

1. Write an alternate quicksort algorithm as discussed in class. The partitioning will be with the help of two pointers  $l$ ,  $r$ .  $l$  moves left to right and  $r$  moves right to left from the end. And everything that is to the left of  $l$  is less than the pivot, and everything to the right of  $r$  is greater than the pivot.
2. Here is an alternative sorting algorithm called Pancake sorting which uses only one operation `flip(arr, i)` which flips the elements  $0 \dots i$ . For example `flip([1,2,3,4,5],2)` returns `[3,2,1,4,5]`. The sorting algorithm is as follows

```

pancake_sort(array, n)
    cur_size = n
    while cur_size > 1
        max_index = find_max(arr[:cur_size])
        if max_index != (cur_size - 1)
            flip(arr, max_index)
            flip(arr, cur_size-1)
        cur_size = cur_size - 1

```

Code up the algorithm and the functions i.e. `flip`, `find_max` and `pancake_sort`

3. Write a function `product_map` which when given an array of elements `arr` output a new list `out` such that, `out[i]` is the product of the first largest, second largest and third largest elements among `arr[0..i]`. If there is less than 3 elements output -1. For example :  
`product_map([1,2,3,4,5]) = [-1,-1,6,24,60]`

Hint: Use the heap implementation.

4. Implement a class `Matrix` which represents a two dimensional matrix.
  - (a) The constructor will receive an array `arr`, two integer values  $n$  and  $m$ . Where  $n$  represents the number of rows and  $m$  represents the number of columns. `arr` contains the elements left to right of a row and rows are ordered top to bottom.  
 For example

$$M = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix}$$

the matrix will be instantiated as follows

```
m = Matrix([1,2,3,4,5,6], 2, 3)
```

- (b) Implement a member function `row` which takes the index of the row and returns the elements of that row.
- (c) Implement a member function `column` which takes the index of the column and returns the elements of that column.

- (d) Implement a member function `transpose` which transposes (interchanges rows and columns) the current matrix and changes the dimensions respectively. For example, transpose of

$$M = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix}$$

will be

$$M = \begin{bmatrix} 1 & 4 \\ 2 & 5 \\ 3 & 6 \end{bmatrix}$$