

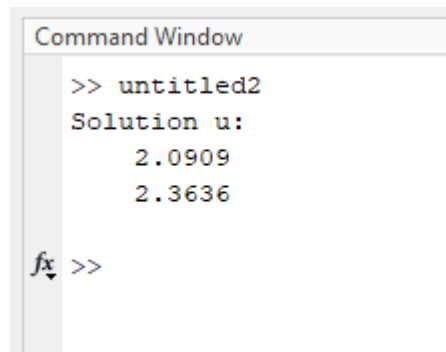
## TASK 5

**Q1) Utilize MATLAB's linear equation solvers (e.g., direct solvers, iterative methods) to solve the FEA system.**

### MATLAB'S Code using Direct Solver:

```
K = [4, -1; -1, 3];  
f = [6; 5];  
  
% Here I am using the direct solver method to solve fea  
u = K \ f;  
  
disp("Solution u:");  
disp(u);
```

### MATLAB COMMAND WINDOW OUTPUT:



### MATLAB'S Code using Iterative Solver:

```
K = [4, -1; -1, 3];  
f = [6; 5];  
  
% Set up the GMRES solver parameters  
tolerance = 1e-6;  
maxIterations = 2;  
  
% Solve the FEA system using GMRES iterative solver  
[u, flag, relres, iter] = gmres(K, f, [], tolerance, maxIterations);  
  
disp("Solution u:");  
disp(u);  
disp("GMRES solver info:");  
disp("Flag: " + flag);  
disp("Relative residual: " + relres);  
disp("Iterations: " + iter);
```

### MATLAB COMMAND WINDOW OUTPUT:

```
Command Window

>> untitled2
Solution u:
    2.0909
    2.3636

GMRES solver info:
Flag: 0
Relative residual: 0
    "Iterations: 1"    "Iterations: 2"

fx >>
```

**Q2) Check the accuracy of the results against known analytical solutions or commercial FEA software.**

### MATLAB'S Code:

```
K = [4, -1; -1, 3];
f = [6; 5];

% Analytical solution
u_analytical = inv(K) * f;

disp("Analytical Solution:");
disp(u_analytical);
```

**The results for the analytically solved question is:**

```
Command Window

>> untitled2
Relative error between FEA and analytical solutions:
    1

>> untitled2
Analytical Solution:
    2.0909
    2.3636
```

**Relative Error between u\_direct and u\_analytical:**

$$\text{relative\_error\_direct} = \text{norm}(u_{\text{direct}} - u_{\text{analytical}}) / \text{norm}(u_{\text{analytical}})$$

For the first value of u\_direct, u\_analytical that is **2.0909**.

$$= \frac{2.0909 - 2.0909}{2.0909}$$

$$= 0\% \text{ error}$$

For 2<sup>nd</sup> value of u\_direct and u\_analytical is **2.3636**.

$$= \frac{2.3636 - 2.3636}{2.3636}$$

$$= 0\% \text{ error}$$

**Relative Error between u\_iterative and u\_analytical:**

$$\text{relative\_error\_iterative} = \text{norm}(u_{\text{iterative}} - u_{\text{analytical}}) / \text{norm}(u_{\text{analytical}})$$

For the first value of u\_iterative, u\_analytical that is **2.0909**.

$$= \frac{2.0909 - 2.0909}{2.0909}$$

$$= 0\% \text{ error}$$

For 2<sup>nd</sup> value of u\_iterative and u\_analytical is **2.3636**.

$$= \frac{2.3636 - 2.3636}{2.3636}$$

$$= 0\% \text{ error}$$

**Conclusion:**

This means that FEA results (both direct and iterative) match the analytical solution perfectly in this case.