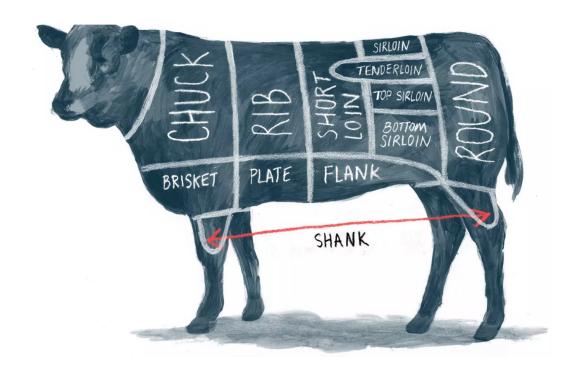


04835370 人工智能芯片设计导论 Fall 2023 Deep Learning Basics

燕博南

计算机工程中常用的深度学习算法基础





- Fully
- Convolution
- 其它算子
- Residual Network
- Depthwise Separable
- •

以"用"的角度去学

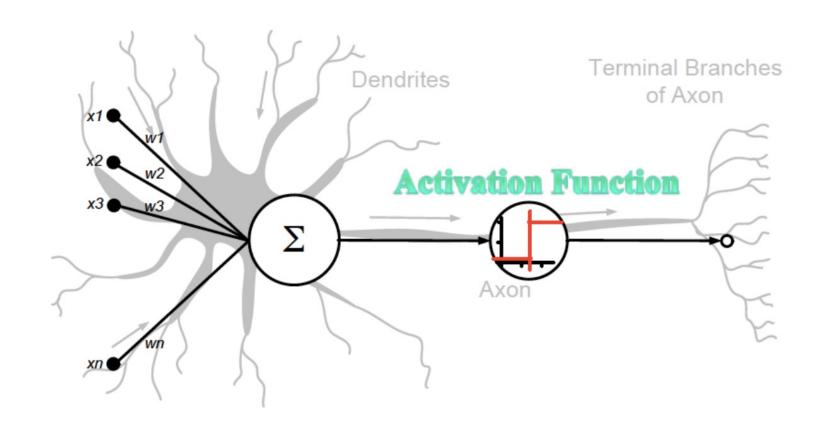


Neural Networks



Human brain is made up of >100 billion neurons

- Neurons receive electric signals at the dendrites and send them to the axon
- Dendrites can perform complex **non-linear** computations
- Synapses are not a single weight but a **complex** non-linear dynamical system



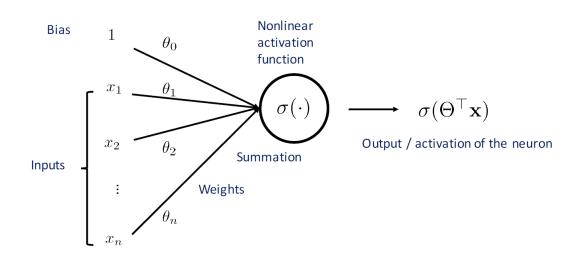


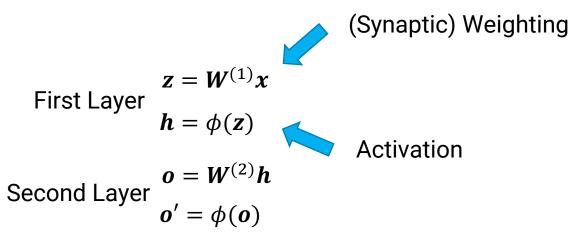
Artificial Neural Networks to Deep Neural Networks



Artificial neural networks

• A **simplified** version of biological neural network





Forward propagation in inference 推理

主要的计算量: 乘加 (multiply-accumulate, MAC)



Deep Learning



Forward propagation:



(Synaptic) Weighting

$$z = W^{(1)}x$$
 First Layer

$$h = \phi(z)$$



Activation

Second Layer
$$egin{aligned} oldsymbol{o} &= oldsymbol{W}^{(2)} oldsymbol{h} \ oldsymbol{o}' &= \phi(oldsymbol{o}) \end{aligned}$$

$$o' = \phi(o)$$

Evaluate the network:

$$L = l(\boldsymbol{o}, y)$$



Loss function

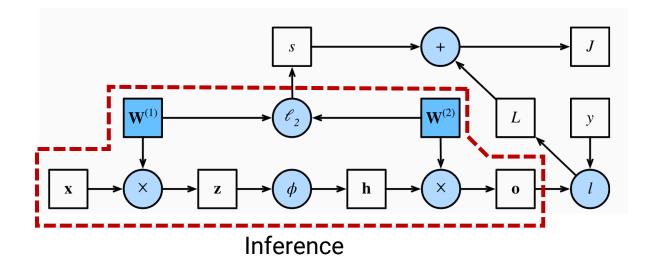


$$s = \frac{\lambda}{2}(||W^{(1)}||^2 + ||W^{(2)}||^2)$$

Regularization

Training: Minimize (L+s)

Computational Graph



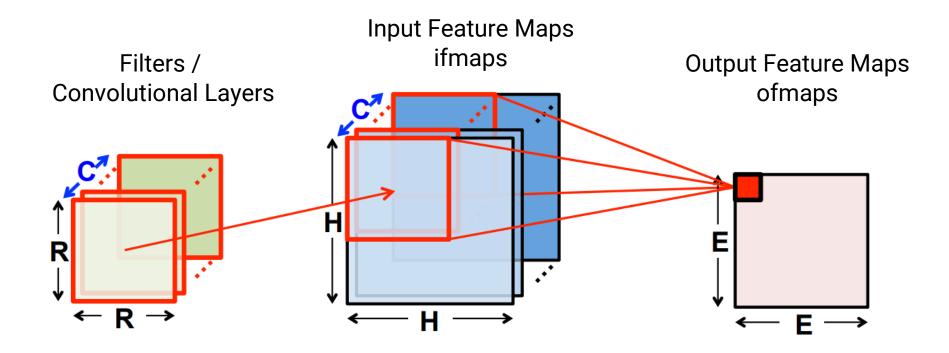


Convolutional Layer



$$\mathbf{O}[z][u][x][y] = \mathbf{B}[u] + \sum_{k=0}^{C-1} \sum_{i=0}^{R-1} \sum_{j=0}^{R-1} \mathbf{I}[z][k][Ux+i][Uy+j] \times \mathbf{W}[u][k][i][j],$$

$$0 \le z < N, 0 \le u < M, 0 \le x, y < E, E = (H - R + U)/U.$$



N: batch size

M: # of ofmap channels

C: # of ifmap filter channels

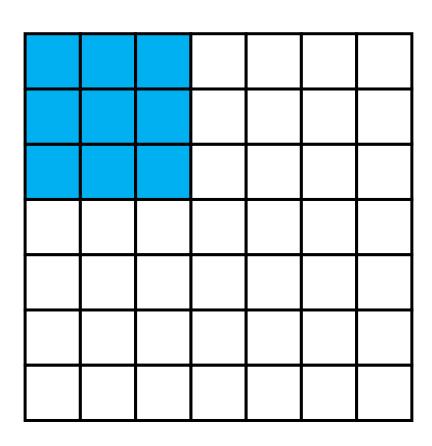
H: ifmap height/width

R: filter plan height/width

E: ofmap height/width

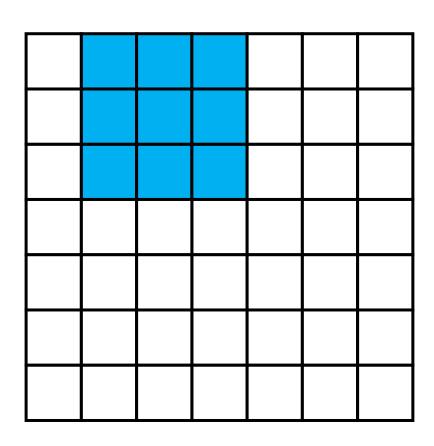






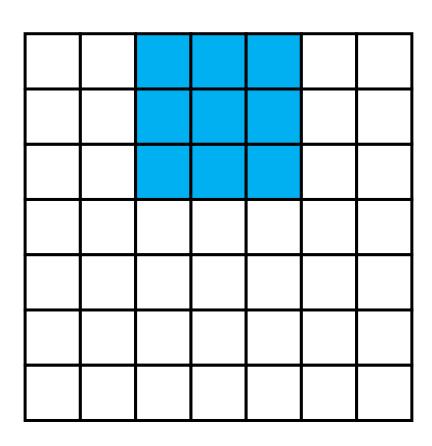






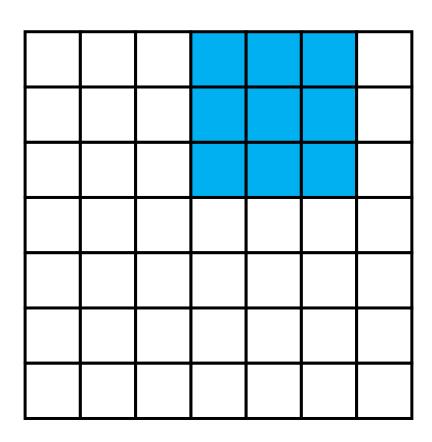










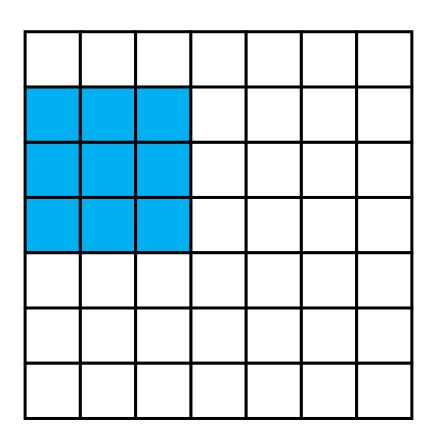












Output: 5×5



Convolutional Layer - Example



0	0	0	0	0	0	0	0	0
0								0
0								0
0								0
0								0
0								0
0								0
0								0
0	0	0	0	0	0	0	0	0



Padding



Convolutional Layer - Example



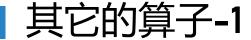
0	0	0	0	0	0	0	0	0
0								0
0								0
0								0
0								0
0								0
0								0
0								0
0	0	0	0	0	0	0	0	0



Convolutional Layer - Example



0	0	0	0	0	0	0	0	0
0								0
0								0
0								0
0								0
0								0
0								0
0								0
0	0	0	0	0	0	0	0	0



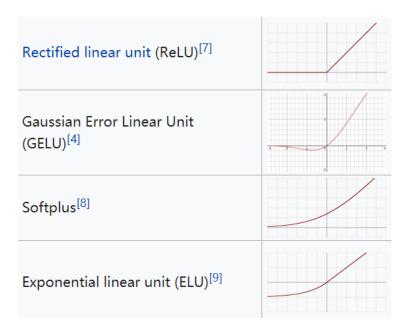


Activation

- Relu
- Tanh
- Sigmoid
- Softmax

•

Identity	
Binary step	
Logistic, sigmoid, or soft step	
Hyperbolic tangent (tanh)	



硬件上如何最简单地实现?





Pooling

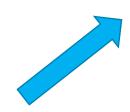
- Max pooling
- Average pooling
- Stochastic pooling

• ...



12	13	30	1
9	12	2	0
33	98	37	4
100	73	25	12

Example of max pooling:



13	30
100	37





12	8
76	20



Example of average pooling:

其它的算子-3



Normalization

- Batch Normalization (BN)
- Group Normalization (GN)

•

Input: Values of x over a mini-batch: $\mathcal{B} = \{x_{1...m}\}$; Parameters to be learned: γ , β Output: $\{y_i = BN_{\gamma,\beta}(x_i)\}$

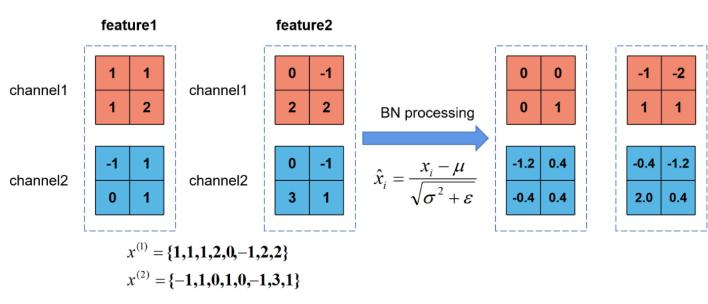
$$\mu_{\mathcal{B}} \leftarrow \frac{1}{m} \sum_{i=1}^{m} x_i$$
 // mini-batch mean

$$\sigma_{\mathcal{B}}^2 \leftarrow \frac{1}{m} \sum_{i=1}^m (x_i - \mu_{\mathcal{B}})^2$$
 // mini-batch variance

$$\widehat{x}_i \leftarrow \frac{x_i - \mu_{\mathcal{B}}}{\sqrt{\sigma_{\mathcal{B}}^2 + \epsilon}}$$
 // normalize

$$y_i \leftarrow \gamma \hat{x}_i + \beta \equiv \text{BN}_{\gamma,\beta}(x_i)$$
 // scale and shift

Example of BN:



$$\mu_{1} = \frac{1}{m} \sum_{i=1}^{m} x_{i}^{(1)} = 1 \qquad \sigma_{1}^{2} = \frac{1}{m} \sum_{i=1}^{m} (x_{i}^{(1)} - \mu_{1})^{2} = 1$$

$$\mu_{2} = \frac{1}{m} \sum_{i=1}^{m} x_{i}^{(2)} = 0.5 \qquad \sigma_{2}^{2} = \frac{1}{m} \sum_{i=1}^{m} (x_{i}^{(2)} - \mu_{2})^{2} = 1.5$$

$$\mu = \begin{bmatrix} 1 \\ 0.5 \end{bmatrix} \quad \sigma^{2} = \begin{bmatrix} 1 \\ 1.5 \end{bmatrix}$$



Some Famous and Basic NN



- VGG16/19
- Resnets
- Depthwise Convolution Group
 - InceptionNets
 - XceptionNets
 - MobileNet





Network Architecture

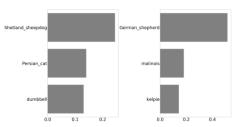
```
_input = Input((224,224,1))
     conv1 = Conv2D(filters=64, kernel size=(3,3), padding="same", activation="relu")( input)
     conv2 = Conv2D(filters=64, kernel_size=(3,3), padding="same", activation="relu")(conv1)
     pool1 = MaxPooling2D((2, 2))(conv2)
 6
     conv3 = Conv2D(filters=128, kernel_size=(3,3), padding="same", activation="relu")(pool1)
     conv4 = Conv2D(filters=128, kernel_size=(3,3), padding="same", activation="relu")(conv3)
 8
     pool2 = MaxPooling2D((2, 2))(conv4)
 9
10
     conv5 = Conv2D(filters=256, kernel size=(3,3), padding="same", activation="relu")(pool2)
11
     conv6 = Conv2D(filters=256, kernel_size=(3,3), padding="same", activation="relu")(conv5)
12
     conv7 = Conv2D(filters=256, kernel size=(3,3), padding="same", activation="relu")(conv6)
13
14
     pool3 = MaxPooling2D((2, 2))(conv7)
15
     conv8 = Conv2D(filters=512, kernel_size=(3,3), padding="same", activation="relu")(pool3)
16
     conv9 = Conv2D(filters=512, kernel size=(3,3), padding="same", activation="relu")(conv8)
17
     conv10 = Conv2D(filters=512, kernel size=(3,3), padding="same", activation="relu")(conv9)
18
     pool4 = MaxPooling2D((2, 2))(conv10)
19
20
     conv11 = Conv2D(filters=512, kernel_size=(3,3), padding="same", activation="relu")(pool4)
21
     conv12 = Conv2D(filters=512, kernel_size=(3,3), padding="same", activation="relu")(conv11)
22
23
     conv13 = Conv2D(filters=512, kernel size=(3,3), padding="same", activation="relu")(conv12)
     pool5 = MaxPooling2D((2, 2))(conv13)
24
25
    flat = Flatten()(pool5)
26
     dense1 = Dense(4096, activation="relu")(flat)
     dense2 = Dense(4096, activation="relu")(dense1)
28
29
     output = Dense(1000, activation="softmax")(dense2)
```

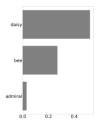


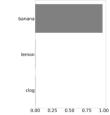












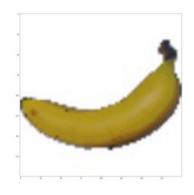


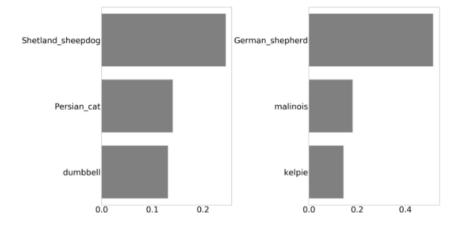
Performance

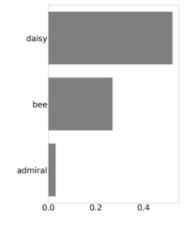


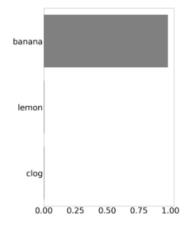














Residual Network

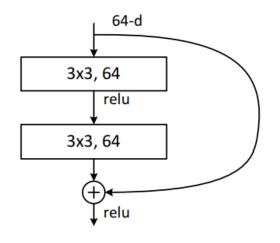


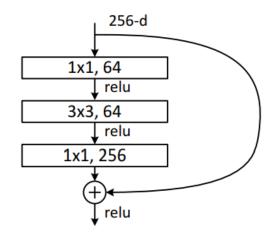
When DNN goes deeper:

- Network becomes difficult to optimize
- Vanishing / Exploding Gradients
- Degradation Problem (accuracy first saturates and then degrades)

$\mathcal{F}(\mathbf{x}) \qquad \begin{array}{c} \mathbf{x} \\ \text{weight layer} \\ \text{weight layer} \\ \end{array} \qquad \mathbf{x} \\ \text{identity} \\ \mathcal{F}(\mathbf{x}) + \mathbf{x} \qquad \begin{array}{c} \mathbf{x} \\ \text{relu} \\ \end{array}$

Examples:



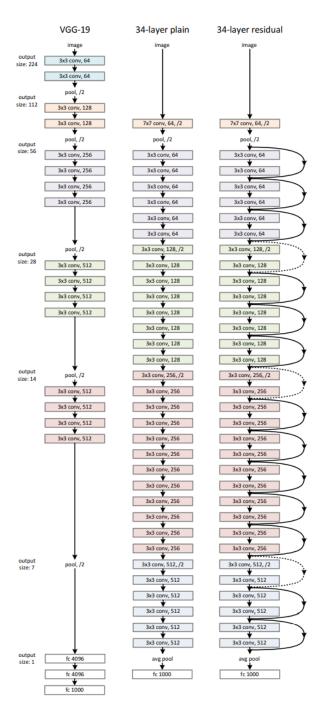


注意BN的位置!

Bottleneck block



Dotted lines means Increased dimension



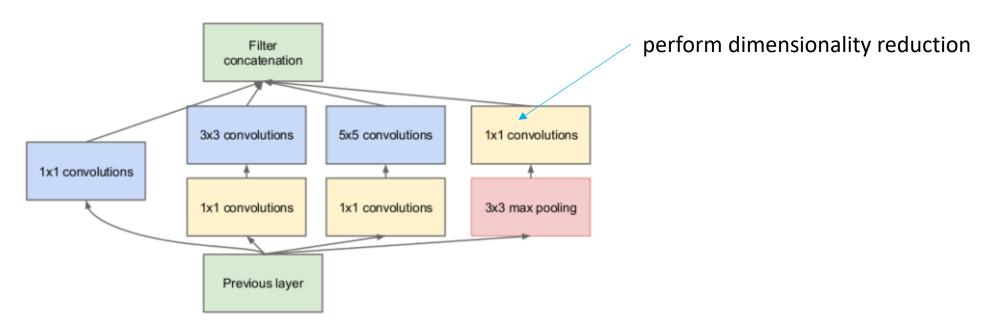






 Also known as GoogleNet consists of total 22 layers and was the winning model of 2014 image net challenge.

Inception Module:

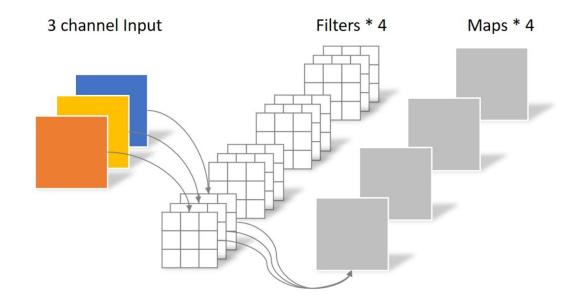




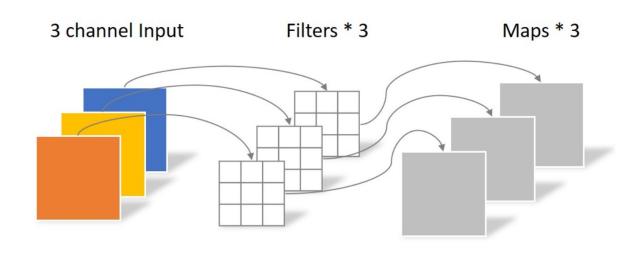
Depthwise Separable Convolution



Normal Convolution



Depthwise Convolution



Parameter Number: 4*3*3*3=108

Parameter Number: 3*3*3=27



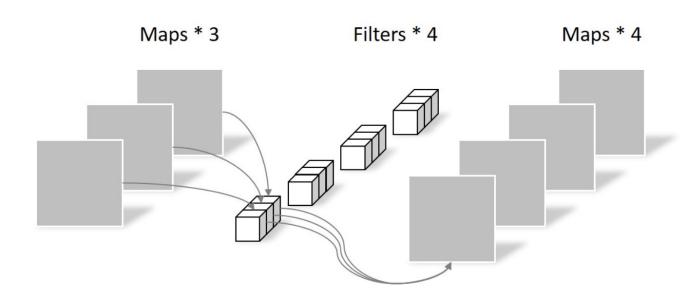
Depthwise Separable Convolution



Normal Convolution

3 channel Input Filters * 4 Maps * 4

Pointwise Convolution



Parameter Number: 4*3*3*3=108

Parameter Number: 4*3*1*1=12



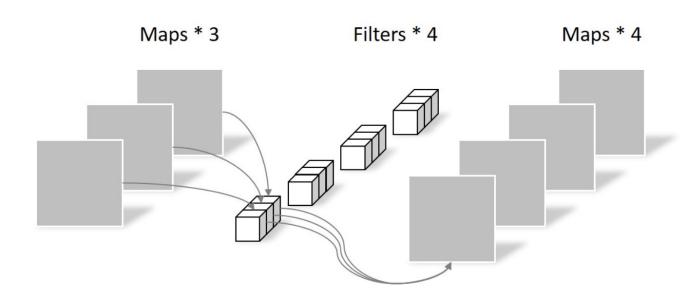
Depthwise Separable Convolution



Normal Convolution

3 channel Input Filters * 4 Maps * 4

Pointwise Convolution

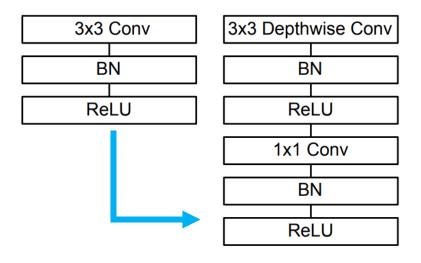


Parameter Number: 4*3*3*3=108

Parameter Number: 4*3*1*1=12







Parameter Number: 4*3*3*3=108

Parameter Number: Depthwise+Pointwise=27+12=39

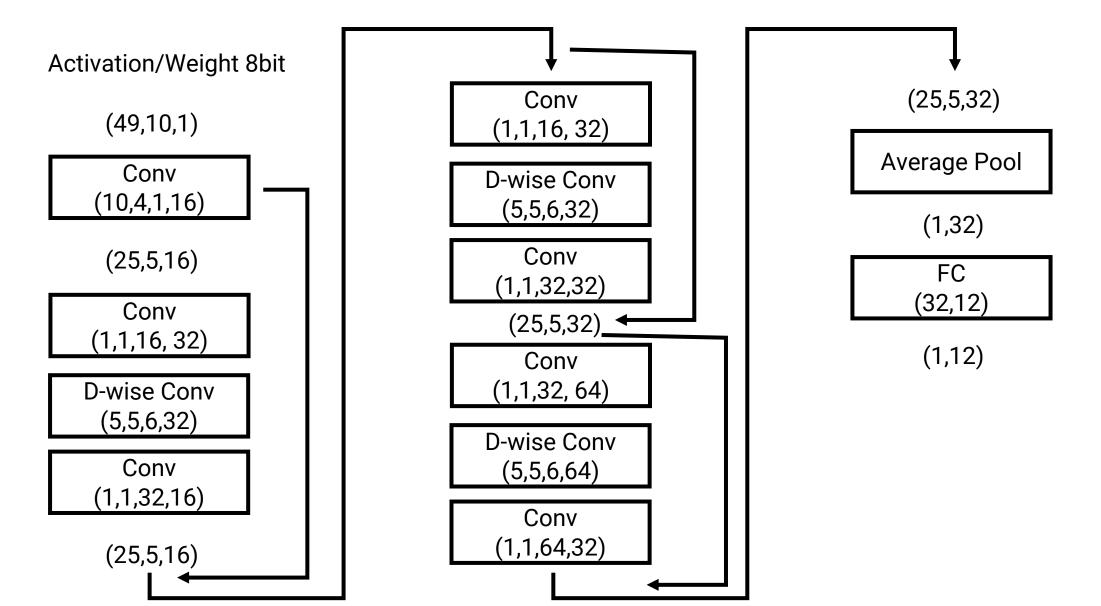
减少计算量!

Type / Stride	Filter Shape	Input Size
Conv / s2	$3 \times 3 \times 3 \times 32$	$224 \times 224 \times 3$
Conv dw / s1	$3 \times 3 \times 32 \text{ dw}$	$112 \times 112 \times 32$
Conv / s1	$1 \times 1 \times 32 \times 64$	$112 \times 112 \times 32$
Conv dw / s2	$3 \times 3 \times 64 \text{ dw}$	$112 \times 112 \times 64$
Conv / s1	$1 \times 1 \times 64 \times 128$	$56 \times 56 \times 64$
Conv dw / s1	$3 \times 3 \times 128 \text{ dw}$	$56 \times 56 \times 128$
Conv / s1	$1 \times 1 \times 128 \times 128$	$56 \times 56 \times 128$
Conv dw / s2	$3 \times 3 \times 128 \text{ dw}$	$56 \times 56 \times 128$
Conv / s1	$1 \times 1 \times 128 \times 256$	$28 \times 28 \times 128$
Conv dw / s1	$3 \times 3 \times 256 \text{ dw}$	$28 \times 28 \times 256$
Conv / s1	$1 \times 1 \times 256 \times 256$	$28 \times 28 \times 256$
Conv dw / s2	$3 \times 3 \times 256 \text{ dw}$	$28 \times 28 \times 256$
Conv / s1	$1 \times 1 \times 256 \times 512$	$14 \times 14 \times 256$
$\frac{\text{Conv dw / s1}}{5 \times 6}$	$3 \times 3 \times 512 \text{ dw}$	$14 \times 14 \times 512$
Onv / s1	$1 \times 1 \times 512 \times 512$	$14 \times 14 \times 512$
Conv dw / s2	$3 \times 3 \times 512 \text{ dw}$	$14 \times 14 \times 512$
Conv / s1	$1 \times 1 \times 512 \times 1024$	$7 \times 7 \times 512$
Conv dw / s2	$3 \times 3 \times 1024 \text{ dw}$	$7 \times 7 \times 1024$
Conv / s1	$1 \times 1 \times 1024 \times 1024$	$7 \times 7 \times 1024$
Avg Pool / s1	Pool 7×7	$7 \times 7 \times 1024$
FC / s1	1024×1000	$1 \times 1 \times 1024$
Softmax / s1	Classifier	$1 \times 1 \times 1000$



Example NN Architecture



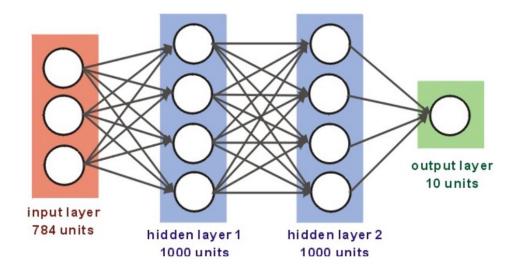




NN Coding Example ... in C



- C/C++ is the reliable contract between software and hardware
- Implement in CPU
- Ref: MNIST CNN coded in C [0.995] | Kaggle







```
int layerSizes[10] = {0,0,0,0,0,0,784,1000,1000,10};
    float* layers[10] = {0};
    float* errors[10] = {0};
    float* weights[10] = {0};
     // INITIALIZATION
 5
     void initNet(){
         // ALOCATE MEMORY
 7
         layers[0] = (float*)malloc((layerSizes[0]+1) * sizeof(float));
 8
 9
         errors[0] = (float*)malloc(layerSizes[0] * sizeof(float));
         for (i=1;i<10;i++){
10
             layers[i] = (float*)malloc((layerSizes[i]+1) * sizeof(float));
11
             errors[i] = (float*)malloc(layerSizes[i] * sizeof(float));
12
13
             weights[i] = (float*)malloc(layerSizes[i] * (layerSizes[i-1]+1) * sizeof(float));
14
         // RANDOMIZE WEIGHTS AND BIAS
15
16
         float scale;
         for (i=0;i<10;i++) layers[i][layerSizes[i]]=1.0;</pre>
17
         for (j=1; j<10; j++){}
18
19
             scale = 2.0 * sqrt(6.0/(layerSizes[j] + layerSizes[j-1]));
             if (j!=9 && activation==1) scale = scale * 1.41; // RELU
20
             else if (j!=9) scale = scale * 4.0; // TANH
21
             for (i=0;i<layerSizes[j] * (layerSizes[j-1]+1);i++)</pre>
22
23
                 weights[j][i] = scale * ( (float)rand()/RAND MAX - 0.5 );
             for (i=0;i<layerSizes[j];i++) // BIASES</pre>
24
                 weights[j][(layerSizes[j-1]+1)*(i+1)-1] = 0.0;
25
26
27
```



Forward Pass (Inference)

```
北京大学
PEKING UNIVERSITY
```

```
int activation = 1; //ReLU
     // FORWARD PROPAGATION
     int forwardProp(int x){
         int i,j,k,imax;
         float sum, esum, max;
         // INPUT LAYER - RECEIVES 28X28 IMAGES
         for (i=0;i<784;i++) layers[10-numLayers][i] = trainImages[x][i];</pre>
         // HIDDEN LAYERS - RELU ACTIVATION
 8
         for (k=11-numLayers;k<9;k++)</pre>
 9
         for (i=0;i<layerSizes[k];i++){</pre>
10
             sum = 0.0;
11
             for (j=0;j<layerSizes[k-1]+1;j++)</pre>
12
                 sum += layers[k-1][j]*weights[k][i*(layerSizes[k-1]+1)+j];
13
             if (activation==1) layers[k][i] = ReLU(sum);
14
             else if (activation==2) layers[k][i] = TanH(sum);
15
16
```

```
// OUTPUT LAYER - SOFTMAX ACTIVATION
17
18
         esum = 0.0;
         for (i=0;i<layerSizes[9];i++){</pre>
19
             sum = 0.0;
20
             for (j=0;j<layerSizes[8]+1;j++)</pre>
21
22
                 sum += layers[8][j]*weights[9][i*(layerSizes[8]+1)+j];
23
             if (sum>30) return -1; //GRADIENT EXPLODED
             layers[9][i] = \exp(sum);
24
             esum += layers[9][i];
25
26
27
         // SOFTMAX FUNCTION
         max = layers[9][0]; imax=0;
28
         for (i=0;i<layerSizes[9];i++){</pre>
29
             if (layers[9][i]>max){
30
31
                 max = layers[9][i];
32
                 imax = i;
33
             layers[9][i] = layers[9][i] / esum;
34
35
         return imax;
37
```



Here The Accelerator Comes!



```
int activation = 1; //ReLU
     // FORWARD PROPAGATION
    int forwardProp(int x){
        int i,j,k,imax;
        float sum, esum, max;
        // INPUT LAYER - RECEIVES 28X28 IMAGES
        for (i=0;i<784;i++) layers[10-numLayers][i] = trainImages[x][i];</pre>
        // HIDDEN LAYERS - RELU ACTIVATION
        for (k=11-numLayers;k<9;k++)</pre>
        for (i=0;i<layerSizes[k];i++){</pre>
            sum = 0.0;
11
            for (j=0;j<layerSizes[k-1]+1;j++)</pre>
12
                sum += layers[k-1][j]*weights[k][i*(layerSizes[k-1]+1)+j]
13
            if (activation==1) layer
14
            else if (activation==2) l ers[k][i] = TanH(sum);
15
16
```

```
17
         // OUTPUT LAYER - SOFTMAX ACTIVATION
18
         esum = 0.0;
         for (i=0;i<layerSizes[9];i++){</pre>
20
             sum = 0.0;
             for (j=0;j<layerSizes[8]+1;j++)</pre>
21
22
                  sum += layers[8][j]*weights[9][i*(layerSizes[8]+1)+j];
             if (sum>30) return -1; //GRADIENT EXPLODED
23
             layers[9][i] = \exp(sum);
24
             esum += layers[9][i];
25
27
         // SOFTMAX FUNCTION
         max = layers[9][0]; imax=0;
28
         for (i=0;i<layerSizes[9];i++){</pre>
29
             if (layers[9][i]>max){
30
31
                 max = layers[9][i];
32
                 imax = i;
33
             layers[9][i] = layers[9][i] / esum;
34
35
         return imax:
37
```

Sum = AcceleratorVMM(*inputs, *weights, *outputs)



C Function Access PIM Function



```
Sum = AcceleratorVMM(*inputs, *weights, *outputs)
```

C Program: XXX.c

```
#include <stdio.h>
extern int AcceleratorVMM(*inputs, *weights, *outputs);
Int function () {
...
Sum = AcceleratorVMM(*inputs, *weights, *outputs)
...
}
```



C Function Access PIM Function



Sum = AcceleratorVMM(*inputs, *weights, *outputs)

C Intrinsic: XXX.s

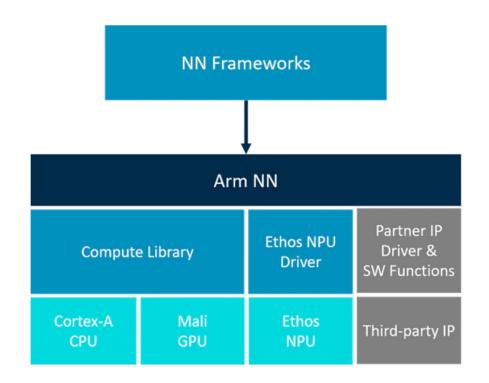
```
.section text
.global AcceleratorVMM
.type AcceleratorVMM, @function

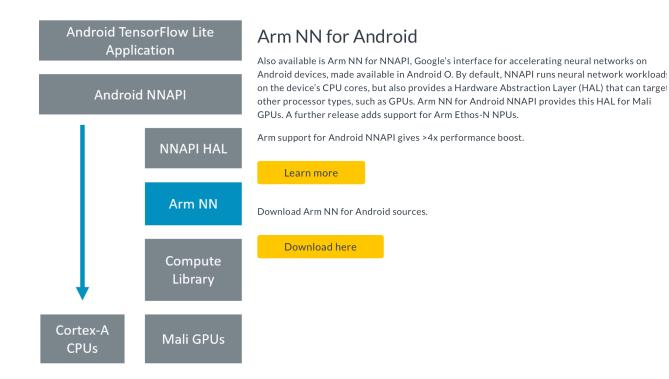
AcceleratorVMM:
        sw a0, a1
        ld a0, a1
        ...
```





Yes!



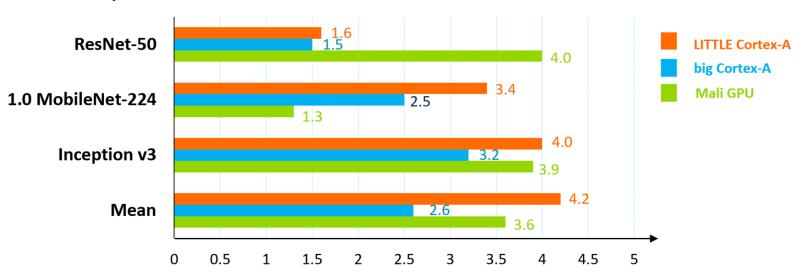


https://developer.arm.com/ip-products/processors/machine-learning/arm-nn.





Arm NN performance relative to other NN frameworks



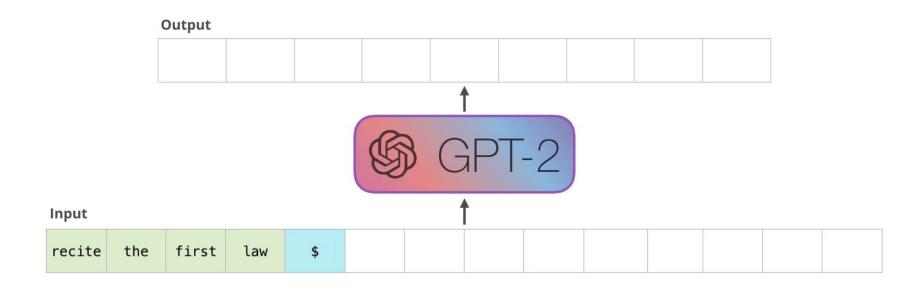
Mean improvements of Arm NN relative to multiple industry inference engines on CPU

- Arm NN open-source collaboration enables optimal third-party implementations
- Deployed in multiple production devices (>250Mu)



Transformer & Large Language Model (LLM)



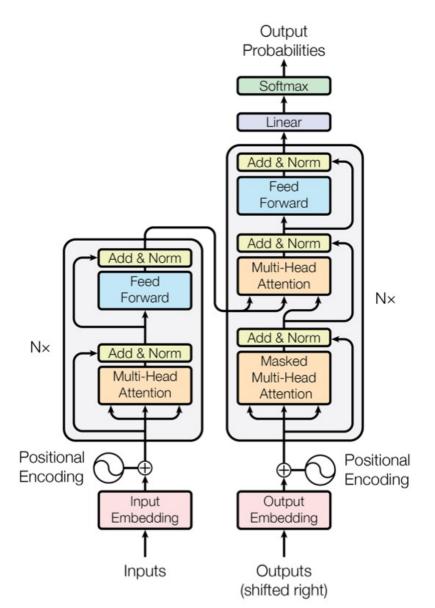


- LLM is a regressive model that generates text.
- Thousands of attention modules construct the entire GPT models.



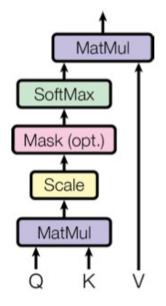
Additional: Attention in Transformer

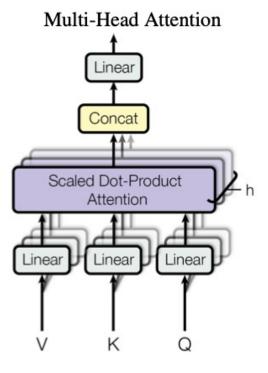




Vaswani, Ashish, et al. "Attention is all you need." *Advances in neural information processing systems* 30 (2017).

Scaled Dot-Product Attention







Additional: Attention in Transformer



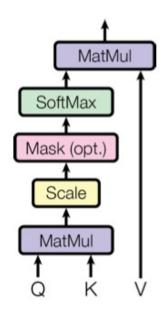
Vaswani, Ashish, et al. "Attention is all you need." *Advances in neural information processing systems* 30 (2017).

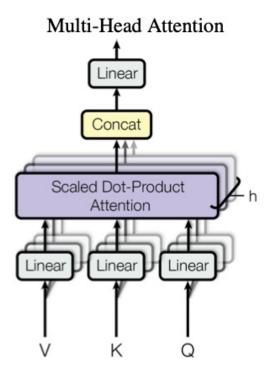
$$Q = xW_Q, K = xW_K, V = xW_V$$

$$\operatorname{Attention}(Q, K, V) = \operatorname{softmax}(\frac{QK^T}{\sqrt{d_k}})V$$

https://zhuanlan.zhihu.com/p/624740065

Scaled Dot-Product Attention

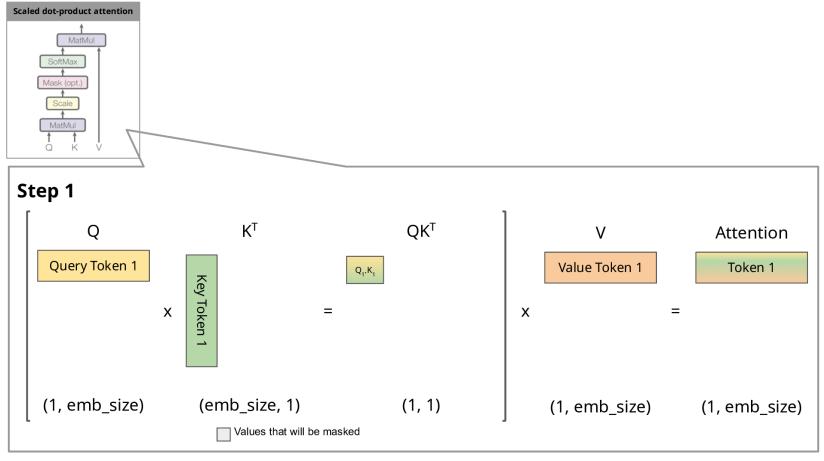






Transformer & Large Language Model (LLM)



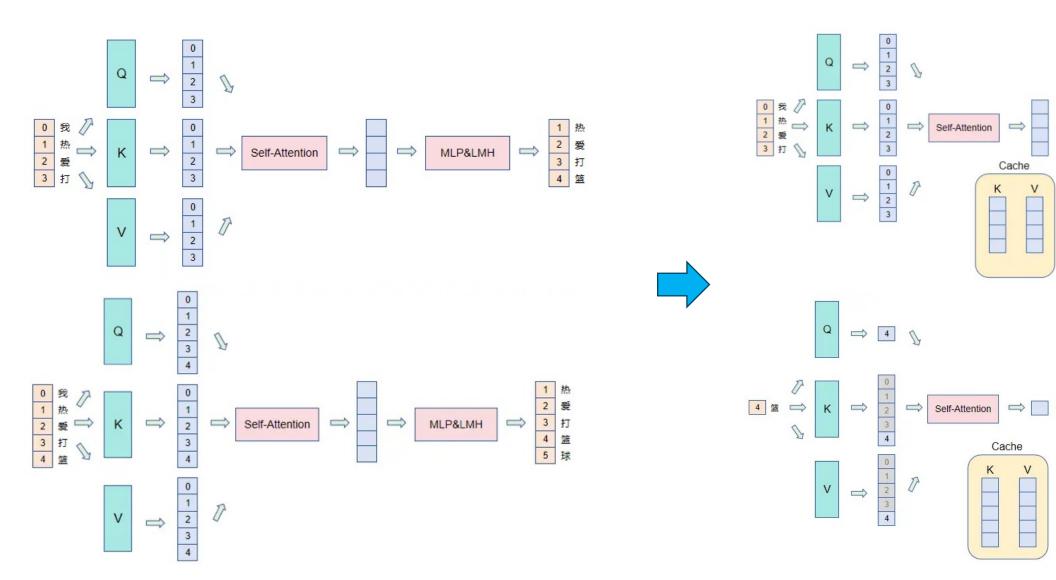


Zoom-in! (simplified without Scale and Softmax)



KV-Cache Optimization





https://juejin.cn/post/7287768247889559611#





- https://github.com/tinygrad/tinygrad
- tinygrad/examples/transformer.py





Get familiar with Attention model computation