



Functional Programming Concepts

Features

- Defines output of a program as a function of input
- Miranda, Haskell, PH, Sisal, Single Assignment C
- **Features**
- First class function values & higher order functions
 - Can be passed as parameter, returned from function or assigned into a variable
- Extensive polymorphism
- Supports list types and operators
- Structured function returns
- Constructors for structured objects
- Garbage collection

Scheme

- Dialect of Lisp
- Emerged from MIT in mid 1990
- Small size
- Use of static scoping
- Function is a first class entity

Scheme Interpreter

- Read-eval-print loop
- EVAL function

$(+3\ 4) \Rightarrow 7$

$7 \Rightarrow 7$

- Each parameter expression is evaluated
- Primitive function '+' is applied
- Result is displayed
- Read i/p from file
- `(load"my_scheme_pgm")`

- $+, -, *, /$
- $*$ and $+$ takes 0 or more parameters
- If $*$ is given no parameter
- It returns 1
- If $+$ is given no parameter
- -It returns 0
- $/$ - takes 2 or more parameters
- Uses Cambridge polish notation for expressions

- $(+ 3 4) \Rightarrow 7$
- $((+ 3 4)) \Rightarrow \text{error}$
- When inner parenthesis found
 - Calls function '+' passing 3 and 4 as arguments
- When outer parenthesis found
 - Calls 7 as a zero argument function which is a runtime error
- **Sqrt**
- Returns square root of non-negative numeric parameters

Defining Functions

- Scheme program is a collection of functions
- Nameless functions are defined using lambda expressions
- Lambda expressions are unnamed functions of the form:
- (lambda(id..) exp)
- (id...) -> list of formal parameters
- exp --> body of lambda expression

`((lambda (x) (* x x))`

`((lambda (x) (* x x)) 3) \Rightarrow 9`

- `x`-> bound variable
- Keyword `DEFINE` serves 2 purposes
- To bind a name to value
- To bind a name to a lambda expression

To Bind a Name to Value

- (define symbol expression)
- (define pi 3.14)
- (define two_pi(* 2 pi))
 pi=> 3.14
 two_pi=> 6.28
- Rules for creating names:
 - Can have letters,digits and special symbols
 - Paranthesis must be used
 - Must not begin with digit
 - They are case sensitive

- `(define(function-name parameters)
(expression))`
- `(define (square number)(* number number))`
- `(square 5) => 25`
- `(define min (lambda (a b) (if (< a b) a b)))`
- `(min 123 456) => 123`


Output Functions

- (display expression)
- (newline)

Numeric Predicate Functions

- Predicate functions return a boolean value

Function	Meaning
=	Equal
<>	Not equal
>	Greater than
<	Less than
>=	Greater than or equal to
<=	Less than or equal to
Even?	Is it an even number?
Odd?	Is it an odd number?
Zero?	Is it zero?
(boolean? X)	Is x a boolean?


- 
- (char? x) ; is x a character?
 - (string? x) ; is x a string?
 - (symbol? x) ; is x a symbol?
 - (number? x) ; is x a number?
 - (list? x) ; is x a (proper) list?

Example

- (negative?-6) returns t
- (zero?44) return f
- (>6,2) returns t

Symbols

- procedure: symbol?Object
 - Returns true if the object is a symbol, otherwise returns false
 - (symbol? 'x\$_%:&=*!)
- \implies #t


- 
- Type is not determined at runtime
 - `(if(> a 0)(+2 3)(+ 2 "foo"))`
 - Will evaluate to 5 if 'a' is positive
 - Will produce a type clash error if 'a' is negative or 0

Quote

- Prevent interpreter from evaluating an expression
- $(\text{quote } A) \iff '(A) \implies A$
- $(\text{quote } (+\ 3\ 4)) \implies '(+\ 3\ 4) \implies (+\ 3\ 4)$
- $'3; \implies 3$
- $""hi"; \implies "hi"$
- $'a; \implies a$
- $'(+3\ 4); \implies (\text{list}' +\ '3\ '4)$
- $'(abc); \implies (\text{list}\ 'a\ 'b\ 'c)$

Control Flow

- If and cond constructs are available
- If has 3 parameters
- (if predicate then_expression else_expression)
- $\text{if}(<2\ 3)4\ 5) \Rightarrow 4$
- $\text{(if \#f 2 3) } \Rightarrow 3$




```
(define (compare x y)
  (cond
    ((> x y)" x is greater than y")
    ((< x y)"y is greater thanx")
    (else "x and y are equal")
  )
)
```

Bindings- Nested Scope

- Names can be bound to values by introducing a nested scope:
- 'let' creates a new local static scope
- Short hand for lambda expressions

```
(let ((alpha 7))  
  (* 5 alpha)  
)
```



```
(let ((a 3)
```

```
(b 4)
```

```
(square (lambda (x) (* x x)))
```

```
(plus +))
```

```
(sqrt (plus (square a) (square b))))  $\Rightarrow$  5.0
```

- let evaluates all bindings with respect to the level above it
- let* does it sequentially

(let ((a 3))

(let ((a 4)

(b a)) -Since b is assigned a before the definition for
2nd a is completed, b takes the value of 1st a

(+ a b))) \Rightarrow 7

(let ((a 3))

(let* ((a 4)

(b a)) -Since b is assigned a, it takes the value of a just
above it

(+ a b))) \Rightarrow 8

- letrec allows to bind recursive values
- (letrec ((fact (lambda (n)
- (if (=n 1)
- 1
- (* n(fact(-n 1)))))))
- (fact 5)=> 120

List and Numbers

- 3 main functions to manipulate lists
- car - which returns the head of a list
- cdr - everything after the head
- cons-joins a head to the rest of a list

$(\text{car } '(2\ 3\ 4)) \Rightarrow 2$

$(\text{cdr } '(2\ 3\ 4)) \Rightarrow (3\ 4)$

$(\text{cons } 2\ '(3\ 4)) \Rightarrow (2\ 3\ 4)$

Equality Testing and Searching

- General Purpose - eq? eqv? equal? can be used
- Eq? check if 2 parameters represent the same object
- Eqv? – if they have same value
- Equal? – checks for recursive values
- (eq? x y)

- `eqv?` returns true for same primitive values
`(eqv? 2 2) => t`
`(eqv? "a" "a") => t`
- `equal?` - test lists, vectors etc.,

```
(define(x '(2 3))  
(define(y '(2 3))  
(eq?(x y)) => #f  
(equal? x y) => t  
(define y x)  
(eq? x y) => t
```


Search elements in List

- 3 functions are there- memq, memv and member
- Each one takes an element and a list as argument and returns longest suffix of list
- memq uses eq, memv uses eqv and member uses equal
- $(\text{memq } 'z \text{ } (x \ y \ z \ w)) \implies (z \ w)$
- $(\text{memv } '(z) \text{ } (x \ y \ (z) \ w)) \implies \#f$
(recursive)
- $(\text{member } '(z) \text{ } (x \ y \ (z) \ w)) \implies ((z) \ w)$

Association (A-list)

- The functions `assq`, `assv`, and `assoc` search for values in *association lists*
- *List is a dictionary*
- *1st element – key*
- *2nd element- information*
- `Assq` uses `eq` , `assv` uses `eqv`, and `assoc` uses `equal` to search in alist

- `(define e '((a 1)(b 2) (c 3)))`
- `(assq 'a e) => (a 1)`
- `(assq 'b e) => (b 2)`
- `(assq 'd e) => f`
- `(assoc '(a) '(((a)) ((b)) ((c)))) => ((a))`
- `(assv 5 '((2 3) (5 7) (11 13))) => (5 7)`

- 
- Scheme do not support side effect
 - It is supported by
 1. Assignment
 2. Iteration
 3. Sequencing

Assignment

(let ((x 2) ; initialize x to 2

(l '(a b))) ; initialize l to (a b)

(set! x 3) ; assign x the value 3

(set-car! l '(c d)) ; assign head of l the value
(c d)

(set-cdr! l '(e)) ; assign rest of l the value (e)

... $x \Rightarrow 3$

... $l \Rightarrow ((c\ d)\ (e))$

Sequencing

Controls the flow of control

```
(begin  
  (display "hi ")  
  (display "mom"))
```


Iteration - do

```
(do ((<var1> <init> <step>))  
    (<test> <exp>)  
    <command>)  
(define i 0)  
(do()  
  ((=i 5))  
  (display i)  
  (set! i(+ i 1))))  
01234
```


for-each

- `(for-each (lambda (a b) (display (* a b))
(newline)))`
- `'(2 4 6)`
- `'(3 5 7))`
- `// a and b are 2list`
- `6 20 42 ()`

Programs as Lists

```
(define compose  
  (lambda (f g)  
    (lambda (x) (f (g x)))))  
((compose car cdr) '(1 2 3))  $\Rightarrow$  2
```

- Compose takes a pair of function as arguments
- It returns a function that takes x as parameter, as result



```
(define compose2
  (lambda (f g)
    (eval (list 'lambda '(x) (list f (list g 'x)))
          (scheme-report-environment 5))))
((compose2 car cdr) '(1 2 3))  $\Rightarrow$  2
```

- eval function evaluates a list
- compose2 performs same function
- Function list returns a list that is evaluated
- 2nd argument to eval is the RE in which expression is to be evaluated

Eval *and* Apply

Takes scheme object and evaluates it

```
(define fn '*)
```

```
(define x 3)
```

```
(define y(list '+ x 5))
```

```
(define z(list fn 10 y))
```

```
x => 3
```

```
y => (+3 5)
```

```
(eval y) => 8
```

```
(eval z) => 80
```

Example 2

- `(define a 'b)`
- `(define b 'c)`
- `(define c 50)`
- `a=>b`
- `(eval a) = c`
- `(eval(eval a)) =>50`

Apply

- Apply takes two arguments: a function and a list
- Apply a function to an expression
- `(apply factorial '(3)) => 6`
- `(apply + '(1 2 3 4)) => 10`
- `(define (sum s) (apply + s))`
- `(sum '(1 2 3)) => 6`

Evaluation Order

- Applicative order: Evaluate arguments before
- Normal Order: Pass arguments unevaluated
- Scheme -> Applicative order
- (define double(lambda(x)(+x x)))

Applicative Order Evaluation

```
(define double(lambda(x)(+ x x)))
```

```
(double(* 3 4))
```

```
(double(12))
```

```
=> (+ 12 12)
```

```
=> 24
```

Normal Order Evaluation

```
(define double(lambda(x)(+ x x)))
```

```
(double (* 3 4))
```

```
 $\Rightarrow (+ (* 3 4) (* 3 4))$ 
```


```
 $\Rightarrow (+ 12 (* 3 4))$ 
```


```
 $\Rightarrow (+ 12 12)$ 
```

```
 $\Rightarrow 24$ 
```

Strictness and Lazy Evaluation

- Evaluation order effects execution speed and program correctness
- Program that finds dynamic semantic error or infinite loop in applicative order may terminate in normal order
- Applicative order - faster

- 
- A strict function denoted an expression which does not return a normal value
 - either because it loops endlessly
 - because it aborts due to an error such as division by zero
 - A function which is not strict is called **non strict**

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- Strict language - functions are always strict
 - NonStrict language - allow non strict functions
 - Strict language follows applicative order evaluation
 - ML and Scheme - strict
 - Miranda and Haskell - nonstrict

Lazy Evaluation

- Lazy evaluation uses normal order evaluation
 - - Arguments are not evaluated unnecessarily
- Tag every argument with a memo indicating that its value is known
- Attempt to evaluate argument sets value in memo or returns value if already set
- Useful for infinite data structures

Example

- ```
(define double(lambda(x)(+ x x)))
(define f
 (lambda ()
 (let ((done #f) ; memo initially unset
 (memo '())
 (code (lambda () (* 3 4))))
 (if done memo ; if memo is set, return it
 (begin
 (set! memo (code)) ; remember value (set! done #t)
 memo)))))) ; and return it

...
(double (f))
=> (+ (f) (f))
=> (+ 12 (f)) ; first call computes value
=> (+ 12 12) ; second call returns remembered value
=> 24
```

# Delay and force

- Lazy evaluation is available in Scheme
- The delay primitive returns a promise
- redeemed by the force primitive

- (delay expr) => promise
- (force promise) => value

- | ● <b>Expression</b>               | <b>Value</b> |
|-----------------------------------|--------------|
| ● (delay(+ 5 4))                  | #Promise     |
| ● (let((delayed(delay (+ 5 6 )))) |              |
| ● (force delayed))                | 11           |