



### Master's thesis in Applied Computer Science

## CoolingGen

A parametric 3D-modeling software for turbine blade cooling geometries using NURBS

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I hereby declare that this thesis has been written by myself and no other resources than those mentioned have been used.

Göttingen, July 11, 2022

#### Abstract

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### Zusammenfassung

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# Contents

1	Introduction 1		
	1.1	Motivation	1
	1.2	State of the Art	1
	1.3	Problem Statement	1
2	Methods		
	2.1	Bézier Curves	2
		2.1.1 Definition	2
		2.1.2 Properties	3
		2.1.3 De Casteljau's Algorithm	3
	2.2	Non-Uniform Rational B-Splines (NURBS)	3
		2.2.1 Definition	3
		2.2.2 Properties	3
		2.2.3 De Boor's Algorithm	3
	2.3	Methods on NURBS Objects	3
		2.3.1 Affine Transformations	3
		2.3.2 The Frenet-Serret Apparatus	3
		2.3.3 Finding Intersections	3
		2.3.4 Interpolation	3
	2.4	Jet Engine Design Specifics	3
		2.4.1 Fundamental Terms	3
		2.4.2 The S2M Net	3
		2.4.3 Fillet Creation	3
3	Res	sults	4
	3.1	Cooling Geometries And Their Parametrizations	4
		3.1.1 Chambers	4
		3.1.2 Turnarounds	4
		3.1.3 Slots	4
		3.1.4 Film Cooling Holes	4
		3.1.5 Impingement Inserts	4
	3.2	Export for CENTAUR	4
	3.3	Export for Open CASCADE	4
4	Dis	cussion	5
	4.1	Future Work	5
	4.2	Conclusion	5
5	Ref	rerences	6

# 1 Introduction

- 1.1 Motivation
- 1.2 State of the Art
- 1.3 Problem Statement

## 2 Methods

### 2.1 Bézier Curves

Bézier curves are named after the french engineer Pierre Bézier, who famously utilized them in the 1960s to design car bodies for the automobile manufacturer Renault [Béz68]. Today, they are used in a wide variety of vector graphics applications (i.e. in font representation on computers). At first glance, the definition of the Bézier curve might seem cumbersome, but given the mathematical foundation and a few graphical representations, it becomes apparent why they are such a powerful tool in computer-aided design.

#### 2.1.1 Definition

**Definition 2.1.1.** The *Bernstein basis polynomials* of degree n on the interval  $[t_0, t_1]$  are defined as

$$b_{n,k,[t_0,t_1]}(t) := \frac{\binom{n}{k}(t_1-t)^{n-k}(t-t_0)^k}{(t_1-t_0)^n},$$
(2.1)

for  $k \in \{0 \dots n\}$ .

**Definition 2.1.2.** A Bézier curve of degree n is a parametric curve  $C_{P,[t_0,t_1]}:[t_0,t_1]\to\mathbb{R}^3$  that has a representation

$$C_{P,[t_0,t_1]}(t) = \sum_{k=0}^{n} b_{n,k,[t_0,t_1]}(t)P_k = \sum_{k=0}^{n} \frac{\binom{n}{k}(t_1-t)^{n-k}(t-t_0)^k P_k}{(t_1-t_0)^n}.$$
 (2.2)

We call the elements of the set  $P = \{P_1, P_2, \dots, P_n\}$  the *control points* of  $C_P$ .

**Remark.** Let  $t_0 = 0$  and  $t_1 = 1$ . Then 2.2 simplifies to

$$b_{n,k}(t) := b_{n,k,[0,1]}(t) = \binom{n}{k} (1-t)^{n-k} t^k.$$
(2.3)

Also, 2.1 simplifies to

$$C_P(t) := C_{P,[0,1]}(t) = \sum_{k=0}^{n} \binom{n}{k} (1-t)^{n-k} t^k P_k.$$
(2.4)

This case is the only case considered in this thesis.

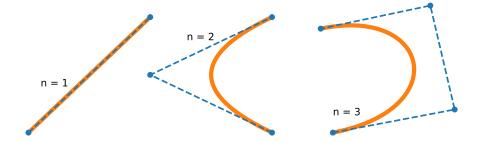


Figure 2.1: Beziér curves of different degrees and their control points

- 2.1.2 Properties
- 2.1.3 De Casteljau's Algorithm
- 2.2 Non-Uniform Rational B-Splines (NURBS)
- 2.2.1 Definition
- 2.2.2 Properties
- 2.2.3 De Boor's Algorithm
- 2.3 Methods on NURBS Objects
- 2.3.1 Affine Transformations
- 2.3.2 The Frenet-Serret Apparatus
- 2.3.3 Finding Intersections
- 2.3.4 Interpolation
- 2.4 Jet Engine Design Specifics
- 2.4.1 Fundamental Terms
- 2.4.2 The S2M Net
- 2.4.3 Fillet Creation

## 3 Results

## 3.1 Cooling Geometries And Their Parametrizations

- 3.1.1 Chambers
- 3.1.2 Turnarounds
- 3.1.3 Slots
- 3.1.4 Film Cooling Holes

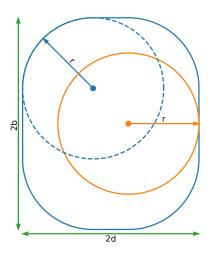


Figure 3.1: yeah

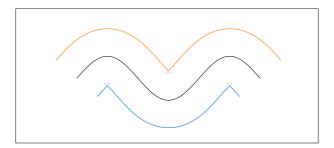


Figure 3.2: yeah

- 3.1.5 Impingement Inserts
- 3.2 Export for CENTAUR
- 3.3 Export for Open CASCADE

# 4 Discussion

- 4.1 Future Work
- 4.2 Conclusion

[Pie97]

# 5 References

- [Béz68] Pierre E. Bézier. "How Renault Uses Numerical Control for Car Body Design and Tooling". In: SAE Technical Paper Series. SAE International, Feb. 1968. DOI: 10. 4271/680010.
- [Pie97] Les A. Piegl. *The NURBS book*. Springer, 1997, p. 646. ISBN: 3540615458.