

## ECS171 HW2

### Note:

- 1) Initial weights are randomized in ann.m.
- 2) All error's are calculated using  $\text{abs}(A-B)$  instead of squared error.
- 3) --inputdata.m reads data from source file
  - converts information to matrix form,
  - gets rid of 1<sup>st</sup> column(useless information)
  - and outputs 1484\*9 matrix.
  - Last column contains numbers instead of class numbers.

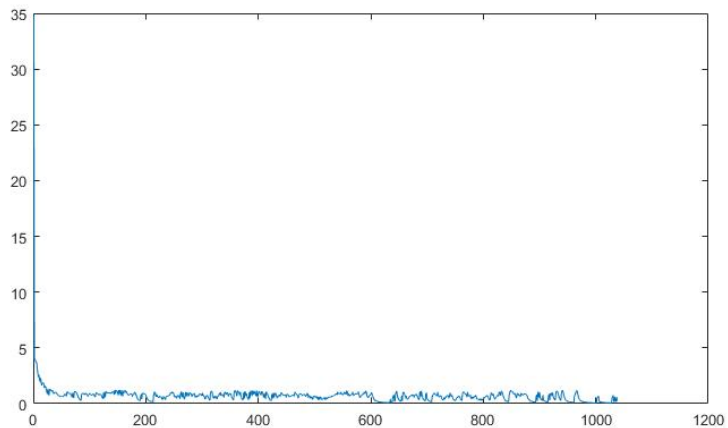
### Problem1:

files: inputdata.m ann.m hidden1node3.m;

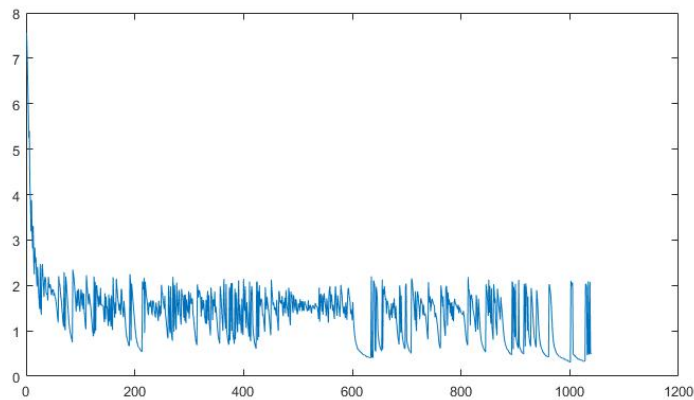
run command: hidden1node3

### Answers:

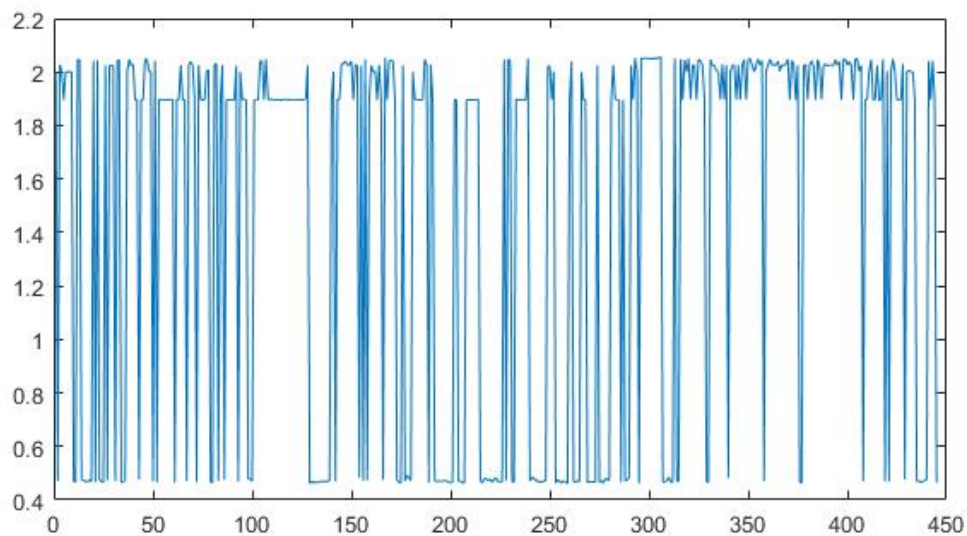
- 1) plot: training set weight change
  - x-axis—iteration from sample1 to 1039
  - y-axis—sum of weight change at each iteration



- 2) plot: training set error change
  - x-axis—iteration from sample1 to 1039
  - y-axis—sum of weight change at each iteration



- 3) testing set prediction outputs  
see variable "resultMatrix" in running result. Each row is a sample output
- 4) plot: testing error  
x-axis—testing sample from 1040 to 1484 (1 to 445)  
y-axis—testing error (sum of abs(y-prediction)), y is a binary vector



### Problem2:

files: inputdata.m ann.m p2.m;

run command: p2

Answers:

- 1) Training error: 2.2316e+3  
Training accuracy: 31.20%
- 2) final activation functions:  

$$\text{layer2 w}_0 = 1/(1-e^{-(0.5799 + 0.2050*x1 + 0.0185*x2 + 0.7567*x3 + 0.2863*x4 + 0.2050*x5 + 0.7936*x6 + 0.8179*x7 + 0.2333*x8)})$$

$$\begin{aligned} \text{layer2 } a_1 &= 1/(1-e^{-(2.4306 + 1.3397*x_1 + 1.4137*x_2 + 1.3028*x_3 + 1.2038*x_4 + 1.2391*x_5 + 0.8369*x_6 + 1.5090*x_7 + 0.6184*x_8)}) \\ \text{layer2 } a_2 &= 1/(1-e^{-(0.7457 + 0.2568*x_1 + 1.0288*x_2 + 0.3887*x_3 + 0.2940*x_4 + 0.2364*x_5 + 0.9021*x_6 + 0.1357*x_7 + 0.2316*x_8)}) \\ \text{layer2 } a_3 &= 1/(1-e^{-(1.9900 + 1.0449*x_1 + 1.4448*x_2 + 0.8066*x_3 + 1.0059*x_4 + 0.9440*x_5 + 0.5672*x_6 + 0.7562*x_7 + 0.2590*x_8)}) \\ \text{layer3 } a_1 &= 1/(1-e^{-(0.3705*w_0 - 0.1689*a_1(\text{layer2}) - 0.4609*a_2(\text{layer2}) - 0.2373*a_3(\text{layer2})))} \\ \text{layer3 } a_2 &= 1/(1-e^{-(0.0151*w_0 - 0.3841*a_1(\text{layer2}) + 0.0524*a_2(\text{layer2}) - 0.9907*a_3(\text{layer2})))} \\ \text{layer3 } a_3 &= 1/(1-e^{-(0.8521*w_0 - 0.8275*a_1(\text{layer2}) - 0.3918*a_2(\text{layer2}) - 0.0651*a_3(\text{layer2})))} \\ \text{layer3 } a_4 &= 1/(1-e^{-(0.8708*w_0 - 0.4023*a_1(\text{layer2}) - 0.5735*a_2(\text{layer2}) - 0.6999*a_3(\text{layer2})))} \\ \text{layer3 } a_5 &= 1/(1-e^{-(1.3159*w_0 - 1.0144*a_1(\text{layer2}) - 0.7337*a_2(\text{layer2}) - 0.6985*a_3(\text{layer2})))} \\ \text{layer3 } a_6 &= 1/(1-e^{-(1.0290*w_0 - 1.0607*a_1(\text{layer2}) - 0.6715*a_2(\text{layer2}) - 0.2691*a_3(\text{layer2})))} \\ \text{layer3 } a_7 &= 1/(1-e^{-(1.0740*w_0 - 0.6608*a_1(\text{layer2}) - 1.6932*a_2(\text{layer2}) - 0.6491*a_3(\text{layer2})))} \\ \text{layer3 } a_8 &= 1/(1-e^{-(1.0353*w_0 - 0.9082*a_1(\text{layer2}) - 0.8234*a_2(\text{layer2}) - 1.1014*a_3(\text{layer2})))} \\ \text{layer3 } a_9 &= 1/(1-e^{-(1.7476*w_0 - 0.9713*a_1(\text{layer2}) - 0.9509*a_2(\text{layer2}) - 0.7257*a_3(\text{layer2})))} \\ \text{layer3 } a_{10} &= 1/(1-e^{-(1.4387*w_0 - 1.0934*a_1(\text{layer2}) - 1.1992*a_2(\text{layer2}) - 1.0989*a_3(\text{layer2})))} \end{aligned}$$

Note:  $w_0$  here represents  $w_0*x_0$  where  $x_0$  is the constant 1

### Problem3:

files: inputdata.m ann.m p3.m;

run command: p3

files for reference: initial\_weights\_first\_round\_weights

Answers:

1) reference file has: initial weights, initial a's, first round weights.

Hand prove: use initial a and w to back propagate and get updated weights

Compare updated weights and first round weights (1<sup>st</sup> iteration of sample 1):

For the 2<sup>nd</sup> layer weights, hand calculation and computer results are extremely similar

For the 1<sup>st</sup> layer weights, hand calculation and computer results differ by a very small amount. It is possibly due to rounding error since I didn't use full floating-point values for my calculation.

Layer 1

$$\frac{\partial RSS}{\partial w_{ji}^1} = - \sum_k f_k^3 \cdot w_{kj}^2 \cdot a_j^2 (1-a_j^2) \cdot a_i^1$$

Layer 2

$$w_{kj}^2 = w_{kj}^2 - 1 \cdot \frac{\partial RSS}{\partial w_{kj}^2}$$

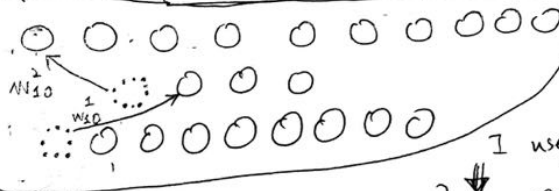
$$\frac{\partial RSS}{\partial w_{kj}^2} = - f_k^3 \cdot a_j^2$$

$$f_k^3 = (y_k - a_k^3) \cdot a_k^3 \cdot (1-a_k^3)$$

$$y = [0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 0 \ 0]$$

3rd

Note: layer 1 first row of  $w$  is never updated because  $w \cdot x_0$  is not involved in activation functions



layer 2

$$w_{10}^2 = w_{10}^2 + 1 \cdot (y_1 - a_1^3) \cdot a_1^3 (1-a_1^3) \cdot a_0^2 = 0.3902$$

$$w_{11}^2 = w_{11}^2 + 1 \cdot (y_1 - a_1^3) \cdot a_1^3 (1-a_1^3) \cdot a_1^2 = 0.4350$$

$$w_{12}^2 = w_{12}^2 + 1 \cdot (y_1 - a_1^3) \cdot a_1^3 (1-a_1^3) \cdot a_2^2 = 0.7127$$

$$w_{13}^2 = w_{13}^2 + 1 \cdot (y_1 - a_1^3) \cdot a_1^3 (1-a_1^3) \cdot a_3^2 = 0.9144$$

$$w_{20}^2 = w_{20}^2 + 1 \cdot (y_2 - a_2^3) \cdot a_2^3 (1-a_2^3) \cdot a_0^2 = 0.5230$$

$$w_{21}^2 = w_{21}^2 + 1 \cdot (y_2 - a_2^3) \cdot a_2^3 (1-a_2^3) \cdot a_1^2 = 0.0030$$

$$w_{30}^2 = w_{30}^2 + 1 \cdot (y_3 - a_3^3) \cdot a_3^3 (1-a_3^3) \cdot a_0^2 = 1.0158$$

$$w_{10,0}^2 = w_{10,0}^2 + (y_1 - a_{1,0}^3) \cdot a_{1,0}^3 (1-a_{1,0}^3) \cdot a_0^2 = 0.5952$$

I used calculator to do the calculation

computer

$$\sim 0.5231$$

$$\sim 0.0031$$

computer

layer 1

$$w_{10}^1 = w_{10}^1 + \sum (y_k - a_k^3) \cdot a_k^3 (1-a_k^3) \cdot w_{k1}^2 \cdot a_1^2 (1-a_1^2) \cdot a_0^1 = 0.7458 \sim 0.7566$$

$$w_{11}^1 = w_{11}^1 + \sum (y_k - a_k^3) \cdot a_k^3 (1-a_k^3) \cdot w_{k1}^2 \cdot a_1^2 (1-a_1^2) \cdot a_1^1 = -0.0219 \sim -0.0151$$

$$w_{12}^1 = w_{12}^1 + \dots \cdot a_2^1 = 0.3899 \sim 0.3965$$

$$w_{34}^1 = w_{34}^1 + \sum (y_k - a_k^3) \cdot a_k^3 (1-a_k^3) \cdot w_{k3}^2 \cdot a_3^2 (1-a_3^2) \cdot a_4^1 = 0.3228 \sim 0.3237$$

$$w_{38}^1 = w_{38}^1 + \dots \cdot a_8^1 = 0.9177 \sim 0.9191$$

**Problem4:**

files: inputdata.m ann.m p4.m;

run command: p4

Answers:

Call function ann recursively to get 3\*4 testing set error matrix

1) Testing set error matrix:

```
780.5943  750.2627  733.4707  1005.679
777.2998  740.4118  728.7110  1676.981
782.5728  739.3853  892.8145  2780.879
```

---After running the code for several times and increasing # nodes per hidden layer/# hidden layers, (I tried 10\*10 matrix) I observed that:

- a) Larger #nodes per hidden layer, larger error
- b) Larger #hidden layers, slightly larger errors (true when learningRate > 1)
- c) Larger #hidden layers, less variation for each prediction output (looking at "resultMatrix" for 445 testing samples)

---I think observations could differ (especially for "a)") if we had a larger sample size so that the program could learn better; increasing # hidden layers largely increases complexity of the model (needs more input information).

---Testing accuracy behaves similar to error, being around 0.3281 for most attribute combinations.

2) For our attribute combinations, I picked 3 nodesPerLayer, 3 hiddenLayers for optimal configuration (for prediction in next problem).

**Problem5:**

files: inputdata.m ann.m p5.m;

run command: p5

Answers:

(use 3 nodesPerHiddenLayer, 3 hiddenLayers)

The unknown sample was classified to:

class 1 for most of the time,

class 2 sometimes since the probability is similar to class 1,  
other classes very rarely.

--Prediction output shown after running the code.

**Problem6:**

files: inputdata.m p6.m;

run command: p6

Answer:

---For uncertainty, I defined a value called "variation".

---First, calculate the means for each feature by averaging the inputs from 1484 samples, calling it "feature\_avg".

---Then, given an unknown sample, I took the abs(feature\_avg[i]-sample\_feature[i]), and then took the sum of the absolute values for 8 features. I called this value "variation"---how far away is the unknown input from the average sample inputs.

---Then for the uncertainty, I divided the variation by the sum of feature\_avg, and multiply it by 100 to get the percent uncertainty.

For the previous unknown sample:

Variation(uncertainty): 0.273039

Uncertainty(percent uncertainty): %8.953347