Table: Language for Tables

- Hybrid paradigm: imperative + relational
- Data types: atomic (integer, string, boolean) and tables (table)
- Program = program [statements] end
 - Definition of variables
 - Assignments (id = expr)
 - Control statements: if-then, if-then-else, while-do
 - Input of variables and output of expressions: read, write
- Expressions:
 - Logical (and, or, not): in short circuit
 - Comparison (==, !=, >, >=, <, <=)
 - Arithmetic (+, -, *, /)
 - Relational (project, select, exists, all, join, update, extend, rename)

Relational Expressions

Operator	Example	
project	<pre>project [a,b] R</pre>	
select	select [a==b and c != 25] R	
exists	exists [a!=b or c] R	
all	all [a and c] R	
join	R join [a==b and c==d] S	
update	<pre>update [a = b+c] R</pre>	
extend	extend [integer d = b-c] R	
rename	rename [x,y,z] R	

Precedence, Associativity, Order of Evaluation

O perator	Туре	Associativity
and, or	binary	left
==, !=, >, >=, <, <=,	binary	nonassoc
+, -	binary	left
*, /, join	binary	left
-, not, project, select, exists, all, update, extend, rename	unary	right

increasing

• Evaluation order of operands: from left to right

Conditional Statement

• if expr then stat-list [else stat-list] end

```
integer a, b, c;
table(integer x, string y) t, r;
. . .
if a==b then
 t = select [x>0] r
else
 a = b+c
end;
if t != r then
 write "Different tables!"
end;
. . .
```

Loop

• while expr do stat-list end

```
integer n, fact;
read n;
fact = 1;
while n > 1 do
  fact = fact * n;
  n = n -1
end;
write fact;
```

Input

• read id

• read [filename] id

```
integer i, j;
table(integer a, string b) t, r, z;
...
read t;
r = select [a == i] t;
read ["t.dat"] t;
z = select [a > j] t;
```

Output

```
• write expr
```

• write [filename] expr

```
integer i, j;
string name;
table(integer a, string b) t;
...
write select [a==i] t;
read name;
write [name] select [a>j] t;
```

BNF

```
program → program stat-list end
stat-list \rightarrow stat; stat-list | stat
stat \rightarrow def-stat | assign-stat | if-stat | while-stat | read-stat | write-stat
def-stat \rightarrow type id-list
id-list \rightarrow id , id-list | id
type \rightarrow atomic-type \mid table-type
atomic-type \rightarrow integer \mid string \mid boolean
table-type \rightarrow table ( attr-list )
attr-list \rightarrow attr-decl, attr-list \mid attr-decl
attr-decl \rightarrow atomic-type id
assign\text{-}stat \rightarrow \mathbf{id} = expr
expr \rightarrow expr \ bool-op \ bool-term \mid bool-term
bool\text{-}op \rightarrow \text{and} \mid \text{or}
bool-term \rightarrow comp-term | comp-term | comp-term
comp-op \rightarrow == |!=| > | >= | < | <=
comp-term → comp-term low-bin-op low-term | low-term
low-bin-op \rightarrow + | -
low-term \rightarrow low-term high-bin-op factor | factor
high-bin-op \rightarrow * | / | join-op
factor \rightarrow unary-op factor \mid (expr) \mid id \mid constant
unary-op \rightarrow - \mid \mathbf{not} \mid project-op \mid select-op \mid exists-op \mid all-op \mid
                 update-op | extend-op | rename-op
```

```
join-op \rightarrow join [expr]
project-op \rightarrow \mathbf{project} [id-list]
select-op \rightarrow select [expr]
exists-op \rightarrow exists [expr]
all-op \rightarrow all [expr]
extend-op \rightarrow extend [ atomic-type id = expr ]
update-op \rightarrow update [id = expr]
rename-op \rightarrow rename [ id-list ]
constant \rightarrow atomic\text{-}const \mid table\text{-}const
atomic-const → intconst | strconst | boolconst
table\text{-}const \rightarrow \{ table\text{-}instance \} 
table-instance \rightarrow tuple-list | atomic-type-list
tuple-list \rightarrow tuple-const, tuple-list | tuple-const
tuple-const \rightarrow (atomic-const-list)
atomic-const-list \rightarrow atomic-const-list
                          atomic-const
atomic-type-list \rightarrow atomic-type, atomic-type-list
                          atomic-type
if-stat \rightarrow if expr then stat-list else-part end
else-part \rightarrow else \ stat-list \mid \epsilon
while-stat \rightarrow while expr do stat-list end
read-stat \rightarrow read specifier id
specifier \rightarrow [expr] \mid \varepsilon
write-stat \rightarrow \mathbf{write} specifier expr
```

EBNF

```
program → program stat-list end
stat-list \rightarrow stat \{ ; stat \}
stat \rightarrow def-stat | assign-stat | if-stat | while-stat | read-stat | write-stat
def-stat \rightarrow type id-list
id-list \rightarrow id \{, id \}
type \rightarrow atomic-type \mid table-type
atomic-type → integer | string | boolean
table-type \rightarrow table ( attr-list )
attr-list \rightarrow attr-decl \{ , attr-decl \}
attr-decl \rightarrow atomic-type id
assign-stat \rightarrow id = expr
expr \rightarrow bool\text{-}term \{ (and | or) bool\text{-}term \}
bool-term \rightarrow comp-term [ (== | != | > | >= | < | <=) comp-term ]
comp\text{-}term \rightarrow low\text{-}term \{ (+ | -) low\text{-}term \}
low-term \rightarrow factor \{ (* | / | join-op) factor \}
factor \rightarrow unary-op factor \mid (expr) \mid id \mid constant
unary-op \rightarrow - \mid \mathbf{not} \mid project-op \mid select-op \mid exists-op \mid all-op \mid
                 update-op | extend-op | rename-op
```

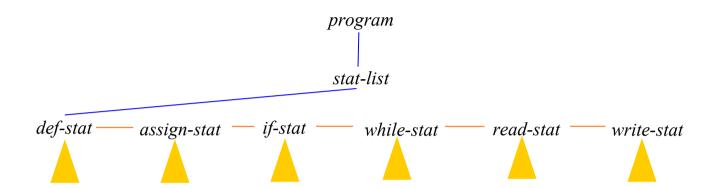
```
join-op \rightarrow join [expr]
project-op \rightarrow project [id-list]
select-op \rightarrow select [expr]
exists-op \rightarrow exists [expr]
all-op \rightarrow all [expr]
extend-op \rightarrow extend [ atomic-type id = expr ]
update-op \rightarrow update [id = expr]
rename-op \rightarrow rename [id-list]
constant \rightarrow atomic\text{-}const \mid table\text{-}const
atomic-const → intconst | strconst | boolconst
table\text{-}const \rightarrow \{ tuple\text{-}list \mid atomic\text{-}type\text{-}list \}
tuple-list \rightarrow tuple-const \{ , tuple-const \}
atomic-type-list \rightarrow atomic-type \{ , atomic-type \}
tuple-const \rightarrow \{ atomic-const \} \}
if-stat \rightarrow if expr then stat-list [ else stat-list ] end
while-stat \rightarrow while expr do stat-list end
read-stat \rightarrow read specifier id
specifier \rightarrow [expr] | \varepsilon
write-stat \rightarrow \mathbf{write} specifier expr
```

Abstract Tree

child brother value line type Node structure: (value: ival, sval)

- type ∈ { N ASSIGN STAT, N ATOMIC TYPE, N ATTR DECL, N BOOLCONST, N COMP EXPR, N DEF STAT, N EXTEND EXPR, N ID, N IF STAT, N INTCONST, N JOIN EXPR, N LOGIC EXPR, N MATH EXPR, N NEG EXPR, N PROGRAM, N PROJECT EXPR, N READ STAT, N RENAME EXPR, N SELECT EXPR, N SPECIFIER, N STAT LIST, N STRCONST, N TABLE CONST, N TABLE TYPE, N TUPLE CONST, N TYPE, N UPDATE EXPR, N WHILE STAT, N WRITE STAT } • type = N ATOMIC TYPE → value.ival ∈ { INTEGER, STRING, BOOLEAN } • type = N COMP EXPR → value.ival ∈ { EQ, NE,'>', GE,'<', LE }
- type = N LOGIC EXPR \rightarrow value.ival \in { AND, OR }
- type = N MATH EXPR → value.ival ∈ { '+', '-', '*', '/' }
- type = N NEG EXPR → value.ival ∈ { '-', NOT }
- type = N SELECT EXPR → value.ival ∈ { SELECT, EXISTS, ALL }

Abstract Tree (ii)



Type Checking

Traversing of the tree starting from the root

Checks:

- 1. Uniqueness of names within environments (attributes in table, variables in blocks)
- 2. Visibility within the **environment hierarchy** of a referenced identifier:

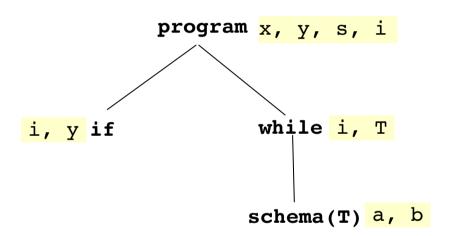
environment hierarchy = context hierarchy + block hierarchy

- 3. Compatibility of an operator with its operands
- 4. Compatibility of the identifier with the assignment expression
- 5. Compatibility of expressions with the relevant statements
- Type inference: computation of result schema in each operation

Environment Hierarchy

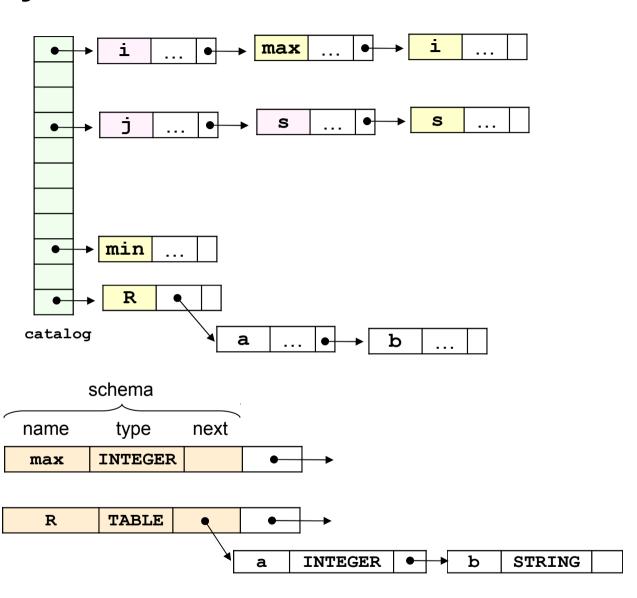
- Problem: binding of a name with the relevant definition
- Search within the environment hierarchy (static scope)

```
program
 real x, y;
 string s;
 integer i;
  . . .
 if(x == y) then
    integer i;
   real y;
 end;
 while i > j do
    integer i;
   table(integer a, string b) T;
   write select [ a > i and b == s ] T
 end
end
```



Symbol Table

```
program
 integer min, max, i;
 string s;
 table(integer a, string b) R;
 if min == max then
   table(string c, boolean d) T;
  read T;
   write project [a, d]
          R join [ b == c ] T;
  else
   while(min != max) do
      integer i, j, s;
      min = i + j - max;
      boolean ok;
      . . .
    end
 end;
  . . .
end
```



Context Hierarchy

• Contextualizing operators: select, exists, all, join, update, extend

```
table(int a, string x) A;
table(int b, bool y) B, C;
...
C = select [ exists [ a > b ] A ] B
```

7
\boldsymbol{H}
$\boldsymbol{\Gamma}$

a	х
3	alpha
8	beta
5	gamma
2	delta
6	epsilon

В

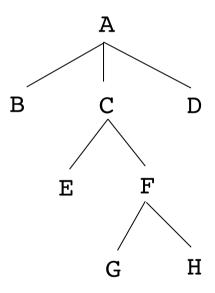
b	У
13	alpha
4	beta
15	gamma
6	delta
24	epsilon
3	zeta



b	У
4	beta
6	delta
3	zeta

Context Hierarchy (ii)

Search for the name by ascending the context hierarchy



• Type checking: keeps a **context stack** for searching identifiers

Logical Expressions (logic-expr)

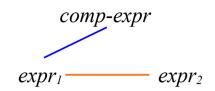
logic-expr $expr_1$ — $expr_2$

• Qualifier: AND, OR

• Constraint: $type(expr_1) = boolean$, $type(expr_2) = boolean$

Result schema: type(logic-expr) = boolean

Comparison Expressions (comp-expr)



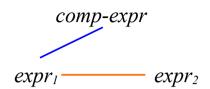
• Qualifier: EQ, NE

• Constraint: $type(expr_1) = type(expr_2)$

Result schema: type(comp-expr) = boolean

Comparison Expressions (comp-expr) (ii)

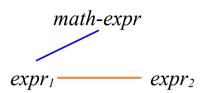
• Qualifier: '>', GE, '<', LE



- Constraint: $(type(expr_1) = int, type(expr_2) = int)$ or $(type(expr_1) = string, type(expr_2) = string)$
- Result schema: type(comp-expr) = boolean

Arithmetic Expressions (*math-expr*)

• Qualifier: '+', '-', '*', '/'

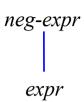


• Constraint: $type(expr_1) = integer$, $type(expr_2) = integer$

Result schema: type(math-expr) = integer

Negation (neg-expr)

• Qualifier: '-'



• Constraint: type(expr) = integer

Result schema: type(neg-expr) = integer

Negation (neg-expr) (ii)

• Qualifier: NOT



• Constraint: type(expr) = boolean

Result schema: type(neg-expr) = boolean

Projection (project-expr)

```
expr —\mathbf{id}_1 - \mathbf{id}_2 — ... — \mathbf{id}_k
```

- Constraint: type(expr) = table, names $(id-list) \subset \text{names}(\text{attributes}(\text{type}(expr))), \text{nodup}(\text{names}(id-list))$
- Result schema: type(project-expr) =
 table(a | a ∈ attributes(type(expr)), name(a) ∈ names(id-list))

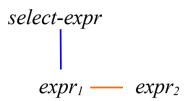
Rename (rename-expr)

```
rename-expr
expr - id_1 - id_2 - ... - id_n
```

- Constraint: type(expr) = table,
 | names(id-list) | = | attributes(type(expr)) | = n,
 nodup(id-list)
- Result schema: $type(rename-expr) = table(id-list[i]: type(expr)[i] | i \in [1..n])$

Selection (select-expr)

• Qualifier: **SELECT**

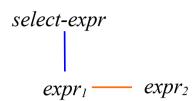


• Constraint: type($expr_2$) = table, type($expr_1$) = boolean

• Result schema: $type(select-expr) = type(expr_2)$

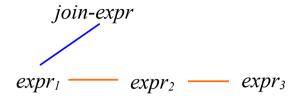
Selection (select-expr) (ii)

• Qualifier: EXISTS, ALL



- Constraint: type($expr_2$) = table, type($expr_1$) = boolean
- Result schema: type(select-expr) = boolean

Join (join-expr)



• Constraint: type $(expr_1)$ = table, type $(expr_3)$ = table, type $(expr_2)$ = boolean, names(attributes(type $(expr_1)$)) \cap names(attributes(type $(expr_3)$)) = \emptyset

• Result schema: $type(join-expr) = type(expr_1) \cup type(expr_3)$

Update (update-expr)

update-expr

```
• Constraint: type(expr_1) = table, expr_1 - id - expr_2 (name(id): domain) \in attributes(type(expr_1)), type(expr_2) = domain
```

• Result schema: $type(update-expr) = type(expr_1)$

Extension (extend-expr)

```
extend-expr
expr_1 — atomic-type — id — expr_2
```

```
    Constraint: type(expr<sub>1</sub>) = table,
    (name(id)) ∉ names(attributes(type(expr<sub>1</sub>))),
    type(expr<sub>2</sub>) = type(atomic-type)
```

• Result schema: $type(extend-expr) = type(expr_1) \cup (name(id): type(atomic-type))$

Definition of Variables (def-stat)

def-stat
$$| type - id_1 - id_2 - ... - id_k$$

• Constraint: $\forall i \in [1 ... k], \forall j \in [1 ... k], i \neq j$, (name(id_i) \neq (name(id_j)), $\forall i \in [1 ... k]$ (name(id_i) \notin Environment)

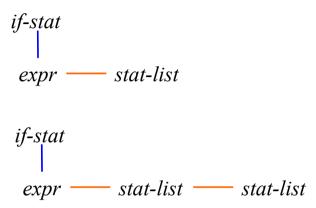
Assignment (assign-stat)

Constraint: visible(name(id)),type(id) = type(expr)



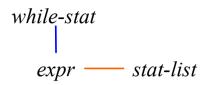
Conditional Statement (if-stat)

• Constraint: type(expr) = boolean



While Statement (while-stat)

• Constraint: type(expr) = boolean



Reading a Variable (read-stat)

```
read-stat
|
specifier — id
```

Constraint: visible(name(id)),
 (type(specifier) = nil or type(specifier) = string)

Compilers

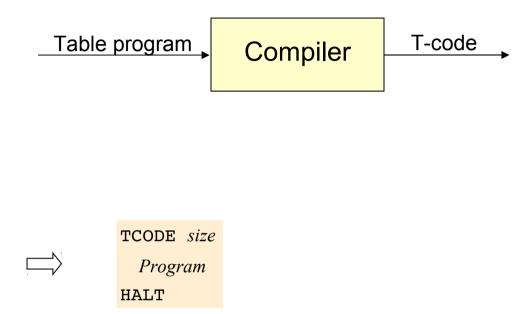
Writing a Value (write-stat)



• Constraint: (type(specifier) = nil or type(specifier) = string)

Intermediate Code Generation

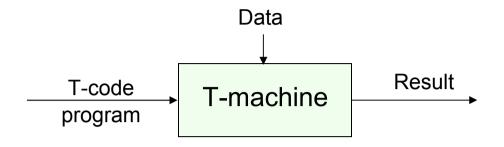
```
program
  integer min, max, i;
  string s;
  table(integer a, string b) R;
  if min == max then
    table(string c, boolean d) T;
    read T;
    write project [a, d]
          R join [ b == c ] T;
  else
    while(min != max) do
      integer i, j, s;
      min = i + j - max;
      boolean ok;
      . . .
    end
  end;
end
```

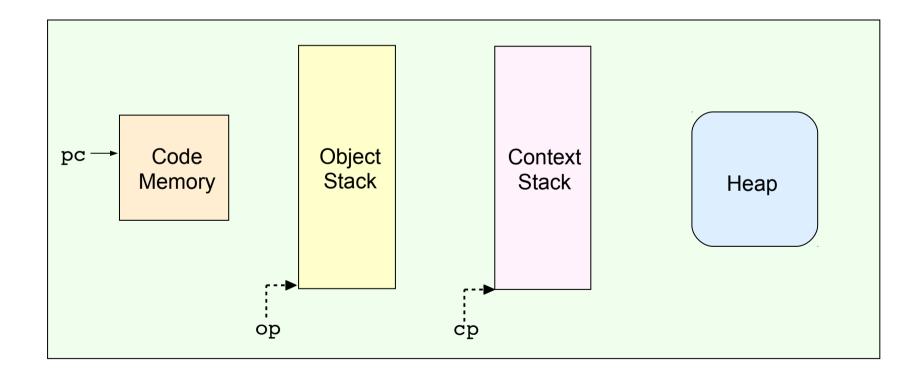


Design Choices

- Code directly addressable (without explicit labels)
- Address of a T-code stat = position of the stat within the generated code
- Variable descriptors allocated in the order in which variables are defined
- Variable identification: *oid* = position of the variable within the stack (0 .. *n*)
- Attribute identification: *context-offset, position-within-schema, attribute-size*
- Management of blocks by stack: exit from block → pop variables in block

Abstract Machine





Definition of Variables

• Two types of objects Atoms

```
integer min, max, i;
string s;
boolean b;
table(integer a, string b) R;
```

 \Rightarrow

```
NEWATOM | integer |
NEWATOM | integer |
NEWATOM | integer |
NEWATOM | string |
NEWATOM | integer |
NEWTAB | integer | + | string |
```

Notes:

■ atom (embedded instance): NEWATOM object-size

• table (instance in heap): NEWTAB tuple-size

Reference to Atomic Constants

Integer constant

y = 25;

LDINT 25

String constant

s = "<mark>alpha"</mark>;



LDSTR "alpha"

Boolean constant

b = true;

LDINT 1

• Note:

Boolean values: true, false → surrogated by integers: 1, 0

Reference to Table Constants

```
IATTR 1
                                                        SATTR "alpha"
table (integer i, string s, boolean b) t;
                                                        IATTR 1
                                                        IATTR 2
t = {(1, "alpha", true),
                                                        SATTR "beta"
     (2, "beta", false),
                                                        IATTR 0
     (3, "gamma, "true")};
                                                        IATTR 3
                                                        SATTR "gamma"
                                                        IATTR 1
                                                      ENDTAB
table (integer i, string s, boolean b) t;
                                                      LDTAB (|integer|+|string|+|integer|) 0
                                                      ENDTAB
t = {integer, string, boolean};
```

• Notes:

- tuple-size = size of tuples
- num-tuples = number of tuples
- \(\alpha \text{attribute loadings}\)\) = sequence of attribute-constant loadings

LDTAB tuple-size num-tuples ⟨attribute loadings⟩ ENDTAB

LDTAB (|integer|+|string|+|integer|) 3

Reference to Identifiers

Variable

```
x = y + 1;
t1 = t2;
tobelow{LOB ^y}
tobelow{LOB ^t2}
```

```
integer x, y;
table(integer a, boolean b) t1, t2;
table(integer c, string d) t3;
```

Attribute within current context

```
write
select [d == "alpha"] t3;
```

Attribute within external context

```
write
select [ exists [a > c] t1 ] t3;
```

Notes:

- Argument of LOB = oid (object identifier)
- Arguments of LAT = context-offset, attribute-offset, attribute-size
- For reference to attributes within predicate of join, attribute-offset in LAT refers to result schema (concatenation of operand schemas)

Assignment

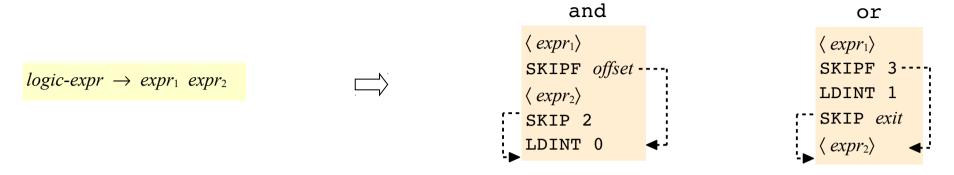
• Computation of assignment expression + assignment statement (STO)

$$x = expr;$$
 \Longrightarrow $\stackrel{\langle expr \rangle}{\Longrightarrow}$ STO \hat{x}

- Note:
 - Arguments of STO = oid (of assigned object)

Logical Operations (and, or)

LOB ^b



```
boolean a, b, c;

a = (b and c) or g;

LOB ^c

SKIPF 2

LDINT 0

SKIPF 3

LDINT 1

SKIPF 3

LDINT 1

SKIPF 2

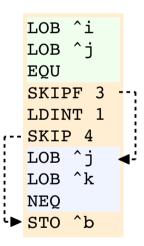
LOB ^g

STO ^a
```

- Short circuit evaluation
- SKIP = unconditional jump
- SKIPF = conditional jump
- Argument of SKIP, SKIPF = length of the jump (offset) $\begin{cases} exit = |\langle expr_2 \rangle| + 1 \\ offset = |\langle expr_2 \rangle| + 2 \end{cases}$

Comparison Operations: ==, !=

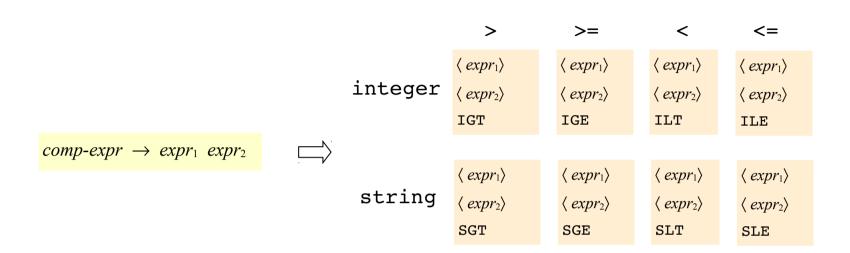
```
integer i, j;
boolean b;
b = (i == j or j != k);
```



• Note:

• EQU, NEQ: polymorphic for all types

Comparison Operations: >, >=, <, <=



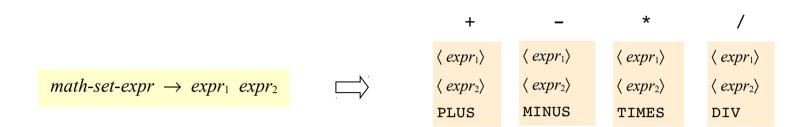
LOB ^i

```
integer i, j;
string x, y;
boolean b;

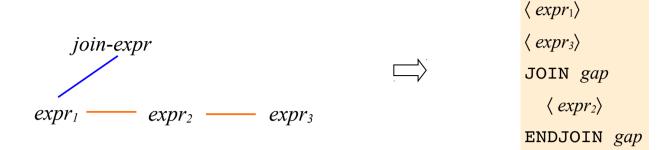
b = (i > j or x < y);

LOB ^j
IGT
SKIPF 3
LDINT 1
LOB ^x
LOB ^x
LOB ^x
LOB ^y
SLT
STO ^b</pre>
```

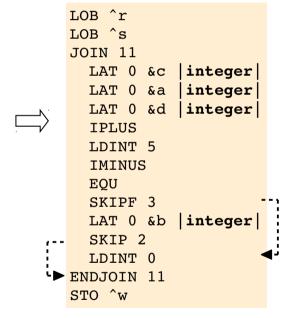
Arithmetic Operations: +, -, *, /,



Join

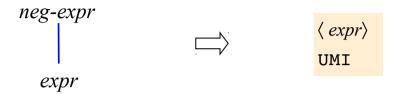


```
table(integer a, boolean b, integer c) r;
table(integer d, integer e) s;
w = r join [ c == a+d-5 and b ] s;
```



- $expr_2$ = predicate of join
- $gap = |\langle expr_2 \rangle|$
- Argument attribute-offset of LAT: computed on result (also for external contexts)
- Argument of ENDJOIN: = implicit jump (backward) to predicate of JOIN

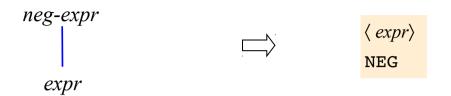
Change of Sign



```
integer i, j;
j = -i + 10;

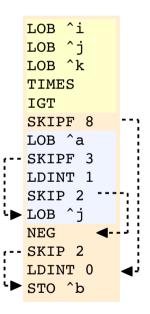
LOB ^i
UMI
LDINT 10
PLUS
STO ^j
```

Logical Negation



```
integer i, j, k;
boolean a, b;

b = i > j * k and not (a or j);
```



Projection

```
project-expr

expr \quad -i\mathbf{d}_{1} - i\mathbf{d}_{2} - \dots - i\mathbf{d}_{k}

PROJ k

ATTR attr-offset_{1} size_{1}

ATTR attr-offset_{2} size_{2}

...

ATTR attr-offset_{k} size_{n}

ENDPROJ

REMDUP
```

```
table(integer a, boolean b, string c) t;

w := project [ a, c ] t;

ENDPROJ

REMDUP

STO ^w
```

- Argument of PROJ (k) = | id-list |
- Each projection attribute is specified by an ATTR
- Need for duplicate removal by REMDUP

Rename

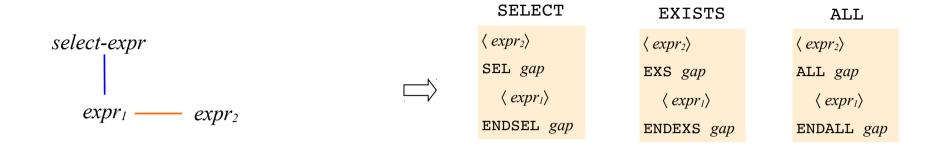


```
table(integer a, boolean b, string c) t;

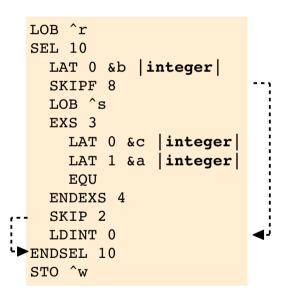
w := rename [ x, y, z ] t;
```

- Rename is relevant to semantic analysis only
- Code of rename coincides with code of its operand

Selection Operations: SELECT, EXISTS, ALL

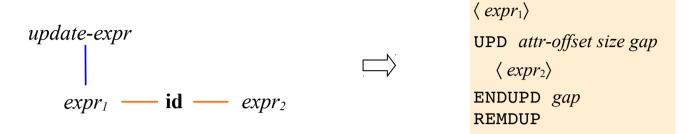


```
table(integer a, boolean b) r;
table(integer c, string d) s;
w = select [ b and exists [ c == a ] s ] r;
```



- *expr*₁ = selection predicate
- $gap = |\langle expr_1 \rangle|$

Update



```
integer i;
table(integer a, string b) t;
w = update [ a = i + 8 ] t;
```

```
LOB ^t
UPD &a |integer| 3
LOB ^i
LDINT 8
PLUS
ENDUPD 3
REMDUP
STO ^w
```

- $expr_2$ = update expression
- $gap = |\langle expr_2 \rangle|$
- need for duplicate removal (REMDUP)

Extend

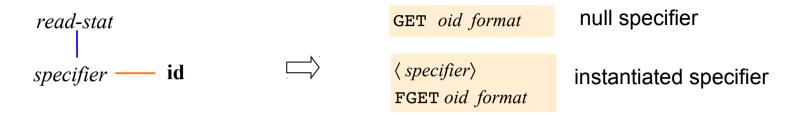
```
integer i;
table(integer a, string b) t;
w = extend [ integer c = a - i ] t;
```

```
LOB ^t
EXT |integer| 3
LAT 0 &a |integer|
LOB ^i
MINUS
ENDEXT 3
STO ^w
```

Notes:

- $expr_2$ = extension expression
- *size* = size of the new attribute
- $gap = |\langle expr_2 \rangle|$

Read



```
boolean k;
string s;
table(integer a, string b) t;

read k;
read t;
read [ s ] t;
GET ^k "b"
GET ^t "(a:i,b:s)"
LOB ^s
FGET ^t "(a:i,b:s)"
```

- oid = object to be instantiated
- format = string specifying the schema of the variable to instantiate

Write



```
⟨expr⟩
PRINT format

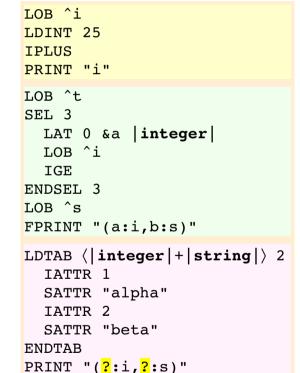
⟨expr⟩
⟨specifier⟩
FPRINT format
```

null specifier

instantiated specifier

```
integer i;
string s;
table(integer a, string b) t;

write i + 25;
write [ s ] select [ a >= i ] t;
write {(1, "alpha"),(2, "beta")};
```



Notes:

- expr = object to print
- specifier (if instantiated) = file name where instance is printed
- format = string specifying the schema of the object to instantiate
- If attribute without name → ?

Conditional Statement: if-then



```
integer i, j, k;
table(integer a, string b) t, r;

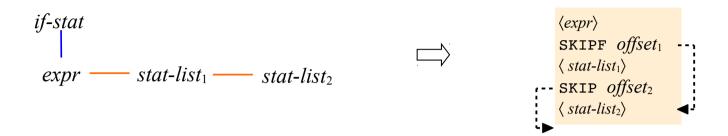
if i == j then
   t = select [ a > 0 ] r
end;
```

```
LOB ^i
LOB ^j
EQU
SKIPF 8
LOB ^r
SEL 3
LAT 0 &a |integer|
LDINT 0
IGT
ENDSEL 3
STO ^t
```

• Note:

• $offset = |\langle stat-list \rangle| + 1$

Conditional Statement: if-then-else

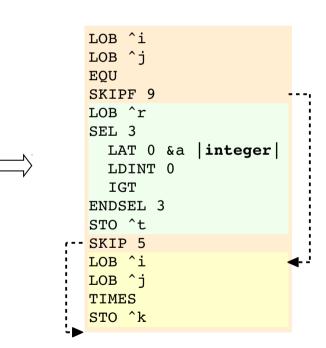


```
integer i, j, k;
table(integer a, string b) t, r;

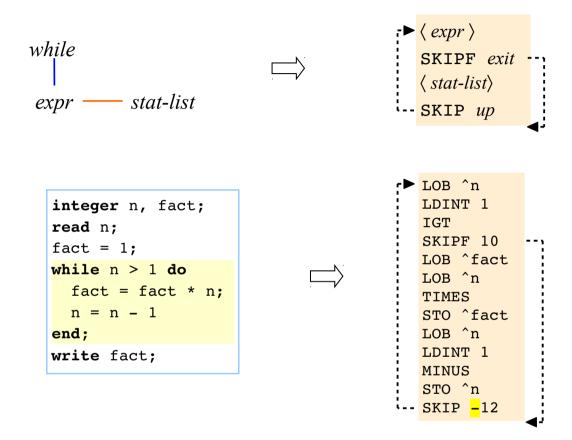
if i == j then
   t = select [ a > 0 ] r
else
   k = i * j
end;
```

Notes:

- $offset_1 = |\langle stat-list_1 \rangle| + 2$
- $offset_2 = |\langle stat-list_2 \rangle| + 1$

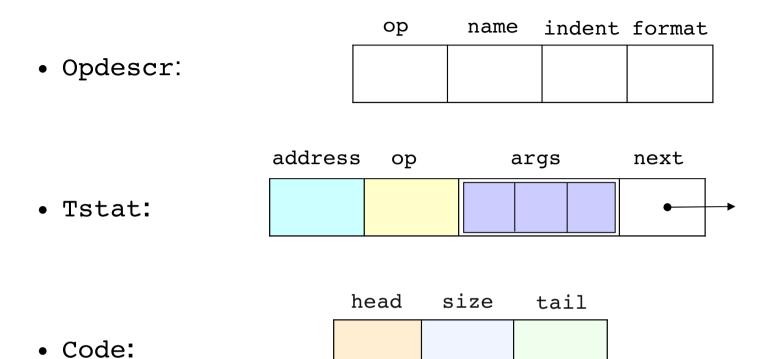


Loop



- $exit = |\langle stat-list \rangle| + 2$
- $up = -(|\langle expr \rangle| + |\langle stat-list \rangle| + 1)$

Data Structures for Code Generation



• Representation of a code segment (list of T-code statements):

