

# FE312: Homework 5

## 1 Martingale Asset Management

1. Go to the website of Martingale Asset management at <http://www.mgale.com/index.html>
2. Read the information about the 130/30 strategies and their low-volatility strategy.
3. A short extension strategy seeks to enhance the return on a benchmark index by relaxing the long-only constraint in traditional active portfolios. This is achieved by shorting a small portion of the portfolio value and offsetting the short positions with an equal value of additional long positions so as to be net 100% long. A structure popular among short extension funds is a long exposure of 130% of equity capital and a short exposure of 30%, for a net long exposure of 100% and a shorting ratio of 30%. Martingale was one of the first asset managers to offer short extension funds in 2004
4. Martingale's strategy consists of over-weighting low-vol (or low beta) stocks and under-weighting high-vol (or high-beta stocks). Do you think this is a good strategy?
5. To help you evaluate the risk and return of the low-vol strategy, I have constructed 5 portfolios of firms sorted on past total vol. You can find the data in HW5\_DATA.xls, part A. I have also included the risk-free rate and excess returns on the market portfolio. Compute:
  - Average returns and standard deviations for these 5 vol-sorted portfolios.
  - Compute the market beta of each portfolio. Are the average returns on these five portfolios proportional to their market beta?
  - Let's construct our own version of Martingale's 130/30 strategy (ignoring transaction costs) as follows:
    - Invest 100% into the market portfolio

- Invest 30% into the low-vol strategy
- Short 30% of the hi-vol strategy

How does this strategy compare with the market portfolio?

6. What do you think of Martingale as a firm? Does it have an edge in investing?
7. Do you believe the Risk Anomaly (the beta-adjusted underperformance of high volatility stocks) will persist? How confident are you that the historical performance isn't simply data mining?

## 2 Dimensional Fund Advisors

Dimensional Fund Advisors (DFA) is a Santa Monica money management firm. Among many of their U.S. equity strategies, the “9-10 Small Company Strategy” invests in securities of U.S. companies whose market capitalization is in the size range of deciles 9 through 10 of the NYSE (bottom 20 percentile). Their second main strategy is the “US 6-10 Value Portfolio”, which invests in securities of U.S. companies whose book-to-market ratio falls in the 6 to 10 deciles of the NYSE (above the median).

The strategies' NASDAQ symbols are dfscx and dfsvx respectively. The dataset for this assignment is HW5\_DATA.xls, part B. It contains monthly returns on the DFA small cap fund (dfscx) and the DFA value fund (dfsvx), along with returns on the market portfolio, the 2 Fama-French Factors SMB and HML, Carhart's “Momentum” factor and the risk-free rate. The sample ranges from January 1982 to January 2009, except for the value fund which was conceived in April 1993.

1. Identify the two worst performing months for dfscx and dfsvx respectively, as well as its two best performing months. During these extreme months, what happened to the market portfolio? What happened to the SMB, HML, and Momentum portfolios?
2. Over the entire sample, how does dfscx and dfsvx perform in comparison with the market portfolio? Report the mean (in excess to the riskfree rate) and the standard deviation of dfscx and dfsvx, and compare them with those of the market portfolio. Does DFA's small company and value strategies have a higher Sharpe Ratio than the market portfolio? Report your numbers in annualized terms.

3. Lets try to explain the monthly realized returns  $R$  using the four empirical factors we examined in Part 1

$$R_{i,t} - R_{f,t} = a + b_i(R_{M,t} - R_{f,t}) + s_i R_{SMB,t} + h_i R_{HML,t} + w_i R_{MOM,t} + u_t$$

where  $a$  is the intercept,  $b$ ,  $s$ ,  $h$ , and  $w$  are the regression coefficients measuring the sensitivity of the “9-10 Small Company Strategy” or the “6-10 Value Portfolio” to the four empirical factors. Run the above multi-factor regression using Stata. Use your regression results to answer the following questions.

4. Given that dfscx follows a small cap strategy, one would assume that  $s$  is a very significant number. Can you confirm that? Also, given that dfsvx is supposedly following a value strategy, one would expect that  $h$  would be statistically significant. Is it true?
5. Is there any evidence that either fund follows the “Momentum” strategy?
6. Overall, how much variation of each funds return can be explained by the four empirical factors?
7. Does either fund provide any statistically positive (or negative) excess return that cannot be explained by the four empirical factors?
8. Compute Jensen’s alpha and the Appraisal Ratio for DFA’s small cap and value strategies. Which of the two funds (if any) would you recommend to investors? Would your answer change if these investors were otherwise restricted to hold the market portfolio?



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## Martingale Asset Management LP in 2008, 130/30 Funds, and a Low-Volatility Strategy

In early July 2008, William (Bill) Jacques, executive vice president, chief investment officer, and one of the founders of Martingale Asset Management, a quantitative, value-oriented investment management firm in Boston, Massachusetts, was busy preparing for an upcoming meeting with the group that made new product decisions within the firm. The objective of the meeting was to review the investment results of a new strategy that Martingale had been running with its own money for six full months and to discuss next steps.

Next to his desk, hanging on the only nonglass wall in his office, was Jacques's favorite artwork. It was a large wooden map of the United States covered with vintage license plates from the 1960s and 1970s cut in the shape of each state. The combination of colors, shapes, numbers, and letters had a pleasant effect on the eye, while at the same time keeping the brain busy reading and searching for information in the old license plates. To Jacques, this artwork epitomized Martingale's approach to investment: innovate by making connections between seemingly disparate ideas and blending them together to create something new and valuable.

The new strategy certainly reflected this motto. It was inspired by published research showing that portfolios of stocks built to have low historical volatility not only continued to have low volatility in subsequent periods but also exhibited returns that were at least as good as the returns on broad-based stock indexes such as the S&P 500 or the Russell 1000. Martingale's insight had been to develop a minimum variance strategy within the framework of a 130/30 fund, of which Martingale had been an early adopter and promoter. Also known as short extension strategies, 130/30 funds were portfolios that relaxed the long-only constraint of traditional managers by allowing a limited amount of shorting. A 130/30 fund typically invested long \$130 for each \$100 of equity capital and took short positions worth \$30.

The performance of the strategy thus far had been strong, confirming the extensive back-testing results that Jacques and his investment team at Martingale had been conducting for months prior to launching the strategy in late December 2007. (See **Exhibit 9** for the performance of Martingale's back-tested portfolio). Yet Jacques felt the group needed to have another in-depth discussion of the strategy. While Jacques believed that markets were not perfectly efficient all the time—Martingale thrived on discovering market anomalies and exploiting them for the benefit of its investors—he felt that this apparent anomaly challenged one of the basic tenets of investing: that broad-based portfolios of assets should exhibit a positive relation between risk and return.

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Professor Luis M. Viceira and Research Associate Helen H. Tung prepared this case. HBS cases are developed solely as the basis for class discussion. Cases are not intended to serve as endorsements, sources of primary data, or illustrations of effective or ineffective management.

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Thus, Jacques still wondered whether this was truly a market anomaly, or whether it was simply a fluke of the data, a spurious pattern that was unlikely to persist in the future. Jacques had some ideas about what might lead investors to not demand higher returns on more volatile stocks that he wanted to discuss with his group. He was particularly eager to discuss them with Arnold (Arnie) Wood, president and a founder of Martingale who was a highly respected expert in behavioral finance. Wood's input would be critical before Jacques encouraged Martingale to offer a 130/30 low-volatility product to outside investors.

## The Firm and Its Investment Process

Martingale, a quantitative, value-oriented investment management firm located in Boston, Massachusetts, was founded in 1987 by Alan Strassman, Arnold (Arnie) Wood, William (Bill) Jacques, and Patricia O'Connor, who all shared a common vision about how to structure an asset manager and a core set of investment beliefs. The founding partners had previously worked together for over 10 years at Batterymarch Financial Management, an asset management firm that had been one of the first to pioneer index investing and value investing strategies packaged for institutional investors in the 1970s.

By 2008, Martingale managed approximately \$5 billion in traditional equity, long/short, and short extension U.S. equity portfolios for 40 institutional clients, which included public and private pension funds, endowments, and state funds. (See **Exhibits 1** and **2** for information on Martingale strategies.)

Martingale had 21 employees, including 12 partners, who all worked in the Boston office. The firm was wholly owned by its employees, with its four founding partners owning the majority of the partnership. The founders remained active in the daily operations of the firm. They also maintained close working relationships with a number of academics and encouraged research in areas of interest to the firm.

Martingale's investment team believed that markets were relatively efficient in the long run and avoided making bets that involved any kind of market timing. But they also believed that mispricing anomalies existed at the individual stock level caused by investors for whom emotions interfered with sound judgment. Martingale pursued research to identify these anomalies and exploited them for the benefit of its clients. The development of investment strategies was supported and enhanced by Wood's expertise in behavioral finance and knowledge of the academic and practitioner research in this area.

But a culture of forward thinking was only the starting point for the development of profitable investment strategies. Martingale's founders also believed in the discipline of quantitative methods for portfolio construction and in the value of execution to minimize implementation costs.

An example of Martingale's approach to investing was the LargeCap Value 200 strategy, launched in 1996. Martingale's insight was that investors probably were significantly underweighting the largest stocks in the market in the belief that they were fairly valued because of their extensive analyst coverage and the tendency of active managers to focus attention on smaller-sized stocks. After careful examination of the prices of these stocks relative to their fundamentals, the insight that large capitalization stocks might be misvalued proved to be correct. This led to a quantitative value strategy that invested in the top 200 stocks in the Russell 1000 Index, which had returned 9.1% per year since inception in July 1996 through June 30, 2008 versus 7.9% in the Russell Top 200 Value Index and 7.3% in the S&P 500.

In selecting stocks, Martingale used a proprietary, multifactor, security valuation model. First, it valued stocks based on ratios such as price-one-year forward earnings, and price-cash earnings. Second, it found undervalued stocks by looking at growth characteristics such as internally financed sustainable growth rates. Other factors in the valuation model included relative strength, management quality, and analysts' earnings estimate revisions. Martingale did not meet with company management or listen to company conference calls in order to avoid the human tendency to develop biased judgment after meeting people. Martingale generated its investment research internally. It did not pay for external research through commissions, and it did not participate in soft dollar trading.

Martingale used these criteria to rank stocks within an industry from undervalued to overvalued. Stocks at the top of the list were potential buys, and the ones at the bottom were possible shorts. In the portfolio construction process, Martingale avoided bets on the direction of the stock market, it was always fully invested—Jacques would say that “not being fully invested is not a safe position; it is an active market bet”—and it sought to neutralize risks relative to the benchmark with respect to sector or industry, size or style, and beta. To keep trading costs low, Martingale maintained a diversified trade list and used principal trading done through a competitive auction process with guaranteed execution, along with conventional agency trading. In addition, Martingale continually evaluated alternative liquidity channels.

## Short Extension Funds

Martingale was one of the first asset management firms to offer short extension funds in 2004. This style category had been growing rapidly since the introduction of the first fund in 2003. By March 31, 2008, short extension funds in the United States had about \$66 billion in assets under management (AUM). Martingale managed about \$1 billion and ranked 14<sup>th</sup> by AUM in the U.S. short extension universe.<sup>1</sup> (See **Exhibit 3** for the top 50 U.S. short extension managers.)

In three years time, total U.S. assets were projected to grow from \$125 billion to \$300 billion due to U.S. institutional investors increasing or initiating investment, mostly as a result of shifting funds from their long-only public equity allocations.<sup>2</sup> Analysts expected that traditional asset managers would move actively into this area and that these funds would capture a significant share of active funds in the near future, with retail-oriented funds being offered as soon as 2009.

A short extension strategy sought to enhance the return on a benchmark index by relaxing the long-only constraint in traditional active portfolios, while keeping the beta exposure with respect to the benchmark at one. This was achieved by shorting a small portion of the portfolio value and offsetting the short positions with an equal value of additional long positions so as to be net 100% long. A structure popular among short extension funds included a long exposure of 130% of equity capital and a short exposure of 30%, for a net long exposure of 100% and a shorting ratio of 30%. This structure was so common that short extension funds were also known as “130/30 funds” regardless of their actual long-short exposure.<sup>3</sup>

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<sup>1</sup> Raquel Pichardo, “Frost Forms on 130/30 Growth,” *Pension and Investment* (April 28, 2008).

<sup>2</sup> “130/30 Portfolios—Here Comes the Wave,” Merrill Lynch, 12.

<sup>3</sup> Other names included enhanced alpha, alpha tilts, short enabled, limited shorting, information efficient. Funds sometimes used different amounts of leverage so that a 120 long and 20 short was called a “120/20.”

The benefit of a short extension was that it allowed fund managers to more fully express positive and negative views on expected individual stock returns than in a long-only fund. The long-only constraint restricted managers' use of their forecasting information and limited their effectiveness in transferring that information into a portfolio structure. A short extension structure allowed managers to better exploit their views on stocks that were expected to underperform by shorting such stocks, and to use the proceeds from the short sale to fund more long positions of stocks expected to outperform.

To illustrate the limitations of a long-only mandate, consider the passive weights associated with a benchmark broad-based index, such as the Russell 1000 Index. Typically, a small number of stocks accounted for a large percentage of the index value. (Exhibit 4 shows a descending rank order list of stocks according to their weights in the Russell 1000 Index as of December 2007.) The largest stock had a weight in the index of 3.5%, 911 stocks (91%) had weights less than 50 basis points (bps), and 775 stocks (78%) had weights less than 10 bps. For a long-only manager, the most bearish position on a stock meant not owning the stock, that is, an underweight equal to the stock's benchmark weight, which for most of the stocks in the index was not meaningful. The smaller the benchmark weight, the lower the ceiling on the potential gains that could be derived from a long-only manager's negative view.

### *Optimal Shorting Ratio*

Regulatory constraints aside, the optimal shorting ratio in a short extension fund depended on a number of factors, of which the ability of the manager to identify profitable risk-adjusted investment opportunities and the investor tolerance for tracking error were important ones. If the manager were skillful, then a higher shorting ratio—or equivalently, a lesser degree of portfolio constraints—might help the manager improve the information ratio of his strategy, as he would be able to translate more effectively his security ranking signals into active portfolio weights.<sup>4</sup> However, as portfolio constraints were relaxed, one might also expect the tracking error of the strategy to increase. Early research on the impact of portfolio constraints on the performance of active stock investment strategies suggested that a 20% to 30% shorting ratio was enough to optimize the information ratio for typical tracking errors of 3% to 4%.<sup>5</sup>

There were regulatory constraints in the United States that limited the maximum amount of shorting that traditional asset managers could adopt. In the United States, mutual funds and other investment companies regulated under the Investment Company Act of 1940 were not allowed to relinquish custody of their long positions to a broker. This in turn limited their leverage to a maximum of 50%, which was the maximum amount of credit that the Federal Reserve Board allowed brokerage firms and dealers to extend to customers for the purchases of securities on margin. This was known as Regulation T.

But other types of investment vehicles, such as separate accounts, were allowed to have stock loan accounts with prime brokers in which a fund manager was counterparty to a stock lending

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<sup>4</sup> The information ratio was defined as the portfolio's expected active return divided by the tracking error. The active return was the portfolio return minus the benchmark return. The tracking error was defined by the standard deviation of the active return. The information ratio was similar to the Sharpe ratio, but the Sharpe ratio compared the excess return to a risk-free rate, while the information ratio compares the active return to a benchmark return.

<sup>5</sup> See Roger Clarke et al., "Toward More Information-Efficient Portfolios," *The Journal of Portfolio Management* (Fall 2004); and Bob Litterman, "Active Alpha Investing," Open Letter to Investors, Goldman Sachs Asset Management, 2005.

transaction and was not subject to the leverage limits of Regulation T. In that case, the prime broker set the leverage limit.<sup>6</sup>

### *Tax Considerations*

Short extension funds, when properly structured, did not generate taxes for an otherwise tax-exempt U.S. investor. In instances where tax-exempt investors borrowed funds to buy stock, they incurred “acquisition indebtedness” and were subject to taxes on Unrelated Business Taxable Income (UBTI). However, this tax could be avoided if the extra long position was bought with proceeds from the short sale and not with a margin loan.<sup>7</sup> Short extension funds entered prime brokerage relationships that allowed them to use the proceeds from short positions to finance their long positions and thus did not involve indebtedness.

Of course, taxable investors would be subject to ordinary income and capital gains taxes on the dividend and capital gains distributions of the fund. U.S. regulations stipulated that returns from short sales were always subject to short-term capital gains taxes, regardless of how long the short position had been open.

### *Costs*

In a short extension fund, there were shorting and borrowing costs associated with the extended portion of the portfolio. These fees were consolidated into what was generally known as a stock loan fee or a stock loan cost. Essentially, the broker allowed the fund manager to have access to the proceeds of the short sales to invest in the extra long positions. The stock loan fee was negotiated and, in general, was in the range of 50 to 75 bps on the value of the extra long positions.

The fund manager paid the securities’ lenders the dividends on the short positions with the dividends from long positions, which, given the strong long bias built into these funds, was typically more than sufficient. The fund manager typically maintained only a small amount of cash.

Trading costs in a short extension fund were higher than in a long-only portfolio due to higher stock turnover. Turnover in a short extension portfolio scaled with leverage. In a 130/30 portfolio, turnover was roughly 60% higher than in a long-only portfolio because there was 60% more to invest (30% short and 30% extra long). Of course, portfolio optimizers took into account the trading costs in their cost benefit analysis in analyzing a trade.

Increased transaction and management costs for short extension portfolios led to higher fees. Fees for short extension funds for U.S. equities ranged from 60 to 100 bps, which were higher than the 50 to -80 bps for an active U.S. large cap strategy or the 30 to 50 bps for an enhanced U.S. index strategy.<sup>8</sup>

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<sup>6</sup> Bruce I. Jacobs and Kenneth N. Levy, “20 Myths about Enhanced Active 120-20 Strategies,” *Financial Analysts Journal* 63, no. 4 (2007).

<sup>7</sup> U.S. IRS Revenue Ruling 95-8 stated that income that a tax exempt organization received that was attributable to a short sale of publicly traded stock through a broker was not treated as UBTI under code section 514. See [www.irs.gov](http://www.irs.gov).

<sup>8</sup> Jay Cooper, “130/30s Pull in \$30 Billion,” *Pensions and Investments* (April 16, 2007).



### *Short Extension Funds at Martingale*

Martingale was one of the first asset managers to offer short extension funds in 2004. By early 2008, Martingale offered four funds based on the 130/30 model. (See **Exhibit 1** for a list of Martingale funds.) Each fund tracked one benchmark index and was designed to be neutral to the benchmark in factors such as size, style, sector, beta, and volatility.

Martingale did not see a short extension strategy as a long-only portfolio and a separately constructed long-short portfolio. Rather, it implemented an integrated optimization algorithm that included all the long and short positions at once, along with the desired benchmark exposure. For example, in late December 2007, the 30% short extension in Martingale's 130/30 LargeCap Core fund was split between the two smallest quintile stocks in the Russell 1000, with about 26% going into the smallest quintile. The 130% long was distributed in the smallest-to-the-largest quintile in percentages equal to 52%, 31%, 14%, 15%, and 18%, respectively.

Stock selection was based on Martingale's proprietary model that evaluated stock characteristics to find the most and least favored stocks. **Exhibits 5a, b, and c** show a list of the top ten holdings, the top ten overweighted stocks, the top ten underweighted stocks held in Martingale's 130/30 LargeCap Core 500 fund in January 2008. **Exhibit 5d** shows the industry composition of the benchmark and the relative long and short positions of the fund in each industry.

### **The Risk Anomaly in the Equity Market**

Historically, riskier asset classes such as equities experienced higher returns than less risky asset classes such as bonds or cash. The historical experience was consistent with the notion that greater risk was rewarded with higher expected return. But recent empirical studies suggested that the risk-return trade-off might not be operating at the individual equity level. In particular, a study of the largest (by market capitalization) 1,000 U.S. stocks from 1968 to 2005 found that stock portfolios constructed to have minimum variance had about 75% of the risk of the market capitalization weighted portfolio, while achieving approximately the same or greater average return.<sup>9</sup>

**Exhibit 6** shows portfolio return statistics for the market and several minimum variance (MV) portfolios constructed using different constraints and portfolio construction techniques. For example, the "Unconstrained MV Bayesian Shrinkage" portfolio had an annualized excess return over T-bills of 6.5% and an annualized standard deviation of 11.7%, which resulted in a Sharpe ratio of 55%.<sup>10</sup> By contrast, the market had an average excess return of 5.6% and a standard deviation of 15.4%, which resulted in a Sharpe ratio of 36%. This suggested that a 1.3x levered version of the MV portfolio could achieve a return of 8.5% per year with the same volatility as the market portfolio.

These results came at the cost of considerably higher turnover for these portfolios when compared to the turnover for the benchmark portfolio. For example, the monthly turnover rate for the Unconstrained MV Bayesian Shrinkage was 11.9% (143% annual), while it was 2% (24% annual) for the benchmark portfolio. But by changing the frequency of portfolio rebalancing from monthly to annual, the annual average turnover fell to 56% per annum, with only a 14 bps increase in monthly standard deviation and a minor change in monthly return of 12 bps. So a leveraged MV portfolio with less frequent rebalancing still outperformed the benchmark.

<sup>9</sup> Roger Clarke, Harinda de Silva, and Steven Thorley, "Minimum-Variance Portfolios in the U.S. Equity Market," *Journal of Portfolio Management* (Fall 2006).

<sup>10</sup> The average T-bill return over this period was 5.9%.

Minimum variance portfolios also exhibited tracking errors that resembled those typical in highly active equity strategies. Tracking errors ranged from 6% to 12%, and were particularly large during the period from 1999 to 2002, when market volatility was also high. (See **Exhibit 7** for the portfolio risks.) Minimum variance portfolios also tended to have a small size and value bias, but not a momentum bias. But the study found that these biases could explain only about 60% of the superior performance of these portfolios. That is, one could construct minimum variance portfolios that were neutral with respect to value and size and that exhibited lower volatility with about the same average return as the market portfolio.

Despite the larger turnover and tracking error of these strategies, institutional investors had shown much interest in them. To help investors better measure MV fund performance and to help grow MV strategies, a new benchmark was created in April 2008 for MV strategies. It was called MSCI World Minimum Volatility Index.

## Minimum Variance Short Extension Fund

A second study found that one could construct long-short portfolios based on stock volatility rankings that generated a subsequent positive return spread while preserving the risk ranking.<sup>11</sup> The study used monthly returns of all U.S. stocks from 1968 to 2005 and grouped the stocks into five volatility quintiles based on the standard deviation in monthly returns over the prior five years. Portfolio returns and portfolio volatility were calculated over the next month. The study found that the lowest quintile portfolio had a higher average return and lower volatility than the highest volatility quintile portfolio. This relationship prevailed in both periods of economic contraction and periods of economic expansions. (See **Exhibits 8a, b, and c** for portfolio statistics of the volatility-ranked quintile portfolios.) It also prevailed if one used beta with respect to the benchmark instead of volatility to rank stocks.

Thus, low-volatility stocks and low-beta stocks exhibited subsequent low volatility and low beta, and experienced higher average returns than high-volatility stocks and high-beta stocks. These results suggested that a long-short strategy that held long low-volatility (or low-beta) stocks and held short high-volatility (or high-beta) stocks might produce a positive risk-adjusted return.

It was precisely this insight that had led Martingale to develop an MV strategy within a 130/30 structure: a short extension fund based on the MV anomaly might augment portfolio returns while not significantly increasing or perhaps even reducing the standard deviation of the fund.

Martingale had developed four versions of its own MV strategy: two long-only strategies—one with no stock alphas (pure minimum variance) and one using Martingale's stock alpha model (minimum variance plus alpha); and two 130/30 strategies—one with no stock alphas (130/30 minimum variance) and one with Martingale's stock alphas (130/30 minimum variance plus alpha). Martingale wanted to separate out the potential value added of each component of the strategy: Would a minimum variance-weighted portfolio do well against the market capitalization weighted index? Would Martingale's stock alpha model add value against the pure minimum variance strategy? And finally, would a 130/30 strategy improve the low-volatility strategy?

To understand the potential performance and value added of each strategy, Martingale had extensively back-tested each of them. Back-testing consisted of running the strategy using historical

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<sup>11</sup> Roger Clarke, Harinda de Silva, and Steven Thorley, "Exploring the Risk Anomaly in the Equity Market," *Economics and Portfolio Strategy* (December 15, 2006).

data to determine how the strategy would have performed in different market environments, had it been implemented in the past. Martingale was well aware of the dangers of back-testing. It realized that with enough tweaking, you could make back-testing show extremely favorable results—a variation of the old adage, “If you torture the data long enough, it will confess to anything.” To defend against this, Martingale’s investment team established a set of rules for back-testing before examining any results.

First, they used a “research” database that included all companies that existed at each point in time when portfolios were rebalanced. That is, they ran their strategies with all the companies that would have been available for investing at each point in time. Many commercially available databases typically dropped stocks when they were delisted because their companies went bankrupt or were merged or acquired by others. Thus, these databases had historical information only about the stocks that had been successful in the past and had survived until the present. Naturally, simulations based only on surviving stocks would have been better, but they would have been unrealistic and flawed. Martingale made sure to use databases that were free of this “survivorship bias.”

Second, the team used their actual stock alphas that existed at each point in time, rather than using recast alphas that might include a “look-ahead bias.” After the fact, you know which factors worked, so if you included these factors or weighted them more heavily in your recast model, the resulting stock alphas would be unrealistically accurate.

Third, the team selected portfolio construction parameters, such as individual stock position limits and industry and sector constraints, with an eye toward managing risk, rather than attempting to optimize these parameters for the highest level of return. For example, industry and sector target weights were established so that no one industry or sector would dominate and at least 20 industries would be represented. Portfolios were optimized versus cash, so risk was defined in terms of total volatility, not tracking error.

**Exhibits 9 and 10** show summary measures of the back-tested portfolio performance of Martingale’s set of MV strategies from October 1995 to December 2007. **Exhibit 11** plots the time series of rolling 36-month average annualized returns on the pure minimum variance strategy and on the Russell 1000 Index over the same period. This exhibit shows that the MV strategy had underperformed the index during the bubble period of the late 1990s and early 2000s, and had outperformed the index in the subsequent period.

Based on these results, Martingale had decided to launch an MV fund and an MV 130/30 fund using its own internal funds in December 2007. In the six months between January 2008 and June 2008, the benchmark index (Russell 1000) had fallen by 11.2%. By contrast, the MV strategy had fallen 6.8%, and the 130/30 MV fund had fallen only by 1.5%. (See **Exhibit 12** for the returns on the portfolios.)

## The Future of Martingale

Jacques was pleased with the results of the new MV strategy, especially the one that combined the 130/30 structure with the MV portfolio. He was looking forward to his meeting with Wood and the rest of the team to discuss whether they should share these results with Martingale’s clients and prospective clients, and whether Martingale was ready to offer this product to outside investors. This decision would ultimately depend on whether they were all convinced that the strategy made sense and was not merely a spurious pattern in the data. Certainly, recent studies by

academics in the United States and in the Netherlands showed that this was a worldwide phenomenon, not just a U.S. anomaly.<sup>12</sup>

Jacques had thought about several possibilities that might explain the persistence of this anomaly. Most prominent among them was that perhaps this was a reflection of the costs and the aversion of investors to short selling. One could view high volatility in the price of a stock as reflecting in part the divergence of opinions about the future prospects for the stock. If investors with negative views of the stock did not engage in enough short selling, the price of the stock might be higher than it should be, and that would explain the lower returns of high-volatility stocks over time. Another possibility could be that the volatility effect was driven by the inability of many institutional clients to tolerate high tracking error. Benchmark-driven investing combined with style box allocation might be limiting the opportunities to exploit the volatility effect.

Looking again at his favorite artwork, Jacques wondered what Strassman and Wood would say about his thoughts and what they might suggest to further strengthen their conviction that this phenomenon was not driven by “data mining.” Brainstorming with the entire investment team would surely lead to discussing other possibilities to grow the strategy. For example, Martingale had limited its investment universe exclusively to U.S. stocks. Should it expand this universe, perhaps by developing a global version of the MV strategy? Was Martingale suited for that?

Jacques was aware that the ability of active managers like Martingale to thrive depended on their ability to innovate. Like sharks, they had to move forward continuously, or else. Through clever innovation, Martingale had certainly moved forward over the last 20-plus years. He had no doubt that Martingale would keep moving forward and serving its investors for the next 20.

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<sup>12</sup> Andrew Ang et al., “High Idiosyncratic Volatility and Low Returns: International and Further U.S. Evidence” (New York: Columbia Business School, 2008); David Blitz and Pim van Vliet, “The Volatility Effect: Lower Risk without Lower Return” (Rotterdam: Erasmus Research Institute of Management, Erasmus University, 2007).

**Exhibit 1** List of Martingale Funds, June 30, 2008

Fund Category	Fund Name (Value)	Fund Name (Core)	Fund Name (Growth)	AUM (\$ million)
Large Cap Equities	LargeCap Value LargeCap Value 500 LargeCap Value 200	LargeCap Core LargeCap Core 500 LargeCap Core 200 AllCap Core	LargeCap Growth	1,200
Mid Cap Equities	MidCap Value	MidCap Core	MidCap Growth	356
Small Cap Equities	SmallCap Value* Small/MidCap Value*	SmallCap Core* Small/MidCap Core*	SmallCap Growth	1,700
Short Extension	LargeCap Value	LargeCap Core LargeCap Core 500	LargeCap Growth	1,000
Equity Market Neutral		Equity Market Neutral		364
Total				4,620

Source: Martingale Asset Management.

\*Closed.

## Exhibit 2 List of Martingale Equities Fund Information (June 30, 2008)

Equity Characteristics	LargeCap Value 200	MidCap Core	SmallCap Value	130/30 LargeCap Core 500	Equity Market Neutral
Inception	7/1/1996	7/1/1995	7/1/1996	10/1/2004	1/1/1991
AUM (millions)	\$43	\$356	\$801	\$80	\$364
Fees	0.70% on the first \$25 million 0.30% thereafter	0.70% on all assets	1.00% on all assets	0.75% on all assets	1.00% of invested capital plus 20% of profits
<b>Benchmark</b>	Russell Top 200 Value Index	Russell Midcap Index	Russell 2000 Value Index	S&P 500 Index	U.S. T-bills
Return on equity (trailing)	Fund 13.1% Bench- mark 11.1	Fund 14.3% Bench- mark 10.7%	Fund 8.5% Bench- mark 5.7%	Fund 18.2% Bench- mark 13.2%	Long side of Fund 13.7% Short side of Fund 7.9%
P/E, average (forward)	10.0x	11.7x	10.0x	10.4x	10.7x
P/Cash flow, average	9.1x	6.8x	5.4x	6.5x	6.3x
Earnings growth rate	11.1%	14.4%	11.6%	16.7%	15.6%
Market cap, weighted average	\$135B	\$7.2B	\$1.1B	\$91B	\$14.3B
Number of positions	74	140	223	273	168
Ten largest holdings, as % of portfolio	46%	15%	14%	24%	10.2%
Turnover, average over last 3 years	100%	102%	110%	151%	159%
Beta (vs. benchmark)	0.99	0.97	0.97	1.00	1.17
<b>Performance Results<sup>a</sup></b> (percent)					-1.18
Annualized return	Fund 13.68 Bench- mark -15.25	Fund -4.09 Bench- mark -7.57	Fund -7.84 Bench- mark -9.84	Fund -5.27 Bench- mark -11.91	Fund 8.25 Bench- mark 0.99
2008 YTD	-16.58	-10.85	-24.11	-6.75	6.00
1 Year	4.41	8.48	-2.87	7.95	6.07
3 Years	8.40	15.15	8.79	N/A	4.57
5 Years	9.08	12.90	11.98	9.22	6.12
Since inception	14.93	15.58	15.86	8.76	5.43
Annualized standard deviation, since inception			15.51	9.73	0.41

Source: Martingale Asset Management.

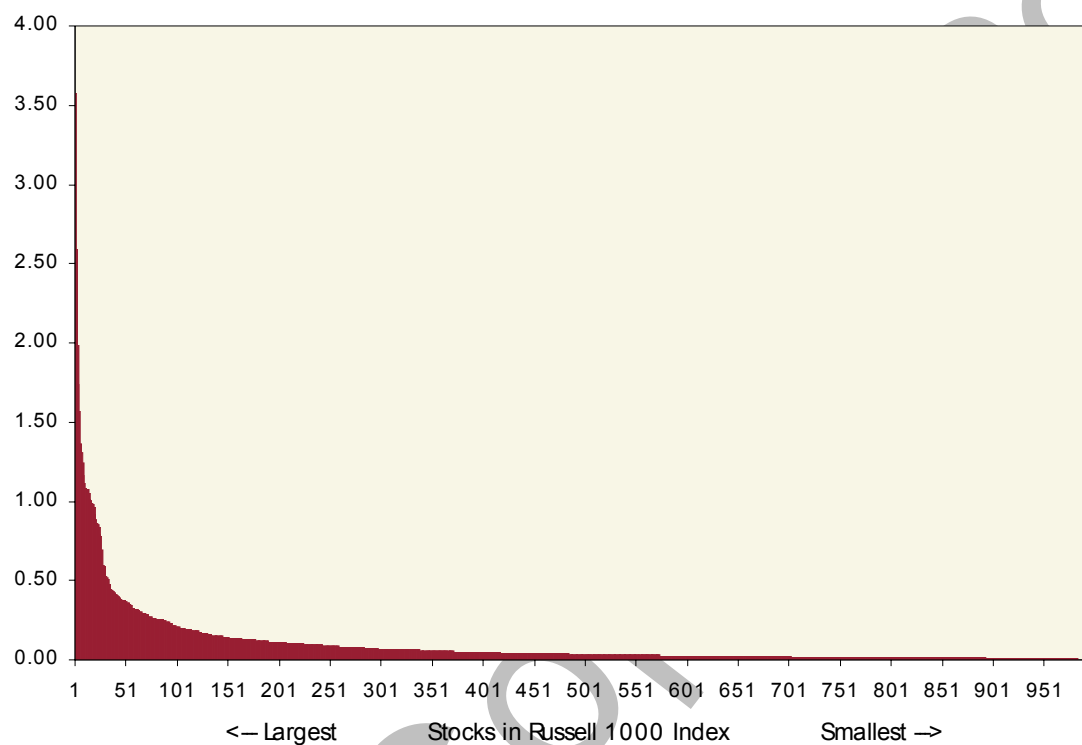
<sup>a</sup>Fund results are gross of management fees but net of transaction fees.

**Exhibit 3** Rank of Short Extension Managers (March 31, 2008)

Manager	Assets (\$ billion)	Manager (continued)	Assets (\$ billion)
State Street Global Advisors	\$12,437	The Boston Co. Asset Mgmt.	\$134
Barclays Global Investors	\$9,300	Pyramis	\$127
JPMorgan	\$8,600	Brandywine	\$109
Jacobs Levy	\$4,857	GMO	\$102
Analytic	\$3,965	Fuller & Thaler	\$87
Aronson, Johnson & Oritz	\$3,500	Deutsche	\$80
Goldman Sachs Asset Mgmt.	\$3,000	RiverSource	\$73
Acadian	\$2,703	SSI	\$70
AXA	\$2,600	Stux	\$65
UBS*	\$2,490	Thomson Horstmann & Bryant	\$60
Numeric	\$2,237	INTECH*	\$41
AQR	\$1,650	Value Works	\$38
Quantitative Mgmt. Assoc.	\$1,504	Northern Trust	\$32
Martingale	\$1,049	Alpha Equity Mgmt.	\$30
Invesco	\$791	AG Asset Mgmt.	\$26
D.E. Shaw	\$631	Shennandoah Asset Mgmt.	\$11
PanAgora	\$617	MFS Investment Mgmt.	\$10
McKinley Capital	\$511	Nicholas-Applegate	\$10
First Quadrant	\$503	Lee Munder	\$10
Mellon Capital*	\$500	Turner	\$8
Franklin Portfolio Assoc.	\$474	Thompson, Siegel & Walmsley	\$8
Los Angeles Capital Mgmt.	\$372	American Century	\$5
NYLIM	\$361	Geode Capital	\$3
Maverick	\$175	Fred Alger	\$3
Glenmede	\$168	TWIN Capital Mgmt.	\$2
Fifth Third	\$163	Freeman	\$1
		<i>Total</i>	\$66,273

Source: Pension and Investments.

\* Assets as of December 31, 2007.

**Exhibit 4** Russell 1000 Stock Weights (December 31, 2007)

Source: Martingale Asset Management.



**Exhibit 5a** Top Ten Holdings in the Martingale 130/30 LargeCap Core 500 Fund (January 2008)

Stock Rank	Stock Symbol	Company Name	Fraction of Portfolio (%)	Cumulative Total (%)
1	XOM	EXXON MOBIL CORP COM	5.31%	5.31%
2	T	AT&T INC COM	3.21%	8.52%
3	MSFT	MICROSOFT CORP COM	3.19%	11.71%
4	COP	CONOCOPHILLIPS COM	2.36%	14.08%
5	IBM	INTL BUSINESS MACH COM	2.33%	16.41%
6	CVX	CHEVRON CORP NEW COM	2.22%	18.63%
7	HPQ	HEWLETT PACKARD CO COM	2.21%	20.84%
8	GE	GENERAL ELECTRIC CO COM	2.09%	22.93%
9	ORCL	ORACLE CORP COM	2.02%	24.95%
10	WMT	WAL MART STORES INC COM	1.76%	26.72%

Source: Martingale Asset Management.

**Exhibit 5b** Top Ten Overweight Stocks in the Martingale 130/30 LargeCap Core 500 Fund (January 2008)

Stock rank	Stock Symbol	Company Name	Fraction of Portfolio (%)	Overweight Relative to S&P (%)
1	ORCL	ORACLE CORP COM	2.02%	1.32%
2	NLY	ANNALY CAP MGMT INC COM	1.31%	1.31%
3	XOM	EXXON MOBIL CORP COM	5.31%	1.28%
4	HUM	HUMANA INC COM	1.38%	1.28%
5	COP	CONOCOPHILLIPS COM	2.36%	1.25%
6	T	AT&T INC COM	3.21%	1.25%
7	AES	AES CORP COM	1.35%	1.23%
8	TRV	TRAVELERS COMPANIES INC	1.49%	1.22%
9	AET	AETNA INC NEW COM	1.44%	1.21%
10	KCI	KINETIC CONCEPTS INC COM NEW	1.21%	1.21%

Source: Martingale Asset Management.

**Exhibit 5c** Top Ten Underweight Stocks in the Martingale 130/30 LargeCap Core 500 Fund (January 2008)

Stock rank	Stock Symbol	Company Name	Fraction of Portfolio (%)	Underweight Relative to S&P (%)
1	PCL	PLUM CREEK TIMBER CO INC COM	-1.21%	-1.27%
2	ERTS	ELECTRONIC ARTS INC COM	-1.09%	-1.23%
3	SE	SPECTRA ENERGY CORP COM	-1.04%	-1.17%
4	SGMS	SCIENTIFIC GAMES CORP CL A	-1.11%	-1.11%
5	PNW	PINNACLE WEST CAP CORP COM	-1.03%	-1.06%
6	PG	PROCTER & GAMBLE CO COM	0.72%	-1.05%
7	INTC	INTEL CORP COM	0.23%	-0.94%
8	WFMI	WHOLE FOODS MKT INC COM	-0.89%	-0.93%
9	PAYX	PAYCHEX INC COM	-0.83%	-0.92%
10	LPX	LOUISIANA PAC CORP COM	-0.89%	-0.89%

Source: Martingale Asset Management.

**Exhibit 5d** Sector Analysis of Martingale 130/30 LargeCap Core 500 Fund (January 2008)

Sector	Benchmark	Long	Short	Net Long	Active (net long – benchmark)
Technology	18.01%	25.30%	-5.23%	20.07%	2.06%
Consumer (cyclical)	6.21%	9.96%	-1.84%	8.13%	1.92%
Commercial Services	2.43%	5.79%	-1.70%	4.10%	1.67%
Telecommunications	3.54%	6.52%	-1.67%	4.85%	1.31%
Industrials	3.37%	4.61%	-0.43%	4.18%	0.82%
Energy	12.47%	14.13%	-1.79%	12.33%	-0.14%
Consumer Services	4.74%	5.63%	-1.88%	3.75%	-0.99%
Health Care	12.47%	14.38%	-2.91%	11.46%	-1.01%
Utility	3.43%	3.77%	-1.48%	2.28%	-1.15%
Financial	18.06%	23.29%	-6.51%	16.78%	-1.28%

Source: Martingale Asset Management.

**Exhibit 6** Excess Returns for the Market and Minimum Variance Portfolios (January 1968 to December 2005)

Portfolio	Monthly Mean Returns (bps)	Monthly Standard Deviation (bps)	Annualized Mean Returns (%)	Annualized Standard Deviation (%)	Sharpe Ratio
Market	46	445	5.6	15.4	0.36
Min-var, Bayesian shrinkage <sup>a</sup>					
Unconstrained	54	337	6.5	11.7	0.55
Factor constrained	46	364	5.6	12.6	0.44
Sensitivity constrained <sup>b</sup>	47	344	5.6	11.9	0.47
Min-var, Principal components <sup>a</sup>					
Unconstrained	56	333	6.7	11.6	0.58
Factor constrained	45	363	5.5	12.6	0.43
Sensitivity constrained	49	339	5.9	11.8	0.50
Long/short, Bayesian <sup>c</sup>					
Unconstrained	45	303	5.5	10.5	0.52
Factor constrained	40	321	4.8	11.1	0.43
Sensitivity constrained	45	300	5.4	10.4	0.52

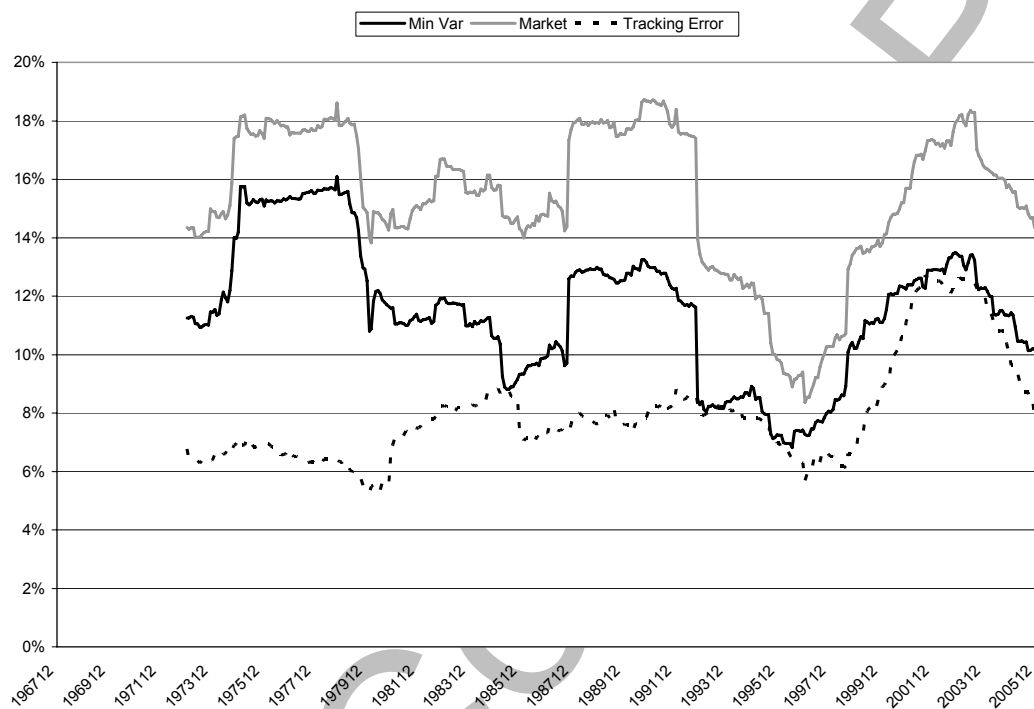
Source: Robert Clarke et al., "Minimum-Variance Portfolios in the U.S. Equity Market," *Journal of Portfolio Management* (Fall 2006).

<sup>a</sup>Bayesian shrinkage and principal components were more recent methods of structuring the security covariance matrixes that, unlike other methods, did not rely on prespecified factor models. The goal was to have more robust empirical results. See referenced paper for more details.

<sup>b</sup>It was believed that a more accurate method to measure a security's factor exposure was to use historical sensitivity to factor returns instead of the stock characteristic. Sensitivity constrained portfolio was constrained using estimated factor sensitivities.

<sup>c</sup>Long-short portfolio did not have short sell constraint, so that security weights could be negative.

**Exhibit 7** Portfolio Risk<sup>a</sup> of the Market and Minimum Variance Portfolios and the Tracking Error of the Minimum Variance Portfolio Relative to Market (January 1968 to December 2005)



Source: Roger Clarke et al., "Minimum-Variance Portfolios in the U.S. Equity Market," *Journal of Portfolio Management* (Fall 2006).

<sup>a</sup>Rolling standard deviation of returns of the trailing five years.

**Exhibit 8a** Portfolio Returns for Volatility Quintile Portfolios (January 1968 to December 2005)

Quintile	Monthly Mean Returns (bps)	Monthly Standard Deviation (bps)	Annualized Mean Returns	Annualized Standard Deviation	Return per Unit of Risk
1 – Low volatility	98	370	11.8%	12.8%	0.92
2	100	460	12.0%	15.9%	0.75
3	106	569	12.7%	19.7%	0.65
4	100	706	12.0%	24.5%	0.49
5 – High volatility	76	882	9.1%	30.6%	0.30
<i>Average</i>	96	597	11.5%	20.7%	0.56

Source: Roger Clarke et al., “Exploring the Risk Anomaly in the Equity Market,” *Economics and Portfolio Strategy* (December 15, 2006) and author’s calculations.

**Exhibit 8b** NBER Contraction Phase Portfolio Returns for Volatility Quintile Portfolios during the Business Cycle from January 1968 to December 2005

Quintile	Monthly Mean Returns (bps)	Monthly Standard Deviation (bps)	Annualized Mean Returns	Annualized Standard Deviation	Return per Unit of Risk
1 – Low volatility	50	516	6.0%	17.9%	0.34
2	2	618	0.2%	21.4%	0.01
3	-20	790	-2.4%	27.4%	-0.09
4	-9	923	-1.1%	32.0%	-0.03
5 – High volatility	-36	1166	-4.3%	40.4%	-0.11
<i>Average</i>	-3	803	-0.3%	27.8%	-0.01

Source: Roger Clarke et al., “Exploring the Risk Anomaly in the Equity Market,” *Economics and Portfolio Strategy* (December 15, 2006) and author’s calculations.

**Exhibit 8c** NBER Expansion Phase Portfolio Returns for Volatility Quintile Portfolios during the Business Cycle from January 1968 to December 2005

Quintile	Monthly Mean Returns (bps)	Monthly Standard Deviation (bps)	Annualized Mean Returns	Annualized Standard Deviation	Return per Unit of Risk
1 – Low volatility	107	335	12.8%	11.6%	1.11
2	118	422	14.2%	14.6%	0.97
3	129	515	15.5%	17.8%	0.87
4	120	657	14.4%	22.8%	0.63
5 – High volatility	97	818	11.6%	28.3%	0.41
<i>Average</i>	114	549	13.7%	19.0%	0.72

Source: Roger Clarke et al., “Exploring the Risk Anomaly in the Equity Market,” *Economics and Portfolio Strategy* (December 15, 2006) and author’s calculations.

**Exhibit 9** Back-tested Portfolio Performance of Martingale's Minimum Variance Strategies (October 1995 to December 2007)

Portfolio	Annualized Mean Returns (%)	Annualized Standard Deviation (%)	Beta	Tracking Error	Turnover Monthly (%)
Market (Russell 1000 Index)	9.7	14.5	1.00	0.0	<1
Min-variance <sup>a</sup>	11.5	10.1	0.67	7.7	4
Min-variance and alpha <sup>b</sup>	12.5	10.4	0.68	7.6	6
130/30 Min-variance <sup>c</sup>	12.0	9.4	0.50	10.4	4
130/30 Min-variance and alpha <sup>d</sup>	14.7	10.0	0.55	10.1	10

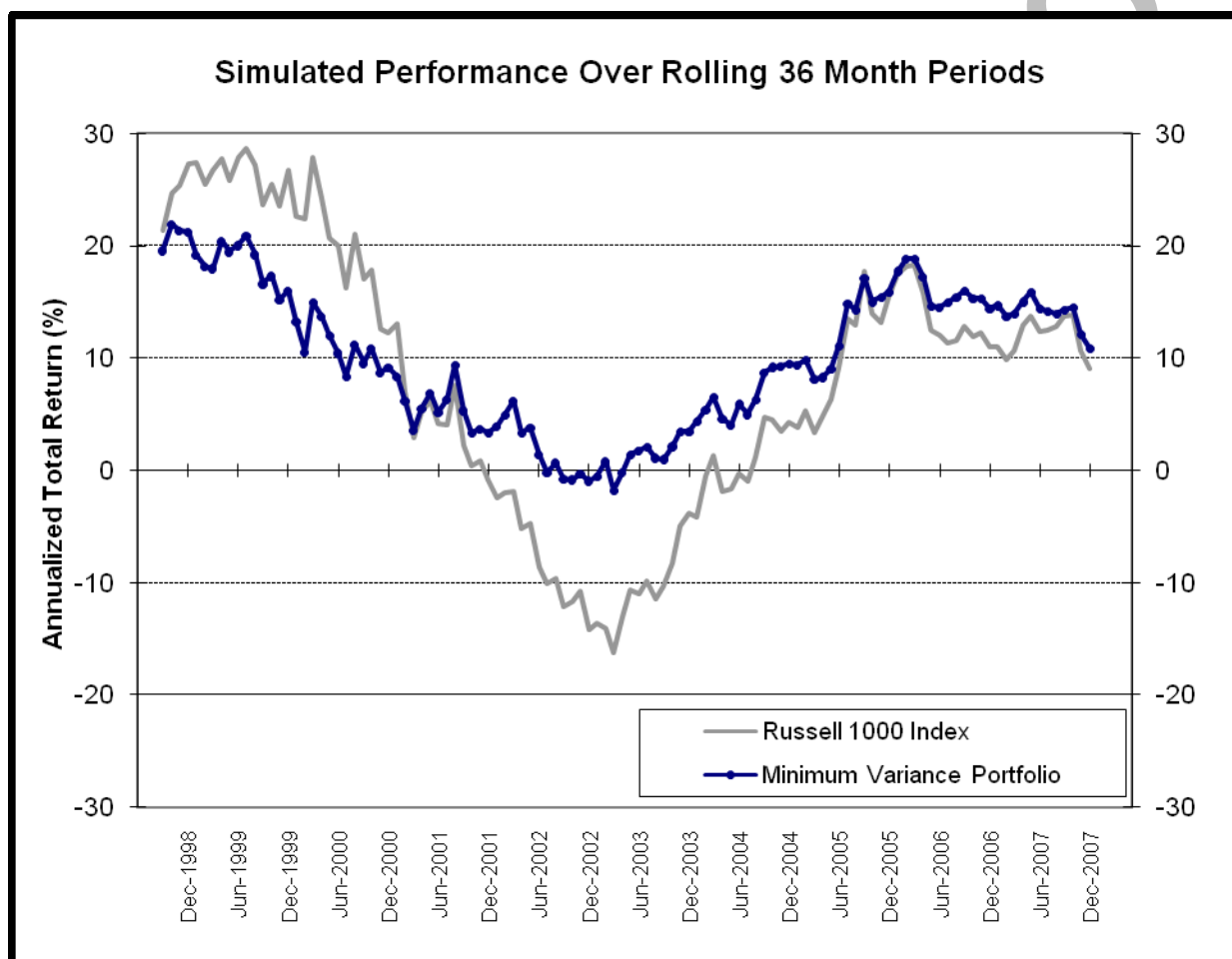
Source: Martingale Asset Management.

<sup>a</sup>Simulated long-only minimum variance portfolio.<sup>b</sup>Simulated long-only minimum variance portfolio plus Martingale stock alpha.<sup>c</sup>Simulated 130/30 minimum variance portfolio.<sup>d</sup>Simulated 130/30 minimum variance portfolio plus Martingale stock alpha.**Exhibit 10** Back-tested Portfolio Performance of Martingale's Minimum Variance Strategies (October 1995 to December 2007)

Geometric Monthly Returns	# of Months	Market (Russell 1000 Index)	Minimum Variance	Minimum Variance + Stock Alpha	130/30 Minimum Variance	130/30 Minimum Variance + Stock Alpha
Mean return-all months	147	0.78%	0.91%	0.98%	0.95%	1.15%
Percent of market return		100%	118%	127%	122%	148%
Mean return- down market months	53	-3.56%	-1.86%	-1.89%	-1.16%	-1.21%
Percent of down market return		100%	52%	53%	33%	34%
Mean return-up market months	94	3.31%	2.51%	2.64%	2.16%	2.50%
Percent of up market return		100%	76%	80%	65%	76%

Source: Martingale Asset Management.

**Exhibit 11** Annualized Returns of the Minimum Variance Portfolio and Russell 1000 Index (October 1995 to December 2007)



Source: Martingale Asset Management.

**Exhibit 12** Return of Minimum Variance Portfolios (June 30, 2008)

	Minimum Variance and Alpha	130/30 Minimum Variance and Alpha
Inception	1/2008	1/2008
Benchmark	Russell 1000	Russell 1000
Benchmark return Since inception	-11.2%	-11.2%
Fund Gross Return Since inception	-6.8%	-1.5%

Source: Martingale Asset Management.



## Disclosures

1. Low volatility strategies employ a systematic process to build a portfolio of undervalued companies selected from approximately 1,000 mid-sized to large U.S. companies. A 130/30 low-volatility strategy holds short positions of 30% of the portfolio's capital to potentially add value. The Russell 1000 Index is an appropriate benchmark index for the strategies; its returns are provided to represent the investment environment existing during the time periods shown. For comparison purposes, the index is fully invested, which includes the reinvestment of income. Index returns do not include any transaction costs, management fees, or other costs.
2. The results presented herein represent simulated, back-tested results. These results do not represent the results of actual trading, but were achieved by means of retroactive application of a valuation model designed with the benefit of hindsight. As a result, it is possible that actual results based on actual trading, without the benefit of hindsight, may materially differ from the simulated, back-tracked results presented here. Alphas used during the simulation were generated from the valuation model in use at each point in time. Further, as with any active equity strategy, there is always the potential for declines in the value of accounts managed pursuant to this strategy. It is possible that market conditions and other economic factors unintentionally impacted the design of this valuation model, thereby producing results that would be difficult or impossible to match without the benefit of hindsight. All investment models are subject to risk, and there can be no assurance that an investment strategy will achieve its stated objective. Market and economic conditions have not affected our performance significantly relative to its respective benchmark.
3. Simulated performance returns were calculated using the total (pure gross) return to a theoretical portfolio including capital gains and dividend income, and are based on end-of-month holdings. Calculations do not reflect any estimated implementation costs or a deduction of investment advisory fees, transaction costs, prime brokerage fees (when applicable), or any other expenses that may be incurred in the management of the account. Actual results will be reduced by advisory fees and other expenses.
4. Actual results presented herein are from a live portfolio funded with Martingale's own capital and is a non-fee-paying account. Its performance calculations are time-weighted rates of return based on trade date valuations and accrual-based accounting for income. Returns are net of both transaction costs and non-reclaimable withholding taxes. Dividends, interest, and other earnings are reinvested. Portfolios are revalued for all cash flows. All valuations and returns are expressed in U.S. dollars. The dispersion of annual returns is measured by the asset weighted standard deviation of portfolio returns represented within the composite for the full year. The performance presented herein represents past performance and is not an indicator of future results. Further, as with any active equity strategy, there is always the potential for declines in the value of accounts employing this strategy.
5. Martingale's investment advisory fees are described in Part II of Form ADV. Net of fee results are calculated by applying the highest fee charged to any account employing these strategies for the performance period. The standard fee schedule for a traditional long-only Low Volatility strategy is 0.70% on the first \$25 million and 0.30% on any balance thereafter. The standard fee schedule for a 130/30 Low Volatility strategy is 0.75% on all assets. Actual advisory fees can vary among clients employing this strategy. Actual advisory fees can vary among clients employing this strategy. For use in one-on-one presentations only.

Please contact Martingale Asset Management for full disclosures on composites presented herein.