

Top Down or Bottom Up

Jamal's trip requires him to drive 20mi to the airport, fly 2,300mi, and then take a bus 6mi to his hotel. His average speed driving to the airport is 40mph, the average speed of an airplane is 575mph, and the average speed of his bus is 15mph. Aside from time waiting for the plane or bus, how long is Jamal in transit?

Bear's Strategy:	Lion's Strategy:
$DriveTime = 20miles \times \frac{1hour}{40miles} = 0.5hours$	$In\ Transit\ Time = Drive\ Time + Fly\ Time + Bus\ Time$
$FlyTime = 2300miles \times \frac{1hour}{575miles} = 4hours$	$DriveTime = 20miles \times \frac{1hour}{40miles} = 0.5hours$
$BusTime = 6miles \times \frac{1hour}{15miles} = 0.4hours$	$FlyTime = 2300miles \times \frac{1hour}{575miles} = 4hours$
$In\ Transit\ Time = Drive\ Time + Fly\ Time + Bus\ Time$	$BusTime = 6miles \times \frac{1hour}{15miles} = 0.4hours$
$0.5 + 4 + 0.4 = 4.9\ hours$	$0.5 + 4 + 0.4 = 4.9\ hours$

1) Whose Strategy was Top Down? How do you know?

2) Whose Strategy was Bottom Up? How do you know?

3) Which way of thinking about the problem makes more sense to you?

What's happening with that Math?!

When calculating Jamal's drive time, we multiplied distance by speed. More specifically, we multiplied the starting value (20 miles) by 1 hour/40 miles. Why? Why not reverse it, to use 40 miles/1 hour, as stated in the problem?

Time is the desired outcome. Looking at the units, we can see that speed must have miles as its denominator to cancel out the miles in the starting value.

$$\frac{20mi}{1} \times \frac{1hour}{40miles} = \frac{20\cancel{miles} \times 1hour}{40\cancel{miles}} = \frac{20}{40}hour = \frac{1}{2}hour$$