

`resophonic::kamasu`

# Computing on the GPU with CUDA and boost::proto

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Washington, DC



# The Underpants Gnomes' Business Plan

1. Collect Underpants
2. ???
3. Profit



# The Kamasu Business Plan

1. Learn boost::proto
2. Learn CUDA
3. Combine
4. ???
5. Profit



# The Kamasu Business Plan

1. Learn boost::proto
2. Learn CUDA
3. Combine
4. ??? <- **You are here**
5. Profit



# Outline

---

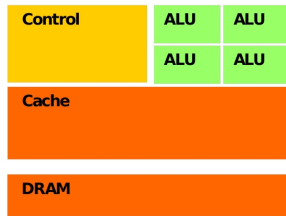
CUDA

boost::proto  
transforms

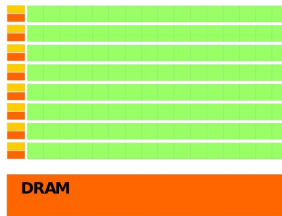
Related efforts

resophonic::kamasu  
benchmarks

# The GPU vs the CPU

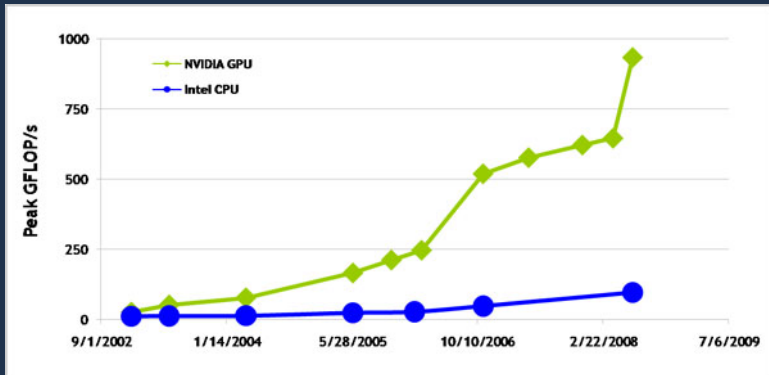


**CPU**



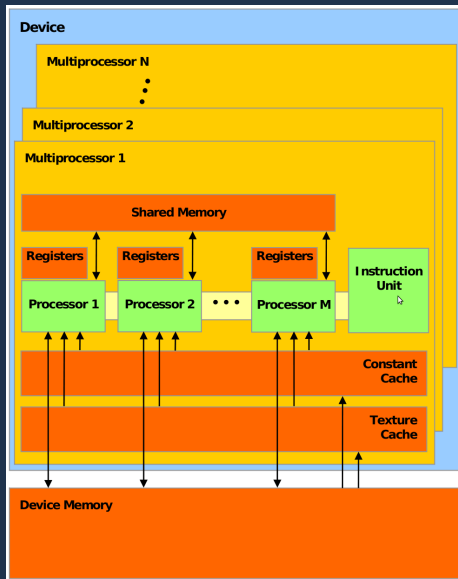
**GPU**

# The GPU vs the CPU



(image courtesy of NVIDIA)

# The GPU





# Building software to run on the gpu

- ▶ “C for CUDA” is (soon C++) with extensions
- ▶ Mix device and host code (and both code)
- ▶ Run the file through NVCC
- ▶ compile the result with gcc, compiled CUDA code is linked into the binary

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## Serially adding a scalar to an array

```
void add(float* data, unsigned size,  
         float scalar)  
{  
    for(unsigned i=0; i<size; i++)  
        data[i] += scalar;  
}
```

## Adding a scalar to an array in cuda-parallel

```
__global__ void  
add(float *data, float scalar)  
{  
    data[threadIdx.x] += scalar;  
}
```

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## Adding a scalar to an array in cuda-parallel

```
__global__ void
add(float *data, float scalar)
{
    data[threadIdx.x] += scalar;
}

int main() {
    int N = 256;
    float *arr = make_vector_on_gpu(N);

    add<<<1, N>>>(arr, 3.14159);
}
```

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```

# CUDA Memory management

```
cudaError_t cudaMalloc(void** devPtr, size_t count );  
cudaError_t cudaFree(void* devPtr);
```

```
cudaError_t cudaMemcpy(void* dst, const void* src,  
                        size_t count,  
                        enum cudaMemcpyKind kind);
```

```
cudaMemcpyHostToHost  
cudaMemcpyHostToDevice  
cudaMemcpyDeviceToHost  
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```

```
cudaError_t cudaMemset(void* devPtr, int value,  
                        size_t count);
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## A holder class

```
template <typename T>
class holder : boost::noncopyable
{
    T* devmem;
    std::size_T size_;

public:

    holder();
    holder(std::size_t n);
    ~holder();
    boost::shared_ptr<holder> clone();
    void resize(std::size_t size);
    T* data() { return devmem; }
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    T* data() { return devmem; }
    std::size_t size() { return size_; }
};
```

## holder<T> implementations

```
template <typename T>
holder<T>::holder(std::size_t s) : size_(s)
{
    cudaMalloc(reinterpret_cast<void*>>(&devmem),
                size_ * sizeof(T));
}
```

```
template <typename T>
holder<T>::~~holder()
{
    if (devmem)
        cudaFree(devmem);
}
```

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```
template <typename T>
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template <typename T>
holder<T>::~~holder()
{
    if (devmem)
        cudaFree(devmem);
}
```

## holder<T> implementations

```
template <typename T>
boost::shared_ptr<holder<T> >
holder<T>::clone()
{
    boost::shared_ptr<holder> nh(new holder(size_));
    cudaMemcpy(devmem, nh->devmem,
               sizeof(T) * size_,
               cudaMemcpyDeviceToDevice);
    return nh;
}
```

## holder<T> implementations

```
template <typename T>
void
holder<T>::put(const T* hostmem, std::size_t s)
{
    if (s != size_)
        resize(s);
    cudaMemcpy(devmem, hostmem, s * sizeof(T),
               cudaMemcpyHostToDevice);
}
```

```
template <typename T>
void
holder<T>::get(T* hostmem)
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    cudaMemcpy(hostmem, devmem, size_ * sizeof(T),
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}
```



## numpy arrays

```
>>> a
array([[ 1.,  2.,  3.,  4.,  5.],
       [ 6.,  7.,  8.,  9., 10.],
       [11., 12., 13., 14., 15.],
       [16., 17., 18., 19., 20.]])
```

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```

```
>>> a[1,:]
array([ 6.,  7.,  8.,  9., 10.] )
```

```
>>> a[3,::-1]
array([20., 19., 18., 17., 16.] )
```

```
>>> a[:,1]
array([ 2.,  7., 12., 17.] )
```

## numpy arrays

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       [11., 12., 13., 14., 15.],
       [16., 17., 18., 19., 20.]])
```

```
>>> a[1:3, 1:4]
array([[ 7.,  8.,  9.],
       [12., 13., 14.]])
```

```
>>> a[2:0:-1, 3:0:-1]
array([[ 9.,  8.,  7.],
       [14., 13., 12.]])
```

## numpy arrays

```
>>> a
array([[ 1.,  2.,  3.,  4.,  5.],
       [ 6.,  7.,  8.,  9., 10.],
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>>> a[1:3, 1:4]
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```
>>> a[2:0:-1, 3:0:-1]
array([[ 9.,  8.,  7.],
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```

```
>>> b = a      # shares data
```

```
>>> b = a[:]    # copies data
```

## Kamasu arrays

```
using resophonic::kamasu::_;  
  
array<float> a(m,n)  
  
array<float> b = a(index_range(_,_), index_range(2));  
  
array<float> c = a(index_range(_,_, -1), index_range(_,_, -1));  
  
float f = c(0,0); // a(9,9)  
  
c = a;           // shares data  
c = a.copy()     // copies data
```



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float f = c(0,0); // a(9,9)  
  
c = a;           // shares data  
c = a.copy()    // copies data
```

## Kamasu array metadata

```
struct view_params {
    std::size_t dims[KAMASU_MAX_ARRAY_DIM];
    std::size_t factors[KAMASU_MAX_ARRAY_DIM];
    int strides[KAMASU_MAX_ARRAY_DIM];

    offset_t offset;
    std::size_t linear_size;
    unsigned nd;
};

template <typename T>
struct array_impl
{
    view_params vp;
    shared_ptr<holder<T> > data;
};
```

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struct view_params {  
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    std::size_t factors[KAMASU_MAX_ARRAY_DIM];  
    int strides[KAMASU_MAX_ARRAY_DIM];  
  
    offset_t offset;  
    std::size_t linear_size;  
    unsigned nd;  
};  
  
template <typename T>  
struct array_impl  
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    view_params vp;  
    shared_ptr<holder<T> > data;  
};
```

## To/from device transfer

```
namespace rk = resophonic::kamasu;
```

```
rk::array<float>          a, b;  
std::vector<float>        vec1(10), vec2(10);  
ublas::matrix<float, column_major> mat1(31,14), mat2(14,31);
```

```
a << vec1;  
b << vec2;  
a = rk::dot(a, b);  
a >> vec1;
```

```
a << mat1;  
b << mat2;
```

```
a = a * b;
```

```
a >> mat1;
```

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a << vec1;
b << vec2;
a = rk::dot(a, b);
a >> vec1;

a << mat1;
b << mat2;

a = a * b;

a >> mat1;
```



## To/from device transfer

```
namespace rk = resophonic::kamasu;

rk::array<float>                                a, b;
std::vector<float>                               vec1(10), vec2(10);
ublas::matrix<float, column_major> mat1(31,14), mat2(14,31);

a << vec1;
b << vec2;
a = rk::dot(a, b);
a >> vec1;

a << mat1;
b << mat2;

a = a * b;

a >> mat1;
```

## To/from device transfer

```
namespace rk = resophonic::kamasu;

rk::array<float>          a, b;
std::vector<float>        vec1(10), vec2(10);
ublas::matrix<float, column_major> mat1(31,14), mat2(14,31);

a << vec1;
b << vec2;
a = rk::dot(a, b);
a >> vec1;

a << mat1;
b << mat2;

a = a * b;

a >> mat1;
```

## To/from device transfer

```
namespace rk = resophonic::kamasu;

rk::array<float>          a, b;
std::vector<float>        vec1(10), vec2(10);
ublas::matrix<float, column_major> mat1(31,14), mat2(14,31);

a << vec1;
b << vec2;
a = rk::dot(a, b);
a >> vec1;

a << mat1;
b << mat2;

a = a * b;

a >> mat1;
```

## To/from device transfer

```
namespace rk = resophonic::kamasu;

rk::array<float>                                a, b;
std::vector<float>                               vec1(10), vec2(10);
ublas::matrix<float, column_major> mat1(31,14), mat2(14,31);

a << vec1;
b << vec2;
a = rk::dot(a, b);
a >> vec1;

a << mat1;
b << mat2;

a = a * b;

a >> mat1;
```

## To/from device transfer

```
namespace rk = resophonic::kamasu;

rk::array<float>          a, b;
std::vector<float>        vec1(10), vec2(10);
ublas::matrix<float, column_major> mat1(31,14), mat2(14,31);

a << vec1;
b << vec2;
a = rk::dot(a, b);
a >> vec1;

a << mat1;
b << mat2;

a = a * b; // calls CUBLAS sgemm()

a >> mat1;
```

## To/from device transfer

```
namespace rk = resophonic::kamasu;

rk::array<float>          a, b;
std::vector<float>        vec1(10), vec2(10);
ublas::matrix<float, column_major> mat1(31,14), mat2(14,31);

a << vec1;
b << vec2;
a = rk::dot(a, b);
a >> vec1;

a << mat1;
b << mat2;

a = a * b;

a >> mat1;
```

## Conventional greedy “old politics”

```
rk::array<float> operator+(const rk::array<float>& a, float f)  
  
rk::array<float> a(10), b(10);  
a = b + 7.0f;
```

## Conventional greedy “old politics”

```
rk::array<float> operator+(const rk::array<float>& a, float f)  
  
rk::array<float> a(10), b(10);  
a = b + 7.0f;
```



b + 7.0f;

```
expr<
  tag::plus,
  list2<
    expr<
      tag::terminal,
      array<float> const&,
    >,
    expr<
      tag::terminal,
      float const&,
    >
  >,
>
```

b + 7.0f;

```
expr<
  tag::plus,
  list2<
    expr<
      tag::terminal,
      array<float> const&,
    >,
    expr<
      tag::terminal,
      float const&,
    >
  >,
>
```

b + 7.0f;

```
expr<
  tag::plus,
  list2<
    expr<
      tag::terminal,
      array<float> const&,
    >,
    expr<
      tag::terminal,
      float const&,
    >
  >,
>
```

**b** + 7.0f;

```
expr<
  tag::plus,
  list2<
    expr<
      tag::terminal,
      array<float> const&,
    >,
    expr<
      tag::terminal,
      float const&,
    >
  >,
>
```

**b** + 7.0f;

```
expr<
  tag::plus,
  list2<
    expr<
      tag::terminal,
      array<float> const&,
    >,
    expr<
      tag::terminal,
      float const&,
    >
  >,
>
```

**b** + 7.0f;

```
expr<
  tag::plus,
  list2<
    expr<
      tag::terminal,
      array<float> const&,
    >,
    expr<
      tag::terminal,
      float const&,
    >
  >,
>
```

**b** + 7.0f;

```
expr<
  tag::plus,
  list2<
    expr<
      tag::terminal,
      array<float> const&,
    >,
    expr<
      tag::terminal,
      float const&,
    >
  >,
>
```

b + 7.0f;

```
expr<
  tag::plus,
  list2<
    expr<
      tag::terminal,
      array<float> const&,
    >,
    expr<
      tag::terminal,
      float const&,
    >
  >,
>
```



b + 7.0f;

```
expr<
  tag::plus,
  list2<
    expr<
      tag::terminal,
      array<float> const&,
    >,
    expr<
      tag::terminal,
      float const&,
    >
  >,
>
```

b + 7.0f;

```
expr<
  tag::plus,
  list2<
    expr<
      tag::terminal,
      array<float> const&,
    >,
    expr<
      tag::terminal,
      float const&,
    >
  >,
>
```

b + 7.0f;

```
expr<
  tag::plus,
  list2<
    expr<
      tag::terminal,
      array<float> const&,
    >,
    expr<
      tag::terminal,
      float const&,
    >
  >,
>
```

b + 7.0f;

```
boost::proto::exprns_::expr<
  boost::proto::tag::plus,
  boost::proto::argsns_::list2<
    boost::proto::exprns_::expr<
      boost::proto::tag::terminal,
      boost::proto::argsns_::term<array<float> >,
      0
    >,
    boost::proto::exprns_::expr<
      boost::proto::tag::terminal,
      boost::proto::argsns_::term<int const&>,
      0
    >
  >,
  2
>
```

b + 7.0f;

```
exprns_::expr<
  tag::plus,
  argsns_::list2<
    exprns_::expr<
      tag::terminal,
      argsns_::term<array<float> >,
      0
    >,
    exprns_::expr<
      tag::terminal,
      argsns_::term<int const&>,
      0
    >
  >,
  2
>
```

b + 7.0f;

```
expr<
  tag::plus,
  list2<
    expr<
      tag::terminal,
      term<array<float> >,
      0
    >,
    expr<
      tag::terminal,
      term<int const&>,
      0
    >
  >,
  2
>
```

b + 7.0f;

```
expr<
  tag::plus,
  list2<
    expr<
      tag::terminal,
      term<array<float> >,
      0
    >,
    expr<
      tag::terminal,
      term<int const&>,
      0
    >
  >,
  2
>
```

b + 7.0f;

```
expr<
  tag::plus,
  list2<
    expr<
      tag::terminal,
      term<array<float> >,
      0    // arity
    >,
    expr<
      tag::terminal,
      term<int const&>,
      0
    >
  >,
  2
>
```



b + 7.0f;

```
expr<
  tag::plus,
  list2<
    expr<
      tag::terminal,
      term<array<float> >,
      0
    >,
    expr<
      tag::terminal,
      term<int const&>,
      0
    >
  >,
  2
>
```

## an array is an expression

```
proto::exprns_::expr<
  proto::tag::terminal,
  proto::argsns_::term<T>,
  0
>
```

```
proto::terminal<T>::type
```

```
namespace bp = boost::proto;
```

```
template <typename T>
struct array_impl { /* data goes here */ };
```

```
template <typename T>
struct array : proto::terminal<array_impl<T> >::type
{ ... };
```

## an array is an expression

```
proto::exprns_::expr<
  proto::tag::terminal,
  proto::argsns_::term<T>,
  0
>
```

```
proto::terminal<T>::type
```

```
namespace bp = boost::proto;
```

```
template <typename T>
struct array_impl { /* data goes here */ };
```

```
template <typename T>
struct array : proto::terminal<array_impl<T> >::type
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```

## an array is an expression

```
proto::exprns_::expr<
  proto::tag::terminal,
  proto::argsns_::term<T>,
  0
>
```

```
proto::terminal<T>::type
```

```
namespace bp = boost::proto;
```

```
template <typename T>
struct array_impl { /* data goes here */ };
```

```
template <typename T>
struct array : proto::terminal<array_impl<T> >::type
{ ... };
```

## an array is an expression

```
proto::exprns_::expr<
  proto::tag::terminal,
  proto::argsns_::term<T>,
  0
>
```

```
proto::terminal<T>::type
```

```
namespace bp = boost::proto;
```

```
template <typename T>
struct array_impl { /* data goes here */ };
```

```
template <typename T>
struct array : proto::terminal<array_impl<T> >::type
{ ... };
```

## an array is an expression

```
proto::exprns_::expr<
  proto::tag::terminal,
  proto::argsns_::term<T>,
  0
>
```

```
proto::terminal<T>::type
```

```
namespace bp = boost::proto;
```

```
template <typename T>
struct array_impl { /* data goes here */ };
```

```
template <typename T>
struct array : proto::terminal<array_impl<T> >::type
{ ... };
```

## an array is an expression

```
proto::exprns_::expr<
  proto::tag::terminal,
  proto::argsns_::term<T>,
  0
>
```

**proto::terminal<T>::type**

```
namespace bp = boost::proto;
```

```
template <typename T>
struct array_impl { /* data goes here */ };
```

```
template <typename T>
struct array : proto::terminal<array_impl<T> >::type
{ ... };
```

## an array is an expression

```
proto::exprns_::expr<
  proto::tag::terminal,
  proto::argsns_::term<T>,
  0
>
```

```
proto::terminal<T>::type
```

```
namespace bp = boost::proto;
```

```
template <typename T>  
struct array_impl { /* data goes here */ };
```

```
template <typename T>  
struct array : proto::terminal<array_impl<T> >::type  
{ ... };
```



## an array is an expression

```
proto::exprns_::expr<
  proto::tag::terminal,
  proto::argsns_::term<T>,
  0
>
```

```
proto::terminal<T>::type
```

```
namespace bp = boost::proto;
```

```
template <typename T>
struct array_impl { /* data goes here */ };
```

```
template <typename T>
struct array : proto::terminal<array_impl<T> >::type
{ ... };
```

# Hello World

```
struct array_impl { };

struct array : bp::terminal<array_impl>::type
{
    template <typename Expr>
    void operator=(const Expr& expr)
    {
        std::cout << name_of(expr);
    }
};

array a, b;
a = b + 7.0f;

boost::proto::exprns_::expr<boost::proto::tag::plus,
boost::proto::argsns_::list2<array&, boost::proto::e
xprns_::expr<boost::proto::tag::terminal, boost::pro
to::argsns_::term<float const&>, 0l> >, 2l>
```

# Hello World

```
struct array_impl { };

struct array : bp::terminal<array_impl>::type
{
    template <typename Expr>
    void operator=(const Expr& expr)
    {
        std::cout << name_of(expr);
    }
};

array a, b;
a = b + 7.0f;

boost::proto::exprns_::expr<boost::proto::tag::plus,
boost::proto::argsns_::list2<array&, boost::proto::e
xprns_::expr<boost::proto::tag::terminal, boost::pro
to::argsns_::term<float const&>, 0l> >, 2l>
```

# Hello World

```
struct array_impl { };

struct array : bp::terminal<array_impl>::type
{
    template <typename Expr>
    void operator=(const Expr& expr)
    {
        std::cout << name_of(expr);
    }
};

array a, b;
a = b + 7.0f;

boost::proto::exprns_::expr<boost::proto::tag::plus,
boost::proto::argsns_::list2<array&, boost::proto::e
xprns_::expr<boost::proto::tag::terminal, boost::pro
to::argsns_::term<float const>, 0l> >, 2l>
```

# Hello World

```
struct array_impl { };

struct array : bp::terminal<array_impl>::type
{
    template <typename Expr>
    void operator=(const Expr& expr)
    {
        std::cout << name_of(expr);
    }
};

array a, b;
a = b + 7.0f;

boost::proto::exprns_::expr<boost::proto::tag::plus,
boost::proto::argsns_::list2<array&, boost::proto::e
xprns_::expr<boost::proto::tag::terminal, boost::pro
to::argsns_::term<float const&>, 01> >, 21>
```

## display\_expr

```
std::ostream& operator<<(std::ostream& s, array_impl)
{
    return s << "array_impl";
}
```

```
struct array : bp::terminal<array_impl>::type
{
    template <typename Expr>
    void operator=(const Expr& expr)
    {
        std::cout << bp::display_expr(expr);
    }
};
```

```
array a, b;
a = b + 7.0f;
```

## display\_expr

```
std::ostream& operator<<(std::ostream& s, array_impl)
{
    return s << "array_impl";
}
```

```
struct array : bp::terminal<array_impl>::type
{
    template <typename Expr>
    void operator=(const Expr& expr)
    {
        std::cout << bp::display_expr(expr);
    }
};
```

```
array a, b;
a = b + 7.0f;
```

## display\_expr

```
std::ostream& operator<<(std::ostream& s, array_impl)
{
    return s << "array_impl";
}
```

```
struct array : bp::terminal<array_impl>::type
{
    template <typename Expr>
    void operator=(const Expr& expr)
    {
        std::cout << bp::display_expr(expr);
    }
};
```

```
array a, b;
a = b + 7.0f;
```



## display\_expr

```
std::ostream& operator<<(std::ostream& s, array_impl)
{
    return s << "array_impl";
}
```

```
struct array : bp::terminal<array_impl>::type
{
    template <typename Expr>
    void operator=(const Expr& expr)
    {
        std::cout << bp::display_expr(expr);
    }
};
```

```
array a, b;
a = b + 7.0f;
```

## display\_expr

```
std::ostream& operator<<(std::ostream& s, array_impl)
{
    return s << "array_impl";
}
```

```
struct array : bp::terminal<array_impl>::type
{
    template <typename Expr>
    void operator=(const Expr& expr)
    {
        std::cout << bp::display_expr(expr);
    }
};
```

```
array a, b;
a = b + 7.0f;
```

## display\_expr

```
std::ostream& operator<<(std::ostream& s, array_impl)
{
    return s << "array_impl";
}
```

```
struct array : bp::terminal<array_impl>::type
{
    template <typename Expr>
    void operator=(const Expr& expr)
    {
        std::cout << bp::display_expr(expr);
    }
};
```

```
array a, b;
a = b + 7.0f;
```

```
plus(
    terminal(array_impl)
    , terminal(7)
)
```

# Operator tags

```
namespace boost {  
  namespace proto {  
    namespace tag {  
      struct terminal;  
      struct unary_plus;  
      struct negate;  
      struct dereference;  
      struct complement;  
      struct address_of;  
      struct logical_not;  
      struct pre_inc;  
      struct pre_dec;  
      struct post_inc;  
      struct post_dec;  
      struct shift_left;  
      struct shift_right;  
      struct multiplies;  
      struct divides;  
      struct modulus;
```

## Operator tags

```
namespace boost {  
    namespace proto {  
        namespace tag {  
            struct plus;  
            struct minus;  
            struct less;  
            struct greater;  
            struct less_equal;  
            struct greater_equal;  
            struct equal_to;  
            struct not_equal_to;  
            struct logical_or;  
            struct logical_and;  
            struct bitwise_and;  
            struct bitwise_or;  
            struct bitwise_xor;  
            struct comma;  
            struct mem_ptr;  
            struct assign;  
            struct shift_left_assign;
```

# Operator tags

```
namespace boost {  
  namespace proto {  
    namespace tag {  
      struct shift_right_assign;  
      struct multiplies_assign;  
      struct divides_assign;  
      struct modulus_assign;  
      struct plus_assign;  
      struct minus_assign;  
      struct bitwise_and_assign;  
      struct bitwise_or_assign;  
      struct bitwise_xor_assign;  
      struct subscript;  
      struct if_else_;  
      struct function;
```

# Operator Swine Flu

```
trespasser s, t;    array m, n;  
m = s & ~n >>= std::cout % m->*t;
```

```
shift_right_assign(  
    bitwise_and(  
        terminal(trespasser)  
        , complement(  
            terminal(array_impl)  
        )  
    )  
    , modulus(  
        terminal(0x607068)  
        , mem_ptr(  
            terminal(array_impl)  
            , terminal(trespasser)  
        )  
    )  
)
```

# Operator Swine Flu

```
trespasser s, t;    array m, n;  
m = s & ~n >>= std::cout % m->*t;
```

```
shift_right_assign(  
    bitwise_and(  
        terminal(trespasser)  
        , complement(  
            terminal(array_impl)  
        )  
    )  
    , modulus(  
        terminal(0x607068)  
        , mem_ptr(  
            terminal(array_impl)  
            , terminal(trespasser)  
        )  
    )  
)
```



# Operator Swine Flu

```
trespasser s, t;    array m, n;  
m = s & ~n >>= std::cout % m->*t;
```

```
shift_right_assign(  
    bitwise_and(  
        terminal(trespasser)  
        , complement(  
            terminal(array_impl)  
        )  
    )  
    , modulus(  
        terminal(0x607068)  
        , mem_ptr(  
            terminal(array_impl)  
            , terminal(trespasser)  
        )  
    )  
)
```

# Operator Swine Flu

```
trespasser s, t;    array m, n;  
m = s & ~n >>= std::cout % m->*t;
```

```
shift_right_assign(  
    bitwise_and(  
        terminal(trespasser)  
        , complement(  
            terminal(array_impl)  
        )  
    )  
    , modulus(  
        terminal(0x607068)  
        , mem_ptr(  
            terminal(array_impl)  
            , terminal(trespasser)  
        )  
    )  
)
```

# Operator Swine Flu

```
trespasser s, t;    array m, n;  
m = s & ~n >>= std::cout % m->*t;
```

```
shift_right_assign(  
    bitwise_and(  
        terminal(trespasser)  
        , complement(  
            terminal(array_impl)  
        )  
    )  
    , modulus(  
        terminal(0x607068)  
        , mem_ptr(  
            terminal(array_impl)  
            , terminal(trespasser)  
        )  
    )  
)
```

# Operator Swine Flu

```
trespasser s, t;    array m, n;  
m = s & ~n >>= std::cout % m->*t;
```

```
shift_right_assign(  
    bitwise_and(  
        terminal(trespasser)  
        , complement(  
            terminal(array_impl)  
        )  
    )  
    , modulus(  
        terminal(0x607068)  
        , mem_ptr(  
            terminal(array_impl)  
            , terminal(trespasser)  
        )  
    )  
)
```

# Operator Swine Flu

```
trespasser s, t;    array m, n;  
m = s & ~n >>= std::cout % m->*t;
```

```
shift_right_assign(  
    bitwise_and(  
        terminal(trespasser)  
        , complement(  
            terminal(array_impl)  
        )  
    )  
    , modulus(  
        terminal(0x607068)  
        , mem_ptr(  
            terminal(array_impl)  
            , terminal(trespasser)  
        )  
    )  
)
```

# Operator Swine Flu

```
trespasser s, t;    array m, n;  
m = s & ~n >>= std::cout % m->*t;
```

```
shift_right_assign(  
    bitwise_and(  
        terminal(trespasser)  
        , complement(  
            terminal(array_impl)  
        )  
    )  
    , modulus(  
        terminal(0x607068)  
        , mem_ptr(  
            terminal(array_impl)  
            , terminal(trespasser)  
        )  
    )  
)
```

# Operator Swine Flu

```
trespasser s, t;    array m, n;  
m = s & ~n >>= std::cout % m->*t;
```

```
shift_right_assign(  
    bitwise_and(  
        terminal(trespasser)  
        , complement(  
            terminal(array_impl)  
        )  
    )  
    , modulus(  
        terminal(0x607068)  
        , mem_ptr(  
            terminal(array_impl)  
            , terminal(trespasser)  
        )  
    )  
)
```

# Operator Swine Flu

```
trespasser s, t;    array m, n;  
m = s & ~n >>= std::cout % m->*t;
```

```
shift_right_assign(  
    bitwise_and(  
        terminal(trespasser)  
        , complement(  
            terminal(array_impl)  
        )  
    )  
    , modulus(  
        terminal(0x607068)  
        , mem_ptr(  
            terminal(array_impl)  
            , terminal(trespasser)  
        )  
    )  
)
```



# Operator Swine Flu

```
trespasser s, t;    array m, n;  
m = s & ~n >>= std::cout % m->*t;
```

```
shift_right_assign(  
    bitwise_and(  
        terminal(trespasser)  
        , complement(  
            terminal(array_impl)  
        )  
    )  
    , modulus(  
        terminal(0x607068)  
        , mem_ptr(  
            terminal(array_impl)  
            , terminal(trespasser)  
        )  
    )  
)
```

# Operator Swine Flu

```
trespasser s, t;    array m, n;  
m = s & ~n >>= std::cout % m->*t;
```

```
shift_right_assign(  
    bitwise_and(  
        terminal(trespasser)  
        , complement(  
            terminal(array_impl)  
        )  
    )  
    , modulus(  
        terminal(0x607068)  
        , mem_ptr(  
            terminal(array_impl)  
            , terminal(trespasser)  
        )  
    )  
)
```

# Transforms

```
struct array_impl { /* pointers, strides, etc. */ };  
struct array : bp::terminal<array_impl>::type  
{ /* ... */};
```

```
array a;
```

```
array_impl& aimpl =  
    a.child0;           // via base class' member  
    bp::value(a);        // free function  
    bp::_value()(a);     // instance of _value  
    bp::_child0()(a);    // instance of _child0  
    bp::child_c<0>(a);  
    bp::child<mpl::long_<0> >(a);  
    bp::_left()(a);      // instance of _left  
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```

# Transforms

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struct array_impl { /* pointers, strides, etc. */ };  
struct array : bp::terminal<array_impl>::type  
{ /* ... */};
```

**array a;**

```
array_impl& aimpl =  
    a.child0;           // via base class' member  
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{ /* ... */};
```

```
array a;
```

```
array_impl& aimpl =
```

```
    a.child0;           // via base class' member  
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```

## More transforms

```
struct array_impl { float value; };  
struct array : bp::terminal<array_impl>::type { ... };  
array t;
```

t + 2

```
expr<                                     plus(  
    tag::plus                             terminal(array_impl)  
, list2<                                , terminal(2)  
    array&                                )  
, expr<  
    tag::terminal  
    , term<int const>  
    , 0  
    >  
    >  
, 2  
>
```



## More transforms

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struct array_impl { float value; };  
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**t + 2**

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expr<                                     plus(  
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## More transforms

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struct array_impl { float value; };  
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, 2  
>
```

## More transforms

```
struct array_impl { float value; };  
struct array : bp::terminal<array_impl>::type { ... };  
array t;
```

**bp::display\_expr(t + 2)**

```
expr<                                     plus(  
    tag::plus                             terminal(array_impl)  
, list2<                                , terminal(2)  
    array&                                )  
, expr<  
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    , 0  
    >  
    >  
, 2  
>
```

## More transforms

```
struct array_impl { float value; };  
struct array : bp::terminal<array_impl>::type { ... };  
array t;
```

```
bp::display_expr(t + 2)
```

```
expr<  
    tag::plus  
, list2<  
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, expr<  
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    , term<int const&>  
    , 0  
    >  
    >  
, 2  
>
```

```
plus(  
    terminal(array_impl)  
    , terminal(2)  
)
```

## More transforms

```
struct array_impl { float value; };  
struct array : bp::terminal<array_impl>::type { ... };  
array t;
```

```
bp::display_expr(t + 2)
```

```
plus(  
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## More transforms

```
struct array_impl { float value; };  
struct array : bp::terminal<array_impl>::type { ... };  
array t;
```

```
bp::display_expr(bp::child1(t + 2))
```

```
terminal(2)
```

## More transforms

```
struct array_impl { float value; };  
struct array : bp::terminal<array_impl>::type { ... };  
array t;  
  
std::cout << bp::value(bp::child1(t + 2))
```

2

## More transforms

```
struct array_impl { float value; };
struct array : bp::terminal<array_impl>::type { ... };
array t;

bp::value(bp::right(bp::left(a++->* 7 /= 4)));

divides_assign(
    mem_ptr(
        post_inc(
            terminal(array_impl)
        )
        , terminal(7)
    )
    , terminal(4)
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## More transforms

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struct array_impl { float value; };  
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```



# Matching expressions A

```
struct Grammar
{
    : bp::terminal<array_impl<float> >,
};
```

```
template <typename Expr>
void
array::operator=(const Expr& expr)
{
    std::cout << bp::matches<Expr, Grammar>() << "\n";
}
```

```
m = n * 17.0f;    // prints '0'
m = n;           // prints '1'
```

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m = n * 17.0f;    // prints '0'
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## Matching expressions

```
struct Grammar
{
    : bp::or_(bp::terminal<array_impl<float> >,
              bp::terminal<float>,
              bp::plus<bp::terminal<array_impl<float> >,
                    bp::terminal<float> >
              >
    { };
```

```
template <typename Expr>
void
array::operator=(const Expr& expr)
{
    std::cout << bp::matches<Expr, Grammar>() << "\n";
}
```

```
m = s & ~m >>= std::cout % n->*t;    // prints '0'
m = n + 7.0f;                        // prints '1'
```

# Matching expressions

```
struct Grammar
    : bp::or_<bp::terminal<array_impl<float> >,
      bp::terminal<float>,
      bp::plus<bp::terminal<array_impl<float> >,
              bp::terminal<float> >
    >
{ };

template <typename Expr>
void
array::operator=(const Expr& expr)
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m = s & ~m >>= std::cout % n->*t;    // prints '0'
m = n + 7.0f;                        // prints '1'
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struct Grammar
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    : bp::or_(<bp::terminal<array_impl<float> >,
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              bp::plus<bp::terminal<array_impl<float> >,
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              >
    { };
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void
array::operator=(const Expr& expr)
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    std::cout << bp::matches<Expr, Grammar>() << "\n";
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template <typename Expr>
void
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}
```

```
m = s & ~m >= std::cout % n->*t;    // prints '0'
m = n + 7.0f;                      // prints '1'
```

## Matching expressions

```
struct Grammar
    : bp::or_<bp::terminal<array_impl<float> >,
              bp::terminal<float>,>
      bp::plus<bp::terminal<array_impl<float> >,>
              bp::terminal<float> >
    >
{ };

template <typename Expr>
void
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m = s & ~m >>= std::cout % n->*t;    // prints '0'
m = n + 7.0f;                      // prints '1'
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## Detecting invalid expressions

```
template <typename Expr>
void
array::operator=(const Expr& expr)
{
    // to come: do something with expr
}

m = s & ~m >>= std::cout % n->*t;
```

## Detecting invalid expressions

```
template <typename Expr>
typename enable_if<bp::matches<Expr, Grammar> >::type
array::operator=(const Expr& expr)
{
    // to come: do something with expr
}

m = s & ~m >>= std::cout % n->*t;
```

## Detecting invalid expressions

```
template <typename Expr>
typename enable_if<bp::matches<Expr, Grammar> >::type
array::operator=(const Expr& expr)
{
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```
m = s & ~m >>= std::cout % n->*t;
error: no match for 'operator=' in 'm = boost::proto::exprns_::operator>= [with Left = boost::proto::exprns_::expr<boost::proto::tag::bitwise_and, boost::proto::argsns_::list2<boost::proto::exprns_::expr<boost::proto::tag::terminal, boost::proto::argsns_::term<trespasser&>, 0l>, const boost::proto::exprns_::expr<boost::proto::tag::complement, boost::proto::argsns_::list1<boost::proto::exprns_::expr<bo...
```

## Detecting invalid expressions

```
template <typename Expr>
void
array::operator=(const Expr& expr)
{
    // to come: do something with expr
    BOOST_MPL_ASSERT( (bp::matches<Expr, Grammar>) );
}

m = s & ~m >>= std::cout % n->*t;
```

## Detecting invalid expressions

```
template <typename Expr>
void
array::operator=(const Expr& expr)
{
    // to come: do something with expr
    BOOST_MPL_ASSERT((bp::matches<Expr, Grammar>));
}

m = s & ~m >>= std::cout % n->*t;
error: no matching function for call to 'assertion_
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<boost::proto::exprns_::expr<boost::proto::tag::ter
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```



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mina .... proto::a>, 2l>, Grammar>::*****)'
```

## Quick reminder

```
int foo(double) { ... }  
  
boost::function<int(double)> foofn = foo;
```

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```
int foo(double) { ... }
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```
int foo(double) { ... }
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```
boost::function<int(double)> foofn = foo;
```

```
struct bar { };  
bar makebar() ...
```

```
bar();
```

```
boost::function<bar()> barfn = makebar;
```

## Quick reminder

```
int foo(double) { ... }
```

```
boost::function<int(double)> foofn = foo;
```

```
struct bar { };  
bar makebar() ...
```

```
bar();
```

```
boost::function<bar()> barfn = makebar;
```

## Quick reminder

```
int foo(double) { ... }  
  
boost::function<int(double)> foofn = foo;  
  
struct bar { };  
bar makebar() ...  
  
bar();  
  
boost::function<bar()> barfn = makebar;
```

## Activating a grammar

```
struct ToString : bp::callable
{
    typedef std::string result_type;

    template <typename T>
    result_type operator()(const T& t)
    {
        return str(boost::format("%s @ %p") % t % &t);
    }
};

struct FloatTerminal
    : bp::when<bp::terminal<float>, ToString(bp::_value)>
{ };

bp::terminal<float>::type f = { 3.14 };
std::cout << FloatTerminal()(f);
"3.14 @ 0x7fff0d839aa0"
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```

## proto::when

```
// a + 777.0f
```

```
struct ArrayTerminal
  : bp::when<bp::terminal<array_impl>, ToString(bp::_value)>
{ };

struct FloatTerminal
  : bp::when<bp::terminal<float>, ToString(bp::_value)>
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struct Grammar :
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          bp::when<bp::plus<bp::terminal<array_impl>,
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                          ToString(bp::_value(bp::_left)),
                          ToString(bp::_value(bp::_right)))>
  >
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    >  
{ };    // struct plus { };
```

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// a + 777.0f
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```

## They recurse!

```
// (a + 777.0f) + (61.0f + a)
```

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struct ArrayTerminal  
  : bp::when<bp::terminal<array_impl>, ToString(bp::_value)>  
{ };
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struct Grammar :  
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## They recurse!

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                        Grammar(bp::_right))>
  >
{ };
```

## Tune up the transform

```
struct ToString : bp::callable
{
    typedef std::string result_type;
    // ...
    result_type operator()(bp::tag::plus,
                           const std::string& lhs,
                           const std::string& rhs)
    {
        return str(boost::format("%s PLUS %s") % lhs % rhs );
    }
};

array a;

std::cout << Grammar()(a + 777);
"array_impl @ 0x7fffe0f3f11f PLUS 777 @ 0x7fffe0f3f10c"
```

## Tune up the transform

```
struct ToString : bp::callable
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    typedef std::string result_type;
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};

array a;

std::cout << Grammar()(a + 777);
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## Tune up the transform

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struct ToString : bp::callable
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    {
        return str(boost::format("%s PLUS %s") % lhs % rhs );
    }
};

array a;

std::cout << Grammar() (a + 777);
"array_impl @ 0x7fffe0f3f11f PLUS 777 @ 0x7fffe0f3f10c"
```

## Tune up the transform

```
struct ToString : bp::callable
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    {
        return str(boost::format("%s PLUS %s") % lhs % rhs );
    }
};

array a;

std::cout << Grammar() (a + 777);
"array_impl @ 0x7fffe0f3f11f PLUS 777 @ 0x7fffe0f3f10c"
```

# Kamasu hello world

```
namespace bp = boost::proto;
namespace rk = resophonic::kamasu;

rk::array<float> a(10,10), b(10,10), c;

c = (a / 3.0f) * (b / 7.0f);

struct Array
    : bp::when<bp::terminal<rk::array_impl<float> >,
              bp::_value>
{ };

struct Scalar
    : bp::when<bp::terminal<float>,
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struct Grammar
    : bp::or_<bp::when<bp::divides<Array, Scalar>,
        ArrayScalarOp(bp::tag::divides(),
            Array(bp::_left),
            Scalar(bp::_right))>,
        bp::when<bp::multiplies<Array, Array>,
            ArrayArrayOp(bp::tag::multiplies(),
                Array(bp::_left),
                Array(bp::_right))>
    >
{ };
```

## Kamasu hello world

```
namespace bp = boost::proto;
namespace rk = resophonic::kamasu;

rk::array<float> a(10,10), b(10,10), c;

c = (a / 3.0f) * (b / 7.0f);

struct Grammar
    : bp::or_  
      bp::when<bp::divides<Array, Scalar>,  
                ArrayScalarOp (bp::tag::divides(),  
                                Array(bp::_left),  
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      bp::when<bp::multiplies<Array, Array>,  
                ArrayArrayOp (bp::tag::multiplies(),  
                                Array(bp::_left),  
                                Array(bp::_right))>  
    >
{ };
```

## Kamasu hello world

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namespace bp = boost::proto;
namespace rk = resophonic::kamasu;

rk::array<float> a(10,10), b(10,10), c;

c = (a / 3.0f) * (b / 7.0f);

struct Grammar
    : bp::or_  
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                ArrayScalarOp(bp::tag::divides(),  
                              Array(bp::_left),  
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                ArrayArrayOp(bp::tag::multiplies(),  
                              Array(bp::_left),  
                              Array(bp::_right))>  
    >
{ };
```

## a / 7.0f: Array-Scalar Transform

```
struct ArrayScalarOp : bp::callable
{
    typedef rk::array_impl<float> result_type;

    template <typename Tag>
    result_type
    operator()(Tag, const rk::array_impl<float>& v,
               const float& f)
    {
        // hop across the compiler firewall
        transform<float, Tag>(v.data(), v.view_p(), scalar);
        return v;
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## a / 7.0f: calculate gridsize, call kernel

```
template <typename T, typename Tag>
void
transform(T* data, const view_params& vp, T scalar)
{
    bd_t bd = gridsize(vp.linear_size, 64);
    transform_knl<T, Tag><<<bd.first,
                                bd.second>>>(data + vp.offset,
                                              vp, scalar);
}
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}
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## out on the device

```
template <typename T, typename Tag>
__global__ void
transform_knl(T* data, view_params vp, T scalar)
{
    unsigned li = linear_index(threadIdx, /* ... etc */);
    if (li >= vp.linear_size) return;

    unsigned off = actual_index(li, vp.nd, vp.factors, vp.stride);

    op_impl_<T, Tag>::impl(data + off, scalar);
}

template <typename T>
struct op_impl_<T, boost::proto::tag::plus>
{
    static void impl(T* t, const T& scalar)
    {
        *t += scalar;
    }
};
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    {
        *t += scalar;
    }
};
```



## Historical curiosity

```
__global__ void
kamasu_elementwise_array_scalar_/*OP*/_/*N*/_knl
(float* data,
 unsigned linear_size,
 /*', '.join(['const std::size_t factor%d' % x for x in range(
 /*', '.join(['const int stride%d' % x for x in range(N)])*/,
 float scalar)
{
    if (INDEX >= linear_size)
        return;

    unsigned actual_index =
        /* ' + '.join(['INDEX/factor%d*stride%d' % (N-1, N-1)]
            + [' unsigned(INDEX %% factor%d)/factor%d*st
                % (n+1,n,n) for n in range(N-1)]) */;

    ...
}
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    ...
}
```

## Avoiding temporaries 1: emulating rvalues

```
// a = b * 3.0f / c * 4.0f;

struct CopyLValue : bp::callable
{
    typedef array_impl<float> result_type;

    result_type
    operator()(const array_impl<float>& a)
    {
        return a.clone();
    }
};

struct RkArrayTerminal
    : bp::when<bp::terminal<rk::array_impl<float> >,
              CopyLValue(bp::_value)>
{ };

struct Grammar : bp::or_<RkArrayTerminal, Scalar, ...
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## Avoiding temporaries 2: reuse the LHS

```
// a = sin(a);  
  
template <typename Expr>  
array<T>::operator=(Expr const& expr)  
{  
    array_impl<T> result = Grammar()(expr);  
    self_.copy_from(result);  
}
```

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## Avoiding temporaries 2: reuse the LHS

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// a = sin(a);
```

```
struct data_t { array_impl<float>* tmp; };
```

```
template <typename Expr>  
array<float>::operator=(Expr const& expr)  
{  
    data_t data; data.tmp = this->base_ptr();  
    array_impl<float> tmp = Grammar()(expr, bool(), data);  
    self_.copy_from(result);  
}
```

```
CopyLValue::result_type
```

```
CopyLValue::operator()(const array_impl<float>& a, data_t& data)  
{  
    if (data.tmp == &a) { data.tmp = 0; return a; }  
    else                 { return a.clone();      }  
}
```

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```

## komrade: norm of vector

```
template <typename T>
struct square {
    __host__ __device__
    T operator()(const T& x) const
    {
        return x * x;
    }
};
```

```
float x[4] = { 1.0, 2.0, 3.0, 4.0 };
komrade::device_vector<float> d_x(x, x + 4);
```

```
square<float>          unary_op;
komrade::plus<float>   binary_op;
float init = 0;
```

```
sqrt( komrade::transform_reduce(d_x.begin(), d_x.end(),
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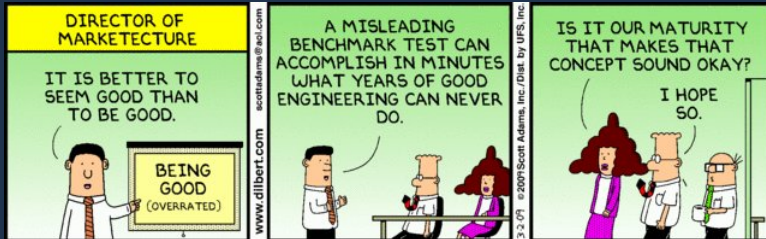
## PyCuda (Andreas Klöckner)

```
import pycuda.autoinit, pycuda.driver as drv, numpy

mod = drv.SourceModule("""
__global__ void multiply_them(float *dest, float *a, float *b)
{
    const int i = threadIdx.x;
    dest[i] = a[i] * b[i];
}
""")

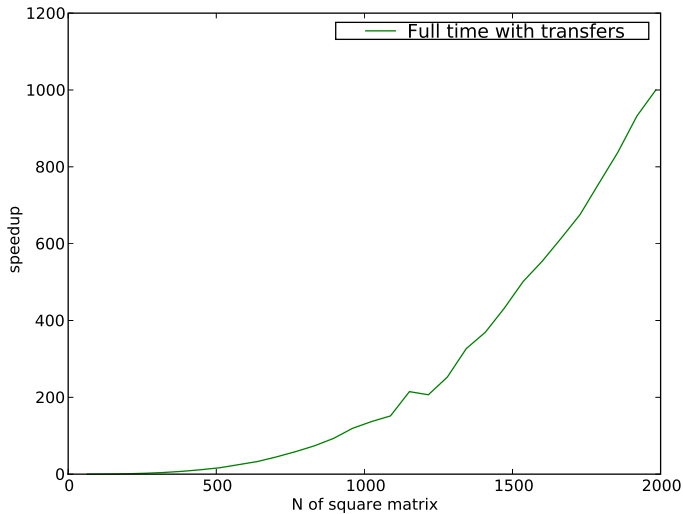
multiply_them = mod.get_function("multiply_them")
a = numpy.random.randn(400).astype(numpy.float32)
b = numpy.random.randn(400).astype(numpy.float32)
dest = numpy.zeros_like(a)
multiply_them(
    drv.Out(dest), drv.In(a), drv.In(b),
    block=(400,1,1))
print dest-a*b
```

# Benchmarks

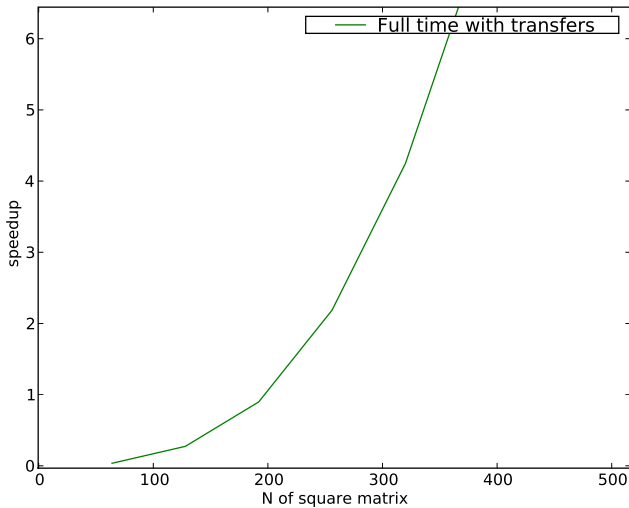




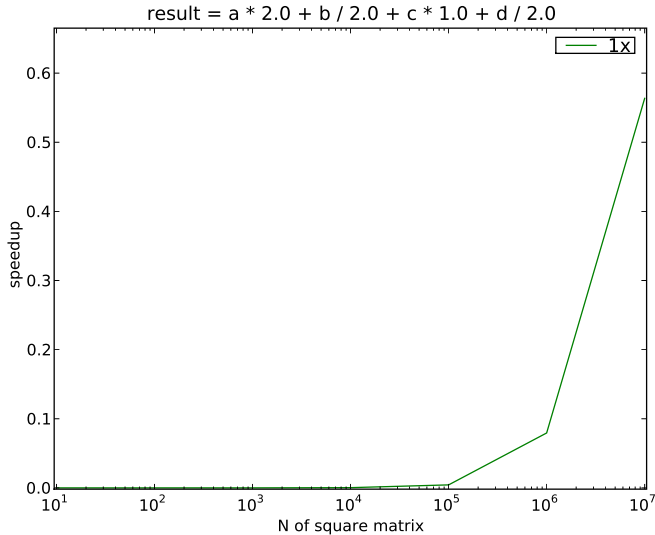
## NxN matrices, $A = B * C$ (via cublas)



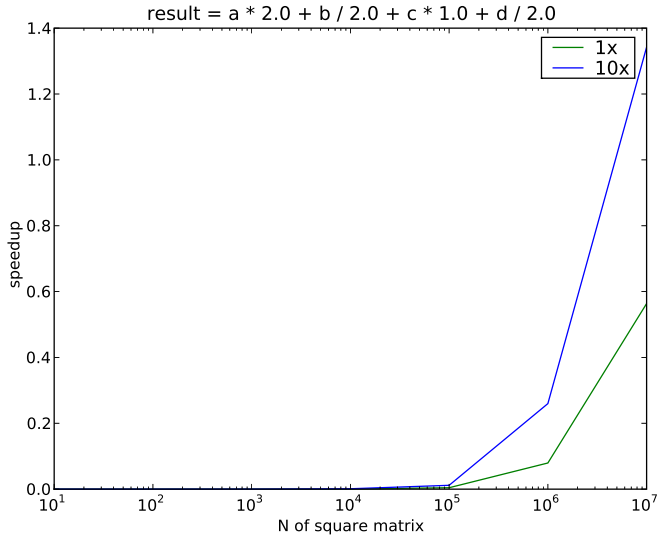
## Breakeven @ 200x200 matrices



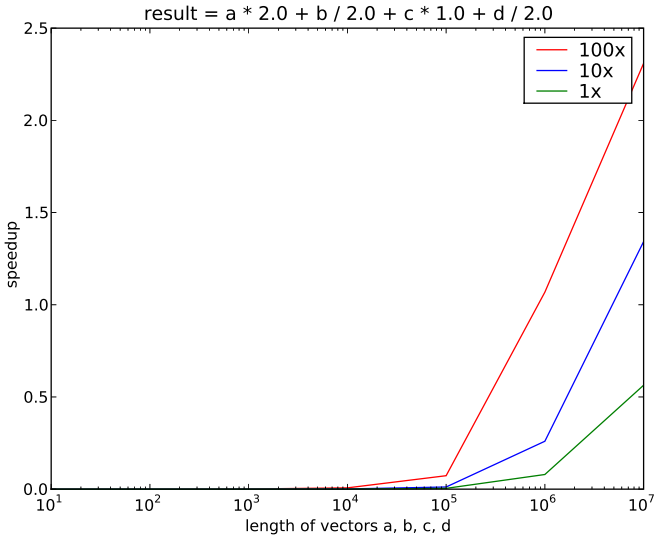
## Low numeric intensity == low performance



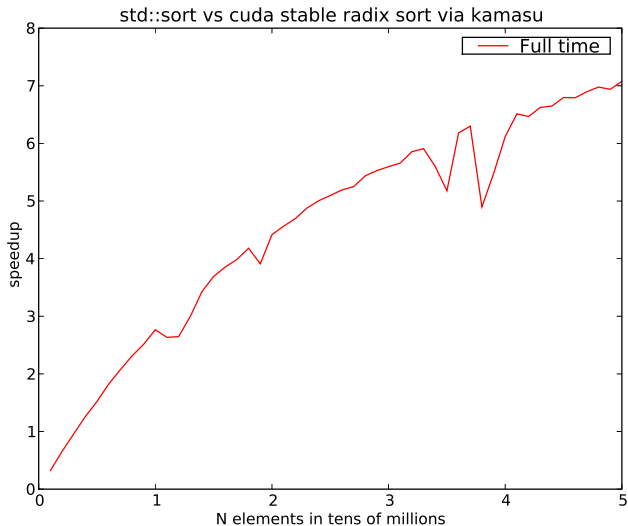
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## Sort – wall clock time including transfers



# Summary

- ▶ An n-dimensional array type with storage on the device
- ▶ Conversions for `boost::ublas` and `std::` types to/from the device
- ▶ A grammar for (very) basic linear algebra operations and some primitive functions
- ▶ Effort hamstrung to-date by previous version of CUDA compiler, NVIDIA appears to be making good progress
- ▶ Nonetheless possible to get a few interesting optimizations via proto
- ▶ Even if wallclock time is worse than a simple CPU implementation, you're still freeing up CPU cycles by moving to the GPU
- ▶ The big questions are granularity and composition (and "streaming")
- ▶ It needs a problem to solve
- ▶ Techniques available expected to expand rapidly soon

Questions?