

$$\xi(x, y) = \sqrt{x^2 + y^2}$$

$$D: (x-2)^2 + y^2 \leq 4$$

ПЕРЕИДЁМ В ПОЛЯРНУЮ
СИСТЕМУ КООРДИНАТ

$$x = r \cdot \cos \varphi$$

$$y = r \cdot \sin \varphi$$

$$\sqrt{x^2 + y^2} = \sqrt{r^2 \cos^2 \varphi + r^2 \sin^2 \varphi} =$$

$$= r \sqrt{\cos^2 \varphi + \sin^2 \varphi} = r$$

$$dx dy = r \cdot dr \cdot d\varphi$$

$$(x-2)^2 + y^2 \leq 4$$

$$(r \cos \varphi - 2)^2 + r^2 \sin^2 \varphi \leq 4$$

$$r^2 \cos^2 \varphi + 4r \cos \varphi + 4 + r^2 \sin^2 \varphi \leq 4$$

$$r^2 + 4r \cos \varphi + 4 \leq 4$$

$$r^2 \leq -4r \cos \varphi \quad \text{T.k. } r \geq 0, \text{ то}$$

$$r \leq -\cos \varphi$$

$$\iint \sqrt{x^2 + y^2} dx dy = \iint r \cdot r dr d\varphi =$$

$$= \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} d\varphi \int_0^{4 \cos \varphi} r^2 dr = \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} d\varphi \left[\frac{r^3}{3} \right]_0^{4 \cos \varphi} =$$

$$= \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \frac{64 \cos^3 \varphi}{3} d\varphi = \frac{64}{3} \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \cos^3 \varphi d\varphi = \frac{64}{3} \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} (1 - \sin^2 \varphi) \cdot (\cos \varphi) d\varphi$$

$$= \left| \frac{\pi}{2} \rightarrow 1, -\frac{\pi}{2} \rightarrow -1 \right| = \frac{64}{3} \int_{-1}^1 (1 - t^2) dt = \frac{64}{3} \left(t - \frac{t^3}{3} \right) \Big|_{-1}^1 =$$

