

CSULB  
CECS225  
Lab3

Show your work

No work, no credit even if the answer is correct

Type your final answers

(Overflow occurs when the result of an addition/subtraction using 2's complement arithmetic is too large or too small to be expressed using the number of bits of the representation used. This results in the overflow flag OF being set to 1.)

1. Add the following unsigned 4-bit binary numbers to get a possible 5-bit result.

Addend 1	Addend 2	5-bit Binary Sum				
1001	0101	0	1	1	1	0
1100	0110	1	0	0	1	0
0011	1100	0	1	1	1	1
0101	0111	0	1	1	0	0
1011	0010	1	0	0	0	0

2. Add the following signed 4-bit binary numbers. Indicate if there is overflow by setting the OF flag.

Addend 1	Addend 2	4-bit Binary Sum				OF
1001	0101	1	1	0	0	0
1100	0110	0	0	1	0	1
0011	1100	1	1	1	1	0
0101	0111	1	1	0	0	0
0001	1111	0	0	0	0	1

3. Add the following decimals by adding their 8-bit 2's complement representations. Indicate if OF.

Addend 1	Addend 2	8-bit Binary Sum								OF
58	-100	1	1	0	1	0	1	1	0	0
-35	-69	1	0	0	1	1	0	0	0	1
89	75	1	0	1	0	0	1	0	0	1
-126	-13	0	1	1	1	1	0	0	1	1
-105	80	1	1	1	0	0	1	1	1	0

4. Convert each decimal to 8-bit binary then find the negative 2's complement by going from the rightmost bit and inverting every digit beyond the first 1 found as you continue to the left.

Decimal	8-bit Binary Representation								2's Complement Value							
44	0	0	1	0	1	1	0	0	1	1	0	1	0	1	0	0
81	0	1	0	1	0	0	0	1	1	0	1	0	1	1	1	1
113	0	1	1	1	0	0	0	1	1	0	0	0	1	1	1	1
62	0	0	1	1	1	1	1	0	1	1	0	0	0	0	1	0
125	0	1	1	1	1	1	0	1	1	0	0	0	0	0	1	1

5. Perform the sum of pair of hexadecimal numbers (unsigned).

Num1	Num2	Sum
6B4 <sub>16</sub>	3FE <sub>16</sub>	AB2 <sub>16</sub>
A49 <sub>16</sub>	6BD <sub>16</sub>	1106 <sub>16</sub>
7C4 <sub>16</sub>	3BE <sub>16</sub>	B82 <sub>16</sub>



1.

- a.  $1001 + 0101 =$   
i. 1001  
ii. + 0101  
iii. = 01110
- b.  $1100 + 0110 =$   
i.  $\overset{11}{1100}$   
ii. + 0110  
iii. = 10010
- c.  $0011 + 1100 =$   
i. 0011  
ii. + 1100  
iii. = 1111
- d.  $0101 + 0111 =$   
i.  $\overset{111}{0101}$   
ii. + 0111  
iii. = 1100
- e.  $0001 + 1111 =$   
i.  $\overset{1111}{0001}$   
ii. + 1111  
iii. = 10000

2.

- a.  $1001 + 0101 =$   
i. 1001  
ii. + 0101  
iii. = 1110
- b.  $1100 + 0110 =$   
i.  $\overset{11}{1100}$   
ii. + 0110  
iii. = 10010
- c.  $0011 + 1100 =$   
i. 0011  
ii. + 1100  
iii. = 1111
- d.  $0101 + 0111 =$   
i.  $\overset{111}{0101}$   
ii. + 0111  
iii. = 1100
- e.  $0001 + 1111 =$   
i.  $\overset{1111}{0001}$   
ii. + 1111  
iii. = 10000

3. First binary, then addition

- a.  $58 - 100$

i. 58

1.  $58 / 2 = 29, R = 0$
2.  $29 / 2 = 14, R = 1$
3.  $14 / 2 = 7, R = 0$
4.  $7 / 2 = 3, R = 1$
5.  $3 / 2 = 1, R = 1$
6.  $1 / 2 = 0, R = 1$
7. 0011 1010

ii. -100

1.  $100 / 2 = 50, R = 0$
2.  $50 / 2 = 25, R = 0$
3.  $25 / 2 = 12, R = 1$
4.  $12 / 2 = 6, R = 0$
5.  $6 / 2 = 3, R = 0$
6.  $3 / 2 = 1, R = 1$
7.  $1 / 2 = 0, R = 1$
8. 0110 0100
9. 1001 1011 + 1 = 1001 1100

iii. <sup>111</sup>00111010

iv. + 10011100

v. = 1101 0110

b.  $-35 - 69 =$

i. -35

1.  $35 / 2 = 17, R = 1$
2.  $17 / 2 = 8, R = 1$
3.  $8 / 2 = 4, R = 0$
4.  $4 / 2 = 2, R = 0$
5.  $2 / 2 = 1, R = 0$
6.  $1 / 2 = 0, R = 1$
7. 0010 0011
8. 1101 1100 + 1 = 1101 1101

ii. -69

1.  $69 / 2 = 34, R = 1$
2.  $34 / 2 = 17, R = 0$
3.  $17 / 2 = 8, R = 1$
4.  $8 / 2 = 4, R = 0$
5.  $4 / 2 = 2, R = 0$
6.  $2 / 2 = 1, R = 0$
7.  $1 / 2 = 0, R = 1$
8. 0100 0101
9. 1011 1010 + 1 = 1011 1011

iii. <sup>111111</sup>1101 1101

iv. + 1011 1011

v. = 1 1001 1000

c.  $89 + 75 =$

i. 89

1.  $89 / 2 = 44, R = 1$
2.  $44 / 2 = 22, R = 0$
3.  $22 / 2 = 11, R = 0$
4.  $11 / 2 = 5, R = 1$
5.  $5 / 2 = 2, R = 1$
6.  $2 / 2 = 1, R = 0$
7.  $1 / 2 = 0, R = 1$
8. 0101 1001

ii. 75

1.  $75 / 2 = 37, R = 1$
2.  $37 / 2 = 18, R = 1$
3.  $18 / 2 = 9, R = 0$
4.  $9 / 2 = 4, R = 1$
5.  $4 / 2 = 2, R = 0$
6.  $2 / 2 = 1, R = 0$
7.  $1 / 2 = 0, R = 1$
8. 0100 1011

iii. 0101 1001

iv. + 0100 1011

v. = 1010 0100

d.  $-126 - 13 =$

i. -126

1.  $126 / 2 = 63, R = 0$
2.  $63 / 2 = 31, R = 1$
3.  $31 / 2 = 15, R = 0$
4.  $15 / 2 = 7, R = 1$
5.  $7 / 2 = 3, R = 1$
6.  $3 / 2 = 1, R = 1$
7.  $1 / 2 = 0, R = 1$
8. 0111 1010
9.  $1000\ 0101 + 1 = 1000\ 0110$

ii. -13

1.  $13 / 2 = 6, R = 1$
2.  $6 / 2 = 3, R = 0$
3.  $3 / 2 = 1, R = 1$
4.  $1 / 2 = 0, R = 1$
5. 0000 1101
6.  $1111\ 0010 + 1 = 1111\ 0011$

iii. 1000 0110

iv. + 1111 0011

v. = 1 0111 1001

e.  $-105 + 80$

- i. -105
  - 1.  $105 / 2 = 52, R = 1$
  - 2.  $52 / 2 = 26, R = 0$
  - 3.  $26 / 2 = 13, R = 0$
  - 4.  $13 / 2 = 6, R = 1$
  - 5.  $6 / 2 = 3, R = 0$
  - 6.  $3 / 2 = 1, R = 1$
  - 7.  $1 / 2 = 0, R = 1$
  - 8. 0110 1001
  - 9.  $1001\ 0110 + 1 = 1001\ 0111$

- ii. 80
  - 1.  $80 / 2 = 40, R = 0$
  - 2.  $40 / 2 = 20, R = 0$
  - 3.  $20 / 2 = 10, R = 0$
  - 4.  $10 / 2 = 5, R = 0$
  - 5.  $5 / 2 = 2, R = 1$
  - 6.  $2 / 2 = 1, R = 0$
  - 7.  $1 / 2 = 0, R = 1$
  - 8. 0101 0000

iii. 1001 0111

iv. + 0101 0000

v. = 1110 0111

4.

a. a. 44

- i.  $44 / 2 = 22, R = 0$
- ii.  $22 / 2 = 11, R = 0$
- iii.  $11 / 2 = 5, R = 1$
- iv.  $5 / 2 = 2, R = 1$
- v.  $2 / 2 = 1, R = 0$
- vi.  $1 / 2 = 0, R = 1$
- vii. 0010 1100
- viii.  $1101\ 0011 + 1 = 1101\ 0100$

b. b. 81

- i.  $81 / 2 = 40.5 = 40\ R = 1$
- ii.  $40 / 2 = 20 = 20\ R = 0$
- iii.  $20 / 2 = 10 = 10\ R = 0$
- iv.  $10 / 2 = 5 = 5\ R = 0$
- v.  $5 / 2 = 2.5 = 2\ R = 1$
- vi.  $2 / 2 = 1 = 1\ R = 0$
- vii.  $1 / 2 = 0.5 = 0\ R = 1$
- viii. 0101 0001
- ix.  $1010\ 1110 + 1 = 1010\ 1111$

c. c. 113

- i.  $113 / 2 = 56.5 = 56\ R = 1$

- ii.  $56 / 2 = 28 = 28 \text{ R} = 0$
- iii.  $28 / 2 = 14 = 14 \text{ R} = 0$
- iv.  $14 / 2 = 7 = 7 \text{ R} = 0$
- v.  $7 / 2 = 3.5 = 3 \text{ R} = 1$
- vi.  $3 / 2 = 1.5 = 1 \text{ R} = 1$
- vii.  $1 / 2 = 0.5 = 0 \text{ R} = 1$
- viii. 0111 0001
- ix.  $1000 \ 1110 + 1 = 1000 \ 1111$

d. d. 62

- i.  $62 / 2 = 31 = 31 \text{ R} = 0$
- ii.  $31 / 2 = 15.5 = 15 \text{ R} = 1$
- iii.  $15 / 2 = 7.5 = 7 \text{ R} = 1$
- iv.  $7 / 2 = 3.5 = 3 \text{ R} = 1$
- v.  $3 / 2 = 1.5 = 1 \text{ R} = 1$
- vi.  $1 / 2 = 0.5 = 0 \text{ R} = 1$
- vii. 0011 1110
- viii.  $1100 \ 0001 + 1 = 1100 \ 0010$

e. e. 125

- i.  $125 / 2 = 62.5 = 62 \text{ R} = 1$
- ii.  $62 / 2 = 31 = 31 \text{ R} = 0$
- iii.  $31 / 2 = 15.5 = 15 \text{ R} = 1$
- iv.  $15 / 2 = 7.5 = 7 \text{ R} = 1$
- v.  $7 / 2 = 3.5 = 3 \text{ R} = 1$
- vi.  $3 / 2 = 1.5 = 1 \text{ R} = 1$
- vii.  $1 / 2 = 0.5 = 0 \text{ R} = 1$
- viii. 0111 1101
- ix.  $1000 \ 0010 + 1 = 1000 \ 0011$

5.

a. a.  $6B4 + 3FE =$

- i.  $6 = 0110$
- ii.  $B = 1011$
- iii.  $4 = 0100$
- iv.  $3 = 0011$
- v.  $F = 1111$
- vi.  $E = 1110$
- vii.  $0110 \ 1011 \ 0100 + 0011 \ 1111 \ 1110 =$
- viii.  $1010 \ 1011 \ 0010$
- ix. AB2

b. b.  $A49 + 6BD =$

- i.  $A = 1010$
- ii.  $4 = 0100$
- iii.  $9 = 1001$
- iv.  $6 = 0110$
- v.  $B = 1011$

- vi.  $D = 1101$
- vii.  $1010\ 0100\ 1001 + 0110\ 1011\ 1101 =$
- viii.  $0001\ 0001\ 0000\ 0110$
- ix.  $1106$
- c.  $c. 7C4 + 3BE =$ 
  - i.  $7 = 0111$
  - ii.  $C = 1100$
  - iii.  $4 = 0100$
  - iv.  $3 = 0011$
  - v.  $B = 1011$
  - vi.  $E = 1110$
  - vii.  $0111\ 1100\ 0100 + 0011\ 1011\ 1110 =$
  - viii.  $1011\ 1000\ 0010$
  - ix.  $B82$
- d.  $d. B69 + 7AD =$ 
  - i.  $B = 1011$
  - ii.  $6 = 0110$
  - iii.  $9 = 1001$
  - iv.  $7 = 0111$
  - v.  $A = 1010$
  - vi.  $D = 1101$
  - vii.  $1011\ 0110\ 1001 + 0111\ 1010\ 1101 =$
  - viii.  $0001\ 0011\ 0001\ 0110$
  - ix.  $1316$

6.

- a.  $AB2\ 16 = 10 \cdot 16^2 + 11 \cdot 16^1 + 2 \cdot 16^0$ 
  - i.  $2738$
- b.  $106\ 16 \Rightarrow (1 \cdot 16^2) + (0 \cdot 16) + (6 \cdot 16^0)$ 
  - i.  $256 + 0 + 6$
  - ii.  $262\ 10$
- c.  $B82\ 16 \Rightarrow (11 \cdot 16^2) + (8 \cdot 16) + (2 \cdot 16^0)$ 
  - i.  $2816 + 128 + 2$
  - ii.  $2946\ 10$
- d.  $16\ 16 \Rightarrow (3 \cdot 16^2) + (1 \cdot 16) + (6 \cdot 16^0)$ 
  - i.  $768 + 16 + 6$
  - ii.  $790\ 10$

7.

- a.  $6B4 - 3FE =$ 
  - i.  $0110\ 1011\ 0100 - 0011\ 1111\ 1110 = 0010\ 1011\ 0110 = 2B6$
  - ii.  $2 \cdot 16^2 + 11 \cdot 16^1 + 6 \cdot 16^0$
  - iii.  $694$
- b.  $b. A49 - 6BD =$ 
  - i.  $1010\ 0100\ 1001 - 0110\ 1011\ 1101 = 0011\ 1000\ 1100 = 38C$



- ii.  $3 \cdot 16^2 + 8 \cdot 16^1 + 12 \cdot 16^0$
  - iii. 908
- c.  $7C4 - 3BE =$ 
  - i.  $0111\ 1100\ 0100 - 0011\ 1011\ 1110 = 0100\ 0000\ 0110 = 406$
  - ii.  $4 \cdot 16^2 + 0 \cdot 16^1 + 6 \cdot 16^0$
  - iii. v. 1030
- d.  $B69 - 7AD$ 
  - i.  $1011\ 0110\ 1001 - 0111\ 1010\ 1101 = 0011\ 1011\ 1100 = 3BC$
  - ii.  $3 \cdot 16^2 + 11 \cdot 16^1 + 12 \cdot 16^0$
  - iii. v. 956

8.

- a. M
  - i. Decimal
    - 1.  $M = 77$
  - ii. Hexadecimal
    - 1.  $77 / 16 = 4, R = 13 = D$
    - 2.  $4 / 16 = 0, R = 4$
    - 3.  $4D_{16}$
  - iii. Binary
    - 1. Using hex,  $4D$
    - 2.  $4 / 2 = 2, R = 0$
    - 3.  $2 / 2 = 1, R = 0$
    - 4.  $1 / 2 = 0, R = 1$
    - 5. 0100
    - 6.  $D = 13 / 2 = 6, R = 1$
    - 7.  $6 / 2 = 3, R = 0$
    - 8.  $3 / 2 = 1, R = 1$
    - 9.  $1 / 2 = 0, R = 1$
    - 10. 1101
    - 11.  $0100\ 1101_2$
  - iv. Octal
    - 1. Using decimal, 77
    - 2.  $77 / 8 = 9, R = 5$
    - 3.  $9 / 8 = 1, R = 1$
    - 4.  $1 / 8 = 0, R = 1$
    - 5.  $115_8$
  - v. Unicode
    - 1. Sd
- b. Z
  - i. Decimal
    - 1.  $Z = 90$
  - ii. Hexadecimal
    - 1.  $90 / 16 = 5, R = 10 =$
    - 2.  $5 / 16 = 0, R = 5$

3.  $5A_{16}$

iii. Binary

1. Using hex, 5A
2.  $5 / 2 = 2, R = 1$
3.  $2 / 2 = 1, R = 0$
4.  $1 / 2 = 0, R = 1$
5. 0101
6.  $A = 10 / 2 = 5, R = 0$
7.  $5 / 2 = 2, R = 1$
8.  $2 / 2 = 1, R = 0$
9.  $1 / 2 = 0, R = 1$
10. 1010
11. 0101 1010<sub>2</sub>

iv. Octal

1. Using decimal 90
2.  $90 / 8 = 11, R = 2$
3.  $11 / 8 = 1, R = 3$
4.  $1 / 8 = 0, R = 1$
5. 132<sub>8</sub>

v. Unicode

9.

a. a. +10.75

- i. Sign = 0 (positive)
- ii.  $10 / 2 = 5, R = 0$
- iii.  $5 / 2 = 2, R = 1$
- iv.  $2 / 2 = 1, R = 0$
- v.  $1 / 2 = 0, R = 1$
- vi. 1010
- vii.  $0.75 * 2 = 1.5 = 1$
- viii.  $0.5 * 2 = 1.0 = 1$
- ix.  $0 * 2 = 0 = 0$
- x.  $0 * 2 = 0 = 0$
- xi. 1100
  1.  $1010 * 1100 = 10101100 * 2^3; \text{exp} = 3$
  2. Mantissa = 0101100000
    - a. Bias =  $127 + 3 = 130$
    - b.  $130 / 2 = 65, R = 0$
    - c.  $65 / 2 = 32, R = 1$
    - d.  $32 / 2 = 16, R = 0$
    - e.  $16 / 2 = 8, R = 0$
    - f.  $8 / 2 = 4, R = 0$
    - g.  $4 / 2 = 2, R = 0$
    - h.  $2 / 2 = 1, R = 0$
    - i.  $1 / 2 = 0, R = 1$

j. Exponent = 1000 0010

b. -76.0625

- i. Sign = 1 (negative)
- ii.  $76 / 2 = 38$ , R = 0
- iii.  $38 / 2 = 19$ , R = 0
- iv.  $19 / 2 = 9$ , R = 1
- v.  $9 / 2 = 4$ , R = 1
- vi.  $4 / 2 = 2$ , R = 0
- vii.  $2 / 2 = 1$ , R = 0
- viii.  $1 / 2 = 0$ , R = 1
- ix. 1001100
- x.  $0.0625 * 2 = 0.125$  = 0
- xi.  $0.125 * 2 = 0.25$  = 0
- xii.  $0.25 * 2 = 0.5$  = 0
- xiii.  $0.5 * 2 = 1$  = 1
- xiv.  $1 * 2 = 2$  = 0
- xv.  $2 * 2 = 4$  = 0
- xvi. 000100
  1. 1001100 \* 000100
  2. 1001100000100 \*  $2^6$ ; exp = 6
  3. Mantissa = 001100000100000000000000
    - a. Bias =  $127 + 6 = 133$
    - b.  $133 / 2 = 66.5 = 66$  R = 1
    - c.  $66 / 2 = 33 = 33$  R = 0
    - d.  $33 / 2 = 16.5 = 16$  R = 1
    - e.  $16 / 2 = 8 = 8$  R = 0
    - f.  $8 / 2 = 4 = 4$  R = 0
    - g.  $4 / 2 = 2 = 2$  R = 0
    - h.  $2 / 2 = 1 = 1$  R = 0
    - i.  $1 / 2 = 0.5 = 0$  R = 1
    - j. Exponent = 10000101

10.

a. 41 86 00 00

- i. 4 = 0100
- ii. 1 = 0001
- iii. 8 = 1000
- iv. 6 = 0110
- v. 0 = 0000
- vi. 0 = 0000
- vii. 0100 0001 1000 0110 0000 0000
- viii. Exponent = 10000011
- ix.  $10000011 = 1*2^7 + 1*2^1 + 1*2^0$
- x.  $128 + 2 + 1 = 131 - 127$  (Bias) = 4; exp = 4
  1.  $0000110000000000 = 1*2^{-5} + 1*2^{-6} = 0.03125 + 0.015625$

$$2. \text{ Mantissa} = 0.046875$$

$$\text{xi. } (-1)^s * (1 + \text{mantissa}) + 2^e$$

$$1. (-1)^0 * (1 + 0.046875) * 2^4$$

$$2. +16.75$$

b. CD 32 A2 00

$$\text{i. } C = 1100$$

$$\text{ii. } D = 1101$$

$$\text{iii. } 3 = 0011$$

$$\text{iv. } 2 = 0010$$

$$\text{v. } A = 1010$$

$$\text{vi. } 2 = 0010$$

$$\text{vii. } 0 = 0000$$

$$\text{viii. } 0 = 0000$$

$$\text{ix. } 1100 \ 1101 \ 0011 \ 0010 \ 1010 \ 0010 \ 0000 \ 0000$$

$$\text{x. Exponent} = 10011010$$

$$\text{xi. } 10011010 = 1*2^7 + 1*2^4 + 1*2^3 + 1*2^1 = 128 + 16 + 8 + 2 = 154 - 127 (\text{Bias}); \text{exp} = 27$$

$$\begin{aligned} \text{a. } 011001010100010000000000 &= 1*2^{-2} + 1*2^{-3} + 1*2^{-6} + 1*2^{-8} + \\ &1*2^{-10} + 1*2^{-14} = 0.25 + 0.125 + 0.015625 + 0.00390625 + \\ &0.000976563 + 0.000061035 \end{aligned}$$

$$\text{b. Mantissa} = 0.395568848$$

$$2. (-1)^s * (1 + \text{Mantissa}) + 2^e$$

$$\text{a. } 0 + 1.395568848 * 2^{27} =$$

$$\text{b. } -187310080$$