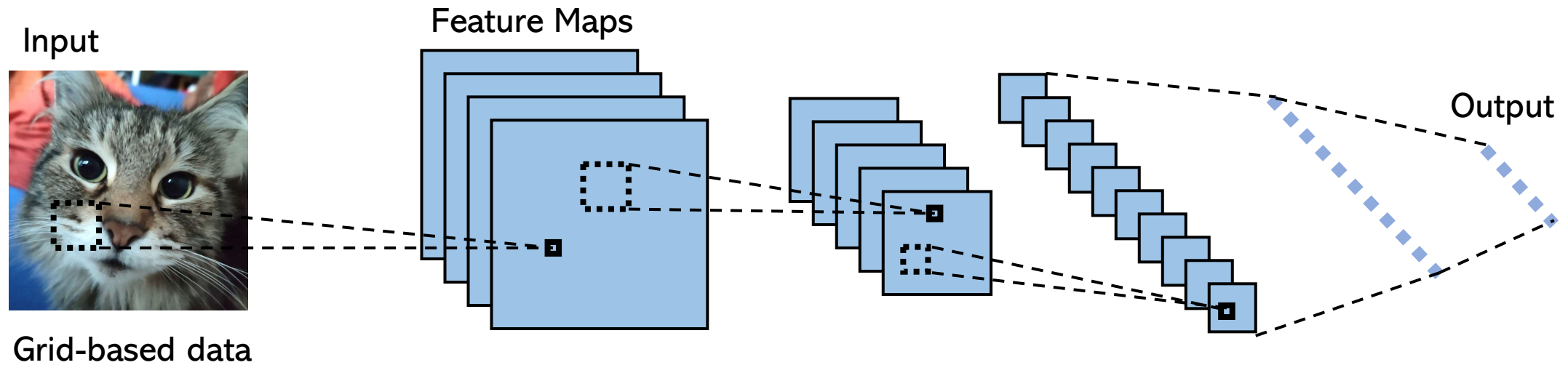


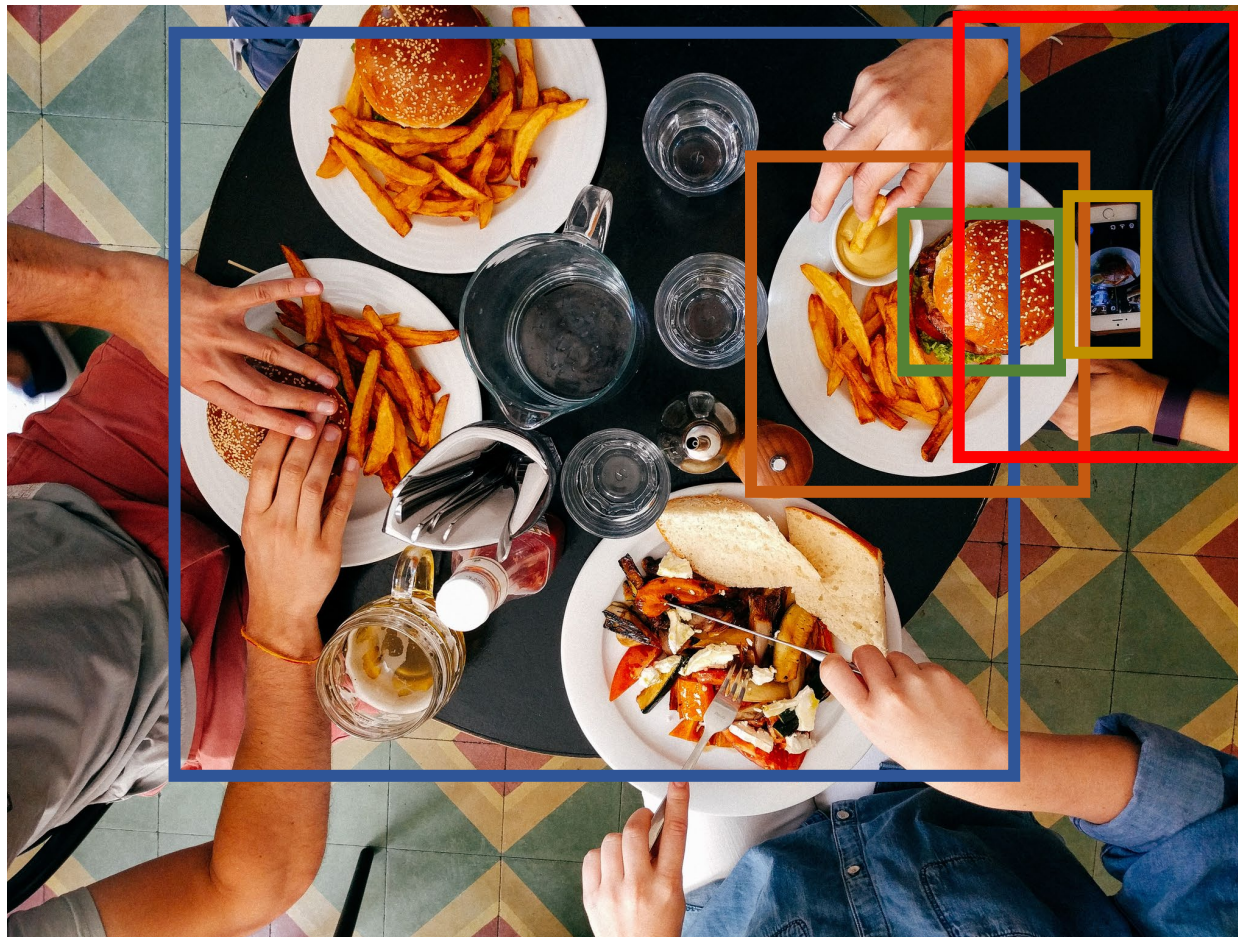
Graph Neural Networks in Vision and Graphics

Jan Eric Lenssen – Stanford Graph Learning Workshop, September 16, 2021

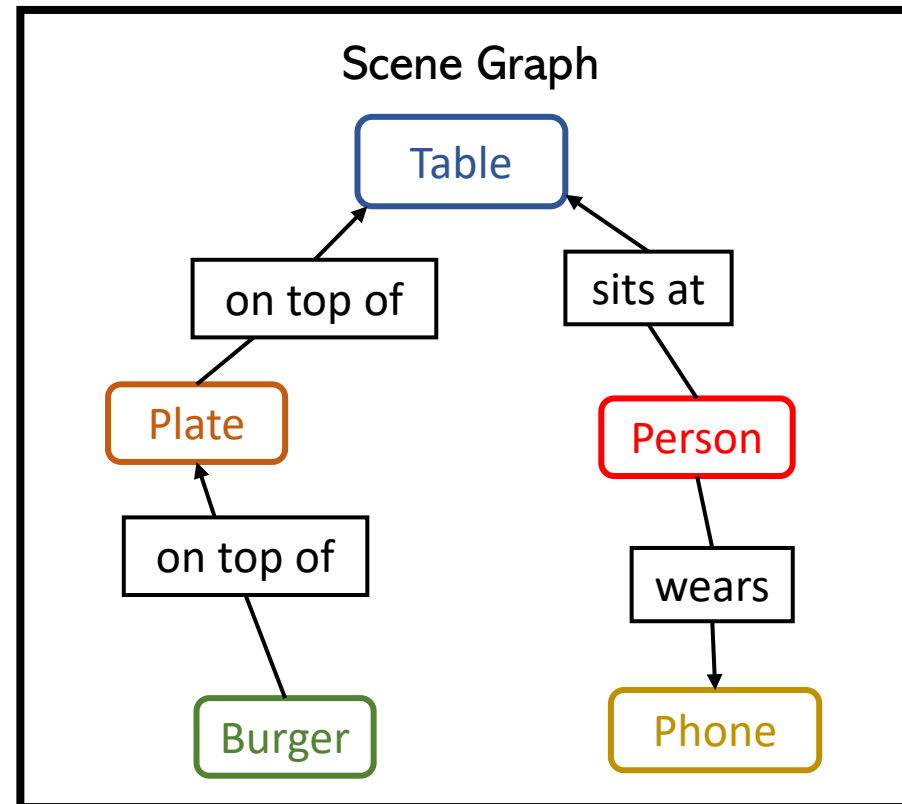
Differentiable programming in CV is dominated by CNNs



What about object hierarchies?



DIV2K dataset



Or graphs with **geometric information**?

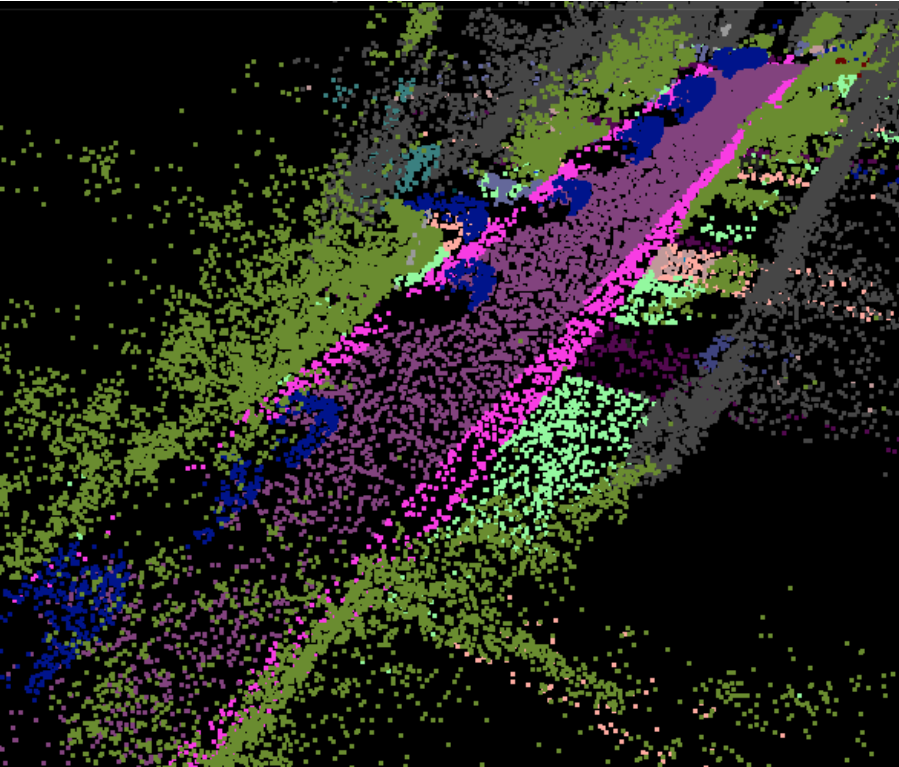


Fey et al., Deep Graph Matching Consensus, ICLR 2020

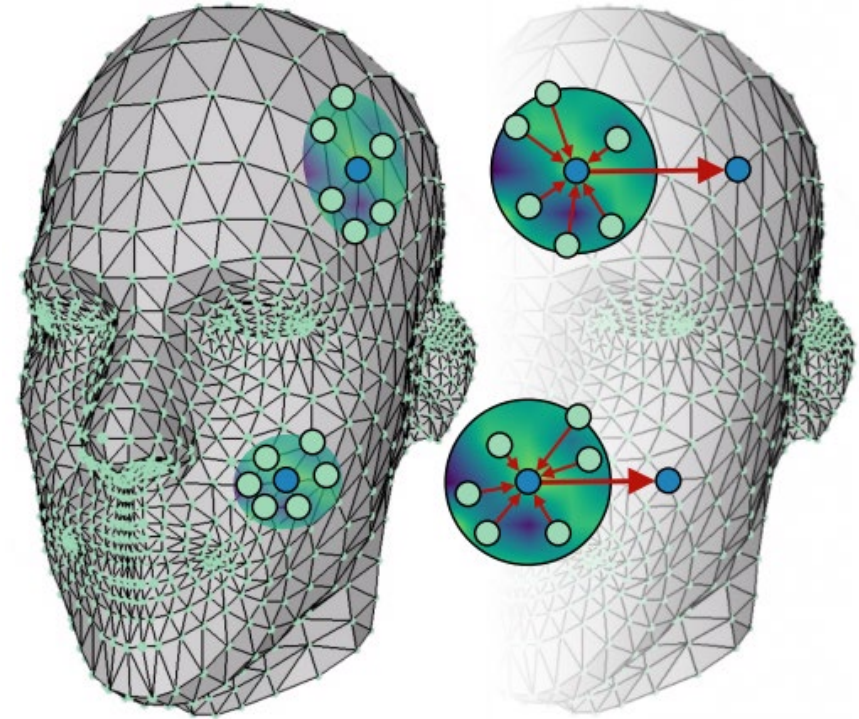


Cao et al., Realtime Multi-Person 2D Pose Estimation using Part Affinity Fields, CVPR 2017

Point Clouds and Meshes?



KITTI dataset



Fey et al., SplineCNN, CVPR 2018

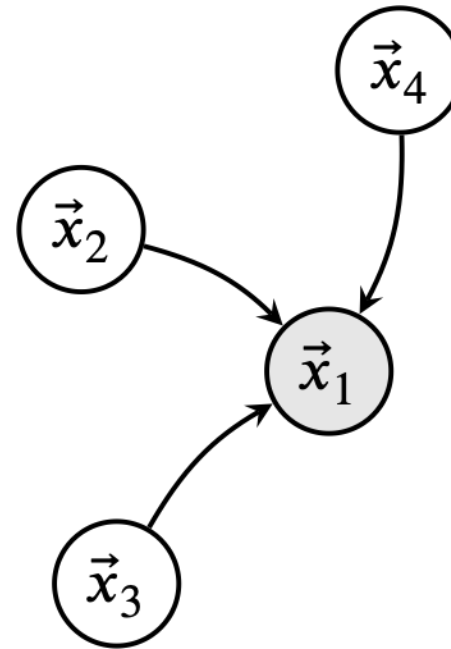
GNNs describe differentiable data flow between entities

Entities can be:

- Nodes
- 3D points
- Scene objects
- Keypoints

Relations can be:

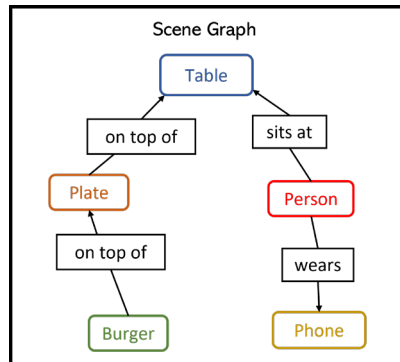
- Cartesian/Polar relationship
- Hierarchical relationship
- Mesh edges
- ...



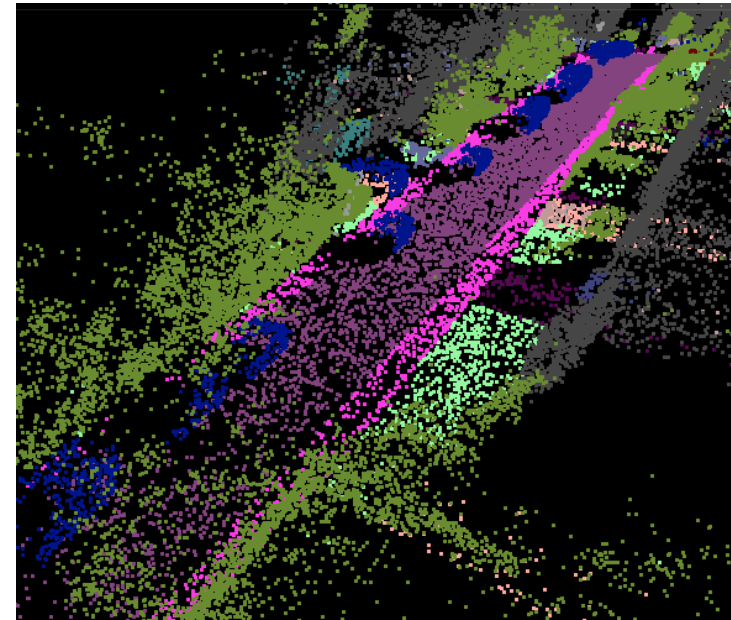
$$\vec{x}'_i = \text{UPDATE} \left(\vec{x}_i, \sum_{j \in \mathcal{N}(i)} \text{MESSAGE}(\vec{x}_i, \vec{x}_j, \vec{e}_{j,i}) \right)$$

GNNs as building block for differentiable programming

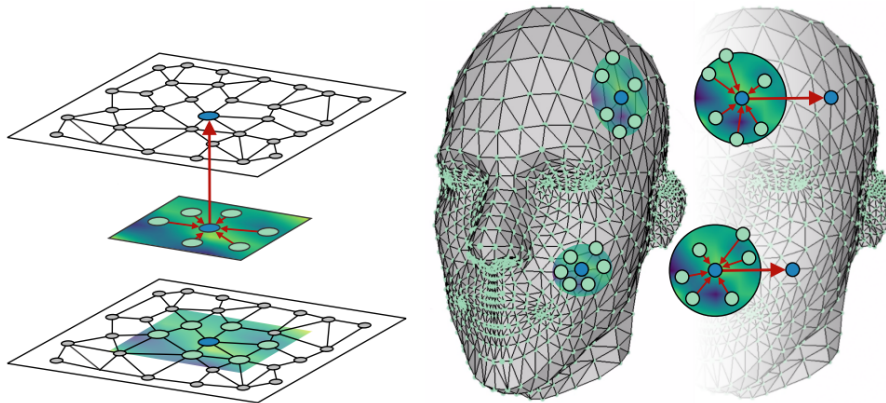
... to fuse data from multiple entities



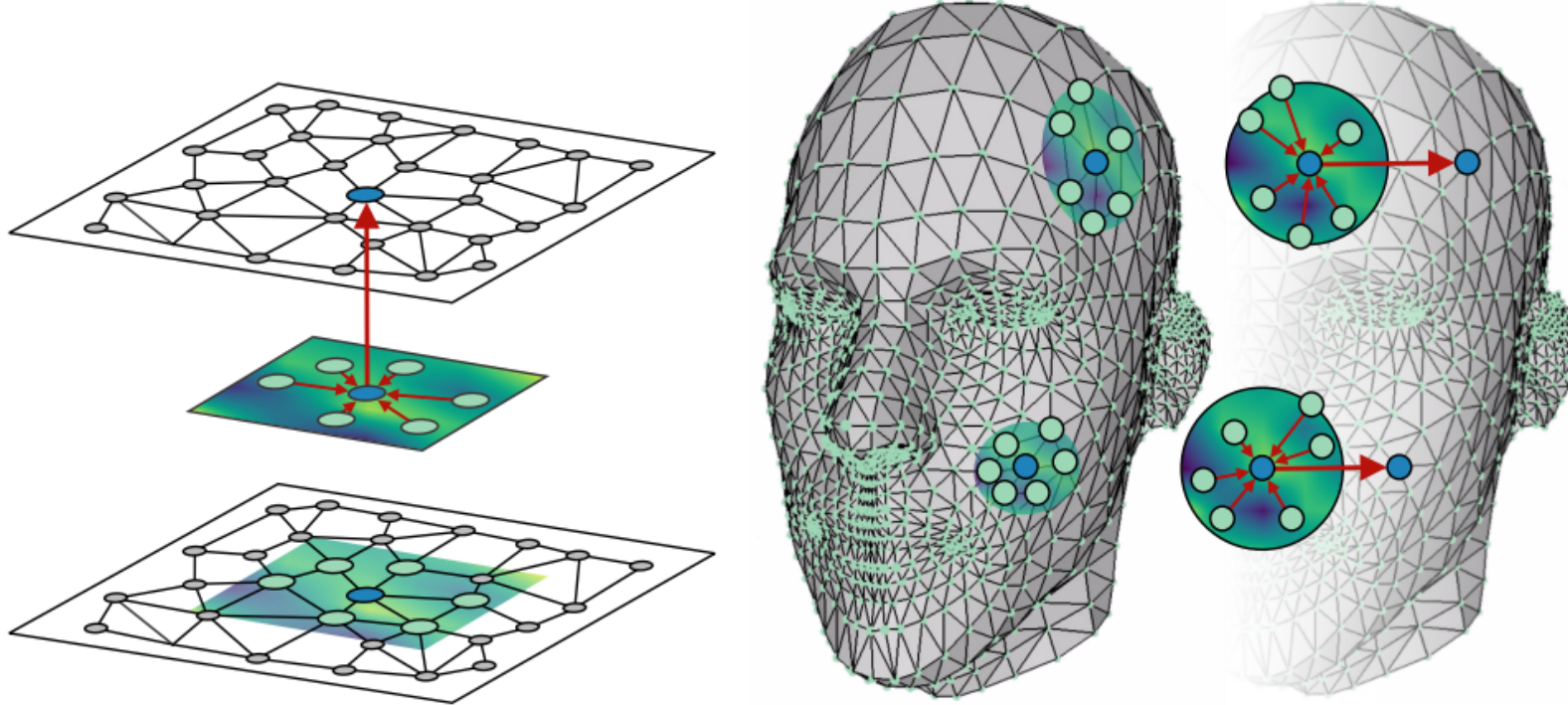
... to analyze geometric structures



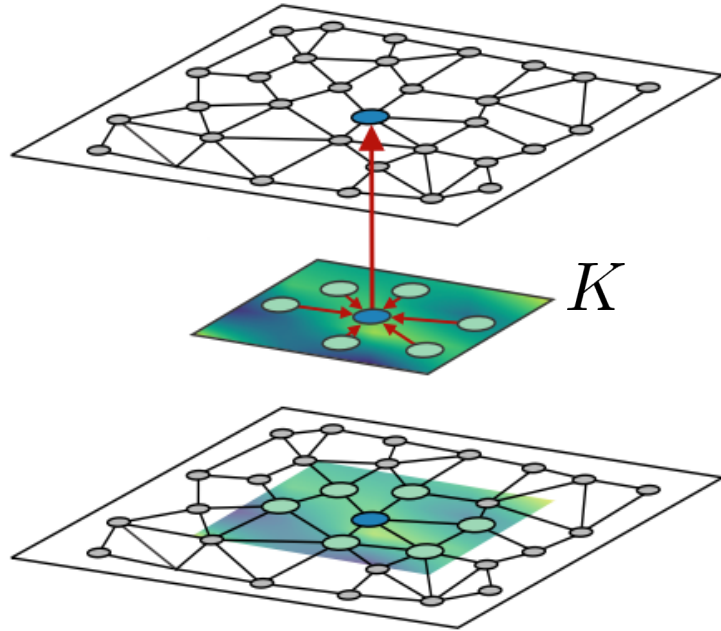
... to process data on irregular domains



GNNs for Continuous Convolution



GNNs for Continuous Convolution



Continuous Convolution:

$$\mathbf{x}_i = \sum_{j \in \mathcal{N}(i)} K(\mathbf{p}_j - \mathbf{p}_i) \cdot \mathbf{x}_j$$

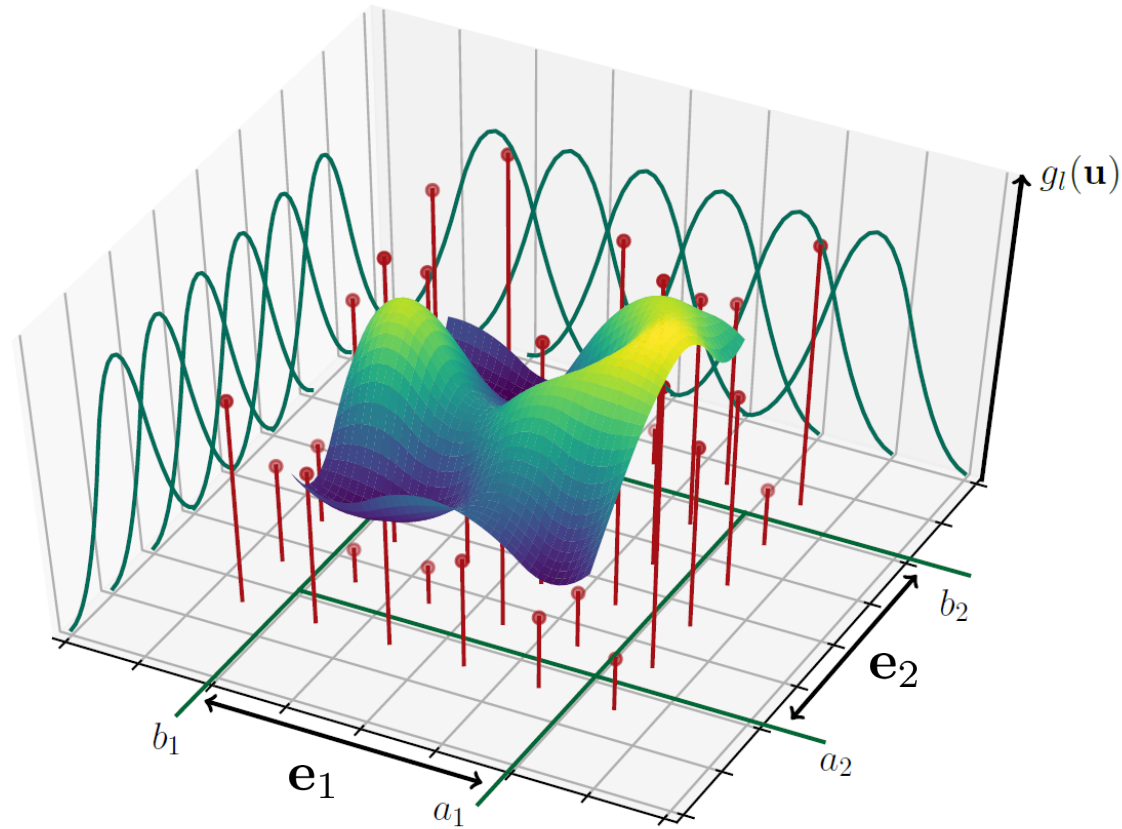
Message Passing:

$$\mathbf{x}_i = \text{Update} \left(\mathbf{x}_i, \sum_{j \in \mathcal{N}(i)} \text{Message}(\mathbf{x}_i, \mathbf{x}_j, \mathbf{e}_{i,j}) \right)$$

Message for Continuous Convolution:

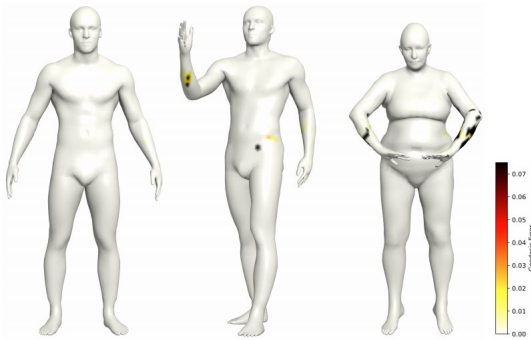
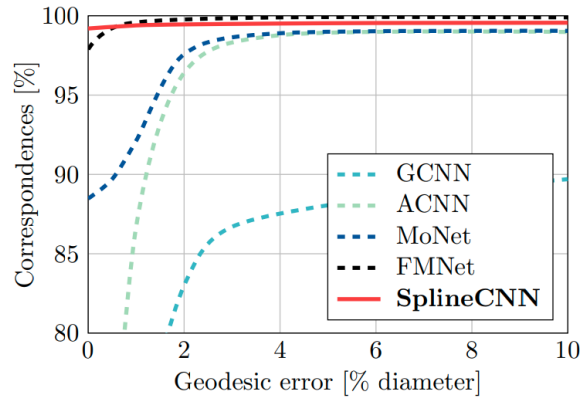
$$\begin{aligned} \text{Message}(\mathbf{x}_j, \mathbf{e}_{j,i} = (\mathbf{p}_j - \mathbf{p}_i)) \\ = K(\mathbf{e}_{j,i}) \cdot \mathbf{x}_j \end{aligned}$$

GNNs for Continuous Convolution



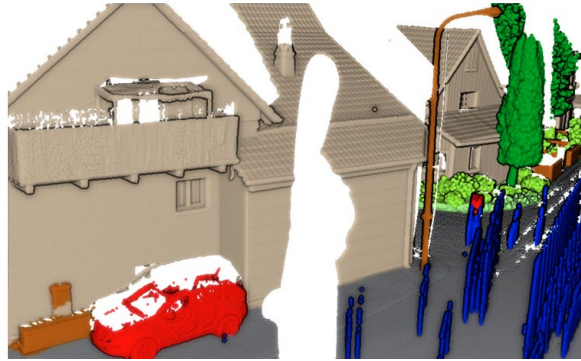
Processing data on irregular, geometric domains

Shape Correspondence



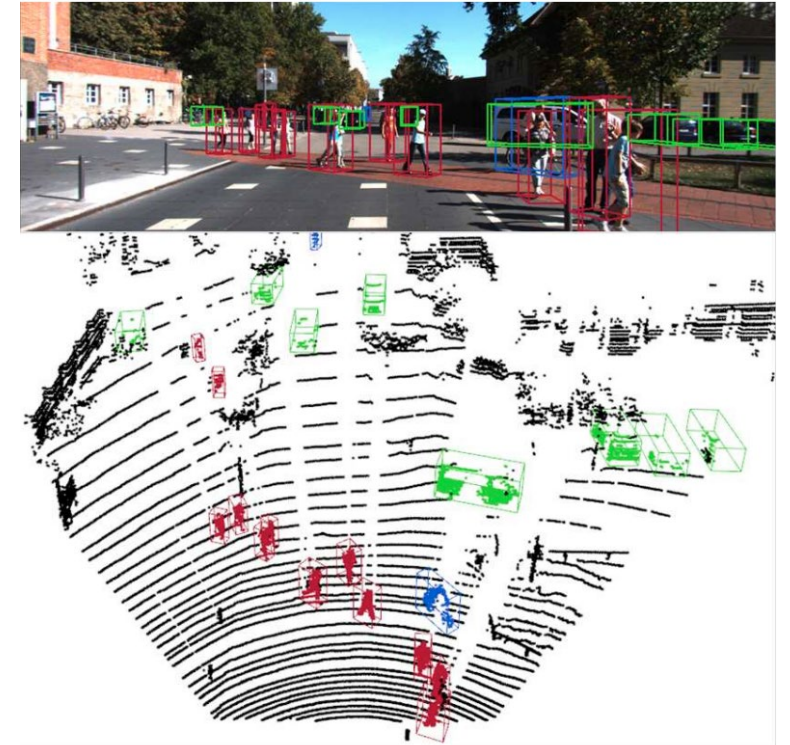
Fey et al., SplineCNN, CVPR 2018

Semantic Segmentation



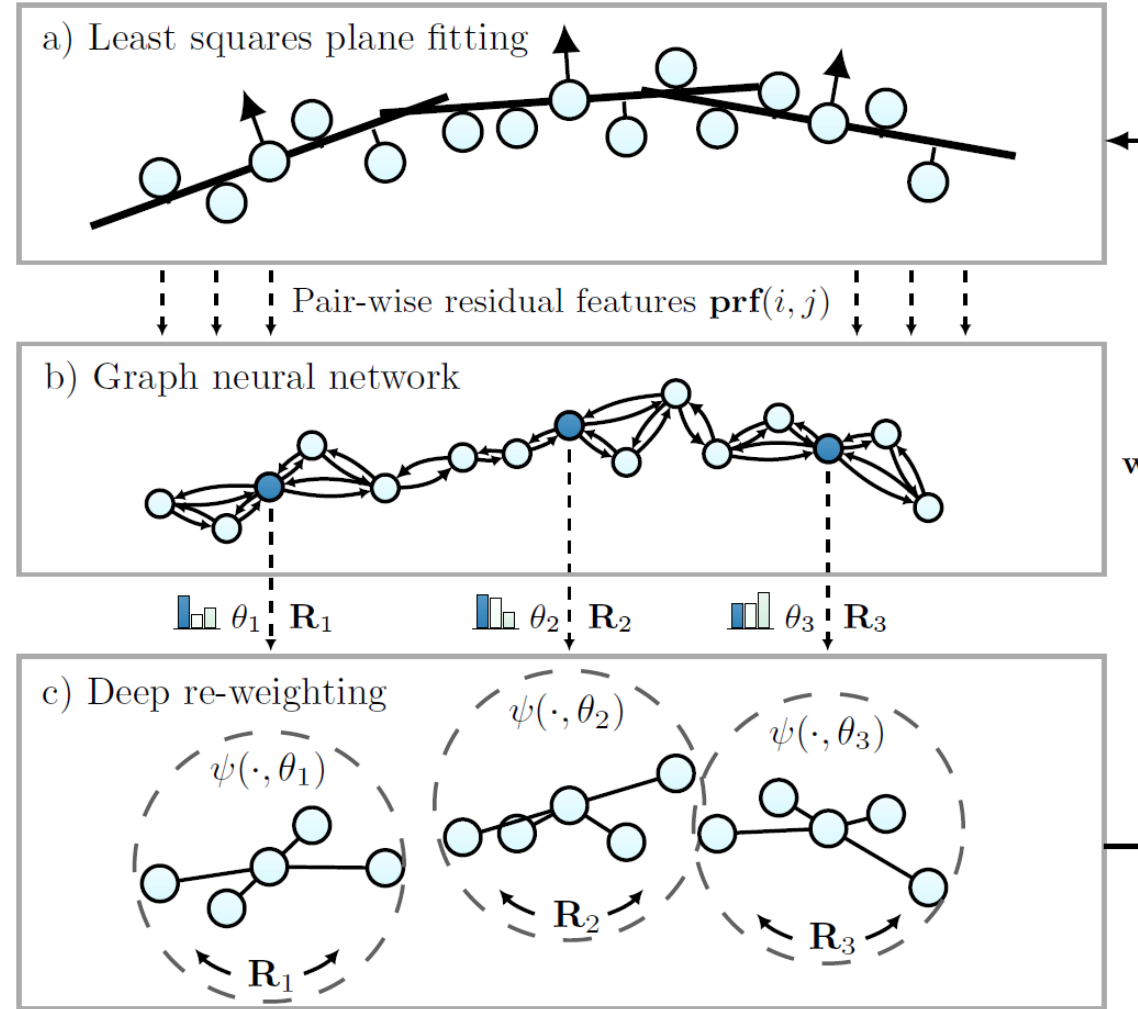
Thomas et al., KPConv, CVPR 2019

3D Object Detection

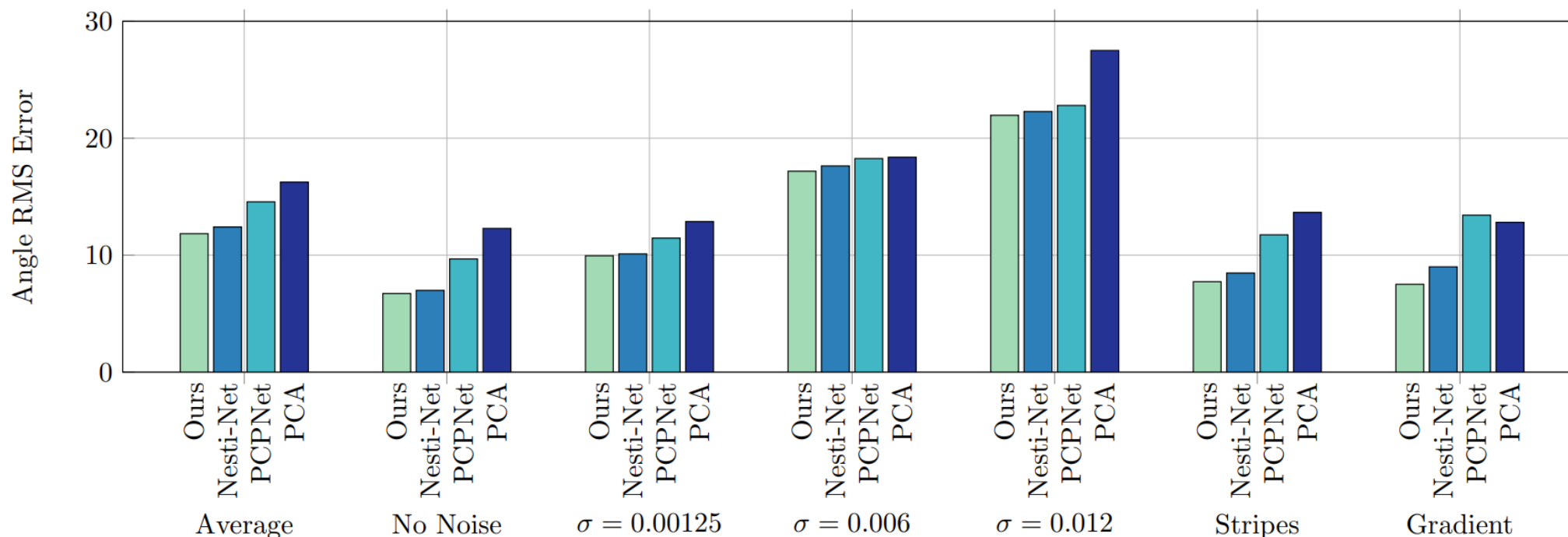


Shi et al., Point-GNN, CVPR 2020

Processing geometric structures



Processing geometric structures



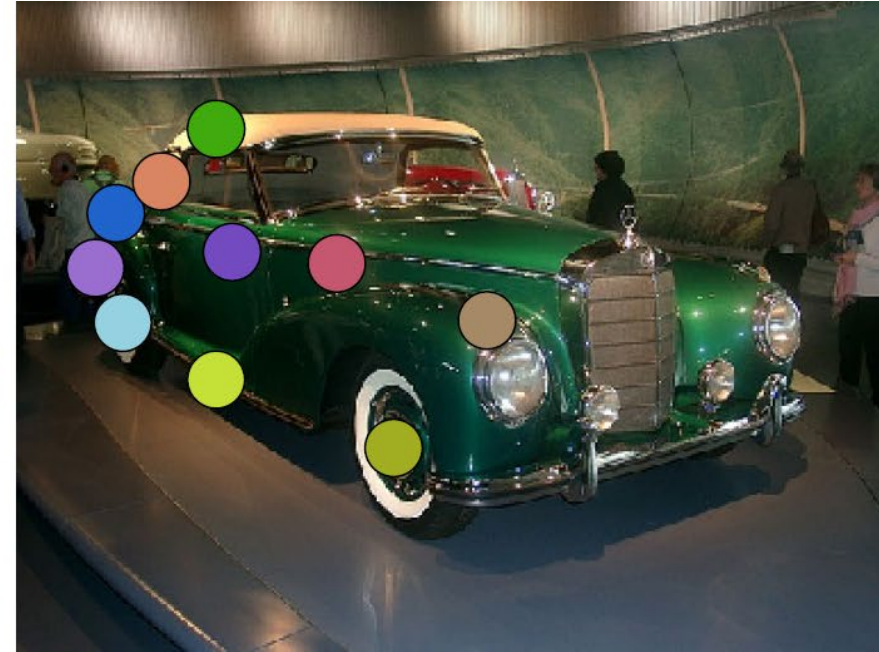
	Ours	Nesti-Net	PCPNet
Number of network parameters	7981	179M	22M
Execution time for 100k points	3.57 s	1350 s	470 s
Relative execution time	1×	378×	131×

Matching geometric graphs



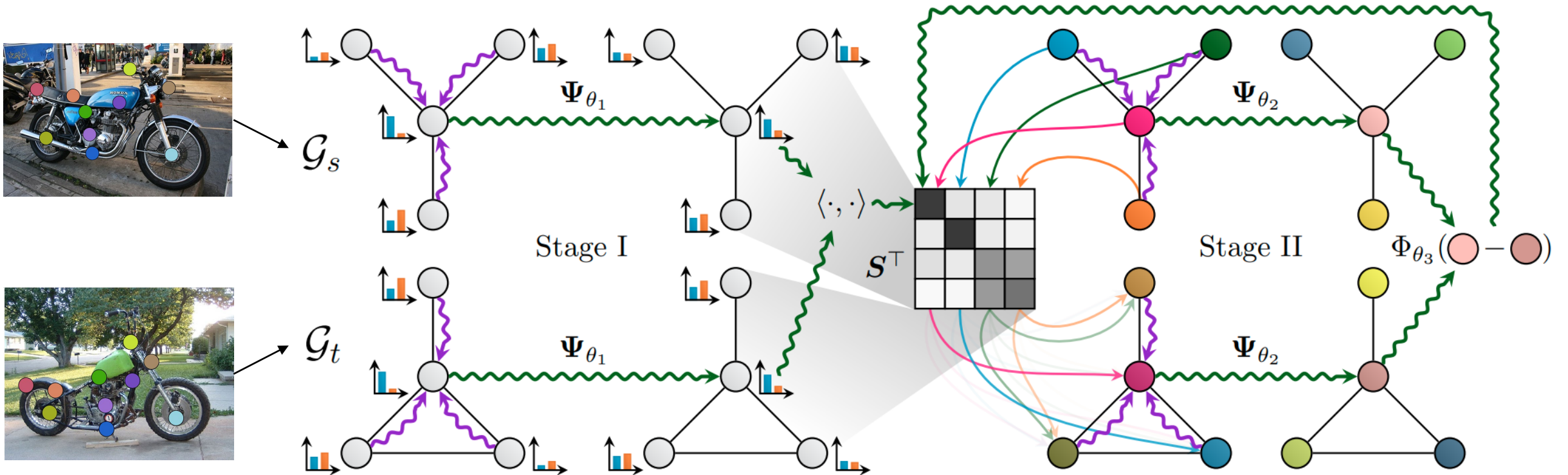
WILLOW-ObjectClass dataset

Matching geometric graphs



WILLOW-ObjectClass dataset

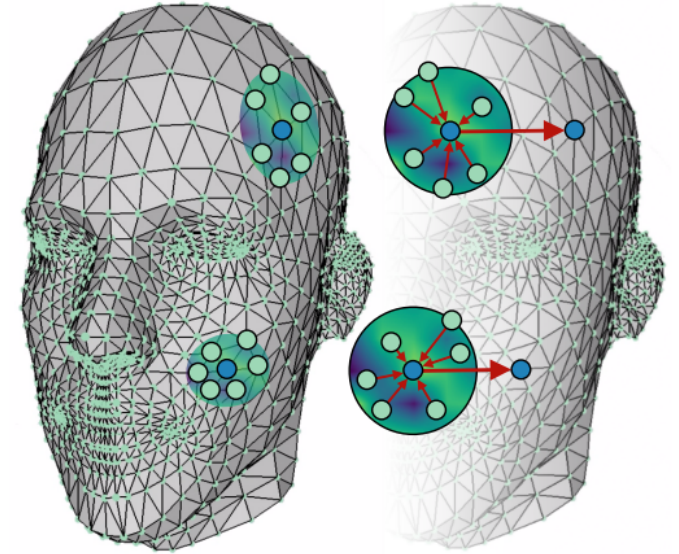
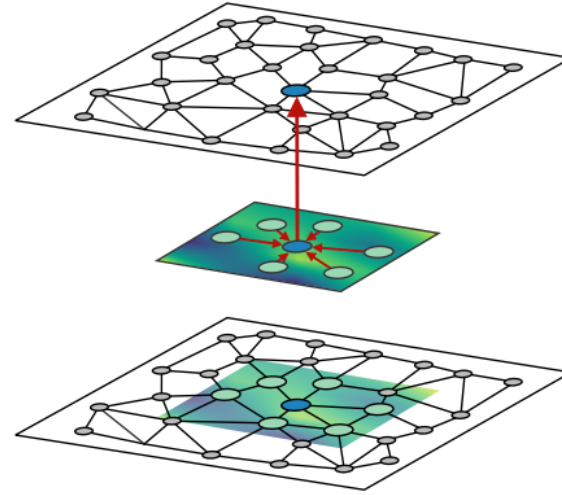
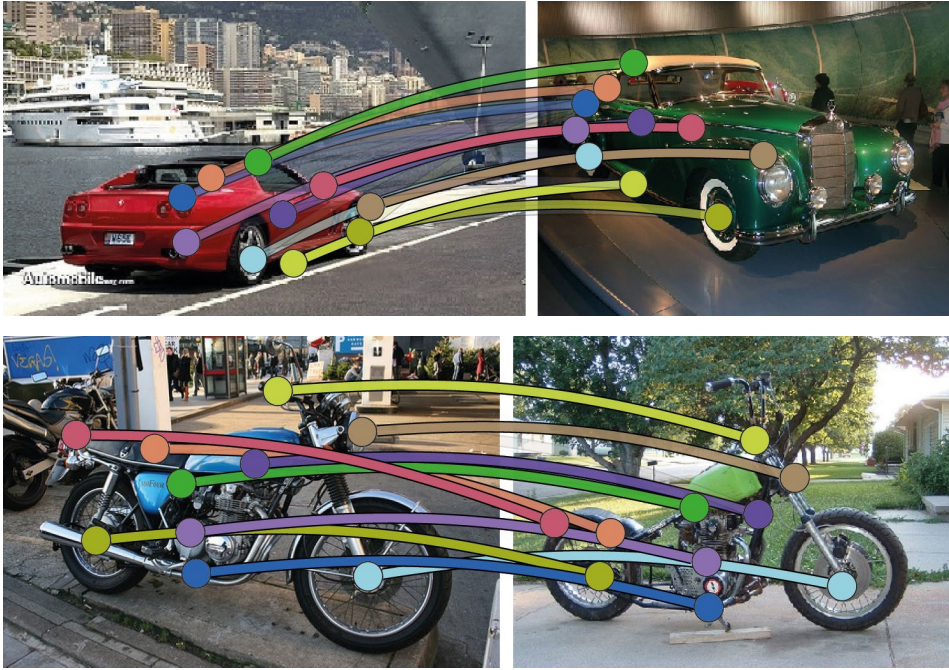
Matching geometric graphs



Matching geometric graphs



WILLOW-ObjectClass dataset



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