

Parsing

Parsing is a process that constructs a syntactic structure(i.e. parse tree) from the stream of tokens

Top-down Parsing

Info

created order : created from root to leaves
traversal of parse tree : preorder traversal
Derivation : left-most derivation

Two Types :

1.Backtracking Parser :

Try different structures and backtrack if it does not matched the input

2.Predictive Parser :

Guess the structure of the parse tree from the next input

Parser have to decide which production rule should be used at each point of time

If using predictive parser how should we guess?

1.next token like Reserved word if,(,etc.

2.structure to be built like if statement,etc.

LL(1) Parsing

Info

L = read input from left to right

L = simulate left most derivation

(1) = 1 lookahead symbol

ใช้ stack ที่ล่างสุดเป็น \$ ถ้าสุดท้ายสามารถอ่านตัวนี้ได้แปลว่า accepted

start the process by adding start symbol

If top is terminal, check if match pop it out

else, replace with P that associated with

lookahead

Aware : $A \Rightarrow XY$ top is X cuz leftmost derivation

First set

Info

First set care λ

$\text{First}(A)$ = set ของ terminal ตัวแรกที่ derived ได้จาก A

- Let X be λ or be in V or T.
- $\text{First}(X)$ is the set of the first terminal in any sentential form derived from X.
- For example: $S \rightarrow (S) S, S \rightarrow \lambda$
The strings derived from S are $\lambda, (), ()(), (()), ()(), \dots$
So, the symbols λ or (must be in $\text{First}(S)$.

Some properties:

$A \Rightarrow XY$

First set of A will be subset of leftmost ones

$\text{First}(A) \subset \text{First}(X)$

③ $\text{exp} \rightarrow \text{term exp}'$

② $\text{exp}' \rightarrow \text{addop term exp}' \mid \lambda$

① $\text{addop} \rightarrow \boxed{+ \mid -}$ all Terminal

② $\text{term} \rightarrow \text{factor term}'$

③ $\text{term}' \rightarrow \text{mulop factor term}' \mid \lambda$

② $\text{mulop} \rightarrow \boxed{*}$ all Terminal

① $\text{factor} \rightarrow \boxed{(\text{exp})} \mid \boxed{\text{num}}$ all Terminal

	First
exp	(, num
exp'	+ , -, λ
addop	+ , -
term	(, num
term'	λ , *
mulop	*
factor	(, num

Follow set

Info

Follow set dont care λ

$\text{Follow}(A)$ = set ของ terminal ตัวที่จะตามมาเมื่อ A ถูก pop

- Let \$ denote the end of input tokens.
- If A is the start symbol, then \$ is in $\text{Follow}(A)$.
- If there is a rule $B \rightarrow X A Y$, then $\text{First}(Y) - \{\lambda\}$ is in $\text{Follow}(A)$.
- For example: $S \rightarrow (S) S$, $S \rightarrow \lambda$

The strings derived from S are λ , (), ()(), (()), (()()), ...

So, the symbols) must be in follow S because there is a rule $S \rightarrow (S)$.

- If there is production $B \rightarrow X A Y$ and λ is in $\text{First}(Y)$, then $\text{Follow}(A)$ contains $\text{Follow}(B)$.

Some properties:

$A \Rightarrow XY$

Follow(leader) will be First(follower) - $\{\lambda\}$

$\text{Follow}(X) = \text{First}(Y) - \{\lambda\}$

Follow set of A will be subset of rightmost ones

$\text{Follow}(A) \subset \text{Follow}(Y)$

but if $\text{First}(Y)$ have λ

$\text{Follow}(A) \subset \text{Follow}(X)$ as well

① $\text{exp} \rightarrow \text{term exp}'$

② $\text{exp}' \rightarrow \text{addop term exp}' \mid \lambda$

③ $\text{addop} \rightarrow + \mid -$

④ $\text{term} \rightarrow \text{factor term}'$

⑤ $\text{term}' \rightarrow \text{mulop factor term}' \mid \lambda$

⑥ $\text{mulop} \rightarrow *$

⑦ $\text{factor} \rightarrow (\text{exp}) \mid \text{num}$

care chain reaction
follow so follow(exp) have)

	First	Follow
exp	(num	\$,)
exp'	λ + -	\$,)
addop	+ -	(, num
term	(num	+ , - \$,)
term'	λ *	+ , - \$,)
mulop	*	(, num
factor	(num	* , + , - \$,)

Constructing Parsing Table

	First	Follow
exp	{(, num}	{\$,)}
exp'	{+, -, λ }	{\$,)}
addop	{+, -}	{(, num}
term	{(, num}	{+, -, \$}
term'	{*, λ }	{+, -, λ , \$}
mulop	{*}	{(, num}
factor	{(, num}	{*, +, -, \$}

- 1 exp \rightarrow term exp'
- 2 exp' \rightarrow addop term exp'
- 3 exp' $\rightarrow \lambda$
- 4 addop $\rightarrow +$
- 5 addop $\rightarrow -$
- 6 term \rightarrow factor term'
- 7 term' \rightarrow mulop factor term'
- 8 term' $\rightarrow \lambda$
- 9 mulop $\rightarrow *$
- 10 factor $\rightarrow (\text{exp})$
- 11 factor $\rightarrow \text{num}$

vign. Audio
to First set
of λ

current derivation	()	+	-	*	num	\$
exp	1					1	
exp'		3	2	2			3
addop			4	5			
term	6					6	
term'		8	8	8	7		8
mulop					9		
factor	10					11	

LL(1) Grammar

Info

A grammar is an LL(1) grammar if its LL(1) parsing table has at most one production in each table entry

example of non-LL(1) grammar parsing table

	()	+	-	*	num	\$
exp	1,2					1,2	
term	3,4					3,4	
factor	5					6	
addop			7	8			
mulop					9		

What causes grammar being non-LL(1)

1. Left-recursion
2. Left factor

Left Recursion

Info

General left recursion : $A \Rightarrow^* AY$

Immediate left recursion :

basic : $A \rightarrow AX \mid Y$

multi : $A \rightarrow AX_1 \mid \dots \mid AX_n \mid Y_1 \mid \dots \mid Y_m$

regular expression : $A = YX^*$

Immediate left recursion can be easily removed
when no empty-string production and no cycle

basic :

$A \rightarrow YA'$

$A' \rightarrow XA' \mid \lambda$

multi :

$A \rightarrow Y_1A' \mid \dots \mid Y_mA'$

$A' \rightarrow X_1A' \mid \dots \mid X_nA' \mid \lambda$

regular expression : $A = YX^*$

$\text{exp} \rightarrow \text{exp} + \text{term} \mid \text{exp} - \text{term} \mid \text{term}$ เพราะสุดท้ายมันจบด้วย term

$\text{term} \rightarrow \text{term} * \text{factor} \mid \text{factor}$

$\text{factor} \rightarrow (\text{exp}) \mid \text{num}$

Not recursion no need change
Remove left recursion

$\text{exp} \rightarrow \boxed{\text{term}} \text{exp}'$

$\text{exp} = \text{term} (\pm \text{term})^*$

$\text{exp}' \rightarrow + \text{term} \text{exp}' \mid - \text{term} \text{exp}' \mid \lambda$

$\text{term} \rightarrow \boxed{\text{factor}} \text{term}'$

$\text{term} = \text{factor} (* \text{factor})^*$

$\text{term}' \rightarrow * \text{factor} \text{term}' \mid \lambda$

$\text{factor} \rightarrow (\text{exp}) \mid \text{num}$

Left-Factor

Info

Left same right diff so Separated

Left factor causes non-LL(1)

- Given $A \rightarrow X Y \mid X Z$. Both $A \rightarrow X Y$ and $A \rightarrow X Z$ can be chosen when A is on top of stack and a token in $\text{First}(X)$ is the next token.

$$A \rightarrow \underline{X} \underline{Y} \mid \underline{X} \underline{Z}$$

can be left-factored as

$$A \rightarrow \underline{X} A' \text{ and } A' \rightarrow \underline{Y} \mid \underline{Z}$$

$$A \rightarrow XY \mid XZ$$

$$A \rightarrow XB$$

$$B \rightarrow Y \mid Z$$

$$\text{ifSt} \rightarrow \underline{\text{if (exp) st}} \underline{\text{else st}} \mid \underline{\text{if (exp) st}} \underline{\hspace{1cm}}$$

can be left-factored as

$$\text{ifSt} \rightarrow \underline{\text{if (exp) st}} \underline{\text{elsePart}}$$

$$\text{elsePart} \rightarrow \underline{\text{else st}} \mid \underline{\lambda}$$

$$\text{seq} \rightarrow \underline{\text{st}} \underline{; \text{seq}} \mid \underline{\text{st}} \underline{\hspace{1cm}}$$

can be left-factored as

$$\text{seq} \rightarrow \underline{\text{st}} \underline{\text{seq}'}$$

$$\text{seq}' \rightarrow \underline{; \text{seq}} \mid \underline{\lambda}$$