts and ends at the depot.

#### Goal

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#### Definition (Feasible Solution)

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**Optimal Solution:** Feasible solution whose total duration time is less than or equal to any other feasible solution's total duration time

# Exact Approach

- Integer Linear Programming
- Method commonly used in mathematics and operations research
- Represent the problem in a mathematical language (e.g. AMPL)
- Solve via generic solver (e.g. GNU Linear Programming Kit)
- Algorithms behind it: Simplex, branch and bound, cutting plane

- Implement a metaheuristic named Firefly Algorithm (FA)
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- Other examples: Simulated annealing, genetic algorithms
- The FA is nature-inspired and applies the concept of swarm intelligence
- Similar to: Ant colony, particle swarm optimization
- Represent the position of a firefly as a vector
- Represent a solution as a firefly (i.e. the vector of its position)

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- The better the solution represented by a firefly, the brighter is its emitted light
- The attractiveness of a firefly **x** to another one **y** is directly proportional to the brightness of **y** and inversely proportional to the distance between them
- Result: Ideally, there will be a convergence of fireflies to the optimum

# Solution Representation

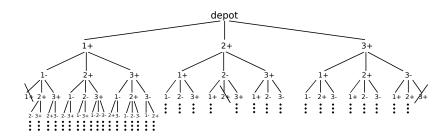
- $\mathbf{v} = (v_1, v_2, ..., v_{k+1})$ , where  $v_1, v_2, ..., v_{k+1} \in \mathbb{N}_{\geq 0}$  and k is the number of vehicles
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- Initial solution easily generated, simply random numbers in an interval
- A value in  $v_1$  represents a unique assignment from requests to vehicles, it may vary between 0 and  $k^n$ , where n is the number of requests

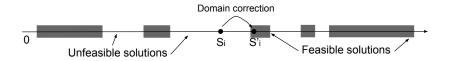
# Solution Representation

- The values in  $v_2, ..., v_{k+1}$  represent each vehicle's routes, analogously to  $v_1$
- The possible arrangement of the requests can be seen as a tree



# Correction of Unfeasibility

- Time constraints cause unfeasibilty of solutions
- Fireflies in these unfeasible regions should be moved into a feasible one
- Constraint satisfaction problem + Arc Consistency #3



#### Generic Solver vs. Metaheristic

- CPU: Intel Xeon 2.3 GHz 64bits, 15GB of RAM, Linux OS
- Generic solver: GNU Linear Programming Kit.
- Metaheuristic implemented in Python with SciPy
- Instances created from an instance of the literature

#### Generic Solver vs. Metaheristic

- Solution through GLPK is impracticable. Exponential growth of time
- Firefly implementation shows a steady growth of CPU time

Table: Results of the first evaluation

| Inst.  | Req. | Opt.  | CPU-GLPK | Firefly Sol. | % Opt. | CPU-Firefly |
|--------|------|-------|----------|--------------|--------|-------------|
| Test-1 | 2    | 58.05 | 0.1      | 69.75        | 83.2%  | 7.4         |
| Test-2 | 4    | 68.10 | 0.9      | 98.51        | 69.1%  | 11.7        |
| Test-3 | 5    | 76.27 | 2.0      | 134.29       | 56.8%  | 2.5         |
| Test-4 | 6    | 96.54 | 45.0     | 149.32       | 64.6%  | 3.3         |
| Test-5 | 8    | -     | -        | 158.67       | -      | 5.7         |

#### Metaheristic with Literature Instances

- 24 instance from the literature
- Smaller instances: 90% of optimality in average
- Deviation to the initial solution varies considerably

Table: Results of the second evaluation — Quality and progress

| Instance | Optimum | Final Sol. | Optimality | Initial Sol. | Dev. to Initial Sol. |
|----------|---------|------------|------------|--------------|----------------------|
| a2-16    | 294.25  | 312.96     | 94.02%     | 335.85       | 6.81%                |
| a2-20    | 344.83  | 373.89     | 92.23%     | 427.48       | 12.54%               |
| a2-24    | 431.12  | 442.85     | 97.35%     | 496.92       | 10.88%               |
| a3-18    | 300.48  | 347.10     | 86.57%     | 374.20       | 7.24%                |
| a3-24    | 344.83  | 409.73     | 84.16%     | 456.86       | 10.32%               |
| a3-30    | 494.85  | 614.13     | 80.58%     | 615.99       | 0.30%                |
| a3-36    | 583.19  | _          | -          | -            | -                    |
| a4-16    | 282.68  | 310.84     | 90.94%     | 354.54       | 12.33%               |

#### Metaheristic with Literature Instances

Optimality sinks as instance sizes rise

Table: Results of the second evaluation — Quality and progress

| Instance | Optimum | Final Sol. | Optimality | Initial Sol. | Dev. to Initial Sol. |
|----------|---------|------------|------------|--------------|----------------------|
| a4-24    | 375.02  | 481.16     | 77.94%     | 567.63       | 15.23%               |
| a4-32    | 485.50  | 639.73     | 75.89%     | 665.27       | 3.84%                |
| a4-40    | 557.69  | 780.13     | 71.49%     | 841.92       | 7.34%                |
| a4-48    | 668.82  | 956.90     | 69.89%     | 1032.38      | 7.31%                |
| a5-40    | 498.41  | 779.32     | 63.95%     | 818.14       | 4.74%                |
| a5-50    | 686.62  | 926.23     | 74.13%     | 1018.84      | 9.09%                |
| a5-60    | 808.42  | 1195.94    | 67.60%     | 1257.38      | 4.89%                |
| a6-48    | 604.12  | 993.08     | 60.83%     | 1025.55      | 3.17%                |

#### Metaheristic with Literature Instances

- Comparison of CPU times to another two approaches
- CPU<sup>1</sup>: Parragh (2011). CPU<sup>2</sup>: Parragh and Schmid (2013).

Table: Results of the second evaluation — Running time

| Instance | CPU <sup>1</sup> | CPU <sup>2</sup> | CPU-Firefly |  |
|----------|------------------|------------------|-------------|--|
| a2-16    | 68.2             | 0.12             | 63.3        |  |
| a2-20    | 133.8            | 0.28             | 160.5       |  |
| a2-24    | 187.8            | 0.35             | 419.3       |  |
| a3-18    | 45.4             | -                | 29.5        |  |
| a3-24    | 86.8             | 0.29             | 77.4        |  |
| a3-30    | 105.6            | 0.50             | 151.2       |  |
| a3-36    | 162.6            | 0.83             | 370.6       |  |
| a4-16    | 26.0             | -                | 14.5        |  |
| a4-24    | 50.8             | -                | 37.0        |  |
| a4-32    | 86.0             | 0.55             | 129.4       |  |
| a4-40    | 130.6            | 0.78             | 233.5       |  |
| a4-48    | 253.8            | 1.62             | 222.3       |  |

#### Conclusion

- Solution via generic solver is impracticable
- Solution via FA can solve much larger instances, though not the largest ones
- Main issue: The time constraints (time windows and ride time)
- How to overcome: Rethink solution representation, for example
- Improve efficiency: Reduce domain corrections and improve transformation functions

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# Thank you for your attention Questions...