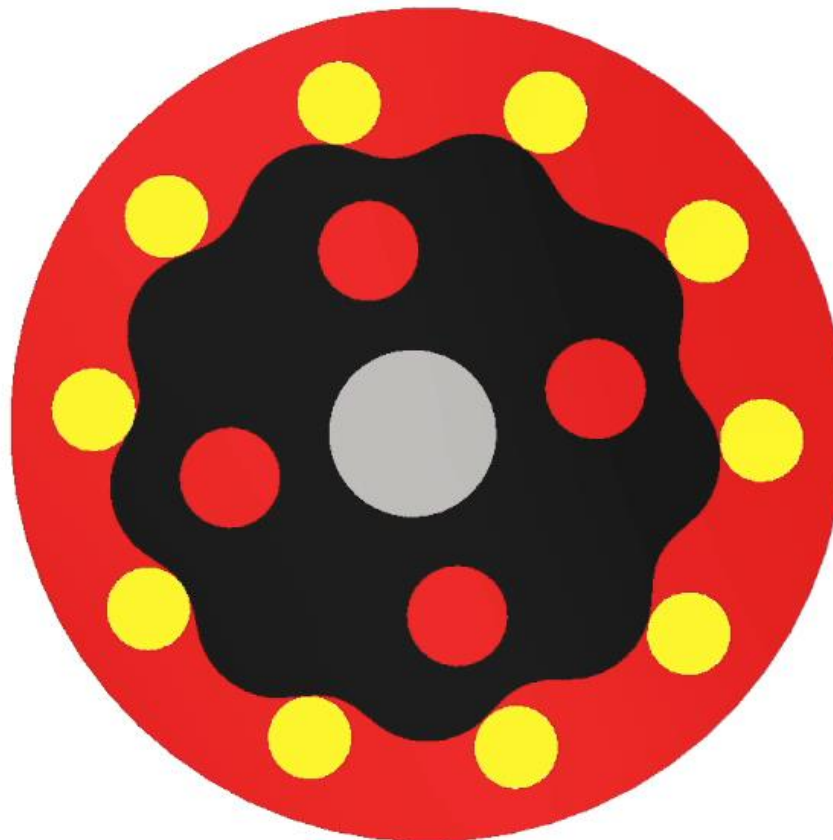


Cycloid Reducer

周奕彬

研究目標

- 擺線減速機誤差分析
- 求等校連桿簡化分析



大綱

- 新擺線輪輪廓解析式
- 等效連桿&曲率半徑
- 位移方程式
- 未來目標

新輪廓解析式

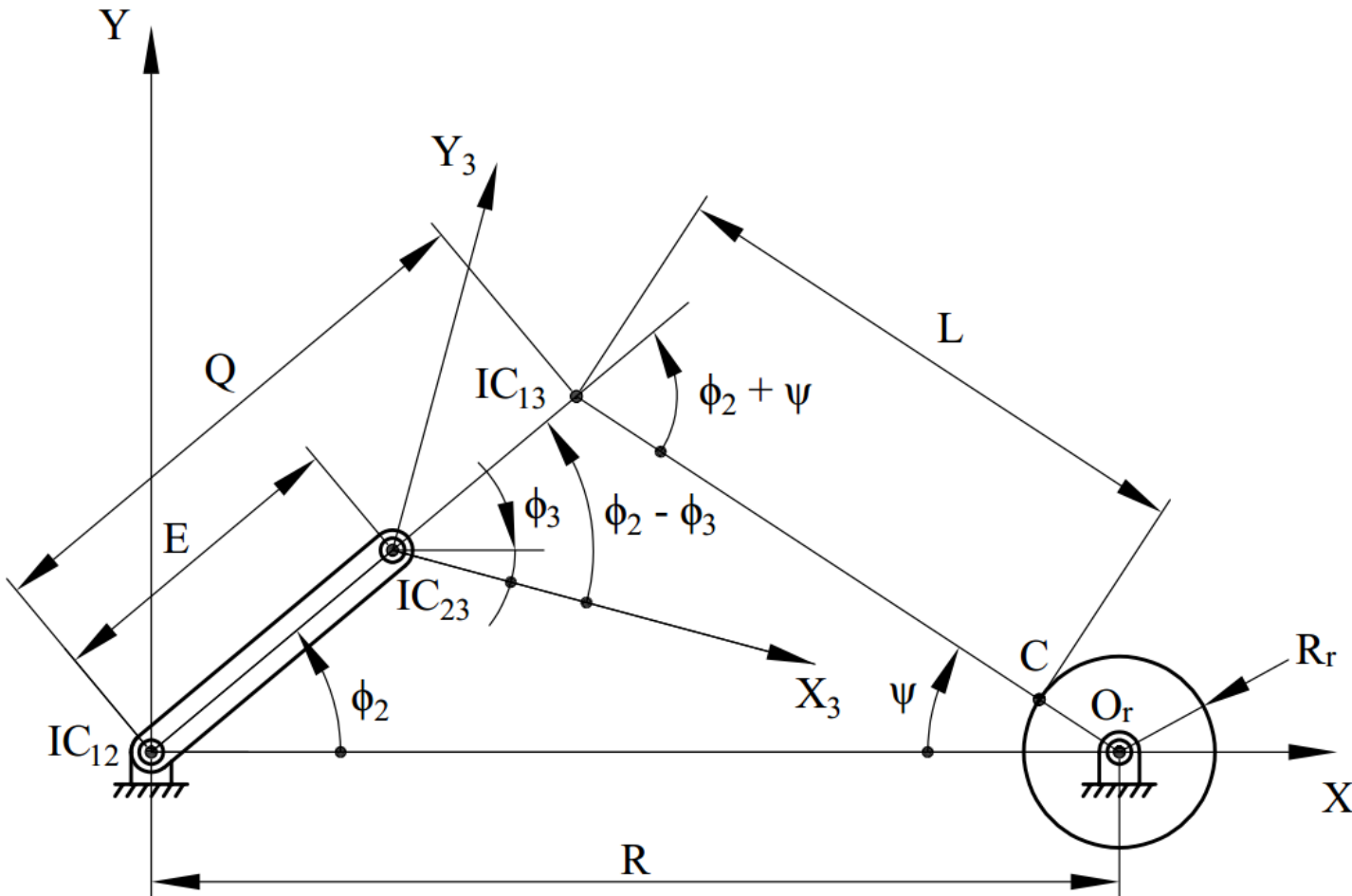
- 原外擺線解析式

$$C_x = R \cos \phi - R_r \cos(\phi + \psi) - E \cos(N\phi)$$

$$C_y = -R \sin \phi + R_r \sin(\phi + \psi) + E \sin(N\phi)$$

$$\psi = \tan^{-1} \left[\frac{\sin(1 - N)\phi}{(R/EN) - \cos(1 - N)\phi} \right] \quad (0^\circ \leq \phi \leq 360^\circ)$$

外擺線解析式

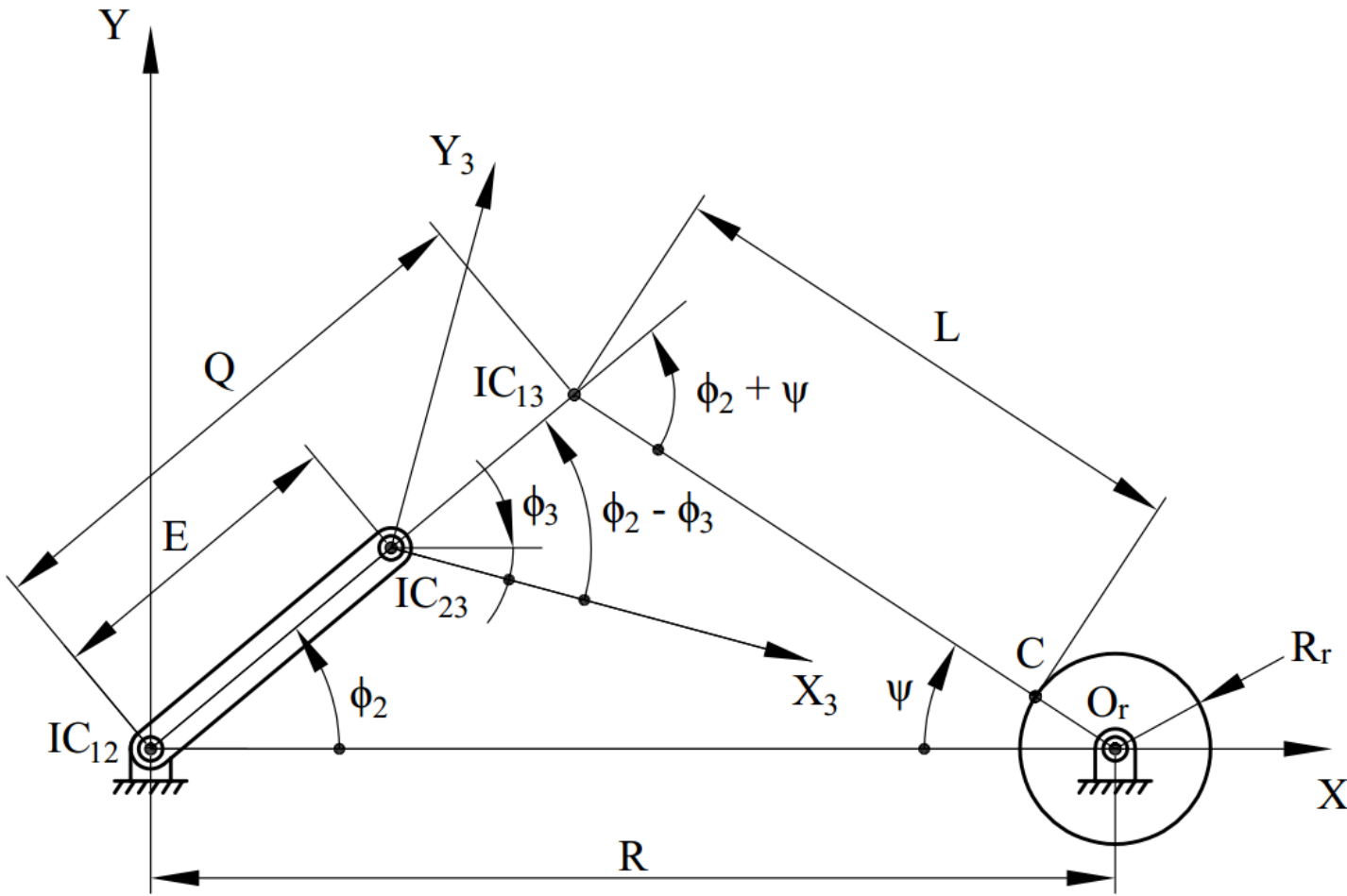


$$\bullet \overrightarrow{IC_{23}IC_{13}} + \overrightarrow{IC_{13}O_r} - \overrightarrow{CO_r}$$

$$\bullet \overline{IC_{23}IC_{13}} = Q - E$$

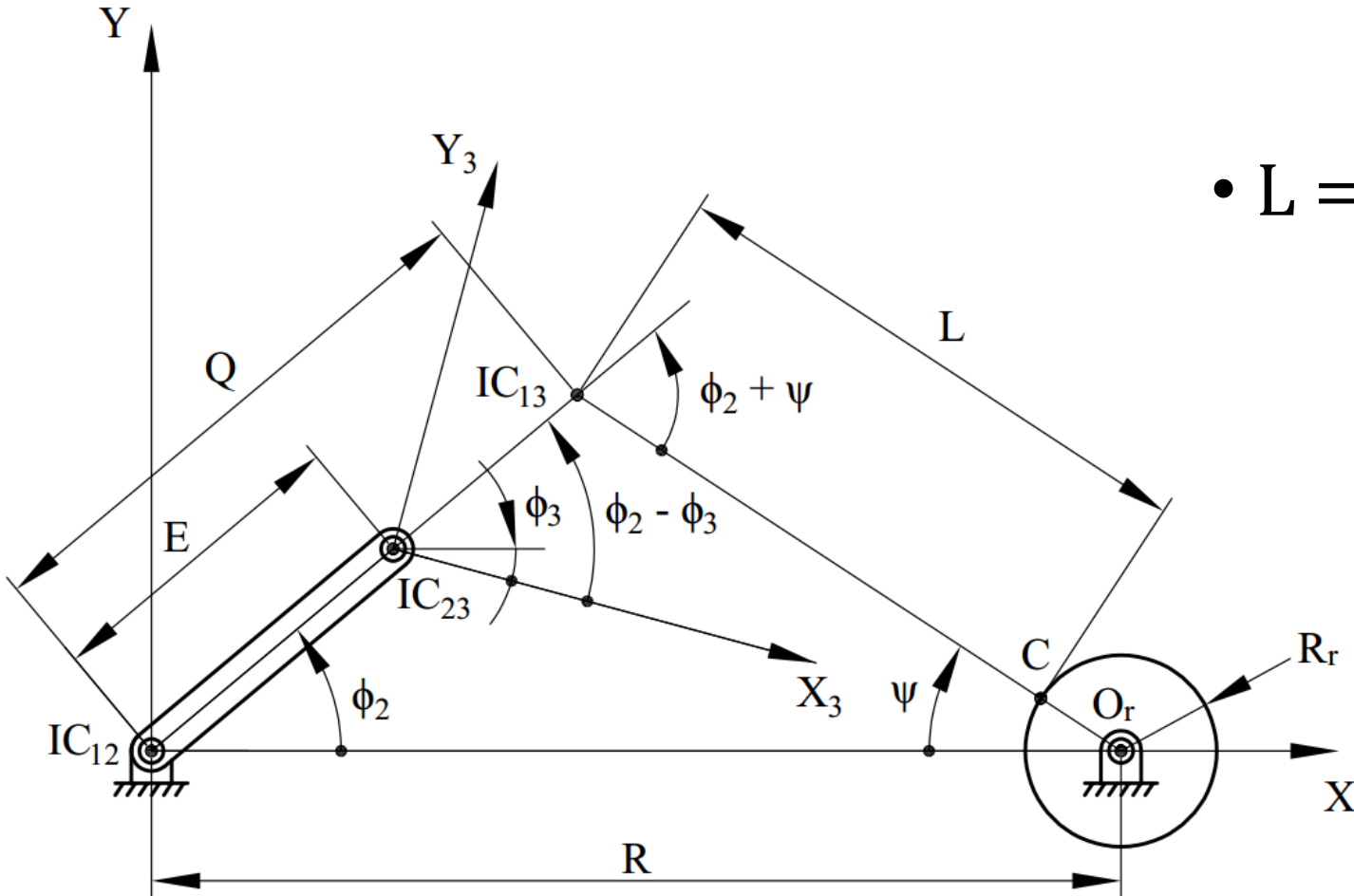
$$\bullet \overline{IC_{13}O_r} - \overline{CO_r} = L$$

外擺線解析式



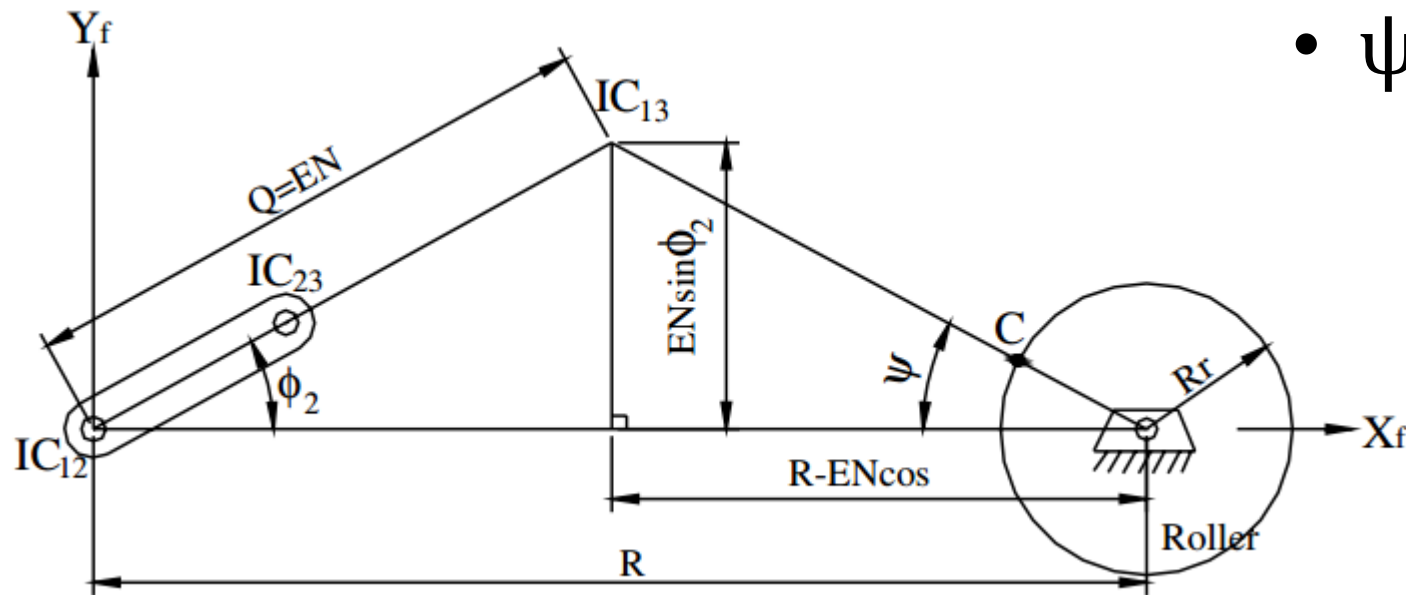
- $\overrightarrow{IC_{23}IC_{13}} + \overrightarrow{IC_{13}C}$
- $C_x = (Q - E)\cos(\phi_2 - \phi_3) + L\cos((\phi_2 - \phi_3) - (\phi_2 + \psi))$
- $C_y = (Q - E)\sin(\phi_2 - \phi_3) + L\sin((\phi_2 - \phi_3) - (\phi_2 + \psi))$

外擺線解析式



$$\bullet L = \sqrt{R^2 + Q^2 - 2RQ\cos(\phi_2)} - R_r$$

外擺線解析式



$$\bullet \psi = \tan^{-1} \frac{Q \sin(\phi_2)}{R - Q \cos(\phi_2)}$$

外擺線解析式

- $C_x = (Q - E)\cos(\phi_2 - \phi_3) + L\cos((\phi_2 - \phi_3) - (\phi_2 + \psi))$
- $C_y = (Q - E)\sin(\phi_2 - \phi_3) + L\sin((\phi_2 - \phi_3) - (\phi_2 + \psi))$
- $L = \sqrt{R^2 + Q^2 - 2RQ\cos(\phi_2)} - R_r$
- $\psi = \tan^{-1} \frac{Q\sin(\phi_2)}{R - Q\cos(\phi_2)}$
- $\phi_3 = \phi$; $\phi_2 = (1 - N)\phi$; $Q = EN$;

外擺線解析式

$$\begin{aligned}C_x &= E\cos(N\emptyset)(N-1) + L\cos(\emptyset + \psi) \\C_y &= -E\sin(N\emptyset)(N-1) - L\sin(\emptyset + \psi)\end{aligned}$$

$$L = \sqrt{R^2 + (EN)^2 - 2REN\cos((1-N)\emptyset)} - R_r$$

$$\psi = \tan^{-1} \frac{\sin((1-N)\emptyset)}{((R/(EN)) - \cos((1-N)\emptyset))}$$

新輪廓解析式

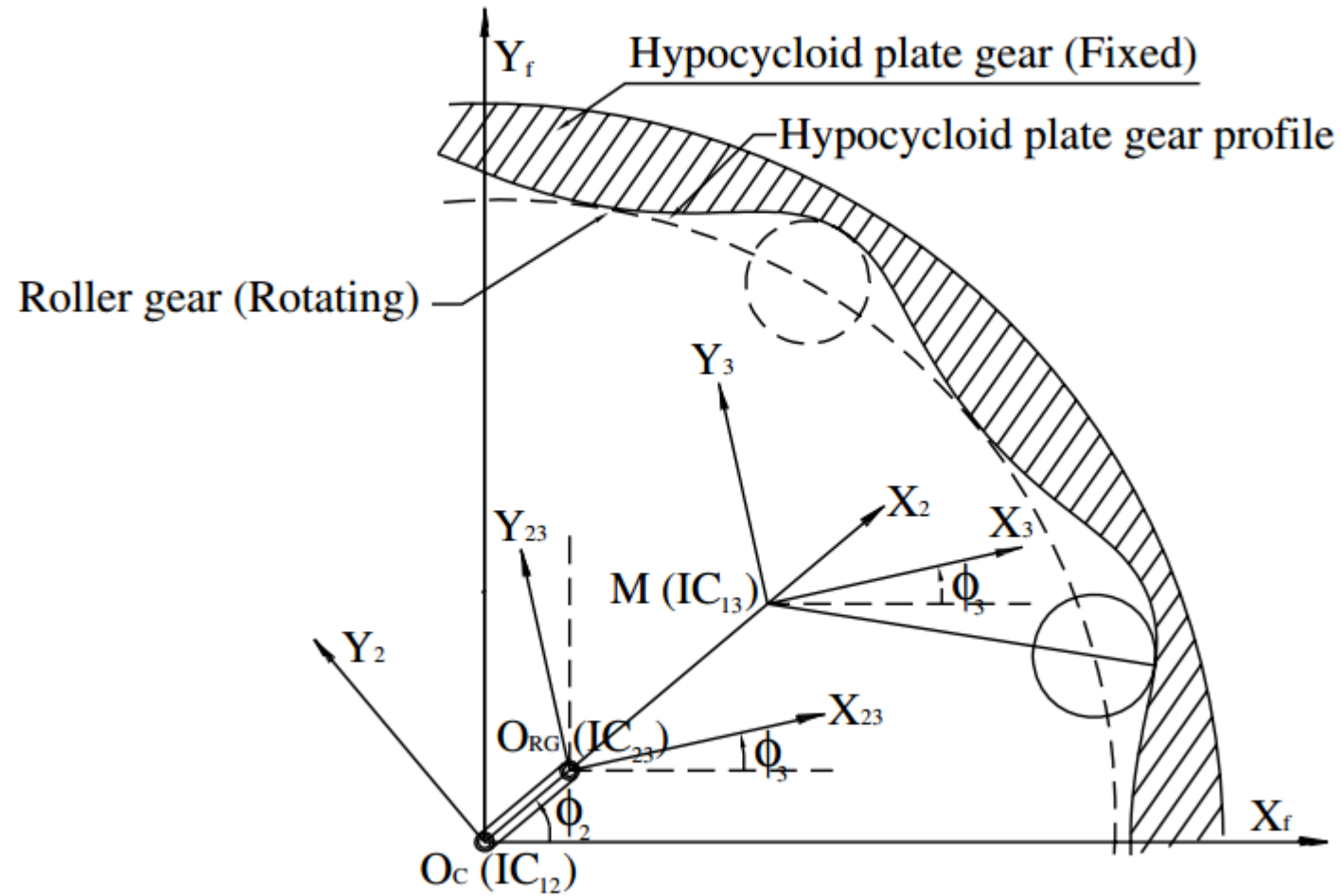
- 原內擺線解析式

$$C_x = R \cos \phi + R_r \cos(\phi - \psi) + E \cos(N\phi)$$

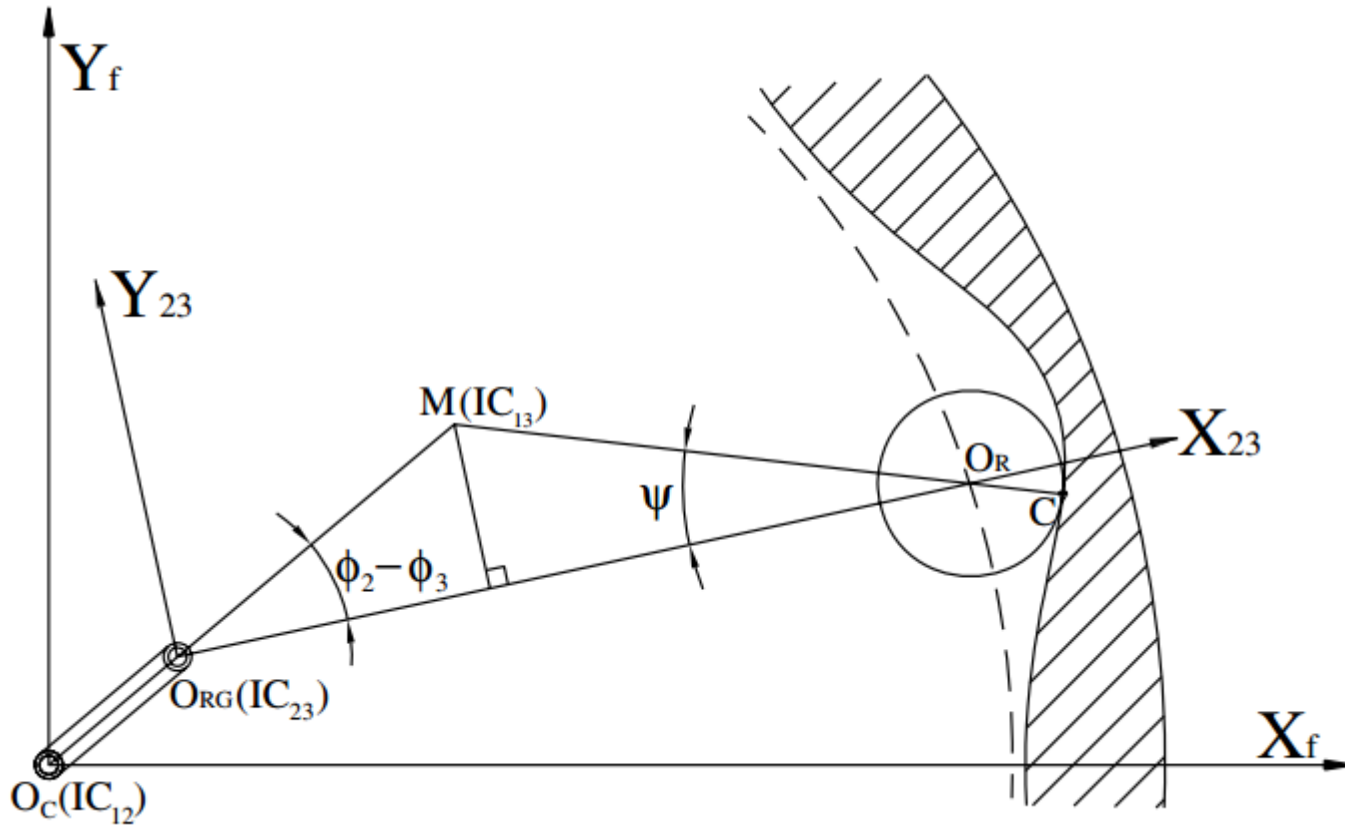
$$C_y = R \sin \phi + R_r \sin(\phi - \psi) - E \sin(N\phi)$$

$$\psi = -\tan^{-1} \left[\frac{\sin(N+1)\phi}{(R/EN) - \cos(N+1)\phi} \right]$$

內擺線解析式



外擺線解析式

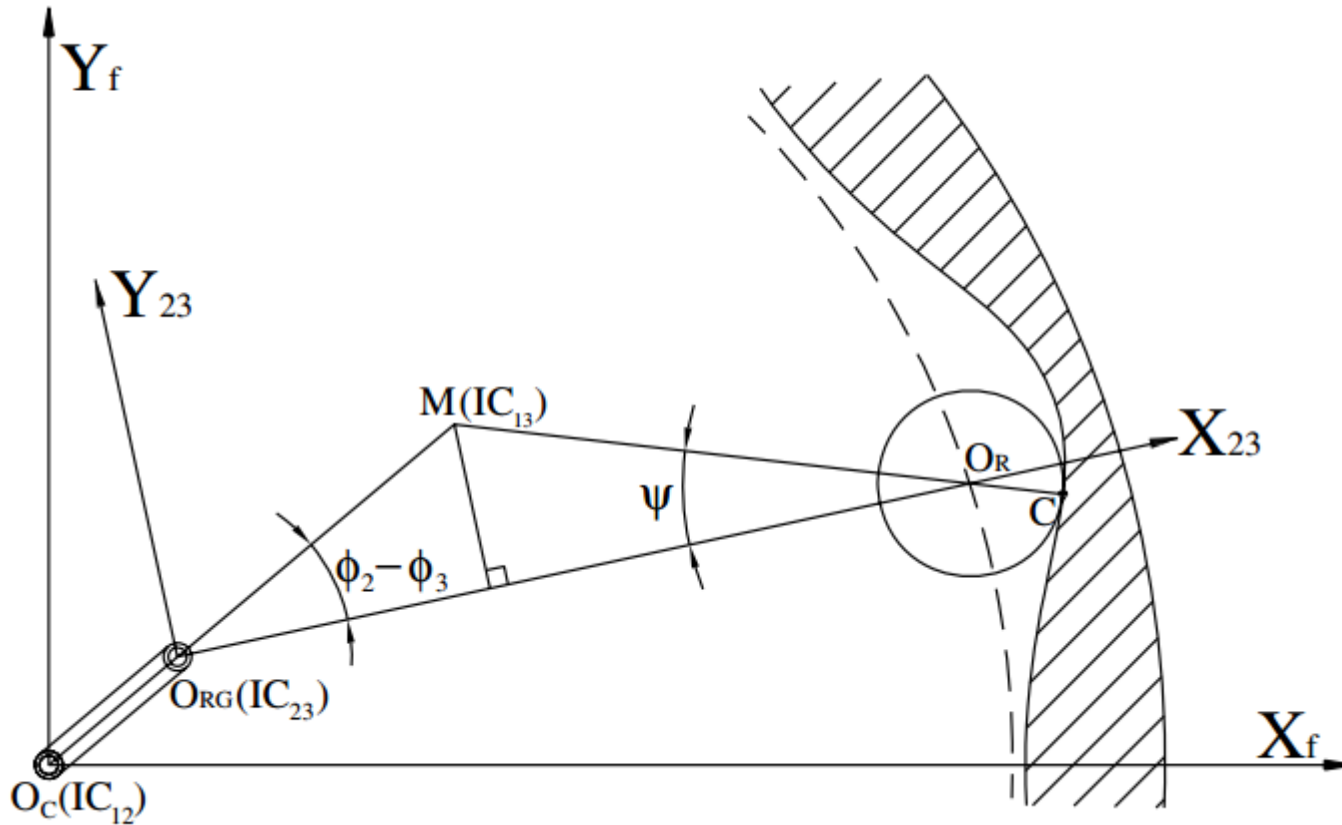


$$\bullet \overrightarrow{IC_{12}IC_{13}} + \overrightarrow{IC_{13}O_R} + \overrightarrow{O_R C}$$

$$\bullet \overline{IC_{12}IC_{13}} = Q$$

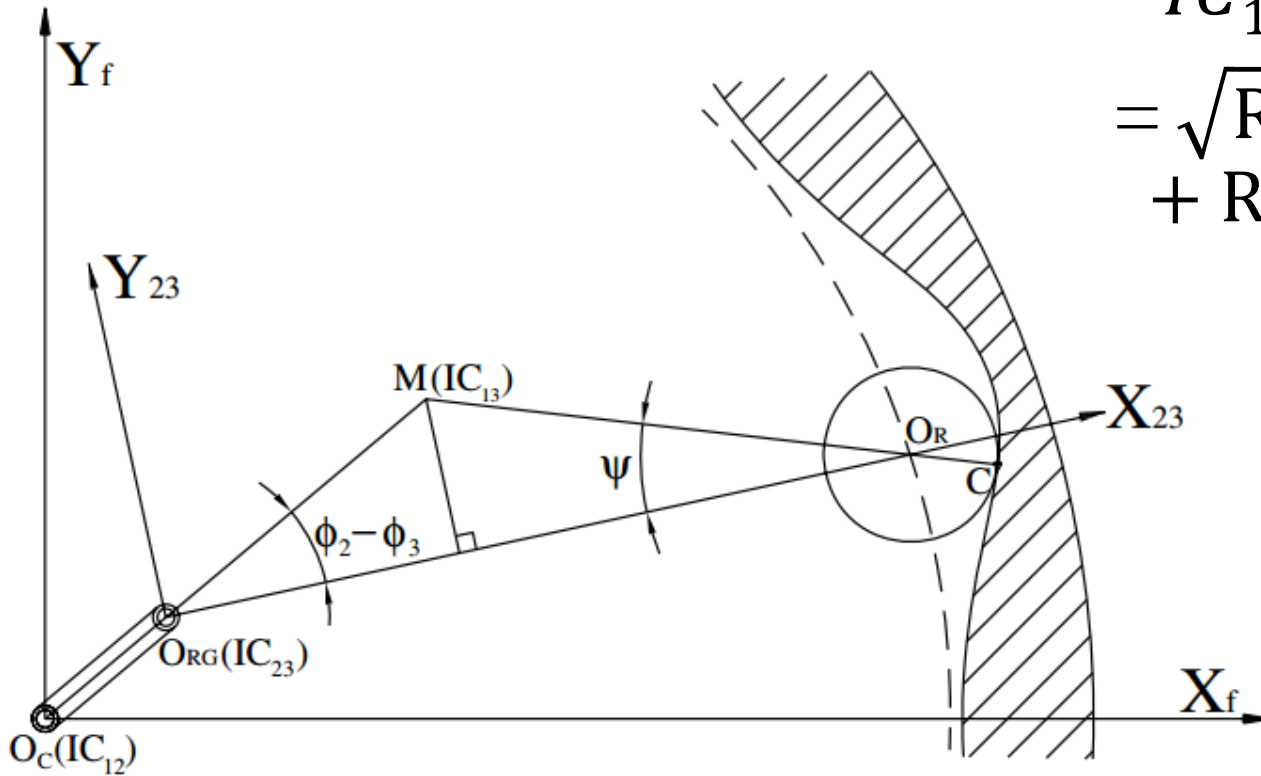
$$\bullet \overline{IC_{13}O_R} + \overline{CO_R} = L$$

外擺線解析式



- $\overrightarrow{IC_{12}IC_{13}} + \overrightarrow{IC_{13}C}$
- $C_x = Q\cos(\phi_2) + L\cos(\phi_2 - (\phi_2 - \phi_3 + \psi))$
- $C_y = Q\sin(\phi_2) + L\sin(\phi_2 - (\phi_2 - \phi_3 + \psi))$

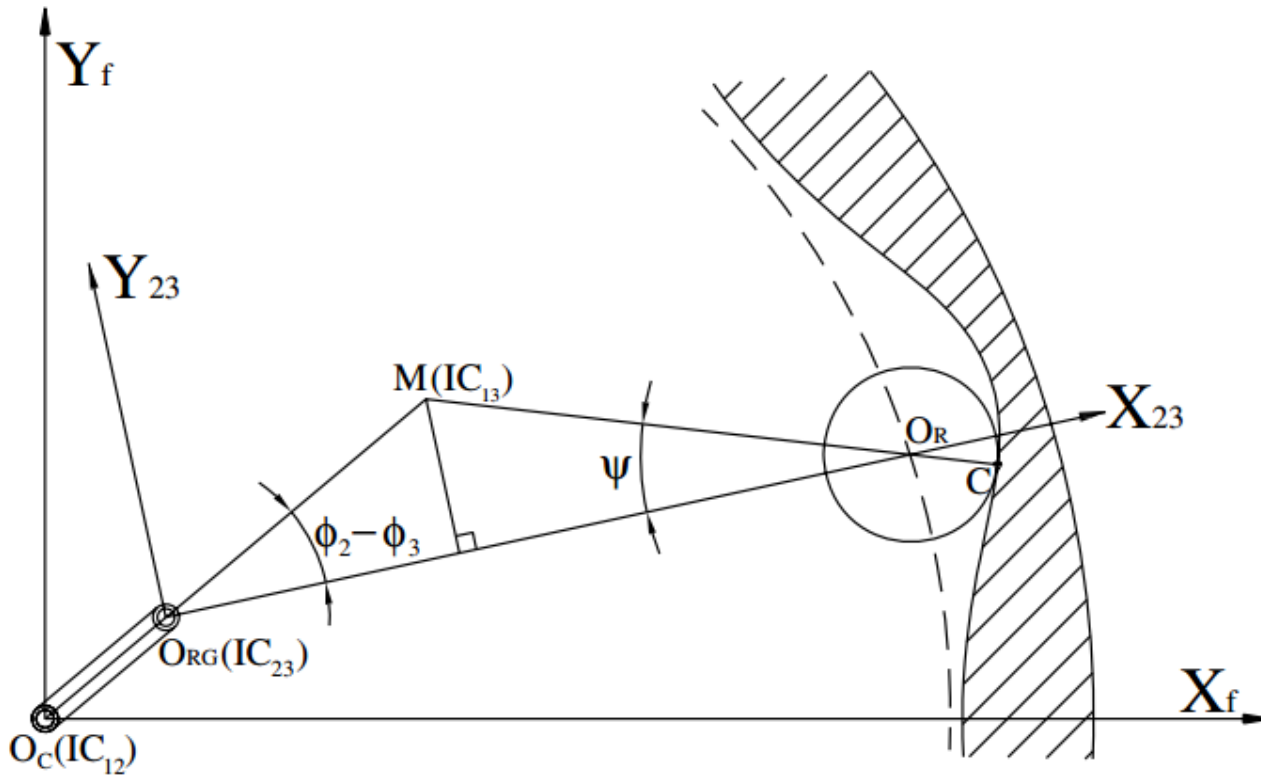
外擺線解析式



$$\bullet \overline{IC_{13}O_r} + \overline{CO_r} = L$$

$$= \sqrt{R^2 + (Q - E)^2 - 2R(Q - E)\cos(\phi_2 - \phi_3)} + R_r$$

外擺線解析式



- $$\psi = \tan^{-1} \frac{(Q-E)\sin(\phi_2 - \phi_3)}{R - (Q-E)\cos(\phi_2 - \phi_3)}$$

外擺線解析式

- $C_x = Q\cos(\phi_2) + L\cos(\phi_2 - (\phi_2 - \phi_3 + \psi))$
- $C_y = Q\sin(\phi_2) + L\sin(\phi_2 - (\phi_2 - \phi_3 + \psi))$
- $L = \sqrt{R^2 + (Q - E)^2 - 2R(Q - E)\cos(\phi_2 - \phi_3)} + R_r$
- $\psi = \tan^{-1} \frac{(Q-E)\sin(\phi_2-\phi_3)}{R-(Q-E)\cos(\phi_2-\phi_3)}$
- $\phi_3 = \phi$; $\phi_2 = -N\phi$; $Q = E(N + 1)$;

外擺線解析式

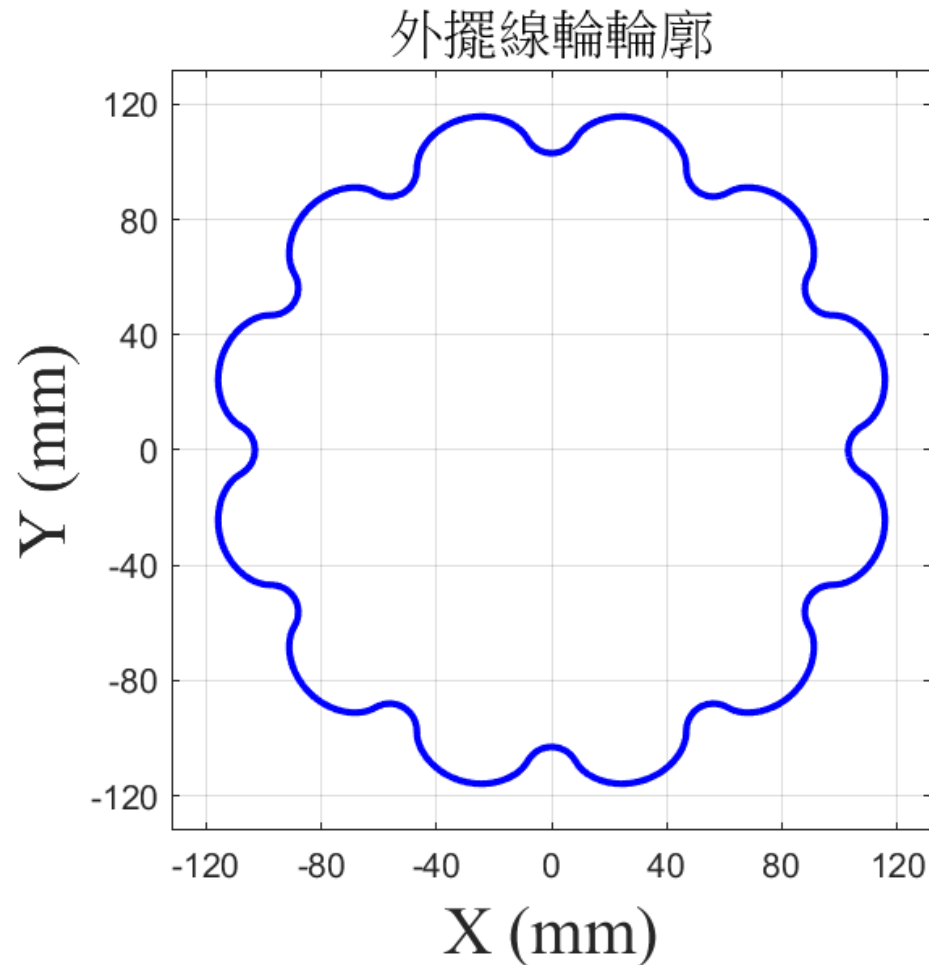
$$\begin{aligned}C_x &= E \cos(N\emptyset)(N+1) + L \cos(\emptyset - \psi) \\C_y &= -E \sin(N\emptyset)(N+1) + L \sin(\emptyset - \psi)\end{aligned}$$

$$L = \sqrt{R^2 + (EN)^2 - 2REN \times \cos((1+N)\emptyset)} + R_r$$

$$\psi = \tan^{-1} \frac{-\sin((1+N)\emptyset)}{((R/(EN)) - \cos((1+N)\emptyset))}$$

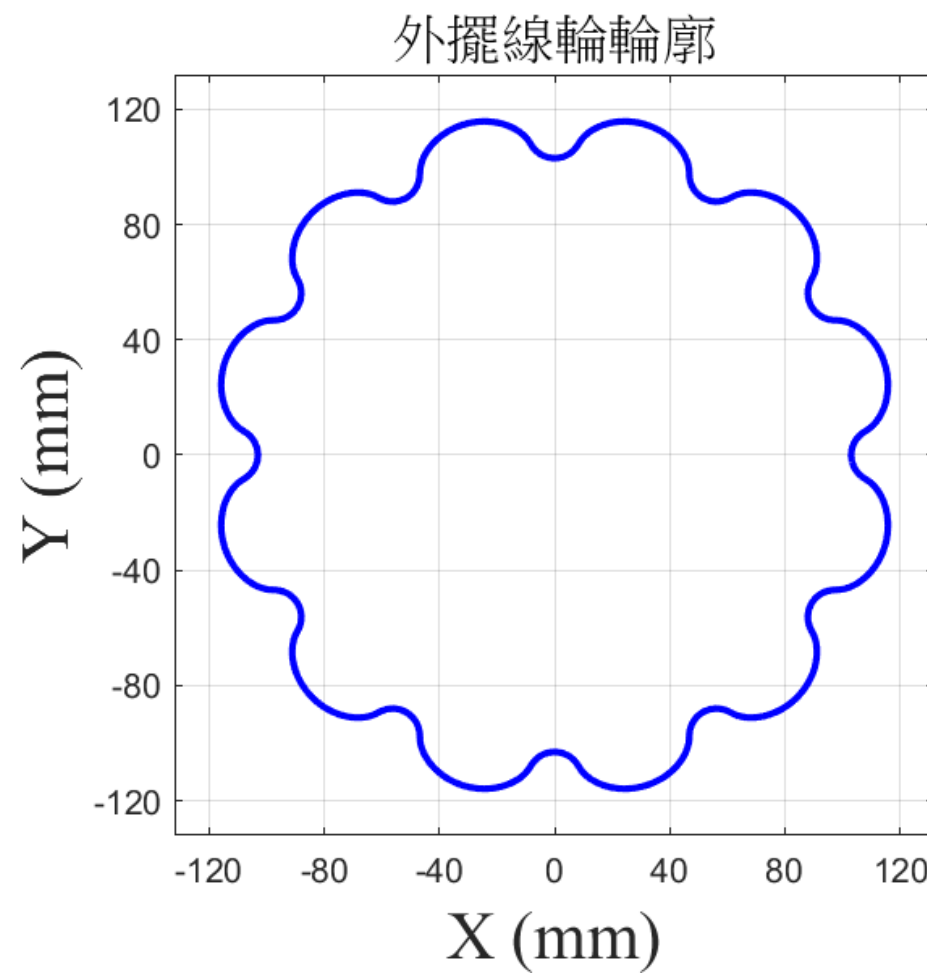
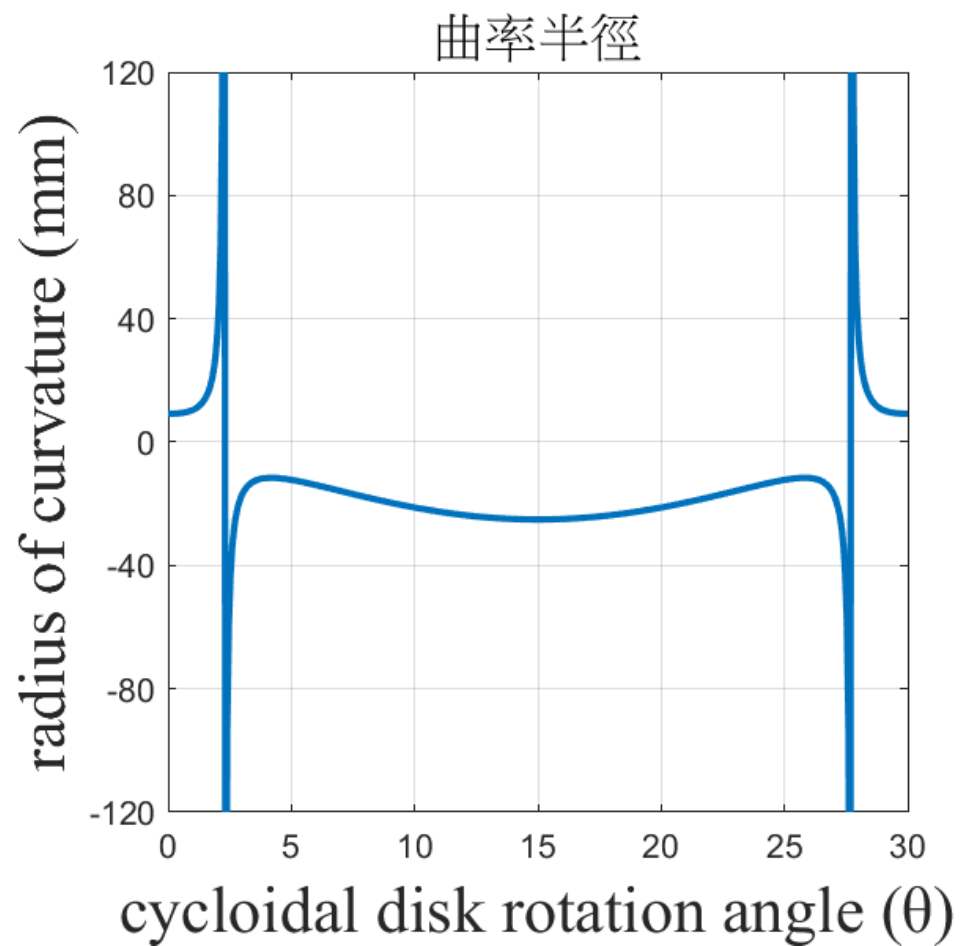
Stationary ring gear type epicycloid reducer		Stationary ring gear type hypocycloid reducer	
$\phi_3 = \phi$	$\phi_2 = (1 - N)\phi$	$\phi_3 = \phi$	$\phi_2 = -N\phi$
$L = \sqrt{R^2 + (EN)^2 - 2REN \times \cos((1 - N)\phi)} - R_r$		$L = \sqrt{R^2 + (EN)^2 - 2REN \times \cos((1 + N)\phi)} + R_r$	
$C_x = E\cos(N\phi)(N - 1) + L\cos(\phi + \psi)$ $C_y = -E\sin(N\phi)(N - 1) - L\sin(\phi + \psi)$		$C_x = E\cos(N\phi)(N + 1) + L\cos(\phi - \psi)$ $C_y = -E\sin(N\phi)(N + 1) + L\sin(\phi - \psi)$	
$\psi = \tan^{-1} \frac{\sin((1 - N)\phi)}{((R/(EN)) - \cos((1 - N)\phi))}$		$\psi = \tan^{-1} \frac{-\sin((1 + N)\phi)}{((R/(EN)) - \cos((1 + N)\phi))}$	

曲率半徑

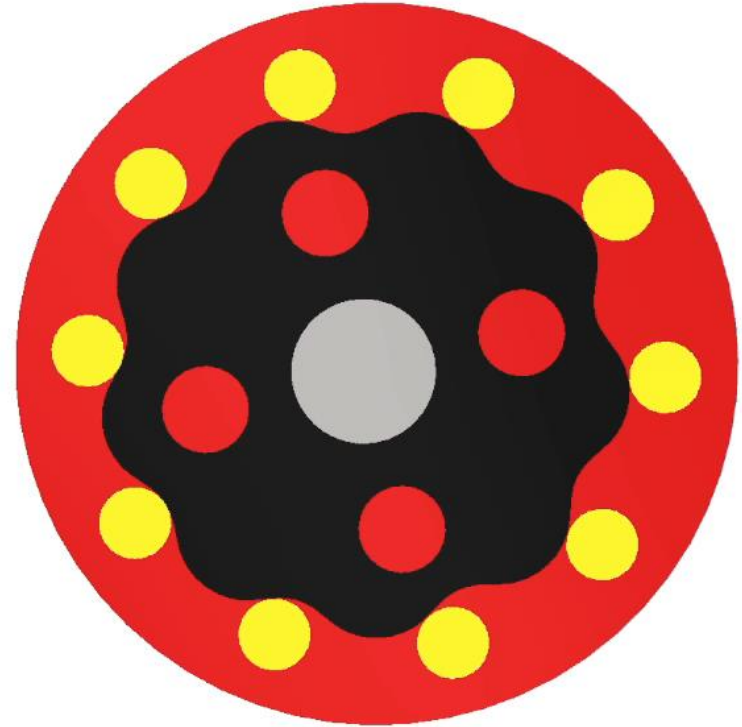
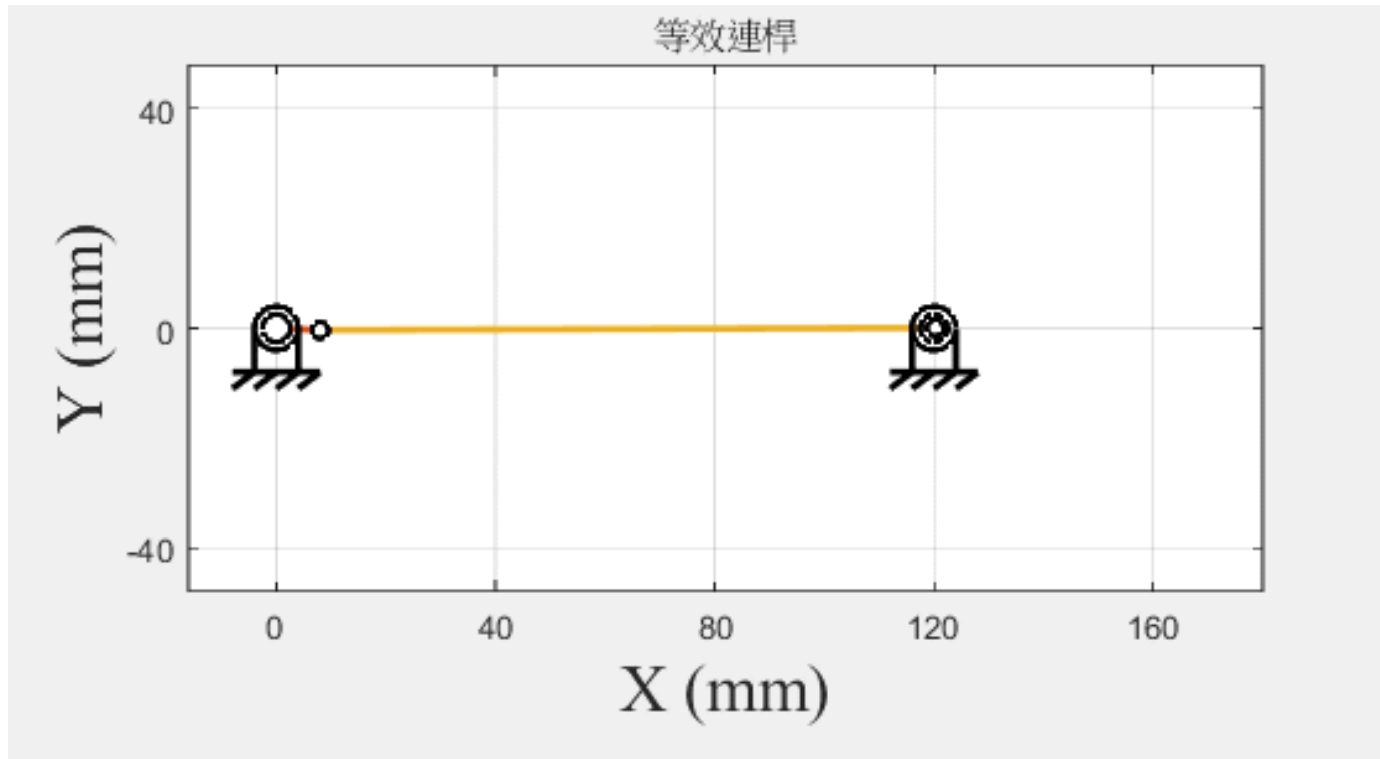


- $N = 13$
- $R_r = 9 \text{ mm}$
- $R = 120 \text{ mm}$
- $E = 8 \text{ mm}$

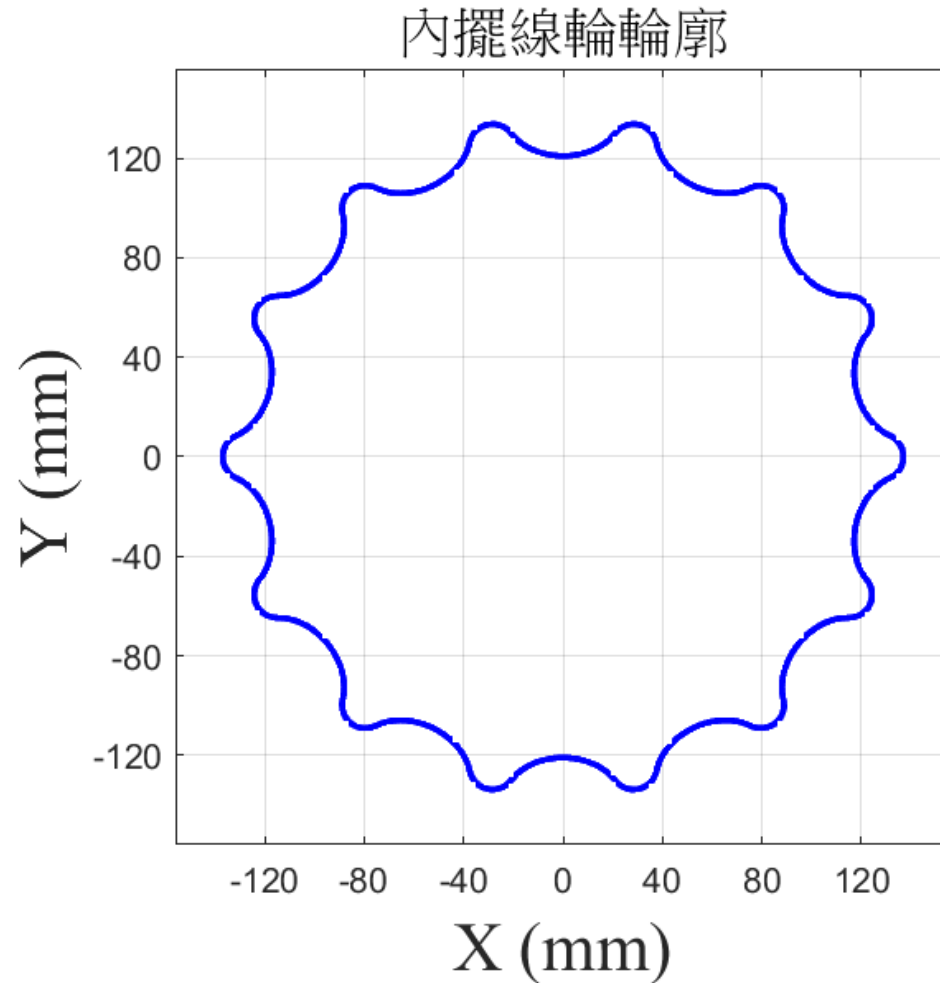
曲率半徑



等效連桿

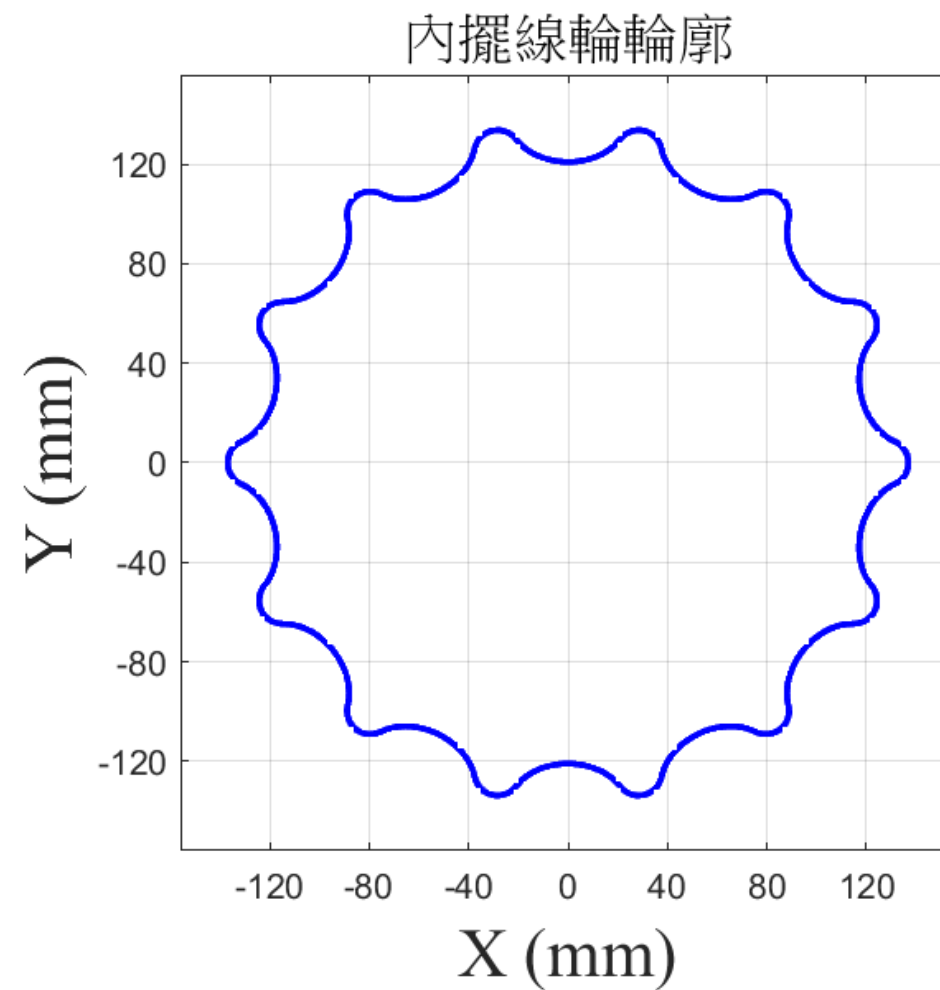
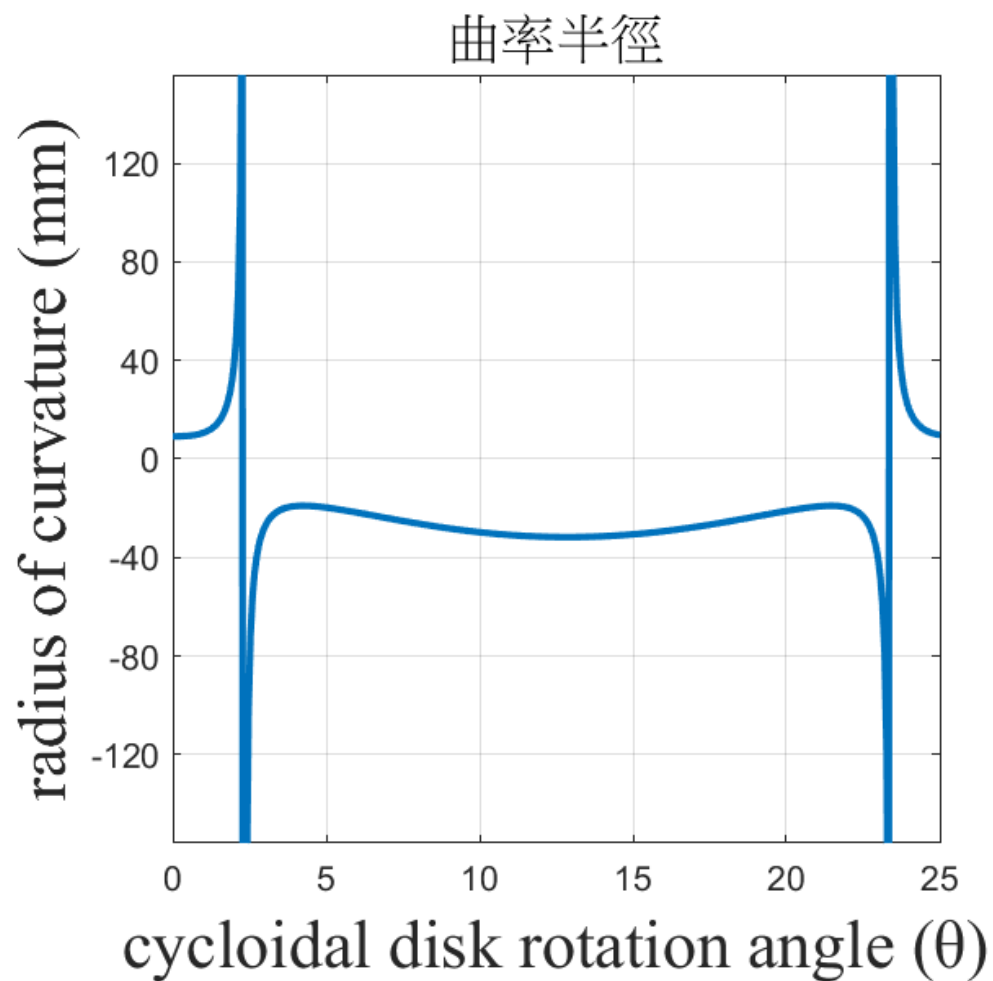


曲率半徑

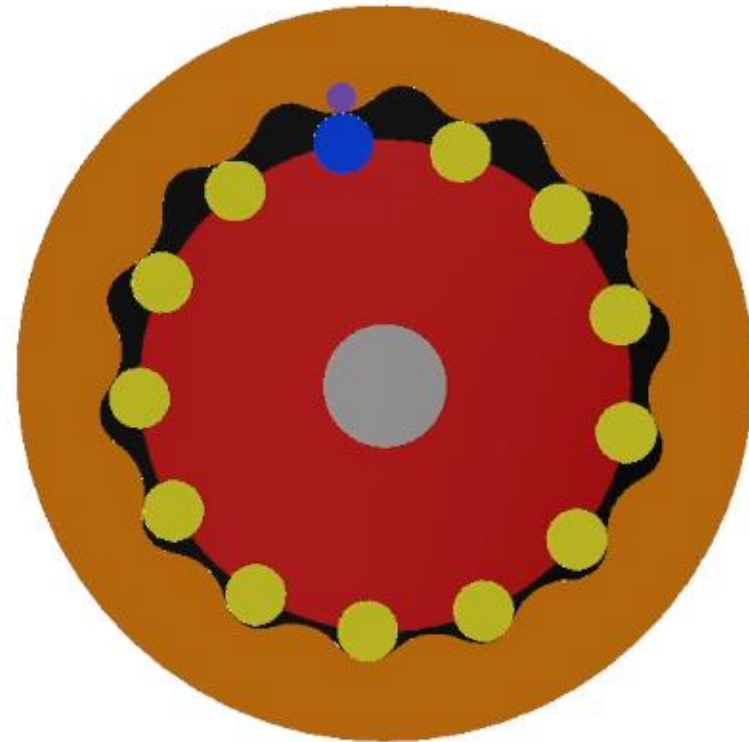
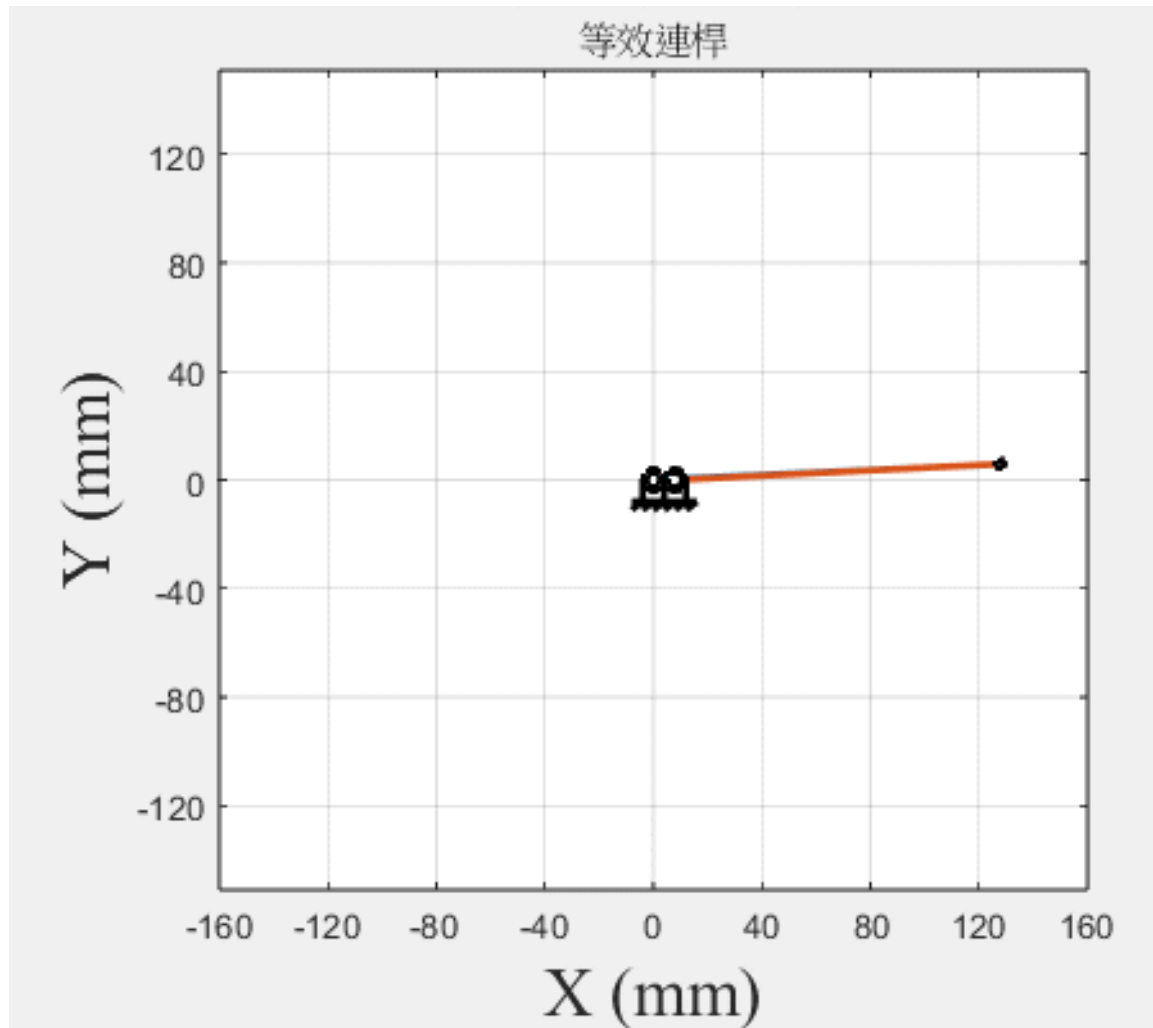


- $N = 13$
- $R_r = 9 \text{ mm}$
- $R = 120 \text{ mm}$
- $E = 8 \text{ mm}$

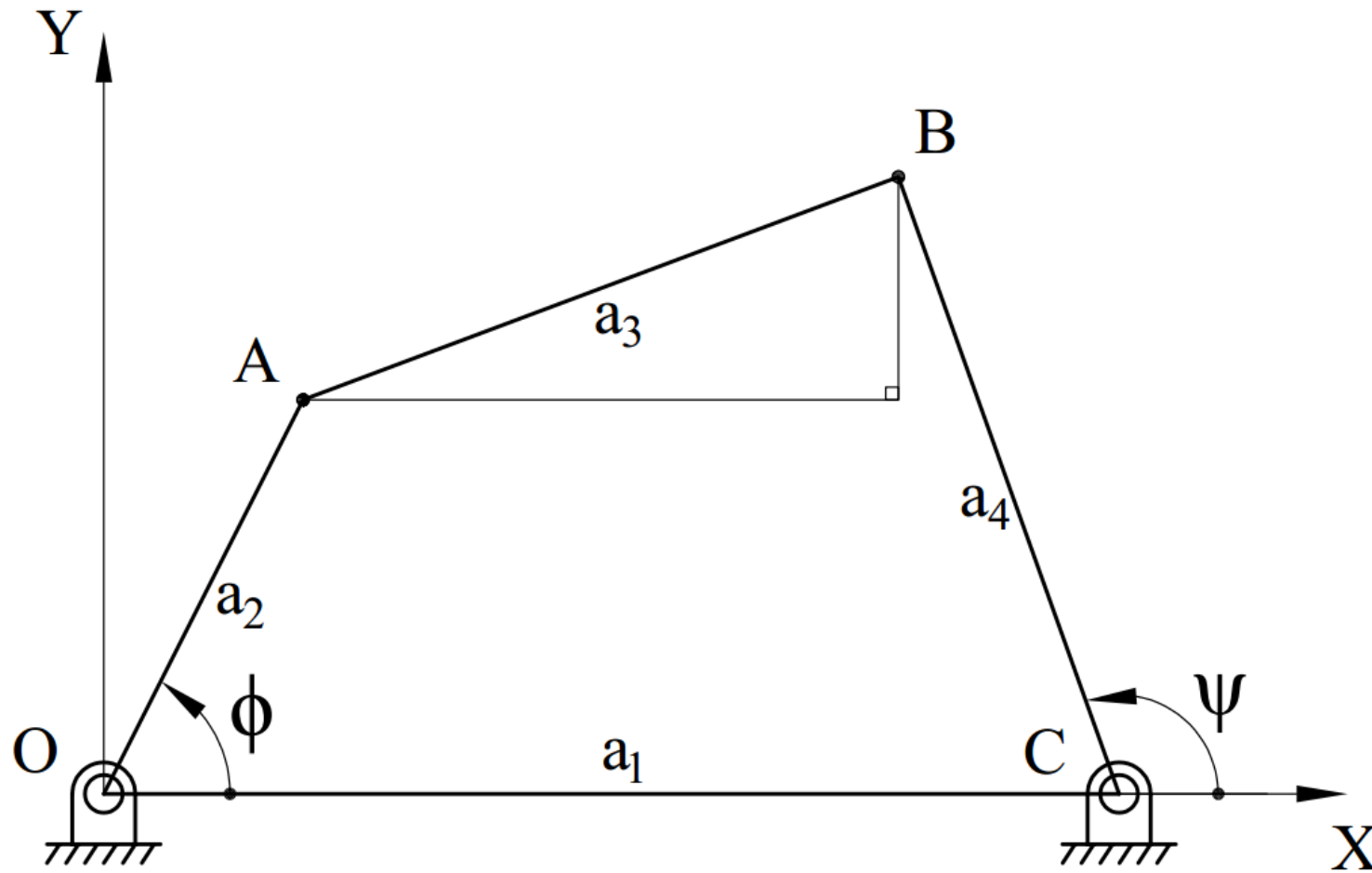
曲率半徑



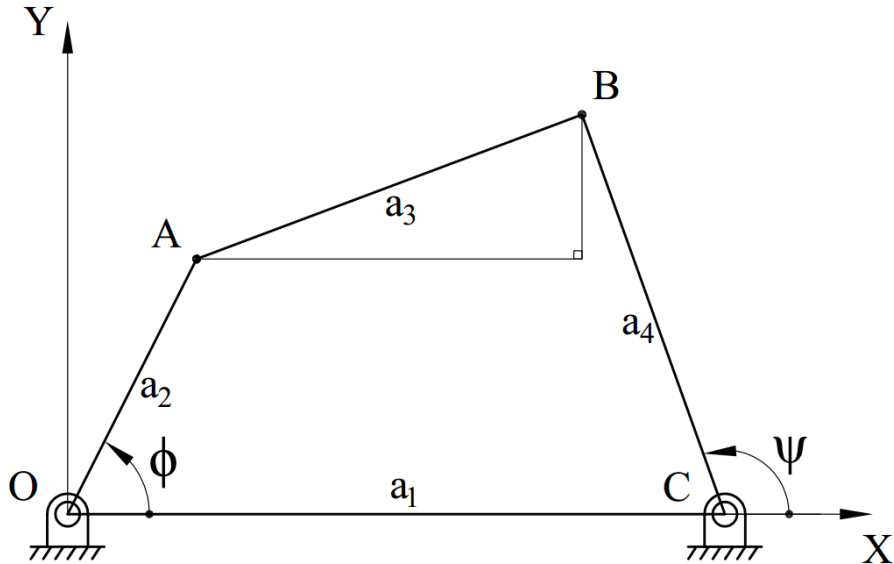
等效連桿



位移方程式



位移方程式



$$A(a_2 \cos \phi, a_2 \sin \phi)$$

$$B(a_1 + a_4 \cos \psi, a_4 \sin \psi)$$

$$(a_1 + a_4 \cos \psi - a_2 \cos \phi)^2 + (a_4 \sin \psi - a_2 \sin \phi)^2 = a_3^2$$

未來目標

- 轉換角
- 將等效連桿參數代入位移方程式
- 做各接觸點誤差分析