

№1.

ПЕРВАТКИН А. ПЗ113

$$\begin{cases} z = x^2 y \\ x = \frac{t}{s} \\ y = 3t - 2s \end{cases} \quad \frac{\partial z}{\partial t} = ? \quad \frac{\partial z}{\partial s} = ?$$

$$\frac{\partial z}{\partial t} = \frac{\partial z}{\partial x} \cdot \frac{\partial x}{\partial t} + \frac{\partial z}{\partial y} \cdot \frac{\partial y}{\partial t} =$$

$$= 2xy \cdot \frac{1}{s} + 3x^2 \cdot \frac{2xy}{s} + 3x^2 \cdot \frac{2 \cdot \frac{t}{s} (3t - 2s)}{s} +$$

$$+ 3 \left( \frac{t}{s} \right)^2 = \frac{2t(3t - 2s) + 3t^2}{s^2} = \frac{6t^2 - 4ts + 3t^2}{s^2} =$$

$$= \frac{9t^2 - 4ts}{s^2} = \frac{t(9t - 4s)}{s^2}$$

$$\frac{\partial z}{\partial s} = \frac{\partial z}{\partial x} \cdot \frac{\partial x}{\partial s} + \frac{\partial z}{\partial y} \cdot \frac{\partial y}{\partial s} = x^2 \cdot (-2) - \frac{2xyt}{s^2}$$

$$= -2 \left( \frac{xyt}{s^2} + x^2 \right) = \frac{-t^2}{s(3t - 2s)} - \frac{t^2}{s^2} =$$

$$= \frac{-3t^3 - 2st^2}{s^3} =$$

$$= \frac{-t^2(3t - 2s)}{s^3}$$

ОТВЕТ:  $\frac{\partial z}{\partial t} = \frac{t(9t - 4s)}{s^2}$

$$\frac{\partial z}{\partial s} = \frac{-t^2(3t - 2s)}{s^3}$$