



# Boost Metaprogramming Concepts & Frameworks

BoostCon 2007 Edition  
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Consulting



# Agenda

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- The What, Why, and How
- Tour of Boost Metaprogramming Library (MPL)
- Using MPL for Dimensional Analysis
- Expression Templates
- Building Finite State Machines
- Tuple Metaprogramming
- Preprocessor Metaprogramming



# Hidden Agenda

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- Functional Programming
- The Role of Polymorphism
- Type Systems
- Domain Specific Languages (DSLs)
- Embedded DSLs



# “Meta:”

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- A prefix meaning one level of description higher. If X is some concept then **meta-X is data about, or processes operating on, X.**

For example, a metasyntax is syntax for specifying syntax, metalanguage is a language used to discuss language, meta-data is data about data, and meta-reasoning is reasoning about reasoning.

- Source: The Free On-line Dictionary of Computing,  
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# “Meta:”

- A prefix meaning one level of description higher. If X is some concept then **meta-X is data about, or processes operating on, X.**

For example, a metasyntax is syntax for specifying syntax, metalanguage is a language used to discuss language, meta-data is data about data, and meta-reasoning is reasoning about reasoning.

This is difficult to explain briefly, but much hacker humour turns on deliberate confusion between meta-levels.

- Source: The Free On-line Dictionary of Computing,  
© 1993-2004 Denis Howe



# Metaprogram: Our Definition

---



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---

- Code that explicitly manipulates or generates program elements such as:
  - Functions
  - Types
  - Classes
  - Variables
  - Constants
  - etc.



# Metaprogram: Our Definition

---

- Code that explicitly manipulates or generates program elements such as:
  - Functions
  - Types
  - Classes
  - Variables
  - Constants
  - etc.
- For example?



# Basic Concepts

---

- Domain: Parsing/translation
- Domain Abstractions: terminals, nonterminals, parse rules, semantic actions
- Domain Language:
  - Syntax (Yacc input syntax + `C' fragments)
  - Semantics (The generated parser)
- Metaprogram Data: Yacc's internal representation of those abstractions

# Parsing Domain Language

---

**expression → term**

**expression → expression '+' term**

**expression → expression '-' term**

**term → factor**

| term '\*' factor

| term '/' factor

**factor → INTEGER**

| group

**group → '(' expression ')'**

# Parsing Domain Language

**expression → term**

**expression → expression '+' term**

**expression → expression '-' term**

**term → factor**

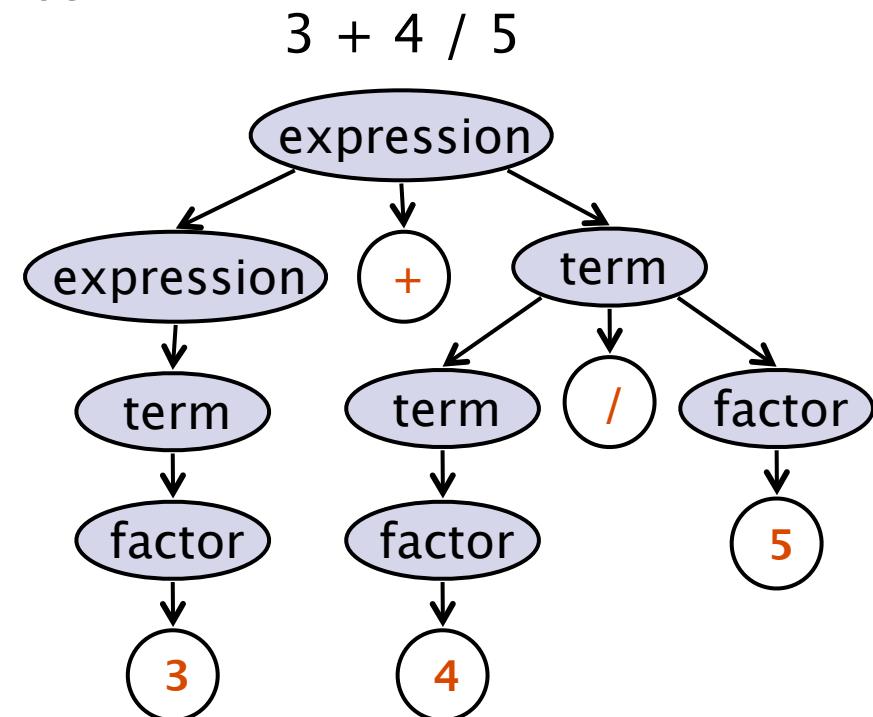
| term '\*' factor

| term '/' factor

**factor → INTEGER**

| group

**group → '(' expression ')'**



# YACC Domain Language

**expression : term**

| **expression '+' term** { \$\$ = \$1 + \$3; }  
| **expression '-' term** { \$\$ = \$1 - \$3; };

**term : factor**

| **term '\*' factor** { \$\$ = \$1 \* \$3; }  
| **term '/' factor** { \$\$ = \$1 / \$3; };

**factor : INTEGER**

| **group;**

**group : '(' expression ')';**

# YACC Target Language (C)

---

```

const short yylhs[] = {
    -1,
    2, 0, 0, 3, 3, 4, 5, 5,
    5, 1,
    1, 1,
};

const short yylen[] = {
    2,
    0, 4, 0, 1, 1, 3, 1, 3,
    3, 1,
    3, 3,
};

const short yydefred[] = { ... };

const short yydgoto[] = { ... };

const short yysindex[] = { ... };

const short yyrindex[] = { ... };

const short yygindex[] = { ... };

```

```

yym = yylen[ynn];
yyval = yyvsp[1-yym];
switch (ynn)
{
case 1:
{ std::printf("= %d\n", yyvsp[0]); std::fflush
  (stdout); }
break;
case 8:
{ yyval = yyvsp[-2] * yyvsp[0]; }
break;
case 9:
{ yyval = yyvsp[-2] / yyvsp[0]; }
break;
case 11:
{ yyval = yyvsp[-2] + yyvsp[0]; }
break;
case 12:
{ yyval = yyvsp[-2] - yyvsp[0]; }
break;
}
yyssp -= yym;
...

```

# Template Metaprogramming

---

- No Target Language
- Data: potential template arguments
- Domain Languages: subsets of native C++
- Downside: users constrained by C++ syntax
- Upside:
  - No hard boundary between metaprograms and “ordinary code”
  - Single Translation Step
  - Deep manipulation of native program elements.

# Embedded Metaprogramming

**integer** ® '-'? **digit+**

**factor** ® **integer**

- | '(' **expr** ')'
- | '-' **factor**

**term** ® **factor** ( '\*' **factor** | '/' **factor** )\*

**expr** ® **term** ( '+' **term** | '-' **term** )\*

# Embedded Metaprogramming

**integer** ®

'-'?

**digit+**

**factor** ® **integer**

| '('      **expr**    ')'

| '-'      **factor**

**term** ® **factor**

( '\*'      **factor** | '/'      **factor** )\*

**expr** ® **term**

( '+'      **term** | '-'      **term** )\*

# Embedded Metaprogramming

```
spirit::rule<> expr, term, factor, integer;
```

```
integer = !ch_lit('-') >> +digit;
```

```
factor = integer
        | '(' >> expr >> ')'
        | '-' >> factor;
```

```
term = factor >> *( '*' >> factor | '/' >> factor );
```

```
expr = term >> *( '+' >> term | '-' >> term );
```

# Compile-Time Computation

---

# Compile-Time Computation

---

binary<1101>::value → 13

```
template <unsigned long N>
struct binary
{
    static unsigned const value
        = N%10
```

# Compile-Time Computation

---

binary<1101>::value → 13

```
template <unsigned long N>
struct binary
{
    static unsigned const value
    = N%10
    + 2 * binary<N/10>::value;
};
```

```
template <>
struct binary<0>
{
```

# Compile-Time Computation

binary<1101>::value → 13

```
template <unsigned long N>
struct binary
{
    static unsigned const value
    = N%10
    + 2 * binary<N/10>::value;
};
```

```
template <>
struct binary<0>
{
    static unsigned const value
```

# Compile-Time Computation

binary<1101>::value → 13

```
template <unsigned long N>
struct binary
{
    static unsigned const value
    = N%10
    + 2 * binary<N/10>::value;
};
```

```
template <>
struct binary<0>
{
    static unsigned const value
    = 0;
```

# Compile-Time Computation

binary<1101>::value → 13

```
template <unsigned long N>
struct binary
{
    static unsigned const value
    = N%10
    + 2 * binary<N/10>::value;
};
```

```
template <>
struct binary<0>
{
    static unsigned const value
    = 0;
};
```

# Compile-Time Computation

binary<1101>::value → 13

```
template <unsigned long N>
struct binary
{
    static unsigned const value
    = N%10
    + 2 * binary<N/10>::value;
};
```

```
template <>
struct binary<0>
{
    static unsigned const value
    = 0;
};
```

binary<1101>::value =

# Compile-Time Computation

---

binary<1101>::value → 13

```
template <unsigned long N>
struct binary
{
    static unsigned const value
    = N%10
    + 2 * binary<N/10>::value;
};
```

```
template <>
struct binary<0>
{
    static unsigned const value
    = 0;
};
```

```
binary<1101>::value =
1 + 2 * binary<110>::value
binary<110>::value =
```

# Compile-Time Computation

---

binary<1101>::value → 13

```
template <unsigned long N>
struct binary
{
    static unsigned const value
    = N%10
    + 2 * binary<N/10>::value;
};
```

```
template <>
struct binary<0>
{
    static unsigned const value
    = 0;
};
```

```
binary<1101>::value =
    1 + 2 * binary<110>::value
binary<110>::value =
    0 + 2 * binary<11>::value
binary<11>::value =
```

# Compile-Time Computation

binary<1101>::value → 13

```
template <unsigned long N>
struct binary
{
    static unsigned const value
    = N%10
    + 2 * binary<N/10>::value;
};
```

```
template <>
struct binary<0>
{
    static unsigned const value
    = 0;
};
```

```
binary<1101>::value =
    1 + 2 * binary<110>::value
binary<110>::value =
    0 + 2 * binary<11>::value
binary<11>::value =
    1 + 2 * binary<1>::value
binary<11>::value =
```

# Compile-Time Computation

binary<1101>::value → 13

```
template <unsigned long N>
struct binary
{
    static unsigned const value
    = N%10
    + 2 * binary<N/10>::value;
};

template <>
struct binary<0>
{
    static unsigned const value
    = 0;
};
```

```
binary<1101>::value =
    1 + 2 * binary<110>::value
binary<110>::value =
    0 + 2 * binary<11>::value
binary<11>::value =
    1 + 2 * binary<1>::value
binary<11>::value =
    1 + 2 * binary<0>::value
binary<0>::value
```

# Compile-Time Computation

`binary<1101>::value → 13`

```
template <unsigned long N>
struct binary
{
    static unsigned const value
    = N%10
    + 2 * binary<N/10>::value;
};

template <>
struct binary<0>
{
    static unsigned const value
    = 0;
};
```

```
binary<1101>::value =
    1 + 2 * binary<110>::value = 13
binary<110>::value =
    0 + 2 * binary<11>::value
binary<11>::value =
    1 + 2 * binary<1>::value
binary<11>::value =
    1 + 2 * binary<0>::value
binary<0>::value
```

# Compile-Time Computation

binary<1101>::value → 13

```
template <unsigned long N>
struct binary
{
    static unsigned const value
    = N%10
    + 2 * binary<N/10>::value;
};

template <>
struct binary<0>
{
    static unsigned const value
    = 0;
};
```

$$\begin{aligned}
 & 1 + 2 * \text{binary}<110>::\text{value} \\
 \text{binary}<110>::\text{value} = \\
 & 0 + 2 * \text{binary}<11>::\text{value} = 6 \\
 \text{binary}<11>::\text{value} = \\
 & 1 + 2 * \text{binary}<1>::\text{value} = 3 \\
 \text{binary}<11>::\text{value} = \\
 & 1 + 2 * \text{binary}<0>::\text{value} = 1 \\
 \text{binary}<0>::\text{value} & = 0
 \end{aligned}$$

# Compile-Time Computation

binary<1101>::value → 13

```
template <unsigned long N>
struct binary
{
    static unsigned const value
    = N%10
    + 2 * binary<N/10>::value;
};

template <>
struct binary<0>
{
    static unsigned const value
    = 0;
};
```

$$\begin{aligned}
 & 0 + 2 * \text{binary}<11>::\text{value} \\
 \text{binary}<11>::\text{value} = & \\
 & 1 + 2 * \text{binary}<1>::\text{value} = 3 \\
 \text{binary}<11>::\text{value} = & \\
 & 1 + 2 * \text{binary}<0>::\text{value} = 1 \\
 \text{binary}<0>::\text{value} & = 0
 \end{aligned}$$

# Compile-Time Computation

`binary<1101>::value → 13`

```
template <unsigned long N>
struct binary
{
    static unsigned const value
    = N%10
    + 2 * binary<N/10>::value;
};

template <>
struct binary<0>
{
    static unsigned const value
    = 0;
};
```

$$\begin{aligned} \text{binary}<11>::value &= \\ &1 + 2 * \text{binary}<1>::value \\ \text{binary}<0>::value &= 0 \end{aligned}$$

# Compile-Time Computation

binary<1101>::value → 13

```
template <unsigned long N>
struct binary
{
    static unsigned const value
    = N%10
    + 2 * binary<N/10>::value;
};
```

```
template <>
struct binary<0>
{
    static unsigned const value
    = 0;
};
```

# Why Metaprogramming?

## ■ Why not runtime computation?

```
int binary(unsigned long n)
{
    return n ? n%10 + binary(n/10) * 2 : 0;
}
```

- Metaprogram is faster at runtime (duh)
- Metaprogram interacts deeply with host language

## ■ Why not user analysis?

```
long odd_bits = binary<1010101>::value;
```

```
long even_bits = 0xAA;
```

- Metaprogram is more convenient
- Metaprogram is more reliable
- Metaprogram brings us closer to the domain abstraction



# It Takes Some Effort

---

Metaprogramming is for Lovers



# It Takes Some Effort

---

Metaprogramming is Library Authors



# Boost Metaprogramming Concepts & Frameworks

## The Boost Metaprogramming Library: A Whirlwind Tour

# Aleksey Gurtovoy (in the hat)



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Monday, January 17, 2011



# Why a TMP Library?

---

- Simplify complicated template system
- Hide low-level hacks
- Smooth over implementation differences
- Readability: reduce the syntactic burden
- Conceptual integrity: like STL, the concepts and idioms shape the way we program.
- Fun: high-level programming is more productive than using template “assembly language”

# MPL Metaprogramming Concept

- A class template
- Operating on types only
- Single return “value” (i.e. a type)
- Called ::type

```
template <class A1, class A2, ...An>
struct identifier
{
    typedef type-expression type;
};
```

- If ::value appears, it's purely optional.

# Metadata Polymorphism?

```
template <class T>
struct foo {};
```

```
int obj;
void f(long);
```

foo<char*>	// OK
foo<1>	// integral constant
foo<f>	// function reference
foo<&f>	// function pointer
foo<obj>	// object reference
foo<&obj>	// object pointer
foo<&pair<int,int>::first>	// pointer to data member
foo<std::vector>	// class template

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# Metadata Polymorphism?

```
template <int N>
struct foo {};
```

```
int obj;
void f(long);
```

foo<char*>	// OK
foo<1>	// integral constant
foo<f>	// function reference
foo<&f>	// function pointer
foo<obj>	// object reference
foo<&obj>	// object pointer
foo<&pair<int,int>::first>	// pointer to data member
foo<std::vector>	// class template

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# Metadata Polymorphism?

```
template <void(&f)(long)>
struct foo {};
```

```
int obj;
void f(long);
```

foo<char*>	// OK
foo<1>	// integral constant
foo<f>	// function reference
foo<&f>	// function pointer
foo<obj>	// object reference
foo<&obj>	// object pointer
foo<&pair<int,int>::first>	// pointer to data member
foo<std::vector>	// class template

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# Metadata Polymorphism?

```
template <void(*pf)(long)>
struct foo {};
```

```
int obj;
void f(long);
```

foo<char*>	// OK
foo<1>	// integral constant
foo<f>	// function reference
foo<&f>	// function pointer
foo<obj>	// object reference
foo<&obj>	// object pointer
foo<&pair<int,int>::first>	// pointer to data member
foo<std::vector>	// class template

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# Metadata Polymorphism?

```
template <int& rx>
struct foo {};
```

```
int obj;
void f(long);
```

foo<char*>	// OK
foo<1>	// integral constant
foo<f>	// function reference
foo<&f>	// function pointer
foo<obj>	// object reference
foo<&obj>	// object pointer
foo<&pair<int,int>::first>	// pointer to data member
foo<std::vector>	// class template

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# Metadata Polymorphism?

```
template <int* px>
struct foo {};
```

```
int obj;
void f(long);
```

foo<char*>	// OK
foo<1>	// integral constant
foo<f>	// function reference
foo<&f>	// function pointer
foo<obj>	// object reference
foo<&obj>	// object pointer
foo<&pair<int,int>::first>	// pointer to data member
foo<std::vector>	// class template

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# Metadata Polymorphism?

```
template <int (pair<int,int>::*pm)>
struct foo {};
```

```
int obj;
void f(long);
```

foo<char*>	// OK
foo<1>	// integral constant
foo<f>	// function reference
foo<&f>	// function pointer
foo<obj>	// object reference
foo<&obj>	// object pointer
foo<&pair<int,int>::first>	// pointer to data member
foo<std::vector>	// class template

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# Metadata Polymorphism?

```
template <template <class,class> class C>
struct foo {};
```

```
int obj;
void f(long);
```

foo<char*>	// OK
foo<1>	// integral constant
foo<f>	// function reference
foo<&f>	// function pointer
foo<obj>	// object reference
foo<&obj>	// object pointer
foo<&pair<int,int>::first>	// pointer to data member
foo<std::vector>	// class template

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# Metadata Polymorphism

---

Solution: turn everything into a type with some kind of wrapper:

```
template <class T, T x>
struct wrap
{};


```

Works for almost everything...

```
wrap<int,5>                                // OK

wrap<                                         // Also OK

    int std::pair<int,int>::*  

    , &std::pair<int,int>::first >  

{};

...except?
```

# MPL Integral Constant

```
template <class T, T n>
struct integral_c
{
    typedef T value_type;
    static T const value = n;

    typedef integral_c<T,n> type; // self
    operator T() const { return n; }
};

template <int n>
struct int_ : integral_c<int,n> {};

template <bool x>
struct bool_ : integral_c<bool,x> {};

...
```



# Type Logic

---

```
typedef bool_<true> true_;  
typedef bool_<false> false_;
```

```
template <  
    class C, class T, class F  
>  
struct if_;
```



# Type Logic

```
typedef bool_<true> true_;
typedef bool_<false> false_;
```

```
template <
    class C, class T, class F
>
struct if_;
```

```
template <class T, class F>
struct if_<true_,T,F>
{
    typedef T type;
};

template <class T, class F>
struct if_<false_,T,F>
{
    typedef F type;
};
```

# Type Sequences

---



# Type Sequences

---

```
typedef mpl::vector<int*,long,char[4]> v1;
```



# Type Sequences

---

```
typedef mpl::vector<int*,long,char[4]> v1;
```

```
typedef mpl::deref<
```



# Type Sequences

---

```
typedef mpl::vector<int*,long,char[4]> v1;
```

```
typedef mpl::deref<
    mpl::begin<v1>::type    // MPL iterators
>::type pointer_to_int;   // *v1.begin()
```



# Type Sequences

---

```
typedef mpl::vector<int*,long,char[4]> v1;
```

```
typedef mpl::deref<
    mpl::begin<v1>::type    // MPL iterators
>::type pointer_to_int;   // *v1.begin()
```



# Type Sequences

---

```
typedef mpl::vector<int*,long,char[4]> v1;
```

```
typedef mpl::deref<
    mpl::begin<v1>::type // MPL iterators
>::type pointer_to_int; // *v1.begin()
```

```
typedef mpl::at<v1, mpl::int_<2> >::type
```



# Type Sequences

---

```
typedef mpl::vector<int*,long,char[4]> v1;
```

```
typedef mpl::deref<
    mpl::begin<v1>::type // MPL iterators
>::type pointer_to_int; // *v1.begin()
```

```
typedef mpl::at<v1, mpl::int_<2> >::type
four_chars;
```



# Type Sequences

---

```
typedef mpl::vector<int*,long,char[4]> v1;
```

```
typedef mpl::deref<
    mpl::begin<v1>::type // MPL iterators
>::type pointer_to_int; // *v1.begin()
```

```
typedef mpl::at<v1, mpl::int_<2> >::type
four_chars;
```



# Type Sequences

---

```
typedef mpl::vector<int*,long,char[4]> v1;
```

```
typedef mpl::deref<
    mpl::begin<v1>::type // MPL iterators
>::type pointer_to_int; // *v1.begin()
```

```
typedef mpl::at<v1, mpl::int_<2> >::type
four_chars;
```

```
typedef mpl::list<int*, long, char[4]> l1;
```



# Type Sequences

---

```
typedef mpl::vector<int*,long,char[4]> v1;
```

```
typedef mpl::deref<
    mpl::begin<v1>::type // MPL iterators
>::type pointer_to_int; // *v1.begin()
```

```
typedef mpl::at<v1, mpl::int_<2> >::type
four_chars;
```

```
typedef mpl::list<int*, long, char[4]> l1;
```

# Algorithms

---



# Algorithms

---

```
template<class Iter, class T> // STL
void replace(Iter first, Iter last, T const& old, T const& new);
```

```
template<class Sequence, class OldType, class NewType...> // MPL
```



# Algorithms

---

```
template<class Iter, class T> // STL
void replace(Iter first, Iter last, T const& old, T const& new);
```

```
template<class Sequence, class OldType, class NewType...> // MPL
struct replace;
```

```
template<class InIter, class OutIter, class UnaryOp> // STL
OutIter transform(InIter first, InIter last, OutIter result, UnaryOp op);
```

# Algorithms

---

```
template<class Iter, class T> // STL
void replace(Iter first, Iter last, T const& old, T const& new);
```

```
template<class Sequence, class OldType, class NewType...> // MPL
struct replace;
```

```
template<class InIter, class OutIter, class UnaryOp> // STL
OutIter transform(InIter first, InIter last, OutIter result, UnaryOp op);
```

```
template <class Sequence, class UnaryOp...> // MPL
struct transform;
```



# Lazy Logic

---

```
struct dumb_add_ptr<class T>
{ typedef T* type; };

template <class T>

struct smart_add_ptr
: mpl::if_<
    is_reference<T>
, T
, dumb_add_ptr<T>::type
> {};

typedef smart_add_ptr<int&>::type oops;
```



# Lazy Logic

---

```
struct dumb_add_ptr<class T>
{ typedef T* type; };

template <class T>

struct smart_add_ptr
: mpl::eval_if<
    is_reference<T>
  , mpl::identity<T>
  , dumb_add_ptr<T>
> {};

typedef smart_add_ptr<int&>::type oops; ok;
```

# Views / Lazy Sequences

---

```
template <class Sequence, class UnaryOp>
struct transform_view;
```

```
template <class Sequence, class Predicate>
struct filter_view;
```

```
template <class SequenceOfSequences>
struct zip_view;
```

```
template <class T, T Start, T Finish>
```

# Example: Dimensional

- Computation with units (typechecking for scientists)
- Newtons Law:  $F = \mathbf{m}a$

- Breakdown:

$$a = \frac{\Delta v}{\Delta t}, \quad v = \frac{\Delta l}{\Delta t}$$

- Units of  $v$ :  $l / t$  e.g. miles per hour
  - Units of  $a$ :  $(l / t) / t = l / t^2$  e.g. feet per sec.  
squared
  - Units of  $F$ :  $ml / t^2$  e.g. kg m/s<sup>2</sup>

# The Challenge

---

- Addition/Subtraction  
boring – can't combine different units

`f(m + l); // error!`

- Multiplication/Division  
interesting – produces new types

`f(m * l); // OK – a type representing ml`

- Challenge: compute the new type

# MPL Integral Sequence

- Convenient shorthand for type sequence of integral constant wrappers

`mpl::list_c<int, i1, i2, ...in>`

≈ `mpl::list<`  
`mpl::int_<i1>, mpl::int_<i1>`  
`, ...mpl::int_<in>`  
`>`

# Representing Units

---

```
typedef list_c<int,1,0,0,0,0,0> mass;
typedef list_c<int,0,1,0,0,0,0> length;
typedef list_c<int,0,0,1,0,0,0> time;
typedef list_c<int,0,0,0,1,0,0> charge;
typedef list_c<int,0,0,0,0,1,0> temperature;
typedef list_c<int,0,0,0,0,0,1> intensity;
typedef list_c<int,0,0,0,0,0,0,1>
    amount_of_substance;
typedef list_c<int,0,0,0,0,0,0> scalar; // e.g. pi
typedef list_c<int,0,1,-2,0,0,0,0> acceleration;
```

# Representing Quantities

- Bind metadata to a runtime value

```
template <class T, class Units>
class quantity
{
public:
    explicit quantity(T x)
        : m_value(x) {}
```

```
    T value() const
        { return m_value; }
```

```
private:
    T m_value;
};
```

```
quantity<float, time> t(99.7);
```

# Addition/Subtraction

---

- Just combine “like quantities”

```
template <class T, class U>
quantity<T,U>
operator+(quantity<T,U> x, quantity<T,U> y)
{
    return quantity<T,U>(x.value() + y.value());
}
```

```
template <class T, class U>
quantity<T,U>
operator-(quantity<T,U> x, quantity<T,U> y)
{
    return quantity<T,U>(x.value() - y.value());
}
```

# Multiplication/Division

---

- Must compute return units

```
template <class T, class U1, class U2>
quantity<T, ?? >
operator*( quantity<T,U1> x, quantity<T,U2> y );
```

```
template <class T, class U1, class U2>
quantity<T, ?? >
operator/( quantity<T,U1> x, quantity<T,U2> y );
```

- Add/subtract corresponding powers:

$$\begin{aligned}
 a = v/t &= (l/t) / t \\
 &= l^{\textcolor{red}{1}} \cdot t^{-1} \cdot t^{-1} = l^{\textcolor{red}{1}} \cdot t^{-2}
 \end{aligned}$$

# Multiplication/Division

---

- Use MPL's transform algorithm:

```
template <class Seq1, class Seq2, class BinaryOp>
struct transform;           → Result Sequence
```

- Similar to STL transform:

```
template <
    class InIter1, class InIter2,
    class OutIter, class BinaryOp
>
void transform(
    InIter1 start1, InIter1 finish1, InIter2 start2
    , OutIter, BinaryOp
)
```



# What is the BinaryOp?

---



# What is the BinaryOp?

---

**ERROR**



# What is the BinaryOp?

- 
- MPL gives us plus/minus

**ERROR**



# What is the BinaryOp?

- MPL gives us plus/minus

```
mpl::plus<mpl::int_<2>, mpl::int_<3> >::type
```

ERROR



# What is the BinaryOp?

- MPL gives us plus/minus

```
mpl::plus<mpl::int_<2>, mpl::int_<3> >::type  
→ mpl::int_<5>
```

ERROR



# What is the BinaryOp?

- MPL gives us plus/minus

```
mpl::plus<mpl::int_<2>, mpl::int_<3> >::type  
→ mpl::int_<5>
```

ERROR



# What is the BinaryOp?

- MPL gives us plus/minus

```
mpl::plus<mpl::int_<2>, mpl::int_<3> >::type  
→ mpl::int_<5>
```

```
mpl::minus<mpl::int_<2>, mpl::int_<3> >::type
```

ERROR



# What is the BinaryOp?

- MPL gives us plus/minus

`mpl::plus<mpl::int_<2>, mpl::int_<3> >::type`  
→ `mpl::int_<5>`

`mpl::minus<mpl::int_<2>, mpl::int_<3> >::type`  
→ `mpl::int_<-1>`

**ERROR**



# What is the BinaryOp?

- MPL gives us plus/minus

`mpl::plus<mpl::int_<2>, mpl::int_<3> >::type`  
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**ERROR**



# What is the BinaryOp?

- MPL gives us plus/minus

```
mpl::plus<mpl::int_<2>, mpl::int_<3> >::type  
→ mpl::int_<5>
```

```
mpl::minus<mpl::int_<2>, mpl::int_<3> >::type  
→ mpl::int_<-1>
```

- Are we done now?

ERROR



# What is the BinaryOp?

- MPL gives us plus/minus

```
mpl::plus<mpl::int_<2>, mpl::int_<3> >::type  
→ mpl::int_<5>
```

```
mpl::minus<mpl::int_<2>, mpl::int_<3> >::type  
→ mpl::int_<-1>
```

- Are we done now?

template <class T, class U1, class U2>

**ERROR**  


# What is the BinaryOp?

- MPL gives us plus/minus

```
mpl::plus<mpl::int_<2>, mpl::int_<3> >::type  
→ mpl::int_<5>
```

```
mpl::minus<mpl::int_<2>, mpl::int_<3> >::type  
→ mpl::int_<-1>
```

- Are we done now?

```
template <class T, class U1, class U2>  
quantity<
```

**ERROR**



# What is the BinaryOp?

- MPL gives us plus/minus

```
mpl::plus<mpl::int_<2>, mpl::int_<3> >::type  
→ mpl::int_<5>
```

```
mpl::minus<mpl::int_<2>, mpl::int_<3> >::type  
→ mpl::int_<-1>
```

- Are we done now?

```
template <class T, class U1, class U2>
```

```
quantity<  
T
```

**ERROR**



# What is the BinaryOp?

---

- MPL gives us plus/minus

`mpl::plus<mpl::int_<2>, mpl::int_<3> >::type`  
 $\rightarrow$  `mpl::int_<5>`

`mpl::minus<mpl::int_<2>, mpl::int_<3> >::type`  
 $\rightarrow$  `mpl::int_<-1>`

- Are we done now?

`template <class T, class U1, class U2>`

`quantity<`

`T`

`, typename mpl::transform<U1,U2,mpl::plus>::type`

**ERROR**

# What is the BinaryOp?

---

- MPL gives us plus/minus

```
mpl::plus<mpl::int_<2>, mpl::int_<3> >::type
→ mpl::int_<5>
```

```
mpl::minus<mpl::int_<2>, mpl::int_<3> >::type
→ mpl::int_<-1>
```

- Are we done now?

```
template <class T, class U1, class U2>
```

```
quantity<
```

```
  T
```

```
    , typename mpl::transform<U1,U2,mpl::plus>::type
  >
```

**ERROR**

# What is the BinaryOp?

---

- MPL gives us plus/minus

```
mpl::plus<mpl::int_<2>, mpl::int_<3> >::type
→ mpl::int_<5>
```

```
mpl::minus<mpl::int_<2>, mpl::int_<3> >::type
→ mpl::int_<-1>
```

- Are we done now?

```
template <class T, class U1, class U2>
```

```
quantity<
```

```
  T
```

```
    , typename mpl::transform<U1,U2,mpl::plus>::type
```

```
>
```

```
operator*(quantity<T,U1> x, quantity<T,U2> y);
```

**ERROR**

# What is the BinaryOp?

---

- MPL gives us plus/minus

```
mpl::plus<mpl::int_<2>, mpl::int_<3> >::type
→ mpl::int_<5>
```

```
mpl::minus<mpl::int_<2>, mpl::int_<3> >::type
→ mpl::int_<-1>
```

- Are we done now?

```
template <class T, class U1, class U2>
```

```
quantity<
```

```
  T
```

```
    , typename mpl::transform<U1,U2,mpl::plus>::type
  >
```

```
operator*(quantity<T,U1> x, quantity<T,U2> y);
```

**ERROR**

~~plus~~

- Templates are not polymorphic metadata (types)!

# Metafunction Classes

---

- Applying familiar type-wrapper idiom:

```
struct plus_f
```

```
{
    template <class T1, class T2>           // nested metafunction
    struct apply
    {
        typedef typename mpl::plus<T1,T2>::type type;
    };
};
```

```
template <class T, class U1, class U2>
quantity<
    T, typename mpl::transform<U1,U2,plus_f>::type // OK
>
operator*(quantity<T,U1> x, quantity<T,U2> y);
```

- Definition: MPL Metafunction Class

01/17/11 a class with a nested metafunction named “apply”  
copyright 2006 David Abrahams, Eric Niebler

# Division – 3 Simplifications

---

# Division – 3 Simplifications

---

- #1: “Metafunction Forwarding”

```
struct minus_f
{
    template <class T1, class T2>
    struct apply : mpl::minus<T1,T2> {};
};
```

# Division – 3 Simplifications

- #1: “Metafunction Forwarding”

```
struct minus_f
{
    template <class T1, class T2>
    struct apply : mpl::minus<T1,T2> {};
};
```

- Replaces

**typedef typename ... ::type type;**

with:

:

# Division – 3 Simplifications

- #1: “Metafunction Forwarding”

```
struct minus_f
{
    template <class T1, class T2>
    struct apply : mpl::minus<T1,T2> {};
};
```

- Replaces

**typedef typename ... ::type type;**

with:

:

- Powerful syntactic trick; use it often...

# Division – 3 Simplifications

- #1: “Metafunction Forwarding”

```
struct minus_f
{
    template <class T1, class T2>
    struct apply : mpl::minus<T1,T2> {};
};
```

- Replaces

**typedef typename ... ::type type;**

with:

:

- Powerful syntactic trick; use it often...

but wrapping metafunctions still boring (no fun)

# Simplification #2:

```
template <class T, class U1, class U2>
quantity<
    T
    , typename mpl::transform<
        U1,U2,mpl::minus<_1,_2>
        >::type
>
operator/(quantity<T,U1> x, quantity<T,U2> y)
{
    return quantity<
        T
        , typename mpl::transform<
            U1,U2,mpl::minus<_1,_2>
            >::type
        >(
            x.value() / y.value()
        );
}
```

- Not boring! Fun!

# Simplification #3: Refactoring

---

```
template <class U1, class U2>
divide_units
: mpl::transform<U1,U2,mpl::minus<_1,_2> >
{};
```

```
template <class T, class U1, class U2>
quantity<T, typename divide_units<U1,U2>::typedivide_units<U1,U2>::type
    >(
        x.value() / y.value()
    );
}
```

# Higher-Order (Meta)

---

- Functions which operate on or return other functions, e.g. transform
- “Higher-order functional programming”
  - Fancy title for a simple concept  
...but well-earned!
- Possible because metafunctions are polymorphic



# Writing a Higher-Order Metaprogram

## ■ The Task:

$$\text{twice}(f,x) := f(f(x))$$

## ■ Implementation for metaprogram class F:

```
template <class F, class X>
struct twice
{
    private:
        typedef typename F::template apply<X>::type once;
    public:
        typedef
            typename F::template apply<once>::type
        type;
};
```

# Writing a Higher-Order Metaprogram

---

- Simplified using forwarding:

```
template <class F, class X>
struct twice
    : F::template apply<
        typename F::template apply<X>::type
    >
{};


```

- Refactored:

```
template <class UnaryMFC, class Arg>
struct apply1
    : UnaryMFC::template apply<Arg>
{};


```

```
template <class F, class X>
struct twice
    : apply1<F, typename apply1<F,X>::type>
{};


```



# Handling Placeholders

---

# Handling Placeholders

---

- Add a number to itself **twice**

```
template <class X>
struct times4
    : twice< mpl::plus<-1,-1>, X > {};
typedef times4<int_-<4>>::type sixteen; // error!
```



# Handling Placeholders

---

- Add a number to itself **twice**

```
template <class X>
struct times4
    : twice< mpl::plus<-1,-1>, X > {};
typedef times4<int_-<4>>::type sixteen; // error!
```

- Why doesn't it work?

```
template <class T1, class T2>
struct plus
{
    typedef ... type;
};
```

# Handling Placeholders

---

- Add a number to itself **twice**

```
template <class X>
struct times4
    : twice< mpl::plus<-1,-1>, X > {};
typedef times4<int_-<4>>::type sixteen; // error!
```

- Why doesn't it work?

```
template <class T1, class T2>
struct plus
{
    typedef ... type;
};
```

# Handling Placeholders

- Add a number to itself **twice**

```
template <class X>
struct times4
    : twice< mpl::plus<-1,-1>, X > {};
typedef times4<int_-<4>>::type sixteen; // error!
```

- Why doesn't it work?

```
template <class T1, class T2>
struct plus
{
    typedef ... type;
};
```

- No nested apply<...> – not a metafunction class

# The Lambda Metaprogramming

- `plus<_1,_1>` is called a “lambda expression”
- `lambda<lambda-expr>::type` → Metaprogramming Class

```
template <class X>
struct times4
: twice<
  typename mpl::lambda<
    mpl::plus<_1,_1>
  >::type, X
>
{};


```

- Note: `lambda<...>` passes metaprogramming classes through untouched

# The Lambda Calculus

- Branch of mathematical logic
- Deals with the application of functions to their arguments
- Developed in the late '30s and early '40s, by...



# The Lambda Calculus

- Branch of mathematical logic
- Deals with the application of functions to their arguments
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Alonzo Church



# Internal Lambda

- MPL algorithms apply lambda so you don't have to
- MPL's flexible version of **apply1**:

```
template <class UnaryOp, class Arg>
struct apply1
    : lambda<UnaryOp>::type
        ::template apply<Arg>
{};
```

- `mpl::apply<F, A1, A2, ...An>` is the *n*-ary version
- To handle both lambda expressions and metafunction classes as arguments, invoke them with **applyN** or **apply**

# The Power of Lambda

- Transform binary → unary metafunction

```
mpl::plus<_1,_1>
```

- Also via currying (arg. binding)

```
mpl::plus<_1, mpl::int_<42> >
```

- Functional Composition:

```
mpl::times<  
    mpl::plus<_1,_2>  
    , mpl::minus<_1,_2>  
>
```



# Boost Metaprogramming Concepts & Frameworks

## Building a Domain-Specific Embedded Language (DSEL)



# Finite State Machines (FSMs)

---

- **Uses:**
  - Embedded system controllers
  - Parsing (YACC parsers are stacks of FSMs)
  - Pattern Matching
  - Hardware Verification
  - Natural Language Processing
  - Any other stateful process
- Not Turing Complete
- Maybe that's a good thing?

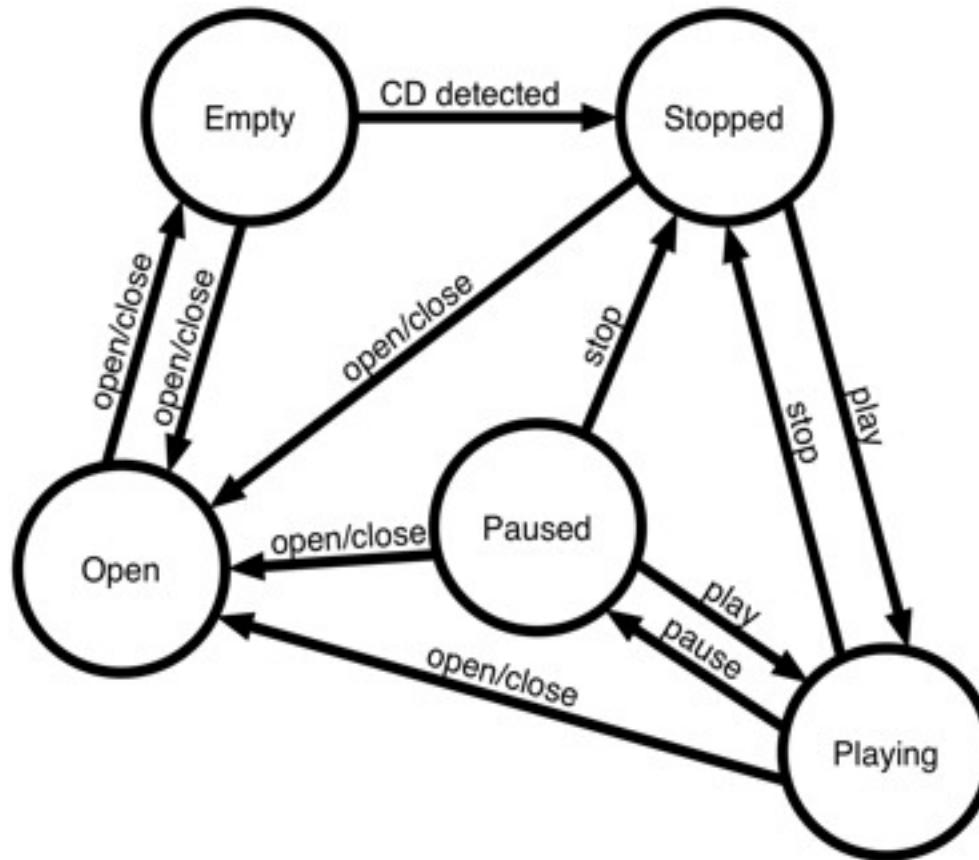


# 1) Understand Domain Abstraction

---

- **States** e.g. locked, unlocked, ready
- **Transitions** define legal paths from state to state, often with an associated **action**.
- **Events** trigger transitions, e.g. coin-inserted, tokens (in a parser). May be internally-generated.

# 2) Review Standard Notations



## Simple CD Player

# State Transition Table (STT)

Current State	Event	Next State	Transition Action
<i>Stopped</i>	<i>play</i>	<i>Playing</i>	start playback
<i>Stopped</i>	<i>open/close</i>	<i>Open</i>	open drawer
<i>Open</i>	<i>open/close</i>	<i>Empty</i>	close drawer; collect CD information
<i>Empty</i>	<i>open/close</i>	<i>Open</i>	open drawer
<i>Empty</i>	<i>cd detected</i>	<i>Stopped</i>	store CD information
<i>Playing</i>	<i>stop</i>	<i>Stopped</i>	stop playback
<i>Playing</i>	<i>pause</i>	<i>Paused</i>	pause playback
<i>Playing</i>	<i>open/close</i>	<i>Open</i>	stop playback; open drawer
<i>Paused</i>	<i>play</i>	<i>Playing</i>	resume playback
<i>Paused</i>	<i>stop</i>	<i>Stopped</i>	stop playback
<i>Paused</i>	<i>open/close</i>	<i>Open</i>	stop playback; open drawer

# 3) Choose an Embedded Notation

---

# 3) Choose an Embedded Notation

---

```

// start event      finish       action
fsm [ stopped, play,      playing,    start_playback ]
     [ playing, pause,     paused,    pause_playback ]...

fsm [ stopped | play   | playing | start_playback ]
     [ playing | pause  | paused  | pause_playback ]...

fsm= +-----+-----+-----+-----+
      +-----+-----+-----+-----+
      ! stopped | on<play>() | playing | start_playback |
      +-----+-----+-----+-----+
      ! playing | on<pause>() | paused  | pause_playback |
      +-----+-----+-----+-----+
      ...end;

// +-----+-----+-----+-----+
row< stopped , play , playing , &p::start_playback >,
// +-----+-----+-----+-----+
row< playing , pause , paused , &p::pause_playback >
// +-----+-----+-----+-----+

```

# 4) Consider Usage of Product

```
int main()
{
    player p;           // FSM object

    p.process_event(drawer()); // user opens CD player
    p.process_event(drawer()); // inserts CD and closes

    p.process_event(          // CD is detected
        cd_detected(
            "louie, louie"
            , std::vector<std::clock_t>( ...track lengths... )
        )
    );
}
```



# Nail Down Representation of Events

---

```
struct play {};
struct open_close {};
struct pause {};

struct cd_detected
{
    cd_detected(
        std::string name,
        std::vector<std::clock_t> const& track_lengths
    )
        : name(name), track_lengths(track_lengths)
    {}

    std::string name;
```

# FSM Declaration

```
class player      // Curiously Recurring Template Pattern
: public state_machine<player>
{
    friend class state_machine<player>;
    enum states { Empty, Open, Stopped, Playing, Paused,
                  initial_state = Empty };

    void start_playback(play const&);    // transition actions
    void open_drawer(drawer const&);
    void close_drawer(drawer const&);
    void store_cd_info(cd_detected const&);
    void stop_playback(stop const&);
    void pause_playback(pause const&);
    void resume_playback(play const&);
    void stop_and_open(drawer const&);
```

# FSM and its use (whole enchilada)

```

class player : public state_machine<player> // player.hpp
{
private:
  // the list of FSM states
  enum states {
    Empty, Open, Stopped, Playing, Paused
    , initial_state = Empty
  };

  void start_playback(play const&);
  void open_drawer(open_close const&);
  void close_drawer(open_close const&);
  void store_cd_info(cd_detected const&);
  void stop_playback(stop const&);
  void pause_playback(pause const&);
  void resume_playback(play const&);
  void stop_and_open(open_close const&);

  friend class state_machine<player>;
  typedef player p; // makes transition table cleaner

  // transition table
  struct transition_table : mpl::vector11<

  // Start   Event     Next     Action
  // +-----+-----+-----+
  row<Stopped , play     , Playing , &p::start_playback>

```

```

// player.cpp
void player::start_playback(play const&){}
void player::open_drawer(open_close const&){}
void player::close_drawer(open_close const&){}
void player::store_cd_info(cd_detected const&){}
void player::stop_playback(stop const&){}
void player::pause_playback(pause const&){}
void player::resume_playback(play const&){}
void player::stop_and_open(open_close const&){}

```

```

// main.cpp
int main()
{
  player p;

  p.process_event(open_close()); // user opens CD player
  p.process_event(open_close()); // inserts CD and closes
  p.process_event(
    cd_detected(
      "louie, louie"
      , std::vector<std::clock_t>(* track lengths * )
    )
  );
  p.process_event(play()); // etc.
  p.process_event(pause());
  p.process_event(play());
  p.process_event(stop());
  return 0;
}

```

# 5) Implementing the

---

- i.e., we need to define the state\_machine<...> class template
- Note that the definition of our FSM, player, contains **no details** about how the state machine is implemented
- We can choose among various implementation strategies.



# Curiously Recurring Template Pattern

---

```
};
```



# Curiously Recurring Template Pattern

---

**class FSM,**

**};**



# Curiously Recurring Template Pattern

```
template <class FSM>
struct state_machine
{
    template <

    > void transition(FSM& m, State from, State to);
};

template <class FSM>
void state_machine::transition(FSM& m, State from, State to)
{
    if (from == to) return;
    if (from->onExit(m)) {
        from->exit(m);
    }
    if (to->onEnter(m)) {
        to->enter(m);
    }
    if (from->onTransition(m, from, to)) {
        from->exit(m);
        to->enter(m);
    }
}
```

# Curiously Recurring Template Pattern

```
template <class FSM>
struct state_machine
{
    template <
        int FromState, class Event, int ToState
        , void (FSM::*action)(Event const&) >
    struct row
    {
    };
};
```



# Curiously Recurring Template Pattern

```
template <class FSM>
struct state_machine
{
    template <
        int FromState, class Event, int ToState
        , void (FSM::*action)(Event const&) >
    struct row
    {
        static int const from_state = FromState;
        static int const to_state = ToState;

    };
};
```



# Curiously Recurring Template Pattern

```
template <class FSM>
struct state_machine
{
    template <
        int FromState, class Event, int ToState
        , void (FSM::*action)(Event const&) >
    struct row
    {
        static int const from_state = FromState;
        static int const to_state = ToState;
        typedef Event event;

    };
};
```



# Curiously Recurring Template Pattern

```
template <class FSM>
struct state_machine
{
    template <
        int FromState, class Event, int ToState
        , void (FSM::*action)(Event const&) >
    struct row
    {
        static int const from_state = FromState;
        static int const to_state = ToState;
        typedef Event event;
        typedef FSM fsm_t;

    };
};
```



# Curiously Recurring Template Pattern

```
template <class FSM>
struct state_machine
{
    template <
        int FromState, class Event, int ToState
        , void (FSM::*action)(Event const&) >
    struct row
    {
        static int const from_state = FromState;
        static int const to_state = ToState;
        typedef Event event;
        typedef FSM fsm_t;

    };
};
```



# Curiously Recurring Template Pattern

```
template <class FSM>
struct state_machine
{
    template <
        int FromState, class Event, int ToState
        , void (FSM::*action)(Event const&) >
    struct row
    {
        static int const from_state = FromState;
        static int const to_state = ToState;
        typedef Event event;
        typedef FSM fsm_t;

    }; static void execute(FSM& fsm, Event const& e)
```



# Curiously Recurring Template Pattern

```
template <class FSM>
struct state_machine
{
    template <
        int FromState, class Event, int ToState
        , void (FSM::*action)(Event const&) >
    struct row
    {
        static int const from_state = FromState;
        static int const to_state = ToState;
        typedef Event event;
        typedef FSM fsm_t;

    }; static void execute(FSM& fsm, Event const& e)
    { (fsm.*action)(e); }
```



# Dispatching Events (By Hand)

```
template <class FSM>
void state_machine<FSM>::process_event(play const& e)
{
    switch (this->state)
    {
        case Stopped:
            this->start_playback(e);
            this->m_state = playing;
            break;
        case Paused:
            this->resume_playback(e);
            this->m_state = playing;
            break;
        default:
            this->no_transition(e);
    }
}
```

# Breakdown for Code



# Breakdown for Code

```
void process_event(play const& e)
{
    this->state = case_Stopped(e);
}
```

```
int case_Stopped(play const& e)
{
    if (this->state == Stopped)
    {
        this->start_playback(e);
        return Playing;
    }
    else
    {
        return this->case_Paused(e);
    }
}
```

# Breakdown for Code

```
void process_event(play const& e)
{
    this->state = case_Stopped(e);
}

int case_Stopped(play const& e)
{
    if (this->state == Stopped)
    {
        this->start_playback(e);
        return Playing;
    }
    else
    {
        return this->case_Paused(e);
    }
}
```

```
int case_default(play const& e)
{
    return this->no_transition(
        this->state, e);
}

int case_Paused(play const& e)
{
    if (this->state == Paused)
    {
        this->resume_playback(e);
        return Playing;
    }
}
```



# Breakdown for Code

```
void process_event(play const& e)
{
    this->state = case_Stopped(e);
}

int case_Stopped(play const& e)
{
    if (this->state == Stopped)
    {
        this->start_playback(e);
        return Playing;
    }
    else
    {
        return this->case_Paused(e);
    }
}
```

```
int case_default(play const& e)
{
    return this->no_transition(
        this->state, e);
}

int case_Paused(play const& e)
{
    if (this->state == Paused)
    {
        this->resume_playback(e);
        return Playing;
    }
    else
    {
        return this->case_default(e);
    }
}
```



# Generating the Dispatch

```
int
case_Stopped(play const& e)
{
    if (this->state == Stopped)
    {
        this->start_playback(e);
        return Playing;
    }
    else
    {
        return
            this->case_Paused(e);
    }
}
```



# Generating the Dispatch

```
int
case_Stopped(play const& e)
{
    if (this->state == Stopped)
    {
        this->start_playback(e);
        return Playing;
    }
    else
    {
        return
            this->case_Paused(e);
    }
}
```

```
template <int State, class E>
int case_(E const& e)
{
    if (fsm.state == State)
    {
        this->??????(e);
        return ?????;
    }
    else
    {
        return
            this->case_<???>(e);
    }
}
```

# Generating the Dispatch

```
template<class Row>
struct event_dispatcher
{
    typedef typename Row::fsm_t fsm_t;
    typedef typename Row::event event;

    static int dispatch(fsm_t& fsm, int state, event const& e)
    {
        if (state == Row::from_state)
        {
            Row::execute(fsm, e);
            return Row::to_state;
        }      ????;
        else
    }
};
```



# Generating the Dispatch

```
template<class Row, class Next>
struct event_dispatcher
{
    typedef typename Row::fsm_t fsm_t;
    typedef typename Row::event event;

    static int dispatch(fsm_t& fsm, int state, event const& e)
    {
        if (state == Row::from_state)
        {
            Row::execute(fsm, e);
            return Row::to_state;
        }      ????;
        else
    }
};
```



# Generating the Dispatch

```
template<class Row, class Next>
struct event_dispatcher
{
    typedef typename Row::fsm_t fsm_t;
    typedef typename Row::event event;

    static int dispatch(fsm_t& fsm, int state, event const& e)
    {
        if (state == Row::from_state)
        {
            Row::execute(fsm, e);
            return Row::to_state;
        }           Next::dispatch(fsm, state, e);
        else
    }
}
```



# “No Transition” Handler

```
struct default_event_dispatcher
{
    template<class FSM, class Event>
    static int dispatch(FSM& m, int state, Event const& e)
    {
        return m.call_no_transition(state, e);
    }
};

template <class FSM>

class state_machine
{
    template <class Event>
    int call_no_transition(int state, Event const& e)
    {
```



# Must Assemble This Dispatcher Type

```
typedef player p;

event_dispatcher<
    row<Stopped, play, Playing, &p::start_playback>,

    event_dispatcher<
        row<Paused, play, Playing, &p::resume_playback>,

        default_event_dispatcher
    >

    >
```

# Generating the Dispatcher

```
template <class Row, class Event>
struct has_event
: boost::is_same<typename Row::event, Event>
{};


```

```
template<class RowSequence, class Event>
struct generate_dispatcher
: mpl::accumulate<           // a.k.a. fold
  // Select all rows with transitions on Event
  mpl::filter_view<RowSequence, has_event<_1,Event> >,
  // Terminating case
  default_event_dispatcher,
  // Accumulator

```

# Finally, the Event Processor

```
template<class Event>
int process_event(Event const& event)
{
    typedef typename generate_dispatcher<
        typename FSM::transition_table, Event
    >::type dispatcher;

    this->state = dispatcher::dispatch(
        static_cast<FSM&>(*this),
        this->state,
        event
    );
}
```



# Final Details of state\_machine<>

```
public:  
    template <class Event>  
    int no_transition(int state, Event const& e)  
    {  
        assert(false);  
        return state;  
    }
```

```
protected:  
    state_machine()  
        : state(FSM::initial_state)  
    {}
```

# What Have We Achieved?

---

- As expressive as custom (text-based) state machine compiler
- Better scalability, maintainability, type safety, expressiveness, and efficiency than State pattern.
- Efficiency comparable to hand-coded FSM
- Fully Declarative: procedural logic fully replaceable



# Boost Metaprogramming Concepts & Frameworks

## Other Metaprogramming Paradigms in C++

# Tuple - The Quantum

---

```
typedef boost::tuple<  
    int, char const*, bool  
> t;
```

```
t s(3, "hello", true);
```

- heterogeneous sequence of values (wave):  
3, "hello", true
  
- also a sequence of types (particle):  
int, char const\*, bool

# Fusion/MPL Interoperability

---

- Every fusion tuple is a valid MPL sequence
- `fusion::as_vector(mpl-sequence-type())` → tuple

# Fusion: Tuple

## ■ Primitives:

- `begin(s), end(s)` → iterators
- `next(p), prior(q)` → adjacent iterators
- Some standard STL iterator operations:  
 $*p$      $p == q$      $p != q$

## ■ Algorithms:

- `for_each(s, unary_function)` → void
- `transform(s, unary_function)` → `transform_view`
- `push_back(s, value)` → ??
- `fold(s, init, binary_function)` → ??

# Why Fusion Algorithms Yield Views

---

```
fusion::tuple<std::string, std::string>    x( "hello", "world" );
```

```
fusion::for_each(
    fusion::push_back(
        fusion::push_back(
            fusion::push_back(x, 1)
            , std::vector<int>(5)
        )
        , 12
    )
    , some_function
);
```

# Why Fusion Algorithms Yield Views

---

```
fusion::tuple<std::string, std::string> x( "hello", "world" );
```

```
fusion::for_each(  
    fusion::push_back(  
        fusion::push_back(  
            fusion::push_back(x, 1)           ← copy two strings?  
            , std::vector<int>(5)  
        )  
    , 12  
)  
, some_function  
);
```

# Why Fusion Algorithms Yield Views

---

```
fusion::tuple<std::string, std::string> x( "hello", "world" );
```

```
fusion::for_each(  
    fusion::push_back(  
        fusion::push_back(  
            fusion::push_back(x, 1)  
            , std::vector<int>(5)  
        )  
    , 12  
)  
, some_function  
);
```

← copy two strings, one int?

# Why Fusion Algorithms Yield Views

---

```
fusion::tuple<std::string, std::string>    x( "hello", "world" );
```

```
fusion::for_each(  
    fusion::push_back(  
        fusion::push_back(  
            fusion::push_back(x, 1)  
            , std::vector<int>(5)  
        )  
    , 12  
)  
, some_function  
);
```

← copy two strings, one int, one vector?

# How to Get a Real Tuple

---

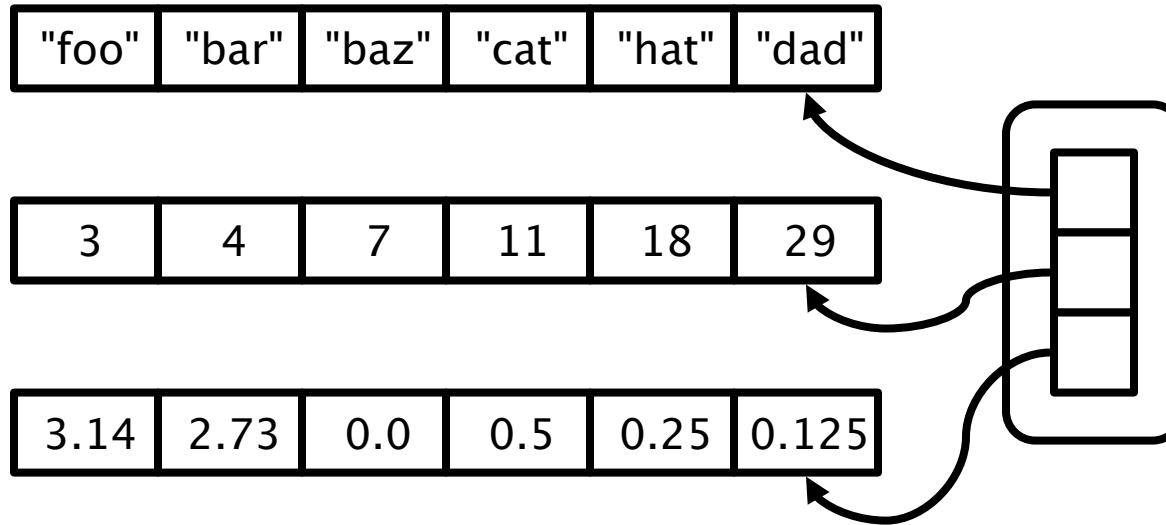
```
fusion::tuple<std::string, std::string> x( "hello",
    "world");
```

```
fusion::as_vector(
    fusion::push_back(
        fusion::push_back(
            fusion::push_back(x, 1)
            , std::vector<int>(5)
        )
    , 12
)
)
```

# Example:

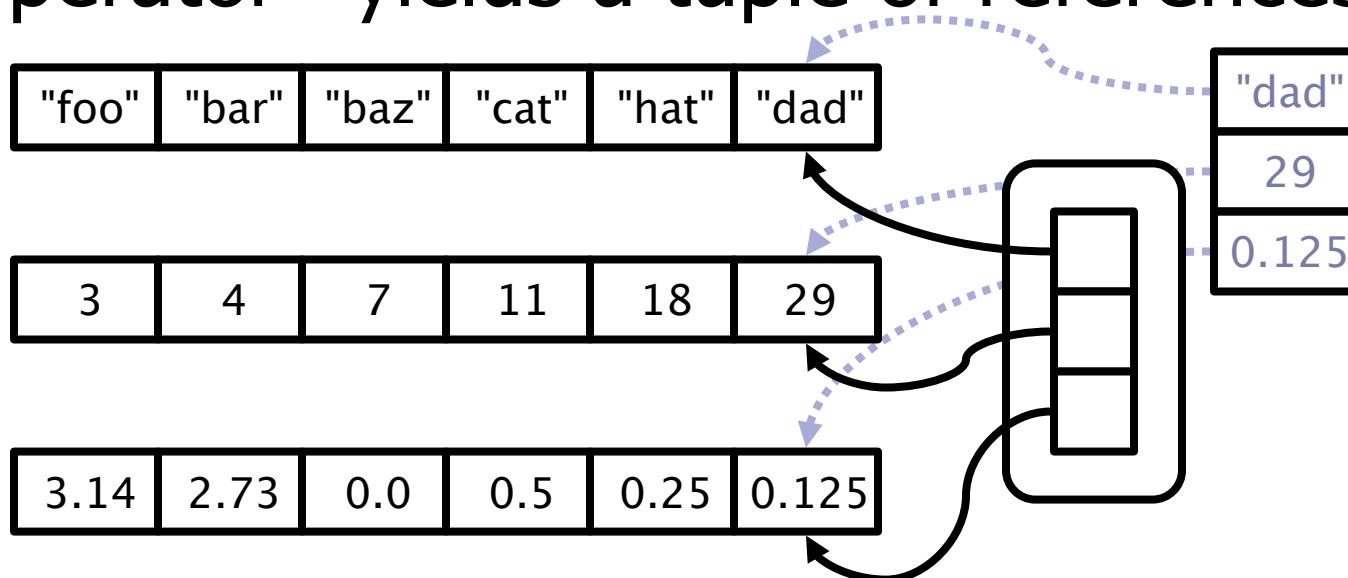
## zip\_iterator<IterTuple>

- Stores a tuple of iterators into different sequences
- Traverses the sequences in parallel
- operator\* yields a tuple of references



# Example: zip\_iterator<IterTuple>

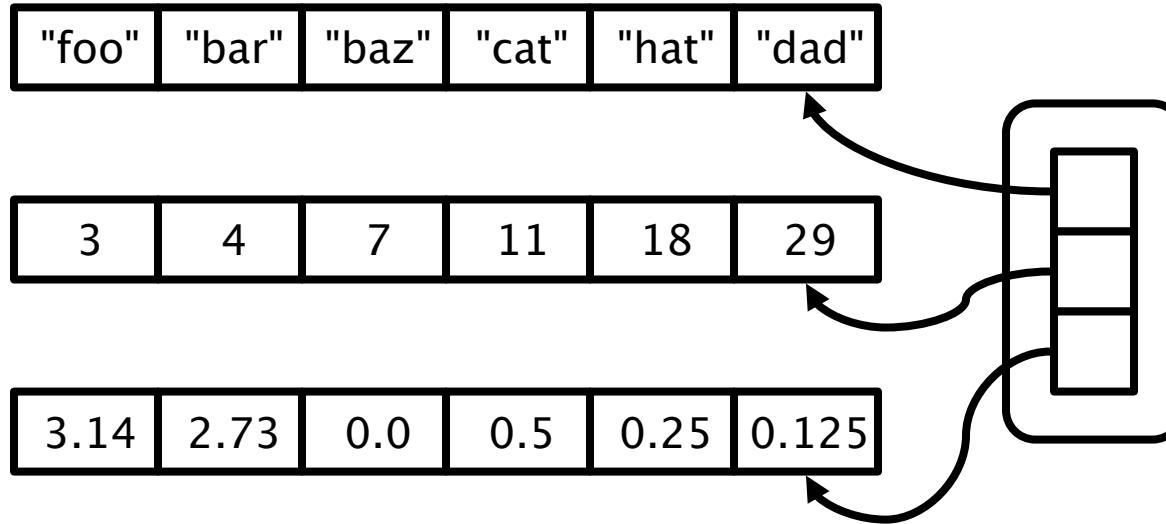
- Stores a tuple of iterators into different sequences
- Traverses the sequences in parallel
- operator\* yields a tuple of references



# Example:

## zip\_iterator<IterTuple>

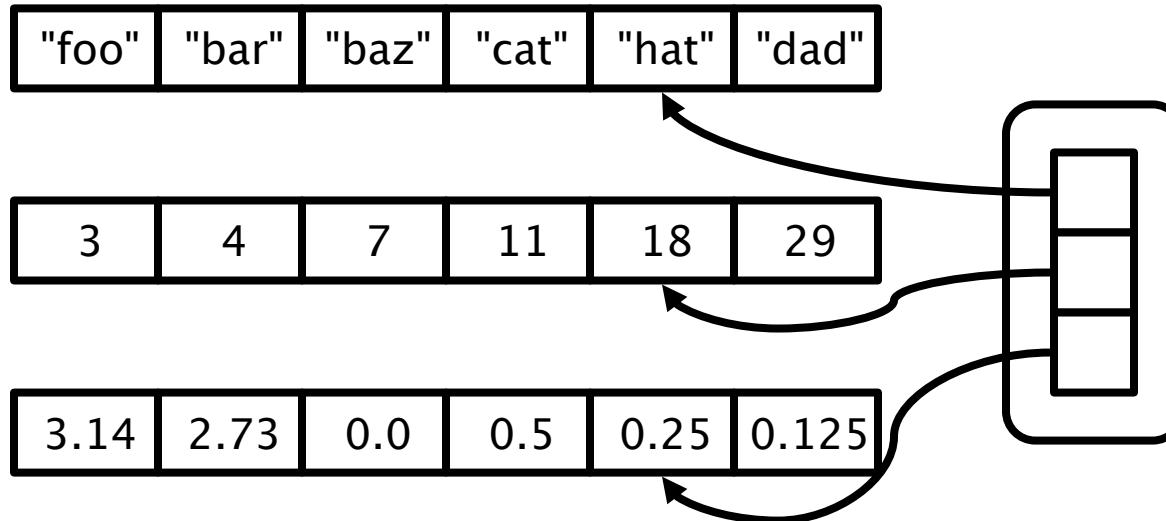
- Stores a tuple of iterators into different sequences
- Traverses the sequences in parallel
- operator\* yields a tuple of references



# Example:

## zip\_iterator<IterTuple>

- Stores a tuple of iterators into different sequences
- Traverses the sequences in parallel
- operator\* yields a tuple of references



# Why zip\_iterator?

---

# Why zip\_iterator?

---

Consider std::transform:



# Why zip\_iterator?

---

Consider std::transform:



# Why zip\_iterator?

---

Consider std::transform:

```
std::transform(start, finish, result, op);
```



# Why zip\_iterator?

---

Consider std::transform:

```
std::transform(start, finish, result, op);  
std::transform(start, finish, start2, result, op);
```



# Why zip\_iterator?

---

Consider std::transform:

```
std::transform(start, finish, result, op);  
std::transform(start, finish, start2, result, op);
```

# Why zip\_iterator?

---

Consider std::transform:

```
std::transform(start, finish, result, op);  
std::transform(start, finish, start2, result, op);
```

```
std::transform(start, finish, start2, start3, result, op);
```

# Why zip\_iterator?

---

Consider std::transform:

```
std::transform(start, finish, result, op);  
std::transform(start, finish, start2, result, op);
```

```
std::transform(start, finish, start2, start3, result, op);  
std::transform(start, finish, start2, start3, start4, result, op);  
std::transform(start, finish, start2, start3, start4, start5, result, op);
```

# Why zip\_iterator?

---

Consider std::transform:

```
std::transform(start, finish, result, op);  
std::transform(start, finish, start2, result, op);
```

```
std::transform(start, finish, start2, start3, result, op);  
std::transform(start, finish, start2, start3, start4, result, op);  
std::transform(start, finish, start2, start3, start4, start5, result, op);  
std::transform(start, finish, start2, start3, start4, start5, start6, result, op);
```

# Why zip\_iterator?

---

Consider std::transform:

```
std::transform(start, finish, result, op);  
std::transform(start, finish, start2, result, op);
```

```
std::transform(start, finish, start2, start3, result, op);  
std::transform(start, finish, start2, start3, start4, result, op);  
std::transform(start, finish, start2, start3, start4, start5, result, op);  
std::transform(start, finish, start2, start3, start4, start5, start6, result, op);  
std::transform(start, finish, start2, start3, start4, start5, start6, start7, result, op);
```

# Why zip\_iterator?

---

Consider std::transform:

```
std::transform(start, finish, result, op);  
std::transform(start, finish, start2, result, op);
```

```
std::transform(start, finish, start2, start3, result, op);  
std::transform(start, finish, start2, start3, start4, result, op);  
std::transform(start, finish, start2, start3, start4, start5, result, op);  
std::transform(start, finish, start2, start3, start4, start5, start6, result, op);  
std::transform(start, finish, start2, start3, start4, start5, start6, start7, result, op);  
std::transform(start, finish, start2, start3, start4, start5, start6, start7, start8, result, op);
```

# Why zip\_iterator?

---

Consider std::transform:

```
std::transform(start, finish, result, op);  
std::transform(start, finish, start2, result, op);
```

```
std::transform(start, finish, start2, start3, result, op);  
std::transform(start, finish, start2, start3, start4, result, op);  
std::transform(start, finish, start2, start3, start4, start5, result, op);  
std::transform(start, finish, start2, start3, start4, start5, start6, result, op);  
std::transform(start, finish, start2, start3, start4, start5, start6, start7, result, op);  
std::transform(start, finish, start2, start3, start4, start5, start6, start7, start8, result, op);
```

# Why zip\_iterator?

---

Consider std::transform:

```
std::transform(start, finish, result, op);  
std::transform(start, finish, start2, result, op);
```

```
std::transform(start, finish, start2, start3, result, op);  
std::transform(start, finish, start2, start3, start4, result, op);  
std::transform(start, finish, start2, start3, start4, start5, result, op);  
std::transform(start, finish, start2, start3, start4, start5, start6, result, op);  
std::transform(start, finish, start2, start3, start4, start5, start6, start7, result, op);  
std::transform(start, finish, start2, start3, start4, start5, start6, start7, start8, result, op);
```

At some point, you want to generalize back to:

# Why zip\_iterator?

---

Consider std::transform:

```
std::transform(start, finish, result, op);  
std::transform(start, finish, start2, result, op);
```

```
std::transform(start, finish, start2, start3, result, op);  
std::transform(start, finish, start2, start3, start4, result, op);  
std::transform(start, finish, start2, start3, start4, start5, result, op);  
std::transform(start, finish, start2, start3, start4, start5, start6, result, op);  
std::transform(start, finish, start2, start3, start4, start5, start6, start7, result, op);  
std::transform(start, finish, start2, start3, start4, start5, start6, start7, start8, result, op);
```

At some point, you want to generalize back to:

# Why zip\_iterator?

---

Consider std::transform:

```
std::transform(start, finish, result, op);  
std::transform(start, finish, start2, result, op);
```

```
std::transform(start, finish, start2, start3, result, op);  
std::transform(start, finish, start2, start3, start4, result, op);  
std::transform(start, finish, start2, start3, start4, start5, result, op);  
std::transform(start, finish, start2, start3, start4, start5, start6, result, op);  
std::transform(start, finish, start2, start3, start4, start5, start6, start7, result, op);  
std::transform(start, finish, start2, start3, start4, start5, start6, start7, start8, result, op);
```

At some point, you want to generalize back to:

```
std::transform(zip_start, zip_finish, result, op);
```

# From zip\_iterator's Implementation

```
struct increment
```

```
{  
    template<typename T>  
    void operator()(T& x) const  
    { ++x; }  
};  
  
template <class IteratorTuple>  
zip_iterator<IteratorTuple>::operator++()  
{  
    fusion::for_each(this->m_iterators, increment());  
};
```

# From zip\_iterator's Implementation

---



# From zip\_iterator's Implementation

---

```
template <class IteratorTuple>
zip_iterator<IteratorTuple>::operator++()
{
    using namespace boost::lambda;
    fusion::for_each( this->m_iterators, ++_1 );
};
```

01/17/11

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# Implementing Dereference

```
struct deref
{
    // return type computation
    template<typename Iterator>
    struct result
    {
        typedef typename
        std::iterator_traits<
            Iterator
        >::reference type;
    };

    // runtime function call
    template<typename Iter>
    typename result<Iter>::type
    operator()(Iter const& it)
    const
    01/17/11
```

```
template <class IteratorTuple>
struct zip_iterator
{
    typedef typename
    mpl::transform<
        IteratorTuple
        , deref::apply<mpl::_1>
    >::type reference;

    reference operator*() const
    {
        return fusion::transform(
            this->m_iterators
            , deref()
        );
    }

    ...
    IteratorTuple m_iterators;
};
```

# Fusion Tuple

---



# Fusion Tuple

---

- Merges pure type manipulation and runtime computation



# Fusion Tuple

---

- Merges pure type manipulation and runtime computation



# Fusion Tuple

---

- Merges pure type manipulation and runtime computation
- Makes manipulation of heterogeneous collections easy



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# Fusion Tuple

---

- Merges pure type manipulation and runtime computation
- Makes manipulation of heterogeneous collections easy
- Interoperates seamlessly with MPL



# Fusion Tuple

---

- Merges pure type manipulation and runtime computation
- Makes manipulation of heterogeneous collections easy
- Interoperates seamlessly with MPL



# Fusion Tuple

---

- Merges pure type manipulation and runtime computation
- Makes manipulation of heterogeneous collections easy
- Interoperates seamlessly with MPL
- A floor wax and a dessert topping.



# Preprocessor

---

- The preprocessor is a text generator

```
#define FOO(x) foo x
```

FOO(bar) → foo bar

- You can program it
- What if you use it to generate C++ program text?



# Preprocessor Abstractions

---

- preprocessing token
- 2 kinds of macros
  - object-like: `#define X y`
  - function-like `#define FOO(x) foo x`
- macro argument
  - Sequence of preprocessing tokens
  - All parens are balanced
  - No commas outside of parens

# Problem: Generate Overload

```
tuple<> make_tuple()  
{ return tuple<>(); }
```

```
template <class A0>  
tuple<A0> make_tuple(A0 x0)  
{ return tuple<A0>(x0); }
```

```
template <class A0, class A1>  
tuple<A0,A1> make_tuple(A0 x0, A1 x1)  
{ return tuple<A0,A1>(x0,x1); }
```

```
template <class A0, class A1, class A3>  
tuple<A0,A1> make_tuple(A0 x0, A1 x1, A3 x3)  
{ return tuple<A0,A1,A3>(x0,x1,x3); }
```

```
template <class A0, class A1, class A3, class A4>  
tuple<A0,A1> make_tuple(A0 x0, A1 x1, A3 x3, A4 x4)  
{ return tuple<A0,A1,A3,A4>(x0,x1,x3,x4); }
```

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# Boost.Preprocessor Solution

```
tuple<> make_tuple()  
{ return tuple<>(); }
```

```
#define FUSION_make_tuple(z, n, unused)           \
template < BOOST_PP_ENUM_PARAMS(n, class A) >      \
tuple< BOOST_PP_ENUM_PARAMS(n, A) >                \
make_tuple( BOOST_PP_ENUM_BINARY_PARAMS(n, A, x ) ) \
{                                                     \
    return tuple< BOOST_PP_ENUM_PARAMS(n, A) >(      \
        BOOST_PP_ENUM_PARAMS(n, x)                   \
    );                                                 \
}
```

```
BOOST_PP_REPEAT_FROM_TO(  
    1, FUSION_MAX_SIZE, FUSION_make_tuple, ~)
```

# Boost.Preprocessor Solution

```
tuple<> make_tuple()  
{ return tuple<>(); }
```

```
#define FUSION_make_tuple(z, n, unused)           \
template < class A0, class A1, class A2, class A3 > \
tuple< BOOST_PP_ENUM_PARAMS(n, A) >               \
make_tuple( BOOST_PP_ENUM_BINARY_PARAMS(n, A, x) )  \
{                                                    \
    return tuple< BOOST_PP_ENUM_PARAMS(n, A) >(      \
        BOOST_PP_ENUM_PARAMS(n, x)                   \
    );                                              \
}
```

```
BOOST_PP_REPEAT_FROM_TO(  
    1, FUSION_MAX_SIZE, FUSION_make_tuple, ~)
```

# Boost.Preprocessor Solution

```
tuple<> make_tuple()  
{ return tuple<>(); }
```

```
#define FUSION_make_tuple(z, n, unused)           \
template < class A0, class A1, class A2, class A3 > \
tuple< A0, A1, A2, A3 >                         \
make_tuple( BOOST_PP_ENUM_BINARY_PARAMS(n, A, x) )  \
{                                                    \
    return tuple< BOOST_PP_ENUM_PARAMS(n, A) >(      \
        BOOST_PP_ENUM_PARAMS(n, x)                   \
    );                                              \
}
```

```
BOOST_PP_REPEAT_FROM_TO(  
    1, FUSION_MAX_SIZE, FUSION_make_tuple, ~)
```

# Boost.Preprocessor Solution

```
tuple<> make_tuple()  
{ return tuple<>(); }
```

```
#define FUSION_make_tuple(z, n, unused)           \
template < class A0, class A1, class A2, class A3 > \
tuple< A0, A1, A2, A3 >                         \
make_tuple( A0 x0, A1 x1, A2 x2, A3 x3 )        \
{                                                    \
    return tuple< BOOST_PP_ENUM_PARAMS(n, A) >(   \
        BOOST_PP_ENUM_PARAMS(n, x)                  \
    );                                              \
}
```

```
BOOST_PP_REPEAT_FROM_TO(  
    1, FUSION_MAX_SIZE, FUSION_make_tuple, ~)
```

# Boost.Preprocessor Solution

```
tuple<> make_tuple()  
{ return tuple<>(); }
```

```
#define FUSION_make_tuple(z, n, unused)           \
template < class A0, class A1, class A2, class A3 > \
tuple< A0, A1, A2, A3 >                         \
make_tuple( A0 x0, A1 x1, A2 x2, A3 x3 )         \
{                                                    \
    return tuple< A0, A1, A2, A3 >(               \
        x0, x1, x2, x3                           \
    );                                              \
}
```

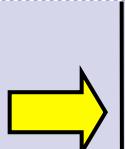
```
BOOST_PP_REPEAT_FROM_TO(  
    1, FUSION_MAX_SIZE, FUSION_make_tuple, ~)
```

# What About Debuggability?

- A macro expansion never contains line breaks – “horizontal repetition”
- All `make_tuple` overloads ultimately generated by a single `BOOST_PP_REPEAT`
- Resulting code all generated on that line

```
template <class A0> tuple<A0> make_tuple(A0 x0) { return tuple<A0>(x0); } template <class A0, class A1> ...
```

- Stepping through `make_tuple` in debugger



```
BOOST_PP_REPEAT_FROM_TO(  
    1, FUSION_MAX_SIZE, FUSION_make_tuple, ~)
```

# Vertical Repetition

```
#ifndef FUSION_MAKE_TUPLE_HPP // #include guard
#define FUSION_MAKE_TUPLE_HPP

tuple<> make_tuple() { return tuple<>(); }

#define BOOST_PP_ITERATION_LIMITS ( 1, FUSION_MAX_SIZE - 1 )
#define BOOST_PP_FILENAME_1 "make_tuple_overload.hpp"
#include BOOST_PP_ITERATE()
-----
#endif // FUSION_MAKE_TUPLE_HPP

// make_tuple_overload.hpp
#define n BOOST_PP_ITERATION()
template < BOOST_PP_ENUM_PARAMS(n, class A) >
tuple< BOOST_PP_ENUM_PARAMS(n, A) >
make_tuple( BOOST_PP_ENUM_BINARY_PARAMS(n, A, x) )
{
    return tuple< BOOST_PP_FNUM_PARAMS(n, A) >(
```

# Vertical Repetition

```
#ifndef FUSION_MAKE_TUPLE_HPP      // #include guard
# define FUSION_MAKE_TUPLE_HPP

tuple<> make_tuple() { return tuple<>(); }

#define BOOST_PP_ITERATION_LIMITS ( 1, FUSION_MAX_SIZE - 1)
#define BOOST_PP_FILENAME_1 "make_tuple_overload.hpp"
#include BOOST_PP_ITERATE()
.....
#endif // FUSION_MAKE_TUPLE_HPP

// make_tuple_overload.hpp
#define n BOOST_PP_ITERATION()
template < BOOST_PP_ENUM_PARAMS(n, class A) >
tuple< BOOST_PP_ENUM_PARAMS(n, A) >
make_tuple( BOOST_PP_ENUM_BINARY_PARAMS(n, A, x ) )
{
    return tuple< BOOST_PP_ENUM_PARAMS(n, A) >(
```

# Self-Iteration

---

```
#ifndef BOOST_PP_IS_ITERATING
# ifndef FUSION_MAKE_TUPLE_HPP
#   define FUSION_MAKE_TUPLE_HPP
tuple<> make_tuple() { return tuple<>(); }

#define BOOST_PP_ITERATION_LIMITS( 1, FUSION_MAX_SIZE - 1)
#define BOOST_PP_FILENAME_1 "make_tuple_overload.hpp"
#include BOOST_PP_ITERATE()
# endif // FUSION_MAKE_TUPLE_HPP
#else
# define n BOOST_PP_ITERATION()

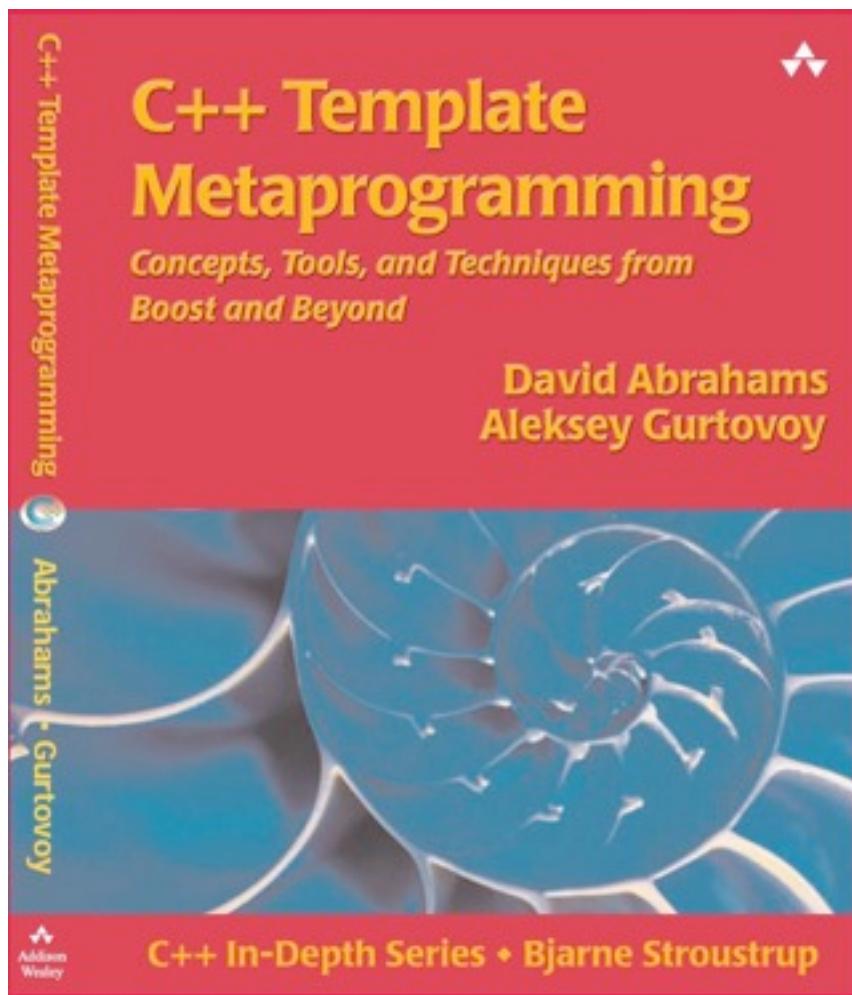
template < BOOST_PP_ENUM_PARAMS(n, class A) >
tuple< BOOST_PP_ENUM_PARAMS(n, A) >
make_tuple( BOOST_PP_ENUM_BINARY_PARAMS(n, A, x ) )
{
    return tuple< BOOST_PP_ENUM_PARAMS(n, A) >(
        BOOST_PP_ENUM_PARAMS(n, x))
```

# Other Boost.Preprocessor Facilities

---

- Sequences: `(foo bar)(baz)(1 + 2)`
- Sequence Algorithms:  
`BOOST_PP_SEQ_FOR_EACH( f, data, seq )`  
`BOOST_PP_SEQ_FOLD_LEFT( f, data, seq )`
- Token Arithmetic: `BOOST_PP_ADD(3, 4) → 7`
- Token Logic: `BOOST_PP_AND( 1, 0 ) → 0`
- Like MPL, Boost.Preprocessor is a complete programming system.

# Further Reading



- Erwin Unruh, Prime number computation. ANSI X3J16-94-0075/ISO WG21-462. 1994.
- Todd Veldhuizen. Using C++ Template Metaprograms, C++ Report, SIGS Publications Inc., ISSN 1040-6042, Vol. 7, No. 4, pp. 36-43. May 1995.
- Krzysztof Czarnecki, Ulrich Eisenecker, Metalisp. <http://home.t-online.de/home/Ulrich.Eisenecker/meta.htm>
- Todd Veldhuizen. Active Libraries and Universal Languages. Doctoral Dissertation, Indiana University Computer Science, 17 May 2004. <http://www.cs.chalmers.se/studium/papers/2004/dissertation.pdf>