

# HG2002: Tutorial

## Sentence Relations and Truth

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1. Take three sentences,  $p$ ,  $q$ , and  $r$  as follows.

$p$ : The sun is shining.

$q$ : The day is warm.

$r$ : The sun is shining and the day is warm.

Let's make the working assumption that we can represent sentence  $r$  by the logical formula  $p \wedge q$ . Use the truth table for  $\wedge$  "logical and" to show the truth-value of  $r$  in the situations below:

S1.  $p$  is true;  $q$  is false.

S2.  $p$  is true;  $q$  is true.

S3.  $p$  is false;  $q$  is true.

S4.  $p$  is false;  $q$  is false.

2. In propositional logic, some may want to assume that  $p \wedge q$  and  $q \wedge p$  are logically equivalent i.e. that the order of the elements is irrelevant. Discuss how the following examples show that this is not true for the way that speakers use English and.

(1) *He woke up and saw on TV that he had won the lottery.*

(2) *Combine the egg yolks with water in a bowl and whisk the mixture until foamy.*

(3) *He made two false starts and was disqualified from the race.*

(4) *Move and I'll shoot!*

3. Prove the Contrapositive ( $p \rightarrow q \equiv \neg q \rightarrow \neg p$ ) using truth tables:
4. Decide if the following pairs of sentences are pairs of entailment or pre-supposition. How did you make your decisions?

(5) a. *Sandy knows that Joe crashed the car.*

b. *Joe crashed the car.*

(6) a. *Australia is bigger than Singapore.*

b. *Singapore is smaller than Australia.*

(7) a. *The minister blames her secretary for leaking the memo to the press.*

b. *The memo was leaked to the press.*

(8) a. *Everyone passed the examination.*

b. *No one failed the examination.*

(9) a. *Fran has resumed their habit of editing Wikipedia.*

b. *Fran has a habit of editing Wikipedia.*

5. What are analytically true statements? Decide which of the following sentences are analytically true. Discuss the reasons for your decision.

- (10) *If it rains, we'll get wet.*
- (11) *The train will either arrive or it won't arrive.*
- (12) *Every doctor is a doctor.*
- (13) *If Bobby killed a deer, Bobby killed an animal.*
- (14) *Madrid is the capital of Spain.*
- (15) *Every city has pollution problems.*

6. Translate the following into predicate logic, using restricted quantifiers  $\forall$  and  $\exists$ . If a sentence is ambiguous, give both readings.

- (16) *Lancelot hated all dragons*
- (17) *Every dragon feared Lancelot*
- (18) *One dragon feared every knight.*
- (19) *Somebody searched for the Holy Grail*
- (20) *Every dragon did not like spinach*
- (21) *Every dragon who did not like spinach feared Lancelot*
- (22) *Not every one searched for the Holy Grail*
- (23) *No dragon searched for Lancelot*

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