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Reconstruction and classification of tau lepton decays with a future Linear Collider

B. Xu,^{a,1} S. Green,^a J. S. Marshall,^a M. A. Thomson^a

^a*Cavendish Laboratory,*

JJ Thomson Avenue, Cambridge, CB3 0HE, UK

E-mail: xu@hep.phy.cam.ac.uk

ABSTRACT: Seven tau lepton decay final states were examined at the future $e^- e^+$ Linear Collider. Tau leptonic physics is important as the branching ratio provides a precision test of the Standard Model. The spin state of the tau can be used to measure the CP of the Higgs using the Higgs decaying to a tau pair channel. The classification efficiencies of hadronic tau decay is also a benchmark test for the detector performance. In this paper, the leptonic, hadronic 1-prong and hadronic 3-prong final states of the tau lepton were classified for the centre of mass (\sqrt{s}) $e^- e^+$ collision energies of 100, 200, 500 and 1000 GeV and for the silicon-tungsten electromagnetic calorimeter (ECal) cell sizes from 3 to 20 mm. The main challenge of the classification is the reconstruction and the separation of nearby photons as individual entities. The correct association of the tracks from the tracking system to the deposited energy shower in the calorimeter is also important for the leptonic final states identification. The overall hadronic decay selection efficiency is over 90% for c.o.m. $\sqrt{s} = 100$ GeV for the range of the ECal cell sizes, whilst the selection efficiency degrades significantly from 3 mm to 20 mm ECal cell size for $\sqrt{s} = 500$ and 1000 GeV.

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¹Corresponding author.

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1 Introduction

Tau lepton has been examined extensively in the past to study its physics and to use it as a detector benchmark test.

The total tau lepton hadronic decay width depends on the strong coupling constant. The branch ratio of tau decay tau provides a precision test of the Standard Model and models beyond the Standard Model. The spin state of the tau lepton could be inferred from the decay product and can be used to measure the CP(the product of charge conjugation and parity symmetries) of the Higgs with a Higgs decaying to a tau pair channel. Many experiments, including the Large Electron Positron Collider (LEP), has studied the tau lepton to a great details [1].

Final state separation of tau decay also provides a good benchmark of the detector performance. The tau lepton has a very short life time and it will decay before reaching the calorimeter. The reconstruction of the multiple nearby photons requires an excellent electromagnetic calorimeter (ECal) resolution, whilst separating different charged particle relies on the performance of the tracking system.

The study presented in this paper was done using the CLIC_ILD detector concept with the PandoraPFA software package. A previous study with the International Large Detector (ILD) in the context of the International Linear Collider (ILC) was performed, where the impact of the varying the magnetic field and the size of the ECal were discussed. The CLIC_ILD detector concept [2] is designed for the Compact LInear Collider (CLIC) based on the ILD detector [3], shown in figure 1, consisting of a vertex detector, tracking detectors, ECal, hadronic calorimeter (HCal) and a muon chamber. The ECal and HCal are designed for the particle flow approach [4] with high granularity in both longitudinal and transverse direction.

The difficulty of the τ decay mode separation is to correctly reconstruct photons in the final states. Two main features of the reconstruction software, PandoraPFA [6], help to separate the final states. Firstly, the iterative track cluster association algorithms connecting reconstructed tracks to the cluster showers in the calorimeters, providing a good identification of the charged particles and leave a cleaner environment for the neutral particles. Secondly, a transverse calorimeter shower profile based photon reconstruction algorithm carefully identifies and separates nearby photons, using a likelihood photon identification algorithm. Along side with other reconstruction algorithms

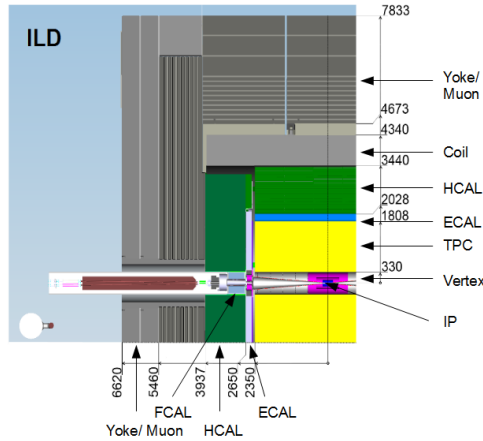


Figure 1. A quadrant of the ILD detector concept. Dimensions are in mm. Plot is taken from [5].

in the PandoraPFA software, charged particles and photons are well reconstructed and used as inputs for τ decay mode separation.

In this paper, we present a study for the separation of tau lepton decay final states, to demonstrate the high classification rate, by varying the size of the ECal cells and the centre of mass energy (\sqrt{s}) of the $e^- e^+ \rightarrow \tau^- \tau^+$ interaction.

2 Simulation and Reconstruction

Simulated Monte Carlo (MC) samples were generated with the generator software WHIZARD 1.95 [7]. PYTHIA 6.4 [8] is used for the hadronisation and is tuned to the LEP results [9]. The interface to TAUOLA [9] is used to describe the τ lepton decays. The initial state radiation (ISR) and the beam induced background were not simulated, but final state radiation (FSR) was simulated.

Around two millions events per ECal cell size and per c.o.m. energy were simulated before any generator level cuts. An event was considered if the event passes a set of cuts at generator level. The cuts are

- the final state photons not converting to electron pair in the tracker,
- the tau leptons decaying in the barrel and the end cap regions, which are 0.3 to 0.6 rad and 0.8 to 1.57 rad
- the visible energy of the tau lepton decay more than 5 GeV.

The visible energy of the tau lepton decay is defined as the energy of the tau minus the energy of the tau neutrino.

Events were simulated with software MOKKA [10] with the CLIC_ILD detector geometry description, based on the GEANT 4 package [11]. Events were reconstructed with ilcsoft version v01-17-07 [12] and PandoraPFA version v02-02-00 [6], where the photon reconstruction is described in [13].

The events were simulated at $\sqrt{s} = 100, 200, 500$ and 1000 GeV, with different ECal square cell sizes of 3, 5, 7, 10, 15 and 20 mm.

3 Analysis strategy

Table 1. Branching fractions of the seven τ^- decays in this study, taken from [14]. τ^+ decays similarly to τ^- .

Decay mode	Branching fraction / %
$e^- \bar{\nu}_e \nu_\tau$	17.83 ± 0.04
$\mu^- \bar{\nu}_\mu \nu_\tau$	17.41 ± 0.04
$\pi^- \nu_\tau$	10.83 ± 0.06
$\rho(\pi^- \pi^0) \nu_\tau$	25.52 ± 0.09
$a_1(\pi^- \pi^0 \pi^0) \nu_\tau$	9.30 ± 0.11
$a_1(\pi^- \pi^- \pi^+) \nu_\tau$	8.99 ± 0.06
$\pi^- \pi^- \pi^+ \nu_\tau$	2.70 ± 0.08

Seven decay final states of the tau lepton shown in table 1 were studied, which cover 92.58 % of all tau decays. The decay modes not covered have branching fractions lower than 1% each. These final states can be classified into three categories: leptonic decays, one-prong with photons and three-prong with photons.

The detector fiducial space is divided into two halves using the thrust axis. Thrust is defined as $T = \max_{\hat{n}} \frac{\sum_i |p_i \cdot \hat{n}|}{\sum_i |p_i|}$, where p_i is the momentum three-vector of a Particle Flow Object (PFO), \hat{n} is the thrust axis, a unit 3-vector that maximise the thrust, T .

Set of variables based on the topological properties of the signal events were calculated for multivariate analysis. Some of the variables with most discriminative power are shown in figure 2.

Due to the excellent photon reconstruction, the number of photon can be used to differentiate different final states. The majority of $\mu^- \bar{\nu}_\mu \nu_\tau$, $\pi^- \nu_\tau$ and $a_1(\pi^- \pi^- \pi^+) \nu_\tau$ final states have zero photon reconstructed. Almost half of the $e^- \bar{\nu}_e \nu_\tau$ final state event have one photon reconstructed, due to the FSR. $\rho(\pi^- \pi^0) \nu_\tau$ and $\pi^- \pi^- \pi^+ \nu_\tau$ have nearly 80% events with two reconstructed photons, whilst $a_1(\pi^- \pi^- \pi^+) \nu_\tau$ have over 60% events with four reconstructed photons. The loss in efficiency is due to the increasing difficulty to separate nearby photons.

The number of charged PFOs can separate the leptonic and 1-prong final states, from the 3-prong final states. The efficiency of leptonic final states are over 98%.

The invariant mass of the visible PFOs shows clear differences between different final states. $\rho(\pi^- \pi^0) \nu_\tau$, $a_1(\pi^- \pi^0 \pi^0) \nu_\tau$ and $a_1(\pi^- \pi^- \pi^+) \nu_\tau$ distribution show clear resonance at ρ (a) and a. $e^- \bar{\nu}_e \nu_\tau$, $\mu^- \bar{\nu}_\mu \nu_\tau$ and $\pi^- \nu_\tau$ distribution show much smaller invariant mass and $\pi^- \pi^- \pi^+ \nu_\tau$ shows a large invariant mass than a.

For the final states with resonance, additional χ^2 minimisation test for particle pairings have been performed. For example, $a_1(\pi^- \pi^0 \pi^0) \nu_\tau$ final state, the χ_a^2 to minimise is,

$$\chi_a^2 = \left(\frac{m_{a,fit} - m_a}{\sigma_a} \right)^2 + \left(\frac{m_{\pi^0,fit} - m_{\pi^0}}{\sigma_{\pi^0}} \right)^2 + \left(\frac{m_{\pi^0^*,fit} - m_{\pi^0}}{\sigma_{\pi^0}} \right)^2, \quad (3.1)$$

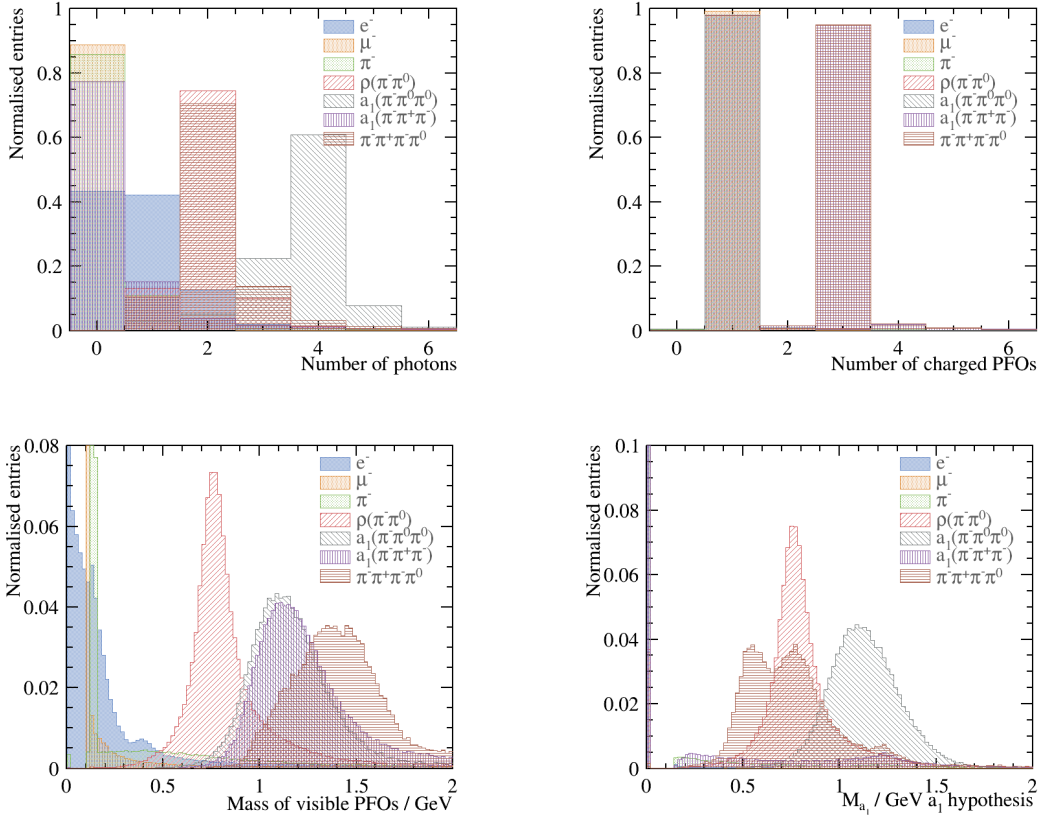


Figure 2. The example normalised distribution for discriminative variables for seven final states, $e^- \bar{\nu}_e$, ν_τ , $\mu^- \bar{\nu}_\mu$, ν_τ , $\pi^- \nu_\tau$, $\rho(\pi^- \pi^0) \nu_\tau$, $a_1(\pi^- \pi^0 \pi^0) \nu_\tau$, $a_1(\pi^- \pi^+ \pi^-) \nu_\tau$ and $\pi^- \pi^+ \pi^- \nu_\tau$, separated with truth information, with $\sqrt{s} = 100$ GeV for nominal CLIC_ILD detector model. The top left and top right, bottom left and bottom right plots are the normalised entries against the number of photons, number of charged PFOs, invariant mass of visible PFOs and the invariant mass of $a_1(\pi^- \pi^0 \pi^0)$ for $a_1(\pi^- \pi^0 \pi^0)$ hypothesis, respectively. There is a clear distinction between different final states in each plot.

where $m_{\pi^0,fit}$ and $m_{\pi^0^*,fit}$ are the invariant masses of all possible two photons combinations, σ_a and σ_{π^0} are the half width of the invariant mass distribution of reconstructed a and π^0 using the truth information, and m_a and m_π are the masses of a and π^0 , taken from [14]. If there are two or three photons, the χ_a^2 expression will be reduced and not including $m_{\pi^0^*,fit}$ term. If there are fewer than two photons, the χ_a^2 expression would only contain $m_{a,fit}$ term.

For the $\rho(\pi^- \pi^0) \nu_\tau$ final state, a similar χ_ρ^2 test for ρ hypothesis is used to extract $m_{\rho,fit}$ and $m_{\pi^0,fit}$ variables. χ_ρ^2 is similar to χ_a^2 with ρ replacing a and only one $m_{\pi^0,fit}$ term.

Figure 2 shows the $m_{a,fit}$ where $\rho(\pi^- \pi^0) \nu_\tau$, $a_1(\pi^- \pi^0 \pi^0) \nu_\tau$ and $\pi^- \pi^+ \pi^- \nu_\tau$ final states contribute to the a resonance, although only $a_1(\pi^- \pi^0 \pi^0) \nu_\tau$ final has a real a resonance. This is due to the structure of the χ_a^2 minimisation function allowing final states with more than two photons and one π^\pm to contribute.

Additional variables are calculated using the calorimeter information, the comparison with the electromagnetic shower profile, the matching between the track and the cluster, the energy and invariant masses for different types of particles. The full list of variables for multivariate analysis is shown in the appendix.

Energy of the τ is assume to be the same as the energy of e^\pm beam, which is half of the \sqrt{s} energy. Recoil momenta were calculated assuming the $e^- e^+$ collision happened at the centre of mass energy. Both assumptions are largely valid when there is no ISR contribution.

For the multivariate analysis, the multiclass class of the TMVA package [15] was used to train the seven final states simultaneously. The multiclass class is an extension of the standard signal-background classifier. For each final state, the multiclass classifier will train the final state as the signal against all other final states as the background. This process is repeated for each final state. The classifier output for a single event is a normalised number for each final state, where the sum is one. The number of a final state of a event can be used as the probability. The event is classified into a particular final state if the final state has the highest classifier output number. The advantage of using the multiclass is that the correction between different final states are accounted for and the classifier output are correctly adjusted for multiple final states, hence one event can only be classified into one final state.

Half of the randomly selected samples were used in the training process and the other half were used for testing.

The TMVA multiclass classifier used is boosted decision tree with gradient boosting (BDTG), as it was found to give for the best performance. The MVA classifier is trained and optimised to give the best overall separation across all final states.

4 Results and discussion

Table 2. The probability of reconstruction of true decay modes in columns in percent, with $\sqrt{s}=100$ GeV for nominal CLIC_ILD detector model. Bold numbers show the correctly reconstructed terms. Numbers less than 0.25% are not shown. Statistical uncertainties are less than 0.25%. Final states include ν_τ , which is not shown.

Reco \downarrow True \rightarrow	$e^- \bar{\nu}_e$	$\mu^- \bar{\nu}_\mu$	π^-	$\rho(\pi^-\pi^0)$	$a_1(\pi^-\pi^0\pi^0)$	$a_1(\pi^-\pi^-\pi^+)$	$\pi^-\pi^-\pi^+$
$e^- \bar{\nu}_e$	99.8	-	0.9	1.1	0.8	-	-
$\mu^- \bar{\nu}_\mu$	-	99.5	0.5	-	-	-	-
π^-	-	0.3	93.2	0.9	-	0.4	-
$\rho(\pi^-\pi^0)$	-	-	4.1	93.0	10.5	0.6	2.8
$a_1(\pi^-\pi^0\pi^0)$	-	-	-	4.3	88.2	-	1.0
$a_1(\pi^-\pi^-\pi^+)$	-	-	1.0	0.3	-	96.6	6.9
$\pi^-\pi^-\pi^+$	-	-	-	0.4	0.4	2.4	89.3

The reconstruction efficiencies for the seven final state of the tau decaying with c.o.m. energy of 100 GeV for the nominal CLIC_ILD detector are shown in the table 2. The perfect reconstruction would result in only diagonal terms. For leptonic decay, the selection efficiency is above 99.5% as the tracking system have much better resolution than the calorimeter. For 1-prong final states,

the confusion between each final states is due to the limit of photon reconstruction and photon resolution. Similarly, the confusion between 3-prong final states are due to photon reconstructions as well. There is also confusion that 1-prong final states being misidentified as $e^- \bar{\nu}_e$, due to the confusion between an early showered π^- and a e^- .

The study was repeated with $\sqrt{s}= 100, 200, 500, 1000$ GeV. The ECal square cell sizes were also varied at 3, 5, 7, 10, 15 and 20 mm, whilst keeping the the total ECal size the same. The results table were are in the appendix X.

To compare the impact of the ECAL cell sizes and the \sqrt{s} energies on the separation of tau final states, the selection efficiencies were plotted in the figure 3. The leptonic decay selection efficiencies are not shown as they are similar across different ECal cell sizes. This is because the e^\pm and μ^\pm identifications mostly rely on the tracking system, which was not varied in this study. The energy deposited in the calorimeter are used for the association to the tracks but it has a small impact on the lepton identification.

Overall, the hadronic decay selection efficiency decreases as the \sqrt{s} energy increases. This is due to the fact that when τ s are boosted at higher \sqrt{s} energies, the separation between decay products is smaller. Hence it is more difficult to reconstruct multi-photon final states correctly.

As the ECal cell sizes increase, the reconstruction efficiencies generally decrease. Larger cell sizes have lower spatial resolutions, making the separating of nearby photons more difficult.

For the $a_1(\pi^-\pi^0\pi^0) \nu_\tau$ final state, the selection efficiency for 500 GeV rises from ECal cell sizes 15 mm to 20 mm and the one for 1000 GeV rises from 7 , to 20 mm actually goes up as cell size increases. This is because when the algorithm can not reconstruct four photons in the $a_1(\pi^-\pi^0\pi^0) \nu_\tau$ final state, and the event topology would be very similar to the $\rho(\pi^-\pi^0) \nu_\tau$ final states.

For the $\sqrt{s}= 100$ and 200 GeV, the selection efficiency of the 5 mm ECal cell size is better than that of the 3 mm. One possible explanation is that the and the PandoraPFA have been optimised for the nominal ILD detector with the 5 mm ECal cell size, which shares the same ECal structure with the nominal CLIC_ILD detector.

In order to compare the overall separation power of all the final states across c.o.m. energy and the ECal cell sizes, we constructed a single parameter function, the τ hadronic decay final state efficiency function,

$$\epsilon_{had} = \frac{(\sum_i Br_i \epsilon_i)}{\sum_i Br_i}, \quad (4.1)$$

where Br_i is the branching fraction of a hadronic final state after the generator level cut, ϵ_i is the selection efficiency of the final state and the i is summing over five hadronic decay final state of τ . Leptonic decays, $e^- \bar{\nu}_e \nu_\tau$ and $\mu^- \bar{\nu}_\mu \nu_\tau$, were not included as the variation of the leptonic decay selection efficiency is small.

In the figure 4, τ hadronic decay final state efficiency, ϵ_{had} , against the ECal cell size with different \sqrt{s} is shown. ϵ_{had} decreases when cell sizes increases and when \sqrt{s} increases. Again, ϵ_{had} of the 5 mm ECal cell size is better than that of the 3 mm for 100 and 200 GeV lines possibly due the optimisation of the software fro the nominal ILD 5 mm cell size.

The ϵ_{had} is above 90% for the ECal cell size from 3 to 20 mm for the $\sqrt{s}= 100$ GeV. For $\sqrt{s}= 200$ GeV, the ϵ_{had} decreases from over 90% to 86% for the ECal cell size from 3 to 20 mm. The

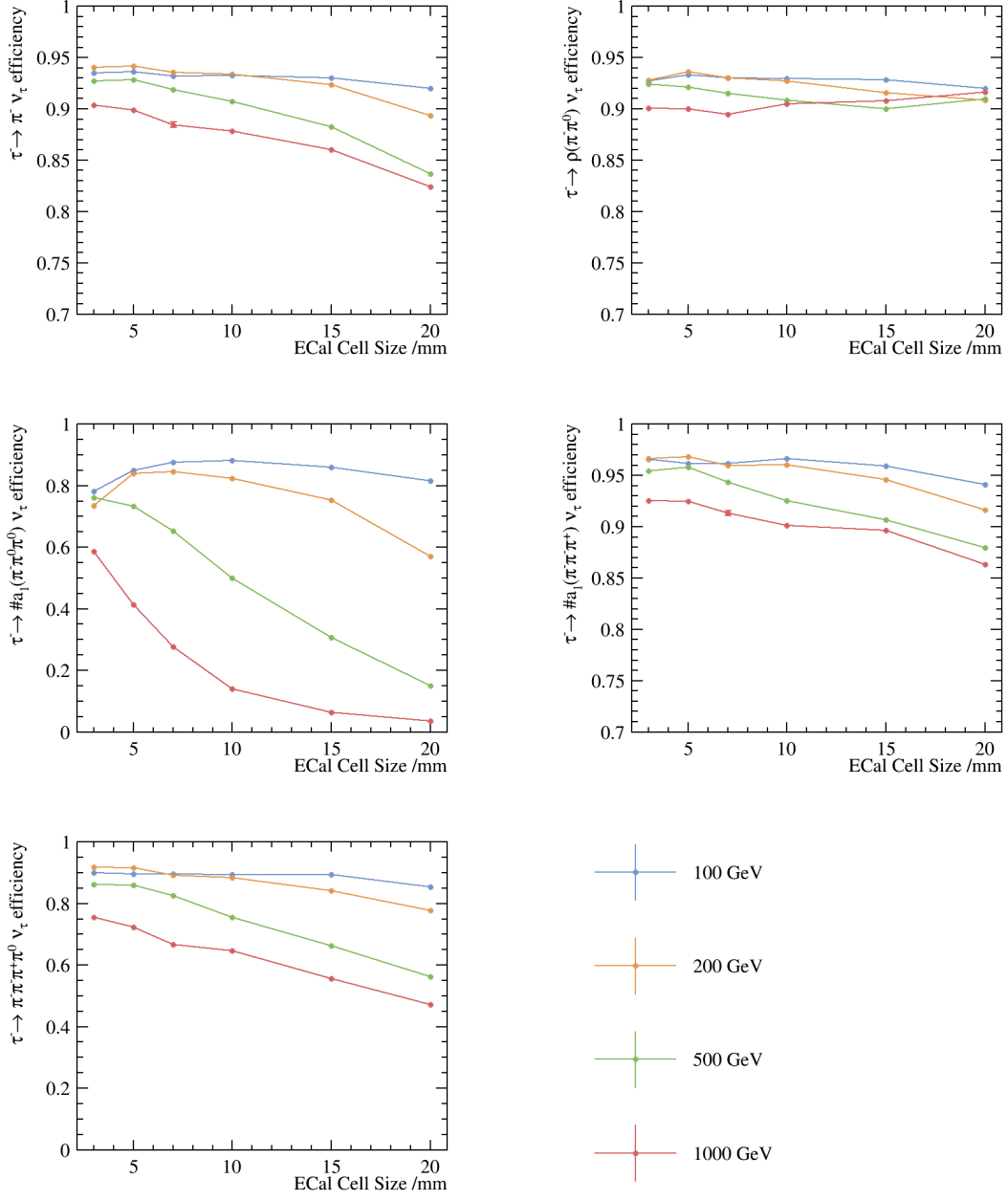


Figure 3. The selection efficiencies for various final states against the ECal cell size for different c.o.m. energies with the nominal CLIC_ILD detector model are shown. The top left, top right, middle left, middle right and bottom left plots are for the $\pi^- \nu_\tau$, $\rho(\pi^-\pi^0) \nu_\tau$, $a_1(\pi^-\pi^0\pi^0) \nu_\tau$, $a_1(\pi^-\pi^+\pi^-) \nu_\tau$ and $\pi^-\pi^+\pi^0 \nu_\tau$ final states respectively. From the top to the bottom, blue, orange, green and red lines are representing the $\sqrt{s}=100, 200, 500$ and 1000 GeV respectively. Note that the y axis are not the same for displaying purpose.

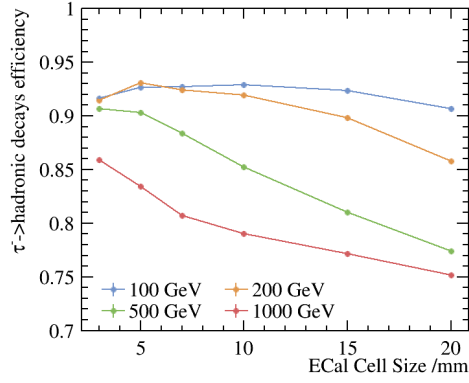


Figure 4. The τ hadronic decay selection efficiency against the ECal cell size for different \sqrt{s} energies with the nominal CLIC_ILD detector model are shown. The blue, orange, green and red lines are representing the $\sqrt{s}= 100, 200, 500$ and 1000 GeV respectively.

degradation of the ϵ_{had} is significant for the 500 and 1000 GeV lines, where the ϵ_{had} drops from over 90% to 77% and from 86% to 75% respectively.

For low \sqrt{s} , namely 100 and 200 GeV, up to 15 mm cell sizes of ECal will give a good performance for τ hadronic decay modes separation, and the ϵ_{had} is above 90%. For the high \sqrt{s} , namely 500 and 1000 GeV, it is preferential to have a small ECal cell size for τ hadronic decay modes separation. There is about 15% degradation of ϵ_{had} for ECal cell size from 3 to 20 mm.

The paper illustrated the usage of reconstruction of the tau decay modes as a benchmark for the detector optimisation.

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