

### 1st Group Problems

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B. Basis 1:  $|w|=3$  aaa ✓

Given:  $|w| \geq 3$

Basis 2:  $|w|=3$  aab ✓

$w$  contains more a's than b's

Basis 3:  $|w|=3$  aba ✓

Basis 4:  $|w|=3$  baa ✓

Inductive step: Assume  $|w| \leq n$  is True, show  $|w| \leq n+1$  is True  
 $3 \leq |w| \leq n \rightarrow 3 \leq n$

Case 1:  $|w|=n+1$ ,  $w$  starts with an a  
then the word minus the first symbol has length  $|w|-1=n$   
by inductive assumption,  $|w|-1=n$  is True  
therefore  $|w|=n+1$  is also True since adding the a back  
in would not remove the subword ✓

Case 2:  $|w|=n+1$ ,  $w$  starts with an b  
then the word minus the first symbol has length  $|w|-1=n$   
by inductive assumption,  $|w|-1=n$  is True  
therefore  $|w|=n+1$  is also True since adding the b  
back in would not remove the subword ✓

A. 1.  $I = (1, 2, 3, 4, 5, 6, 7, 8, \{3, \dots, (\dots)\})$

2.  $w = (\{1, 2, 3, 4, 5, 6, 7, 8\}, \{(1, 3), (1, 4), (1, 5), (1, 6), (2, 3), (2, 4), (2, 6), (2, 8), (3, 5), (3, 6), (4, 5), (4, 7), (5, 6), (7, 8)\})$

A.

$$1. (1, 2, 3, 4, 5, 6, 7, 8, \{, \}, ,, (, >)$$

$$2. W = (\{1, 2, 3, 4, 5, 6, 7, 8\}, \{(1, 3), (1, 4), (1, 5), (1, 6), \\ (2, 3), (2, 4), (2, 6), (2, 8), \\ (3, 5), (3, 6), (4, 5), (4, 7), \\ (5, 6), (7, 8)\})$$