

relax



A program for  
NMR relaxation data analysis

Version respository checkout

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# Abbreviations

**AIC** Akaike's Information Criteria

**AICc** small sample size corrected AIC

**BIC** Bayesian Information Criteria

$C(\tau)$  correlation function

$\chi^2$  chi-squared function

**CSA** chemical shift anisotropy

$\mathfrak{D}$  the set of diffusion tensor parameters

$\mathfrak{D}_{\parallel}$  the eigenvalue of the spheroid diffusion tensor corresponding to the unique axis of the tensor

$\mathfrak{D}_{\perp}$  the eigenvalue of the spheroid diffusion tensor corresponding to the two axes perpendicular to the unique axis

$\mathfrak{D}_a$  the anisotropic component of the Brownian rotational diffusion tensor

$\mathfrak{D}_{iso}$  the isotropic component of the Brownian rotational diffusion tensor

$\mathfrak{D}_r$  the rhombic component of the Brownian rotational diffusion tensor

$\mathfrak{D}_{ratio}$  the ratio of  $\mathfrak{D}_{\parallel}$  to  $\mathfrak{D}_{\perp}$

$\mathfrak{D}_x$  the eigenvalue of the Brownian rotational diffusion tensor in which the corresponding eigenvector defines the x-axis of the tensor

$\mathfrak{D}_y$  the eigenvalue of the Brownian rotational diffusion tensor in which the corresponding eigenvector defines the y-axis of the tensor

$\mathfrak{D}_z$  the eigenvalue of the Brownian rotational diffusion tensor in which the corresponding eigenvector defines the z-axis of the tensor

$\epsilon_i$  elimination value

$J(\omega)$  spectral density function

**NOE** nuclear Overhauser effect

**pdf** probability distribution function

$r$  bond length

$\mathbf{R}_1$  spin-lattice relaxation rate

$\mathbf{R}_2$  spin-spin relaxation rate

$R_{ex}$  chemical exchange relaxation rate

$S^2$ ,  $S_f^2$ , **and**  $S_s^2$  model-free generalised order parameters

$\tau_e$ ,  $\tau_f$ , **and**  $\tau_s$  model-free effective internal correlation times

$\tau_m$  global rotational correlation time

# Chapter 1

## How to use relax

### 1.1 The prompt

The primary interface of relax is the prompt. After typing ‘`relax`’ within a terminal, you will be presented with

```
relax>
```

This is the Python prompt which has been tailored specifically for relax. You will hence have full access, if necessary, to the power of the Python programming language to manipulate your data. You can for instance type

```
relax> print "Hello World"
```

the result being

```
relax> print "Hello World"
Hello World
relax>
```

Or, using relax as a calculator

```
relax> (1.0 + (2 * 3))/10
0.69999999999999996
relax>
```

### 1.2 Python

relax has been designed such that knowledge about Python is not required to be able to fully use the program. A few basics, though, will aid in understanding relax.

A number of simple programming axioms includes that of strings , integers , floating point numbers , and lists . A string is text and within Python (as well as relax) this is delimited by either single or double quotes. An integer is a number with no decimal point while

a float is a number with a decimal point. A list in Python (called an array in other languages) is a list of anything separated by commas and delimited by square brackets, an example is `[0, 1, 2, 'a', 1.2143235]`.

Probably the most important detail is that functions in Python require brackets around their arguments. For example

```
relax> minimise()
```

will commence minimisation however

```
relax> minimise
```

will do nothing.

The arguments to a function are simply a comma separated list within the brackets of the function. For example to save the program's current state, type

```
relax> state.save('save', force=1)
```

Two types of arguments exist in Python, standard arguments and keyword arguments. The majority of arguments you will encounter within relax are keyword arguments however you may, in rare cases, encounter a non-keyword argument. For these standard arguments, just type the values in, although they must be in the correct order. Keyword arguments consist of two parts, the key and the value. For example the key may be `file` while the value you would like to supply is `'R1.out'`. Various methods exist for supplying this argument. Firstly you could simply type `'R1.out'` into the correct position in the argument list. Secondly you can type `file='R1.out'`. The power of this second option is that argument order is unimportant. Therefore if you would like to change the default value of the very last argument, you don't have to supply values for all other arguments. The only catch is that standard arguments must come before the keyword arguments.

### 1.3 User functions

For standard data analysis, a large number of specially tailored functions called 'user functions' have been implemented. These are accessible from the relax prompt by simply typing the name of the function. An example is `'help()'`. An alphabetical listing of all accessible user functions together with full descriptions is presented later within this manual.

A few special objects which are available within the prompt are not actually functions. These objects do not require brackets at their end for them to function. For example to exit relax type

```
relax> exit
```

Another special object is that of the function class `.`. This object is simply a container which holds a number of user functions. You can access the user function within the class by typing the name of the class, then a dot `'.'`, followed by the name of the user function. An example is the user function for reading relaxation data out of a file and loading the data into relax. The function is called `'read'` while the class is called `'relax_data'`. To execute the function, type something like

```
relax> relax_data.read(name, 'R1', '600', 600.0 * 1e6, 'r1.600.out')
```

The relax prompt, on first usage, can be quite daunting. Two features exist, however, to increase the usability of the prompt – the help system and tab completion

## 1.4 The help system

For assistance in using a function, simply type

```
help(function)
```

In addition to functions, if

```
help(object)
```

is typed, the help for the python object is returned. This system is similar to the help function built into the python interpreter, which has been renamed to `help_python`, with the interactive component removed. For the interactive python help system, type

```
help_python()
```

## 1.5 Tab completion

Tab completion is implemented to prevent insanity as the function names can be quite long – a deliberate feature to improve usability. The behaviour of the tab completion is very similar to that of the bash prompt.

Not only is tab completion useful for preventing RSI, but it can also be used for finding out what functions are available. To begin with if you hit the [TAB] key without typing any text, all available functions will be listed (along with function classes and other python objects). This extends to the exploration of user functions within a function class. For example, to list the user functions within the function class `'model_free'`, type

```
relax> model_free.
```

The dot character at the end is essential. After hitting the [TAB] key, you should see something like

```
relax> model_free.
model_free.__class__
model_free.__doc__
model_free.__init__
model_free.__module__
model_free.__relax__
model_free.__relax_help__
model_free.copy
model_free.create_model
model_free.delete
model_free.remove_tm
model_free.select_model
```

```
relax> model_free.
```

All the objects beginning with an underscore are “hidden”, they contain information about the function class and should be ignored. From the listing the user functions ‘copy’, ‘create\_model’, ‘delete’, ‘remove\_tm’, and ‘select\_model’ contained within ‘model\_free’ are all visible.

## 1.6 The ‘run’

Within relax, the majority of operations are assigned to a special construct called a ‘run’. For example, to load relaxation data into the program it must be committed to a pre-created ‘run’. Within one instance of relax, multiple runs can be created and various operations performed in sequence on these runs. This is useful for operations such as model selection whereby the function ‘model\_selection’ can operate on a number of runs corresponding to different models and then assign the results to a newly created run.

The flow of data through relax can be thought of as travelling through pipes – each pipe is synonymous with a run. User functions exist to transfer data between these pipes, while other functions combine data from multiple pipes into one or vice-versa. The simplest invocation of relax would be the creation of a single run and with the data being processed as it is passing through this pipe.

The primary method for creating a run is through the user function ‘run.create’. For example

```
relax> run.create('m1', 'mf')
```

will create a run called ‘m1’. The run is also associated with a type which, in this case, is model-free analysis. The following is a table of all the types which can be assigned to a run.

Run type	Description
‘jw’	Reduced spectral density mapping
‘mf’	Model-free data analysis
‘noe’	Steady state NOE calculation
‘relax_fit’	Relaxation curve fitting
‘srls’	SRLS analysis

Currently only the NOE calculation, model-free analysis, and reduced spectral density mapping features of relax are implemented (if this documentation is out of date, then you may be able to do a lot more).

## 1.7 Scripting

What ever is done within the prompt is also accessible through scripting. Just type your commands into a text file and then at the terminal type



```
$ relax your_script
```

An example of a simple script which will minimise the model-free model ‘m4’ after loading six relaxation data sets is

```
# Create the run.
name = 'm4'
run.create(name, 'mf')

# Nuclei type
nuclei('N')

# Load the sequence.
sequence.read(name, 'noe.500.out')

# Load the relaxation data.
relax_data.read(name, 'R1', '600', 600.0 * 1e6, 'r1.600.out')
relax_data.read(name, 'R2', '600', 600.0 * 1e6, 'r2.600.out')
relax_data.read(name, 'NOE', '600', 600.0 * 1e6, 'noe.600.out')
relax_data.read(name, 'R1', '500', 500.0 * 1e6, 'r1.500.out')
relax_data.read(name, 'R2', '500', 500.0 * 1e6, 'r2.500.out')
relax_data.read(name, 'NOE', '500', 500.0 * 1e6, 'noe.500.out')

# Setup other values.
diffusion_tensor.set(name, (2e-8, 1.3, 60, 290), param_types=1, axial_type='prolate',
fixed=1)
value.set(name, 1.02 * 1e-10, 'bond_length')
value.set(name, -160 * 1e-6, 'csa')

# Select a preset model-free model.
model_free.select_model(run=name, model=name)

# Grid search.
grid_search(name, inc=11)

# Minimise.
minimise('newton', run=name)

# Finish.
results.write(run=name, file='results', force=1)
state.save('save', force=1)
```

Scripting is much more powerful than the prompt as advanced Python programming can be employed (see the file ‘full\_analysis.py’ in the ‘sample\_scripts’ directory for an example).

## 1.8 Sample scripts

A few sample scripts have been provided in the directory ‘sample\_scripts’. These can be used as a good starting point for using relax.

## 1.9 The GUI

relax has been designed primarily for scripting and, as such, no graphical user interface (GUI) currently exists. The internal structure of the program has been specifically designed so any type of control mechanism can be easily added, including a GUI, therefore in the future one may be written. A GUI will, however, detract from the power and flexibility inherent in the control by scripting.

## 1.10 Access to the internals of relax

For highly advanced Python scripting or control of relax, almost every part of relax has been designed in an object oriented fashion. If you would like to play with internals of the program, the entirety of relax is accessible within the object called ‘`self.relax`’. To access the raw objects within relax which contain the program data, all data is stored within the object called ‘`self.relax.data`’.

## 1.11 Usage of the name relax

The program relax is so relaxed that the first letter should always be in lower case!

## Chapter 2

# Values, gradients, and Hessians

### 2.1 Introduction

#### 2.1.1 Chi-squared function – $\chi^2(\theta)$

For the minimisation of models, a chain of calculations using different theories is required. At the highest level, the function which is actually minimised is the chi-squared function

$$\chi^2(\theta) = \sum_{i=1}^n \frac{(R_i - R_i(\theta))^2}{\sigma_i^2}, \quad (2.1)$$

where the index  $i$  is the summation index ranging over all the experimentally collected relaxation data,  $R_i$ , including the  $R_1$ ,  $R_2$ , and NOE data at all field strengths belonging to the set data set  $R$  for an individual residue, a collection of residues, or the entire macromolecule,  $R_i(\theta)$  is the back calculated relaxation data belonging to the set  $R(\theta)$ ,  $\theta$  is the model parameter vector which, when minimised, is denoted by the symbol  $\hat{\theta}$ , and  $\sigma_i$  are the experimental errors.

The significance of equation (2.1) is that the function returns a single value.

#### 2.1.2 Relaxation equations – $R_i(\theta)$

The chi-squared equation is itself dependent on the relaxation equations through the back calculated relaxation data  $R(\theta)$ . These data are the spin-lattice, spin-spin, and cross-relaxation rates of Abragam (1961) and are respectively

$$R_1(\theta) = d \left( J(\omega_H - \omega_X) + 3J(\omega_X) + 6J(\omega_H + \omega_X) \right) + cJ(\omega_X), \quad (2.2)$$

$$R_2(\theta) = \frac{d}{2} \left( 4J(0) + J(\omega_H - \omega_X) + 3J(\omega_X) + 6J(\omega_H) + 6J(\omega_H + \omega_X) \right) + \frac{c}{6} \left( 4J(0) + 3J(\omega_X) \right) + R_{ex}, \quad (2.3)$$

$$\sigma_{\text{NOE}}(\theta) = d \left( 6J(\omega_H + \omega_X) - J(\omega_H - \omega_X) \right), \quad (2.4)$$

$$(2.5)$$

where  $J(\omega)$  is the power spectral density function,  $R_{ex}$  is the relaxation due to chemical exchange, and the dipolar and CSA constants are defined in SI units as

$$d = \frac{1}{4} \left( \frac{\mu_0}{4\pi} \right)^2 \frac{(\gamma_H \gamma_X \hbar)^2}{\langle r^6 \rangle}, \quad (2.6)$$

$$c = \frac{(\omega_H \Delta\sigma)^2}{3}, \quad (2.7)$$

where  $\mu_0$  is the permeability of free space,  $\gamma_H$  and  $\gamma_X$  are the gyromagnetic ratios of the  $H$  and  $X$  spins respectively,  $\hbar$  is Plank's constant divided by  $2\pi$ ,  $r$  is the bond length, and  $\Delta\sigma$  is the chemical shift anisotropy measured in ppm. The cross-relaxation rate  $\sigma_{\text{NOE}}$  is related to the steady state NOE by the equation

$$\text{NOE}(\theta) = 1 + \frac{\gamma_H}{\gamma_X} \frac{\sigma_{\text{NOE}}(\theta)}{R_1(\theta)}. \quad (2.8)$$

### 2.1.3 Transformed relaxation equations – $R'_i(\theta)$

Letting the relaxation equations,  $R_i(\theta)$  be the  $R_1(\theta)$ ,  $R_2(\theta)$ , and  $\text{NOE}(\theta)$ , an additional layer of abstraction can be used to simplify the calculation of the gradients and Hessians. This involved decomposing the NOE equation into the cross relaxation rate constant  $\sigma_{\text{NOE}}(\theta)$  and the auto relaxation rate  $R_1(\theta)$ . Taking equation (2.8), the relaxation equations are

$$R'_1(\theta) = R_1(\theta) \quad (2.9)$$

$$R'_2(\theta) = R_2(\theta) \quad (2.10)$$

$$\text{NOE}(\theta) = 1 + \frac{\gamma_H}{\gamma_X} \frac{\sigma_{\text{NOE}}(\theta)}{R_1(\theta)}. \quad (2.11)$$

while the transformed relaxation equations are  $\{R'_1(\theta), R'_2(\theta), \sigma_{\text{NOE}}(\theta)\}$ .

### 2.1.4 Spectral density functions – $J(\omega)$

The relaxation equations are themselves dependent on the calculation of the spectral density values  $J(\omega)$ . Within model-free analysis, these are modelled by the original model-free formula (Lipari and Szabo, 1982a,b)

$$J(\omega) = \frac{2}{5} \sum_{i=-k}^k c_i \cdot \tau_i \left( \frac{S^2}{1 + (\omega\tau_i)^2} + \frac{(1 - S^2)(\tau_e + \tau_i)\tau_e}{(\tau_e + \tau_i)^2 + (\omega\tau_e\tau_i)^2} \right), \quad (2.12)$$

where  $S^2$  is the square of the Lipari and Szabo generalised order parameter and  $\tau_e$  is the effective correlation time. The order parameter reflects the amplitude of the motion while the correlation time is an indication of the time scale of that motion. The theory was

extended by Clore et al. (1990) by the modelling of two independent internal motions using the equation

$$J(\omega) = \frac{2}{5} \sum_{i=-k}^k c_i \cdot \tau_i \left( \frac{S^2}{1 + (\omega\tau_i)^2} + \frac{(1 - S_f^2)(\tau_f + \tau_i)\tau_f}{(\tau_f + \tau_i)^2 + (\omega\tau_f\tau_i)^2} + \frac{(S_f^2 - S^2)(\tau_s + \tau_i)\tau_s}{(\tau_s + \tau_i)^2 + (\omega\tau_s\tau_i)^2} \right). \quad (2.13)$$

where  $S_f^2$  and  $\tau_f$  are the amplitude and timescale of the faster of the two motions while  $S_s^2$  and  $\tau_s$  are those of the slower motion.  $S_f^2$  and  $S_s^2$  are related by the formula  $S^2 = S_f^2 \cdot S_s^2$ .

### 2.1.5 Brownian diffusion

In equations (2.12) and (2.13), the generic Brownian diffusion NMR correlation function presented in ? has been used. This function is

$$C(\tau) = \frac{1}{5} \sum_{i=-k}^k c_i \cdot e^{-\tau/\tau_i}, \quad (2.14)$$

where the summation index  $i$  ranges over the number of exponential terms within the correlation function. This equation is generic in that it describes the diffusion of an ellipsoid, a spheroid, and a sphere.

#### Ellipsoid

For the ellipsoid defined by the parameter set  $\{\mathfrak{D}_{iso}, \mathfrak{D}_a, \mathfrak{D}_r, \alpha, \beta, \gamma\}$  the variable  $k$  is equal to two, therefore the index  $i \in \{-2, -1, 0, 1, 2\}$ . The geometric parameters  $\{\mathfrak{D}_{iso}, \mathfrak{D}_a, \mathfrak{D}_r\}$  are defined as

$$\mathfrak{D}_{iso} = \frac{1}{3}(\mathfrak{D}_x + \mathfrak{D}_y + \mathfrak{D}_z), \quad (2.15a)$$

$$\mathfrak{D}_a = \mathfrak{D}_z - \frac{1}{2}(\mathfrak{D}_x + \mathfrak{D}_y), \quad (2.15b)$$

$$\mathfrak{D}_r = \frac{\mathfrak{D}_y - \mathfrak{D}_x}{2\mathfrak{D}_a}, \quad (2.15c)$$

and are constrained by

$$0 < \mathfrak{D}_{iso} < \infty, \quad (2.16a)$$

$$0 \leq \mathfrak{D}_a < \frac{\mathfrak{D}_{iso}}{\frac{1}{3} + \mathfrak{D}_r} \leq 3\mathfrak{D}_{iso}, \quad (2.16b)$$

$$0 \leq \mathfrak{D}_r \leq 1. \quad (2.16c)$$

The orientational parameters  $\{\alpha, \beta, \gamma\}$  are the Euler angles using the z-y-z rotation notation.

The five weights  $c_i$  are defined as

$$c_{-2} = \frac{1}{4}(d + e), \quad (2.17a)$$

$$c_{-1} = 3\delta_y^2\delta_z^2, \quad (2.17b)$$

$$c_0 = 3\delta_x^2\delta_z^2, \quad (2.17c)$$

$$c_1 = 3\delta_x^2\delta_y^2, \quad (2.17d)$$

$$c_2 = \frac{1}{4}(d - e), \quad (2.17e)$$

where

$$d = 3(\delta_x^4 + \delta_y^4 + \delta_z^4) - 1, \quad (2.18)$$

$$e = -\frac{1}{\Re} \left[ (1 + 3\mathfrak{D}_r)(\delta_x^4 + 2\delta_y^2\delta_z^2) + (1 - 3\mathfrak{D}_r)(\delta_y^4 + 2\delta_x^2\delta_z^2) - 2(\delta_z^4 + 2\delta_x^2\delta_y^2) \right], \quad (2.19)$$

and where

$$\Re = \sqrt{1 + 3\mathfrak{D}_r^2}, \quad (2.20)$$

The five correlation times  $\tau_i$  are

$$1/\tau_{-2} = 6\mathfrak{D}_{iso} - 2\mathfrak{D}_a\Re, \quad (2.21a)$$

$$1/\tau_{-1} = 6\mathfrak{D}_{iso} - \mathfrak{D}_a(1 + 3\mathfrak{D}_r), \quad (2.21b)$$

$$1/\tau_0 = 6\mathfrak{D}_{iso} - \mathfrak{D}_a(1 - 3\mathfrak{D}_r), \quad (2.21c)$$

$$1/\tau_1 = 6\mathfrak{D}_{iso} + 2\mathfrak{D}_a, \quad (2.21d)$$

$$1/\tau_2 = 6\mathfrak{D}_{iso} + 2\mathfrak{D}_a\Re. \quad (2.21e)$$

## Spheroid

The variable  $k$  is equal to one in the case of the spheroid defined by the parameter set  $\{\mathfrak{D}_{iso}, \mathfrak{D}_a, \theta, \phi\}$ , hence  $i \in \{-1, 0, 1\}$ . The geometric parameters  $\{\mathfrak{D}_{iso}, \mathfrak{D}_a\}$  are defined as

$$\mathfrak{D}_{iso} = \frac{1}{3}(\mathfrak{D}_{\parallel} + 2\mathfrak{D}_{\perp}), \quad (2.22a)$$

$$\mathfrak{D}_a = \mathfrak{D}_{\parallel} - \mathfrak{D}_{\perp}. \quad (2.22b)$$

and are constrained by

$$0 < \mathfrak{D}_{iso} < \infty, \quad (2.23a)$$

$$-\frac{3}{2}\mathfrak{D}_{iso} < \mathfrak{D}_a < 3\mathfrak{D}_{iso}, \quad (2.23b)$$

The orientational parameters  $\{\theta, \phi\}$  are the spherical angles defining the orientation of the major axis of the diffusion frame within the lab frame.

The three weights  $c_i$  are

$$c_{-1} = \frac{1}{4}(3\delta_z^2 - 1)^2, \quad (2.24a)$$

$$c_0 = 3\delta_z^2(1 - \delta_z^2), \quad (2.24b)$$

$$c_1 = \frac{3}{4}(\delta_z^2 - 1)^2, \quad (2.24c)$$

The five correlation times  $\tau_i$  are

$$1/\tau_{-1} = 6\mathfrak{D}_{iso} - 2\mathfrak{D}_a, \quad (2.25a)$$

$$1/\tau_0 = 6\mathfrak{D}_{iso} - \mathfrak{D}_a, \quad (2.25b)$$

$$1/\tau_1 = 6\mathfrak{D}_{iso} + 2\mathfrak{D}_a. \quad (2.25c)$$

## Sphere

In the situation of a molecule diffusing as a sphere either described by the single parameter  $\tau_m$  or  $\mathfrak{D}_{iso}$ , the variable  $k$  is equal to zero. Therefore  $i \in \{0\}$ . The single weight  $c_0$  is equal to one, while the single correlation time  $\tau_0$  is equivalent to the global tumbling time  $\tau_m$  given by

$$1/\tau_m = 6\mathfrak{D}_{iso}. \quad (2.26)$$

## 2.2 Minimisation concepts

### 2.2.1 The function value

At the simplest level, all minimisation techniques require at least a function which will supply a single value for different parameter values  $\theta$ . For the modelling of NMR relaxation data, this is given by equation (2.1). For certain algorithms, such a Simplex minimisation, this single value suffices.

### 2.2.2 The gradient

The majority of minimisation algorithms, however, also require the gradient at the point of the given parameter values  $\theta$ . The gradient is a vector of partial derivatives defined as

$$\nabla = \begin{pmatrix} \frac{\partial}{\partial \theta_1} \\ \frac{\partial}{\partial \theta_2} \\ \vdots \\ \frac{\partial}{\partial \theta_n} \end{pmatrix} \quad (2.27)$$

where  $n$  is the total number of parameters in the model.

An example of a powerful algorithm which requires both the value and gradient at given parameter values is BFGS quasi-Newton minimisation.

### 2.2.3 The Hessian

A few algorithms, including the most powerful, require in addition the Hessian at given parameter values  $\theta$ . The Hessian is the matrix of second partial derivatives defined as

$$\nabla^2 = \begin{pmatrix} \frac{\partial^2}{\partial \theta_1^2} & \frac{\partial^2}{\partial \theta_1 \partial \theta_2} & \cdots & \frac{\partial^2}{\partial \theta_1 \partial \theta_n} \\ \frac{\partial^2}{\partial \theta_2 \partial \theta_1} & \frac{\partial^2}{\partial \theta_2^2} & \cdots & \frac{\partial^2}{\partial \theta_2 \partial \theta_n} \\ \vdots & \vdots & \ddots & \vdots \\ \frac{\partial^2}{\partial \theta_n \partial \theta_1} & \frac{\partial^2}{\partial \theta_n \partial \theta_2} & \cdots & \frac{\partial^2}{\partial \theta_n^2} \end{pmatrix} \quad (2.28)$$

The most powerful minimisation algorithm, Newton minimisation, requires the value, gradient, and Hessian at the given parameter values.

## 2.3 Value, gradient, and Hessian dependency chain

The dependency chain outlined in the introduction to this chapter, that the chi-squared function is dependent on the relaxation equations which are dependent on the transformed relaxation equations which themselves are dependent on the spectral density functions, combine with the values, gradients, and Hessians to create a complex web of dependencies. The relationship between all the values, gradients, and Hessians are outlined in Figure 2.1.

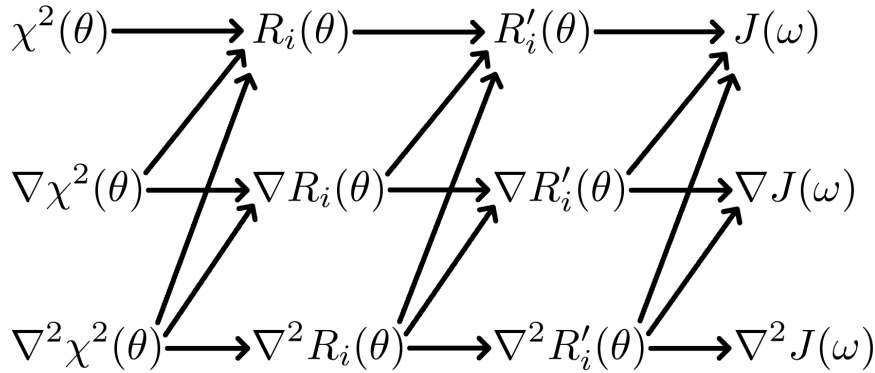


Figure 2.1: Dependencies between the  $\chi^2$ , transformed relaxation, relaxation, and spectral density equations, gradients, and Hessians.

## 2.4 $\chi^2$ values, gradients, and Hessians

### 2.4.1 $\chi^2$ values

The  $\chi^2$  value is

$$\chi^2(\theta) = \sum_{i=1}^n \frac{(R_i - R_i(\theta))^2}{\sigma_i^2}, \quad (2.29)$$

which is the same as equation (2.1) on page 7.



### 2.4.2 $\chi^2$ gradients

The  $\chi^2$  gradient is

$$\nabla \chi^2(\theta) = 2 \sum_{i=1}^n \frac{(R_i - R_i(\theta))^2}{\sigma_i^2} \nabla R_i(\theta). \quad (2.30)$$

### 2.4.3 $\chi^2$ Hessians

The  $\chi^2$  Hessian is

$$\nabla^2 \chi^2(\theta) = 2 \sum_{i=1}^n \frac{1}{\sigma_i^2} (\nabla R_i(\theta) \cdot \nabla R_i(\theta)^T - (R_i - R_i(\theta)) \nabla^2 R_i(\theta)). \quad (2.31)$$

## 2.5 $R_i(\theta)$ values, gradients, and Hessians

### 2.5.1 $R_i(\theta)$ values

The  $R_i(\theta)$  values are given by

$$R_1(\theta) = R'_1(\theta), \quad (2.32)$$

$$R_2(\theta) = R'_2(\theta), \quad (2.33)$$

$$\text{NOE}(\theta) = 1 + \frac{\gamma_H}{\gamma_X} \frac{\sigma_{\text{NOE}}(\theta)}{R_1(\theta)}. \quad (2.34)$$

### 2.5.2 $R_i(\theta)$ gradients

The  $R_i(\theta)$  gradients are

$$\nabla R_1(\theta) = \nabla R'_1(\theta), \quad (2.35)$$

$$\nabla R_2(\theta) = \nabla R'_2(\theta), \quad (2.36)$$

$$\nabla \text{NOE}(\theta) = \frac{\gamma_H}{\gamma_X} \frac{1}{R_1(\theta)^2} \left( R_1(\theta) \nabla \sigma_{\text{NOE}}(\theta) - \sigma_{\text{NOE}}(\theta) \nabla R_1(\theta) \right). \quad (2.37)$$

### 2.5.3 $R_i(\theta)$ Hessians

The  $R_i(\theta)$  Hessians are

$$\nabla^2 R_1(\theta) = \nabla^2 R'_1(\theta), \quad (2.38)$$

$$\nabla^2 R_2(\theta) = \nabla^2 R'_2(\theta), \quad (2.39)$$

$$\begin{aligned} \nabla^2 \text{NOE}(\theta) = \frac{\gamma_H}{\gamma_X} \frac{1}{R_1(\theta)^3} & \left[ \sigma_{\text{NOE}}(\theta) \left( 2 \nabla R_1(\theta) \cdot \nabla R_1(\theta)^T - R_1(\theta) \nabla^2 R_1(\theta) \right) \right. \\ & \left. - R_1(\theta) \left( \nabla \sigma_{\text{NOE}}(\theta) \cdot \nabla R_1(\theta)^T - R_1(\theta) \nabla^2 \sigma_{\text{NOE}}(\theta) \right) \right]. \end{aligned} \quad (2.40)$$

## 2.6 $R'_i(\theta)$ values, gradients, and Hessians

The partial and second partial derivatives of the transformed relaxation equations,  $R'_i(\theta)$ , are different for each parameter of the vector  $\theta$ . The vector representation of the gradient,  $\nabla R'_i(\theta)$ , and the matrix representation of the Hessian,  $\nabla^2 R'_i(\theta)$ , can be reconstructed from the individual elements presented below.

### 2.6.1 Components of the $R'_i(\theta)$ equations

To simplify the calculations of the gradients and Hessians, the  $R'_i(\theta)$  equations have been broken down into their various components. These include the dipolar and CSA constants as well as the dipolar and CSA spectral density terms for each of the three transformed relaxation data types,  $R_1$ ,  $R_2$ , and  $\sigma_{\text{NOE}}$ . The segregation of these components simplifies the maths as many partial derivatives of the components are zero.

#### Dipolar constant

The dipolar constant is defined as

$$d = \frac{1}{4} \left( \frac{\mu_0}{4\pi} \right)^2 \frac{(\gamma_H \gamma_X \hbar)^2}{\langle r^6 \rangle}. \quad (2.41)$$

This component of the relaxation equations is independent of the parameter of the spectral density function,  $\theta_j$ , the chemical exchange parameter,  $\sigma_{ex}$ , and the CSA parameter,  $\Delta\sigma$ . Therefore, the partial and second partial derivatives with respect to these parameters is zero. Only the partial derivative with respect to the bond length,  $r$ , is non-zero, being

$$d' \equiv \frac{dd}{dr} = -\frac{3}{2} \left( \frac{\mu_0}{4\pi} \right)^2 \frac{(\gamma_H \gamma_X \hbar)^2}{\langle r^7 \rangle}. \quad (2.42)$$

The double partial derivative with respect to the bond length twice is

$$d'' \equiv \frac{d^2d}{dr^2} = \frac{21}{2} \left( \frac{\mu_0}{4\pi} \right)^2 \frac{(\gamma_H \gamma_X \hbar)^2}{\langle r^8 \rangle}. \quad (2.43)$$

#### CSA constant

The CSA constant is defined as

$$c = \frac{(\omega_X \cdot \Delta\sigma)^2}{3}. \quad (2.44)$$

The partial derivative of this component with respect to all parameters but the CSA parameter  $\Delta\sigma$  is zero. This partial derivative is

$$c' \equiv \frac{dc}{d\Delta\sigma} = \frac{2\omega_X^2 \cdot \Delta\sigma}{3}. \quad (2.45)$$

The CSA constant double partial derivative with respect to  $\Delta\sigma$  is

$$c'' \equiv \frac{d^2c}{d\Delta\sigma^2} = \frac{2\omega_X^2}{3}. \quad (2.46)$$

**Spectral density terms of the  $R_1$  dipolar component**

For the dipolar component of the  $R_1$  equation, the spectral density terms are

$$J_d^{R_1} = J(\omega_H - \omega_X) + 3J(\omega_X) + 6J(\omega_H + \omega_X). \quad (2.47)$$

The partial derivative of these terms with respect to the parameter of the spectral density function  $\theta_j$  is

$$J_d^{R_1'} \equiv \frac{\partial J_d^{R_1}}{\partial \theta_j} = \frac{\partial J(\omega_H - \omega_X)}{\partial \theta_j} + 3 \frac{\partial J(\omega_X)}{\partial \theta_j} + 6 \frac{\partial J(\omega_H + \omega_X)}{\partial \theta_j}. \quad (2.48)$$

The second partial derivative with respect to the parameter of the spectral density function  $\theta_j$  and  $\theta_k$  is

$$J_d^{R_1''} \equiv \frac{\partial^2 J_d^{R_1}}{\partial \theta_j \cdot \partial \theta_k} = \frac{\partial^2 J(\omega_H - \omega_X)}{\partial \theta_j \cdot \partial \theta_k} + 3 \frac{\partial^2 J(\omega_X)}{\partial \theta_j \cdot \partial \theta_k} + 6 \frac{\partial^2 J(\omega_H + \omega_X)}{\partial \theta_j \cdot \partial \theta_k}. \quad (2.49)$$

**Spectral density terms of the  $R_1$  CSA component**

For the CSA component of the  $R_1$  equation, the spectral density terms are

$$J_c^{R_1} = J(\omega_X). \quad (2.50)$$

The partial derivative of these terms with respect to the parameter of the spectral density function  $\theta_j$  is

$$J_c^{R_1'} \equiv \frac{\partial J_c^{R_1}}{\partial \theta_j} = \frac{\partial J(\omega_X)}{\partial \theta_j}. \quad (2.51)$$

The second partial derivative with respect to the parameter of the spectral density function  $\theta_j$  and  $\theta_k$  is

$$J_c^{R_1''} \equiv \frac{\partial^2 J_c^{R_1}}{\partial \theta_j \cdot \partial \theta_k} = \frac{\partial^2 J(\omega_X)}{\partial \theta_j \cdot \partial \theta_k}. \quad (2.52)$$

**Spectral density terms of the  $R_2$  dipolar component**

For the dipolar component of the  $R_2$  equation, the spectral density terms are

$$J_d^{R_2} = 4J(0) + J(\omega_H - \omega_X) + 3J(\omega_X) + 6J(\omega_H) + 6J(\omega_H + \omega_X). \quad (2.53)$$

The partial derivative of these terms with respect to the parameter of the spectral density function  $\theta_j$  is

$$J_d^{R_2'} \equiv \frac{\partial J_d^{R_2}}{\partial \theta_j} = 4 \frac{\partial J(0)}{\partial \theta_j} + \frac{\partial J(\omega_H - \omega_X)}{\partial \theta_j} + 3 \frac{\partial J(\omega_X)}{\partial \theta_j} + 6 \frac{\partial J(\omega_H)}{\partial \theta_j} + 6 \frac{\partial J(\omega_H + \omega_X)}{\partial \theta_j}. \quad (2.54)$$

The second partial derivative with respect to the parameter of the spectral density function  $\theta_j$  and  $\theta_k$  is

$$J_d^{R_2''} \equiv \frac{\partial^2 J_d^{R_2}}{\partial \theta_j \cdot \partial \theta_k} = 4 \frac{\partial^2 J(0)}{\partial \theta_j \cdot \partial \theta_k} + \frac{\partial^2 J(\omega_H - \omega_X)}{\partial \theta_j \cdot \partial \theta_k} + 3 \frac{\partial^2 J(\omega_X)}{\partial \theta_j \cdot \partial \theta_k} + 6 \frac{\partial^2 J(\omega_H)}{\partial \theta_j \cdot \partial \theta_k} + 6 \frac{\partial^2 J(\omega_H + \omega_X)}{\partial \theta_j \cdot \partial \theta_k}. \quad (2.55)$$

### Spectral density terms of the $R_2$ CSA component

For the CSA component of the  $R_2$  equation, the spectral density terms are

$$J_c^{R_2} = 4J(0) + 3J(\omega_X). \quad (2.56)$$

The partial derivative of these terms with respect to the parameter of the spectral density function  $\theta_j$  is

$$J_c^{R_2'} \equiv \frac{\partial J_c^{R_2}}{\partial \theta_j} = 4 \frac{\partial J(0)}{\partial \theta_j} + 3 \frac{\partial J(\omega_X)}{\partial \theta_j}. \quad (2.57)$$

The second partial derivative with respect to the parameter of the spectral density function  $\theta_j$  and  $\theta_k$  is

$$J_c^{R_2''} \equiv \frac{\partial^2 J_c^{R_2}}{\partial \theta_j \cdot \partial \theta_k} = 4 \frac{\partial^2 J(0)}{\partial \theta_j \cdot \partial \theta_k} + 3 \frac{\partial^2 J(\omega_X)}{\partial \theta_j \cdot \partial \theta_k}. \quad (2.58)$$

### Spectral density terms of the $\sigma_{\text{NOE}}$ dipolar component

For the dipolar component of the  $\sigma_{\text{NOE}}$  equation, the spectral density terms are

$$J_d^{\sigma_{\text{NOE}}} = 6J(\omega_H + \omega_X) - 6J(\omega_H - \omega_X). \quad (2.59)$$

The partial derivative of these terms with respect to the parameter of the spectral density function  $\theta_j$  is

$$J_d^{\sigma_{\text{NOE}}'} \equiv \frac{\partial J_d^{\sigma_{\text{NOE}}}}{\partial \theta_j} = 6 \frac{\partial J(\omega_H + \omega_X)}{\partial \theta_j} - 6 \frac{\partial J(\omega_H - \omega_X)}{\partial \theta_j}. \quad (2.60)$$

The second partial derivative with respect to the parameter of the spectral density function  $\theta_j$  and  $\theta_k$  is

$$J_d^{\sigma_{\text{NOE}}''} \equiv \frac{\partial^2 J_d^{\sigma_{\text{NOE}}}}{\partial \theta_j \cdot \partial \theta_k} = 6 \frac{\partial^2 J(\omega_H + \omega_X)}{\partial \theta_j \cdot \partial \theta_k} - 6 \frac{\partial^2 J(\omega_H - \omega_X)}{\partial \theta_j \cdot \partial \theta_k}. \quad (2.61)$$

### 2.6.2 $R'_i(\theta)$ values

The three relaxation equations, utilising the above components, can be expressed as

$$R_1(\theta) = dJ_d^{R_1} + cJ_c^{R_1}, \quad (2.62)$$

$$R_2(\theta) = \frac{d}{2}J_d^{R_2} + \frac{c}{6}J_c^{R_2}, \quad (2.63)$$

$$\sigma_{\text{NOE}}(\theta) = dJ_d^{\sigma_{\text{NOE}}}. \quad (2.64)$$

### 2.6.3 $R'_i(\theta)$ gradients

The partial derivatives with respect to the parameter of the spectral density functions, the chemical exchange parameter, CSA parameter, and bond length parameters are all different and are presented below.

#### Spectral density function parameter

The partial derivatives of the relaxation equations with respect to the parameter of the spectral density function  $\theta_j$  are

$$\frac{\partial R_1(\theta)}{\partial \theta_j} = dJ_d^{R_1'} + cJ_c^{R_1'}, \quad (2.65)$$

$$\frac{\partial R_2(\theta)}{\partial \theta_j} = \frac{d}{2}J_d^{R_2'} + \frac{c}{6}J_c^{R_2'}, \quad (2.66)$$

$$\frac{\partial \sigma_{\text{NOE}}(\theta)}{\partial \theta_j} = dJ_d^{\sigma_{\text{NOE}}'}. \quad (2.67)$$

#### Chemical exchange parameter

The partial derivatives of the relaxation equations with respect to the chemical exchange parameter  $R_{ex}$  are

$$\frac{\partial R_1(\theta)}{\partial R_{ex}} = 0, \quad (2.68)$$

$$\frac{\partial R_2(\theta)}{\partial R_{ex}} = 1, \quad (2.69)$$

$$\frac{\partial \sigma_{\text{NOE}}(\theta)}{\partial R_{ex}} = 0. \quad (2.70)$$

### CSA parameter

The partial derivatives of the relaxation equations with respect to the CSA parameter  $\Delta\sigma$  are

$$\frac{\partial R_1(\theta)}{\partial \Delta\sigma} = c' J_c^{R_1}, \quad (2.71)$$

$$\frac{\partial R_2(\theta)}{\partial \Delta\sigma} = \frac{c'}{6} J_c^{R_2}, \quad (2.72)$$

$$\frac{\partial \sigma_{\text{NOE}}(\theta)}{\partial \Delta\sigma} = 0. \quad (2.73)$$

### Bond length parameter

The partial derivatives of the relaxation equations with respect to the bond length parameter  $r$  are

$$\frac{\partial R_1(\theta)}{\partial r} = d' J_d^{R_1}, \quad (2.74)$$

$$\frac{\partial R_2(\theta)}{\partial r} = \frac{d'}{2} J_d^{R_2}, \quad (2.75)$$

$$\frac{\partial \sigma_{\text{NOE}}(\theta)}{\partial r} = d' J_d^{\sigma_{\text{NOE}}}. \quad (2.76)$$

#### 2.6.4 $R'_i(\theta)$ Hessians

The second partial derivatives with respect to the parameter of the spectral density functions, the chemical exchange parameter, CSA parameter, and bond length parameters are presented below.

#### Spectral density function parameter - Spectral density function parameter

The second partial derivatives of the relaxation equations with respect to the parameter of the spectral density functions  $\theta_j$  and  $\theta_k$  are

$$\frac{\partial^2 R_1(\theta)}{\partial \theta_j \cdot \partial \theta_k} = d J_d^{R_1''} + c J_c^{R_1''}, \quad (2.77)$$

$$\frac{\partial^2 R_2(\theta)}{\partial \theta_j \cdot \partial \theta_k} = \frac{d}{2} J_d^{R_2''} + \frac{c}{6} J_c^{R_2''}, \quad (2.78)$$

$$\frac{\partial^2 \sigma_{\text{NOE}}(\theta)}{\partial \theta_j \cdot \partial \theta_k} = d J_d^{\sigma_{\text{NOE}}''}. \quad (2.79)$$

**Spectral density function parameter - Chemical exchange parameter**

The second partial derivatives of the relaxation equations with respect to the parameter of the spectral density function  $\theta_j$  and the chemical exchange parameter  $R_{ex}$  are

$$\frac{\partial^2 R_1(\theta)}{\partial \theta_j \cdot \partial R_{ex}} = 0, \quad (2.80)$$

$$\frac{\partial^2 R_2(\theta)}{\partial \theta_j \cdot \partial R_{ex}} = 0, \quad (2.81)$$

$$\frac{\partial^2 \sigma_{\text{NOE}}(\theta)}{\partial \theta_j \cdot \partial R_{ex}} = 0. \quad (2.82)$$

**Spectral density function parameter - CSA parameter**

The second partial derivatives of the relaxation equations with respect to the parameter of the spectral density function  $\theta_j$  and the CSA parameter  $\Delta\sigma$  are

$$\frac{\partial^2 R_1(\theta)}{\partial \theta_j \cdot \partial \Delta\sigma} = c' J_c^{\text{R}_1'}, \quad (2.83)$$

$$\frac{\partial^2 R_2(\theta)}{\partial \theta_j \cdot \partial \Delta\sigma} = \frac{c'}{6} J_c^{\text{R}_2'}, \quad (2.84)$$

$$\frac{\partial^2 \sigma_{\text{NOE}}(\theta)}{\partial \theta_j \cdot \partial \Delta\sigma} = 0. \quad (2.85)$$

**Spectral density function parameter - Bond length parameter**

The second partial derivatives of the relaxation equations with respect to the parameter of the spectral density function  $\theta_j$  and the bond length parameter  $r$  are

$$\frac{\partial^2 R_1(\theta)}{\partial \theta_j \cdot \partial r} = d' J_d^{\text{R}_1'}, \quad (2.86)$$

$$\frac{\partial^2 R_2(\theta)}{\partial \theta_j \cdot \partial r} = \frac{d'}{2} J_d^{\text{R}_2'}, \quad (2.87)$$

$$\frac{\partial^2 \sigma_{\text{NOE}}(\theta)}{\partial \theta_j \cdot \partial r} = d' J_d^{\sigma_{\text{NOE}}'}. \quad (2.88)$$

**Chemical exchange parameter - Chemical exchange parameter**

The second partial derivatives of the relaxation equations with respect to the chemical exchange parameter  $R_{ex}$  twice are

$$\frac{\partial^2 R_1(\theta)}{\partial R_{ex}^2} = 0, \quad (2.89)$$

$$\frac{\partial^2 R_2(\theta)}{\partial R_{ex}^2} = 0, \quad (2.90)$$

$$\frac{\partial^2 \sigma_{\text{NOE}}(\theta)}{\partial R_{ex}^2} = 0. \quad (2.91)$$

### Chemical exchange parameter - CSA parameter

The second partial derivatives of the relaxation equations with respect to the chemical exchange parameter  $R_{ex}$  and the CSA parameter  $\Delta\sigma$  are

$$\frac{\partial^2 R_1(\theta)}{\partial R_{ex} \cdot \partial \Delta\sigma} = 0, \quad (2.92)$$

$$\frac{\partial^2 R_2(\theta)}{\partial R_{ex} \cdot \partial \Delta\sigma} = 0, \quad (2.93)$$

$$\frac{\partial^2 \sigma_{\text{NOE}}(\theta)}{\partial R_{ex} \cdot \partial \Delta\sigma} = 0. \quad (2.94)$$

### Chemical exchange parameter - Bond length parameter

The second partial derivatives of the relaxation equations with respect to the chemical exchange parameter  $R_{ex}$  and the bond length parameter  $r$  are

$$\frac{\partial^2 R_1(\theta)}{\partial R_{ex} \cdot \partial r} = 0, \quad (2.95)$$

$$\frac{\partial^2 R_2(\theta)}{\partial R_{ex} \cdot \partial r} = 0, \quad (2.96)$$

$$\frac{\partial^2 \sigma_{\text{NOE}}(\theta)}{\partial R_{ex} \cdot \partial r} = 0. \quad (2.97)$$

### CSA parameter - CSA parameter

The second partial derivatives of the relaxation equations with respect to the CSA parameter  $\Delta\sigma$  twice are

$$\frac{\partial^2 R_1(\theta)}{\partial \Delta\sigma^2} = c'' J_c^{R_1}, \quad (2.98)$$

$$\frac{\partial^2 R_2(\theta)}{\partial \Delta\sigma^2} = \frac{c''}{6} J_c^{R_2}, \quad (2.99)$$

$$\frac{\partial^2 \sigma_{\text{NOE}}(\theta)}{\partial \Delta\sigma^2} = 0. \quad (2.100)$$

### CSA parameter - Bond length parameter

The second partial derivatives of the relaxation equations with respect to the CSA parameter  $\Delta\sigma$  and the bond length parameter  $r$  are

$$\frac{\partial^2 R_1(\theta)}{\partial \Delta\sigma \cdot \partial r} = 0, \quad (2.101)$$

$$\frac{\partial^2 R_2(\theta)}{\partial \Delta\sigma \cdot \partial r} = 0, \quad (2.102)$$

$$\frac{\partial^2 \sigma_{\text{NOE}}(\theta)}{\partial \Delta\sigma \cdot \partial r} = 0. \quad (2.103)$$



### Bond length parameter - Bond length parameter

The second partial derivatives of the relaxation equations with respect to the bond length parameter  $r$  twice are

$$\frac{\partial^2 R_1(\theta)}{\partial r^2} = d'' J_d^{R_1}, \quad (2.104)$$

$$\frac{\partial^2 R_2(\theta)}{\partial r^2} = \frac{d''}{2} J_d^{R_2}, \quad (2.105)$$

$$\frac{\partial^2 \sigma_{\text{NOE}}(\theta)}{\partial r^2} = d'' J_d^{\sigma_{\text{NOE}}}. \quad (2.106)$$

## 2.7 Ellipsoidal diffusion tensor

### 2.7.1 Ellipsoid weight derivatives



## Chapter 3

# Alphabetical listing of user functions

The following is a listing with descriptions of all the user functions available within the relax prompt and scripting environments. These are simply an alphabetical list of the docstrings which can normally be viewed in prompt mode by typing `'help(function)'`.

### 3.1 A warning about the formatting

The following documentation of the user functions has been automatically generated by a script which extracts and formats the docstring associated with each function. There may therefore be instances where the formatting has failed or where there are inconsistencies.

### 3.2 The list of functions

Each user function is presented within it's own subsection with the documentation broken into multiple parts, the synopsis, the default arguments, and the sections from the function's docstring.

#### 3.2.1 The synopsis

The synopsis presents a brief description of the function. It is taken as the first line of the docstring when browsing the help system .

#### 3.2.2 Defaults

This section lists all the arguments taken by the function and their default values. To invoke the function, type the function name then in brackets type a comma separated list of arguments.

The first argument printed is always ‘self’ but you can safely ignore it. ‘self’ is part of the object oriented programming within Python and is automatically prefixed to the list of arguments you supply. Therefore you can’t provide ‘self’ as the first argument, even if you do try.

### **3.2.3 Docstring sectioning**

All other sections are created from the sectioning within the actual docstring.

### 3.2.4 angles

#### Synopsis

Function for calculating the angles between the XH bond vector and the diffusion tensor.

#### Defaults

**angles**(self, run=None)

#### Keyword Arguments

run: The name of the run.

#### Description

If the diffusion tensor is isotropic for the run, then nothing will be done.

If the diffusion tensor is axially symmetric, then the angle  $\alpha$  will be calculated for each XH bond vector.

If the diffusion tensor is asymmetric, then the three angles will be calculated.

### 3.2.5 calc

#### Synopsis

Function for calculating the function value.

#### Defaults

**calc**(self, run=None, print\_flag=1)

#### Keyword Arguments

run: The name of the run.

### 3.2.6 `diffusion_tensor.copy`

#### Synopsis

Function for copying diffusion tensor data from run1 to run2.

#### Defaults

**`diffusion_tensor.copy`**(self, run1=None, run2=None)

#### Keyword Arguments

run1: The name of the run to copy the sequence from.

run2: The name of the run to copy the sequence to.

#### Description

This function will copy the diffusion tensor data from ‘run1’ to ‘run2’. ‘run2’ must not contain any diffusion tensor data.

#### Examples

To copy the diffusion tensor from run ‘m1’ to run ‘m2’, type:

```
relax> diffusion_tensor.copy('m1', 'm2')
```

### 3.2.7 `diffusion_tensor.delete`

#### Synopsis

Function for deleting diffusion tensor data.

#### Defaults

**`diffusion_tensor.delete`**(self, run=None)

#### Keyword Arguments

run: The name of the run.

#### Description

This function will delete all diffusion tensor data for the given run.



### 3.2.8 `diffusion_tensor.display`

#### Synopsis

Function for displaying the diffusion tensor.

#### Defaults

**`diffusion_tensor.display`**(self, run=None)

#### Keyword Arguments

run: The name of the run.

### 3.2.9 diffusion\_tensor.set

#### Synopsis

Function for setting up the diffusion tensor.

#### Defaults

**diffusion\_tensor.set**(self, run=None, params=None, time\_scale=1.0, d\_scale=1.0, angle\_units='deg', param\_types=0, spheroid\_type=None, fixed=1)

#### Keyword Arguments

**run**: The name of the run to assign the data to.

**params**: The diffusion tensor data.

**time\_scale**: The correlation time scaling value.

**d\_scale**: The diffusion tensor eigenvalue scaling value.

**angle\_units**: The units for the angle parameters.

**param\_types**: A flag to select different parameter combinations.

**spheroid\_type**: A string which, if supplied together with spheroid parameters, will restrict the tensor to either being 'oblate' or 'prolate'.

**fixed**: A flag specifying whether the diffusion tensor is fixed or can be optimised.

#### The sphere (isotropic diffusion)

When the molecule diffuses as a sphere, all three eigenvalues of the diffusion tensor are equal,  $\mathfrak{D}_x = \mathfrak{D}_y = \mathfrak{D}_z$ . In this case, the orientation of the XH bond vector within the diffusion frame is inconsequential to relaxation, hence, the spherical or Euler angles are undefined. Therefore solely a single geometric parameter, either  $\tau_m$  or  $\mathfrak{D}_{iso}$ , can fully and sufficiently parameterise the diffusion tensor. The correlation function for the global rotational diffusion is

$$C(\tau) = \frac{1}{5} e^{-\tau / \tau_m},$$

To select isotropic diffusion, the parameters argument should be a single floating point number. The number is the value of the isotropic global correlation time,  $\tau_m$ , in seconds. To specify the time in nanoseconds, set the 'time\_scale' argument to 1e-9. Alternative parameters can be used by changing the 'param\_types' flag to the following integers

**0** –  $\tau_m$  (Default),

**1** –  $\mathfrak{D}_{iso}$ ,

where

$$1 / \tau_m = 6\mathfrak{D}_{iso}.$$

### The spheroid (axially symmetric diffusion)

When two of the three eigenvalues of the diffusion tensor are equal, the molecule diffuses as a spheroid. Four pieces of information are required to specify this tensor, the two geometric parameters,  $\mathfrak{D}_{iso}$  and  $\mathfrak{D}_a$ , and the two orientational parameters, the polar angle  $\theta$  and the azimuthal angle  $\phi$  describing the orientation of the axis of symmetry. The correlation function of the global diffusion is

$$C(\tau) = \frac{1}{5} \sum_{i=-1}^1 \sum_{j=-1}^1 c_{ij} e^{-\tau / \tau_{ij}},$$

where

$$c_{-1} = 1/4 (3 \delta_z^2 - 1)^2,$$

$$c_0 = 3 \delta_z^2 (1 - \delta_z^2),$$

$$c_1 = 3/4 (\delta_z^2 - 1)^2,$$

and

$$1 / \tau_{-1} = 6\mathfrak{D}_{iso} - 2\mathfrak{D}_a,$$

$$1 / \tau_0 = 6\mathfrak{D}_{iso} - \mathfrak{D}_a,$$

$$1 / \tau_1 = 6\mathfrak{D}_{iso} + 2\mathfrak{D}_a.$$

The direction cosine  $\delta_z$  is defined as the cosine of the angle  $\alpha$  between the XH bond vector and the unique axis of the diffusion tensor.

To select axially symmetric anisotropic diffusion, the parameters argument should be a tuple of floating point numbers of length four. A tuple is a type of data structure enclosed in round brackets, the elements of which are separated by commas. Alternative sets of parameters, ‘param\_types’, are

**0** –  $(\tau_m, \mathfrak{D}_a, \theta, \phi)$  (Default),

$$1 - (\mathfrak{D}_{iso}, \mathfrak{D}_a, \theta, \phi),$$

$$2 - (\tau_m, \mathfrak{D}_{ratio}, \theta, \phi),$$

$$3 - (\mathfrak{D}_{\parallel}, \mathfrak{D}_{\perp}, \theta, \phi),$$

$$4 - (\mathfrak{D}_{iso}, \mathfrak{D}_{ratio}, \theta, \phi),$$

where

$$\tau_m = 1 / 6\mathfrak{D}_{iso},$$

$$\mathfrak{D}_{iso} = 1/3 (\mathfrak{D}_{\parallel} + 2\mathfrak{D}_{\perp}),$$

$$\mathfrak{D}_a = \mathfrak{D}_{\parallel} - \mathfrak{D}_{\perp},$$

$$\mathfrak{D}_{ratio} = \mathfrak{D}_{\parallel} / \mathfrak{D}_{\perp}.$$

The spherical angles  $\{\theta, \phi\}$  orienting the unique axis of the diffusion tensor within the PDB frame are defined between

$$0 \leq \theta \leq \pi,$$

$$0 \leq \phi \leq 2\pi,$$

while the angle  $\alpha$  which is the angle between this axis and the given XH bond vector is defined between

$$0 \leq \alpha \leq 2\pi.$$

The ‘**spheroid\_type**’ argument should be ‘**oblate**’, ‘**prolate**’, or None. The argument will be ignored if the diffusion tensor is not axially symmetric. If ‘**oblate**’ is given, then the constraint  $\mathfrak{D}_a \leq 0$  is used while if ‘**prolate**’ is given, then the constraint  $\mathfrak{D}_a \geq 0$  is used. If nothing is supplied, then  $\mathfrak{D}_a$  will be allowed to have any values. To prevent minimisation of diffusion tensor parameters in a space with two minima, it is recommended to specify which tensor is to be minimised, thereby partitioning the two minima into the two subspaces along the boundry  $\mathfrak{D}_a = 0$ .

### The ellipsoid (rhombic diffusion)

When all three eigenvalues of the diffusion tensor are different, the molecule diffuses as an ellipsoid. This diffusion is also known as fully anisotropic, asymmetric, or rhombic. The full tensor is specified by six pieces of information, the three geometric parameters  $\mathfrak{D}_{iso}$ ,  $\mathfrak{D}_a$ , and  $\mathfrak{D}_r$  representing the isotropic, anisotropic, and rhombic components of the tensor, and the three Euler angles  $\alpha$ ,  $\beta$ , and  $\gamma$  orienting the tensor within the PDB frame. The correlation function is

$$C(\tau) = \frac{1}{5} \sum_{i=-2}^{-2} c_i \cdot e^{-\tau / \tau_i},$$

where the weights on the exponentials are

$$c_{-2} = 1/4 (d + e),$$

$$c_{-1} = 3 \delta_y^2 \delta_z^2,$$

$$c_0 = 3 \delta_x^2 \delta_z^2,$$

$$c_1 = 3 \delta_x^2 \delta_y^2,$$

$$c_2 = 1/4 (d + e).$$

Let

$$\mathfrak{R} = \sqrt{1 + 3\mathfrak{D}_r},$$

then

$$d = 3 (\delta_x^4 + \delta_y^4 + \delta_z^4) - 1,$$

$$e = -1 / \mathfrak{R} ((1 + 3\mathfrak{D}_r)(\delta_x^4 + 2\delta_y^2 \delta_z^2) + (1 - 3\mathfrak{D}_r)(\delta_y^4 + 2\delta_x^2 \delta_z^2) - 2(\delta_z^4 + 2\delta_x^2 \delta_y^2)).$$

The correlation times are

$$1 / \tau_{-2} = 6\mathfrak{D}_{iso} - 2\mathfrak{D}_a \cdot \mathfrak{R},$$

$$1 / \tau_{-1} = 6\mathfrak{D}_{iso} - \mathfrak{D}_a (1 + 3\mathfrak{D}_r),$$

$$1 / \tau_0 = 6\mathfrak{D}_{iso} - \mathfrak{D}_a (1 - 3\mathfrak{D}_r),$$

$$1 / \tau_1 = 6\mathfrak{D}_{iso} + 2\mathfrak{D}_a,$$

$$1 / \tau_2 = 6\mathfrak{D}_{iso} + 2\mathfrak{D}_a \cdot \mathfrak{R}.$$

The three direction cosines  $\delta_x$ ,  $\delta_y$ , and  $\delta_z$  are the coordinates of a unit vector parallel to the XH bond vector. Hence the unit vector is  $[\delta_x, \delta_y, \delta_z]$ .

To select fully anisotropic diffusion, the parameters argument should be a tuple of length six. A tuple is a type of data structure enclosed in round brackets, the elements of which are separated by commas. Alternative sets of parameters, ‘**param\_types**’, are

$$\mathbf{0} = (\tau_m, \mathfrak{D}_a, \mathfrak{D}_r, \alpha, \beta, \gamma) \text{ (Default),}$$

$$\mathbf{1} - (\mathfrak{D}_{iso}, \mathfrak{D}_a, \mathfrak{D}_r, \alpha, \beta, \gamma),$$

$$\mathbf{2} - (\mathfrak{D}_x, \mathfrak{D}_y, \mathfrak{D}_z, \alpha, \beta, \gamma),$$

where

$$\tau_m = 1 / 6\mathfrak{D}_{iso},$$

$$\mathfrak{D}_{iso} = 1/3 (\mathfrak{D}_x + \mathfrak{D}_y + \mathfrak{D}_z),$$

$$\mathfrak{D}_a = \mathfrak{D}_z - (\mathfrak{D}_x + \mathfrak{D}_y)/2,$$

$$\mathfrak{D}_r = (\mathfrak{D}_y - \mathfrak{D}_x)/2\mathfrak{D}_a.$$

The angles  $\alpha$ ,  $\beta$ , and  $\gamma$  are the Euler angles describing the diffusion tensor within the PDB frame. These angles are defined using the z-y-z axis rotation notation where  $\alpha$  is the initial rotation angle around the z-axis,  $\beta$  is the rotation angle around the y-axis, and  $\gamma$  is the final rotation around the z-axis again. The angles are defined between

$$0 \leq \alpha \leq 2\pi,$$

$$0 \leq \beta \leq \pi,$$

$$0 \leq \gamma \leq 2\pi.$$

Within the PDB frame, the XH bond vector is described using the spherical angles  $\theta$  and  $\phi$  where  $\theta$  is the polar angle and  $\phi$  is the azimuthal angle defined between

$$0 \leq \theta \leq \pi,$$

$$0 \leq \phi \leq 2\pi.$$

## Units

The ‘**time\_scale**’ argument should be a floating point number. The only parameter affected by this value is  $\tau_m$ .

The ‘**d\_scale**’ argument should also be a floating point number. Parameters affected by this value are  $\mathfrak{D}_{iso}$ ,  $\mathfrak{D}_{\parallel}$ ,  $\mathfrak{D}_{\perp}$ ,  $\mathfrak{D}_a$ ,  $\mathfrak{D}_x$ ,  $\mathfrak{D}_y$ , and  $\mathfrak{D}_z$ . Significantly,  $\mathfrak{D}_r$  is not affected.

The ‘**angle\_units**’ argument should either be the string ‘**deg**’ or ‘**rad**’. Parameters affected are  $\theta$ ,  $\phi$ ,  $\alpha$ ,  $\beta$ , and  $\gamma$ .

## Examples

To set an isotropic diffusion tensor with a correlation time of 10 ns, assigning it to the run 'm1', type:

```
relax> diffusion_tensor('m1', 10e-9)
relax> diffusion_tensor(run='m1', params=10e-9)
relax> diffusion_tensor('m1', 10.0, 1e-9)
relax> diffusion_tensor(run='m1', params=10.0, time_scale=1e-9, fixed=1)
```

To select axially symmetric diffusion with a  $\tau_m$  value of 8.5 ns,  $\mathcal{D}_{ratio}$  of 1.1,  $\theta$  value of 20 degrees, and  $\phi$  value of 20 degrees, and assign it to the run 'm8', type:

```
relax> diffusion_tensor('m8', (8.5e-9, 1.1, 20.0, 20.0), param_types=1)
```

To select a spheroid diffusion tensor with a  $\mathcal{D}_{\parallel}$  value of 1.698e7,  $\mathcal{D}_{\perp}$  value of 1.417e7,  $\theta$  value of 67.174 degrees, and  $\phi$  value of -83.718 degrees, and assign it to the run 'spheroid', type one of:

```
relax> diffusion_tensor('spheroid', (1.698e7, 1.417e7, 67.174, -83.718), param_types=1)
relax> diffusion_tensor(run='spheroid', params=(1.698e7, 1.417e7, 67.174, -83.718),
param_types=1)
relax> diffusion_tensor('spheroid', (1.698e-1, 1.417e-1, 67.174, -83.718), param_types=1,
d_scale=1e8)
relax> diffusion_tensor(run='spheroid', params=(1.698e-1, 1.417e-1, 67.174, -83.718),
param_types=1, d_scale=1e8)
relax> diffusion_tensor('spheroid', (1.698e-1, 1.417e-1, 1.1724, -1.4612), param_types=1,
d_scale=1e8, angle_units='rad')
relax> diffusion_tensor(run='spheroid', params=(1.698e-1, 1.417e-1, 1.1724, -1.4612),
param_types=1, d_scale=1e8, angle_units='rad', fixed=1)
```

To select ellipsoidal diffusion, type:

```
relax> diffusion_tensor('m5', (1.340e7, 1.516e7, 1.691e7, -82.027, -80.573, 65.568),
param_types=2)
```

To select and minimise a spherical diffusion tensor, type (followed by a minimisation command):

```
relax> diffusion_tensor('diff', 10e-9, fixed=0)
```

### 3.2.10 dx.execute

#### Synopsis

Function for running OpenDX.

#### Defaults

**dx.execute**(self, file='map', dir='dx', dx\_exe='dx', vp\_exec=1)

#### Keyword Arguments

**file**: The file name prefix. For example if file is set to '**temp**', then the OpenDX program temp.net will be loaded.

**dir**: The directory to change to for running OpenDX. If this is set to '**None**', OpenDX will be run in the current directory.

**dx\_exe**: The OpenDX executable file.

**vp\_exec**: A flag specifying whether to execute the visual program automatically at start-up. The default is 1 which turns execution on. Setting the value to zero turns execution off.



### 3.2.11 dx.map

#### Synopsis

Function for creating a map of the given space in OpenDX format.

#### Defaults

```
dx.map(self, run=None, params=None, map_type='Iso3D', res_num=None, inc=20,  
lower=None, upper=None, file='map', dir='dx', point=None, point_file='point',  
remap=None)
```

#### Keyword Arguments

**run:** The name of the run.

**params:** The parameters to be mapped. This argument should be an array of strings, values of which are described below.

**map\_type:** The type of map to create. For example the default, a 3D isosurface, the type is 'Iso3D'. See below for more details.

**res\_num:** The residue number.

**inc:** The number of increments to map in each dimension. This value controls the resolution of the map.

**lower:** The lower bounds of the space. If you wish to change the lower bounds of the map then supply an array of length equal to the number of parameters in the model. A lower bound for each parameter must be supplied. If nothing is supplied then the defaults will be used.

**upper:** The upper bounds of the space. If you wish to change the upper bounds of the map then supply an array of length equal to the number of parameters in the model. A upper bound for each parameter must be supplied. If nothing is supplied then the defaults will be used.

**file:** The file name. All the output files are prefixed with this name. The main file containing the data points will be called the value of 'file'. The OpenDX program will be called 'file.net' and the OpenDX import file will be called 'file.general'.

**dir:** The directory to output files to. Set this to 'None' if you do not want the files to be placed in subdirectory. If the directory does not exist, it will be created.

**point:** An array of parameter values where a point in the map, shown as a red sphere, will be placed. The length must be equal to the number of parameters.

**point\_file:** The name of that the point output files will be prefixed with.

**remap:** A user supplied remapping function. This function will receive the parameter array and must return an array of equal length.

## Map type

The map type can be changed by supplying the ‘map\_type’ keyword argument. Here is a list of currently supported map types:

Surface type	Pattern
3D isosurface	<code>^[Ii]so3[Dd]</code>

Pattern syntax is simply regular expression syntax where square brackets ‘[]’ means any character within the brackets, ‘^’ means the start of the string, etc.

## Examples

The following commands will generate a map of the extended model-free space defined as run ‘m5’ which consists of the parameters  $\{S^2, S_f^2, \tau_s\}$ . Files will be output into the directory ‘dx’ and will be prefixed by ‘map’. The residue, in this case, is number 6.

```
relax> dx.map('m5', ['S2', 'S2f', 'ts'], 6)
relax> dx.map('m5', ['S2', 'S2f', 'ts'], 6, 20, 'map', 'dx')
relax> dx.map('m5', ['S2', 'S2f', 'ts'], res_num=6, file='map', dir='dx')
relax> dx.map(run='m5', params=['S2', 'S2f', 'ts'], res_num=6, inc=20, file='map',
dir='dx')
relax> dx.map(run='m5', params=['S2', 'S2f', 'ts'], res_num=6, type='Iso3D', inc=20,
swap=[0, 1, 2], file='map', dir='dx')
```

To map the model-free space ‘m4’ defined by the parameters  $\{S^2, \tau_e, R_{ex}\}$ , name the results ‘test’, and not place the files in a subdirectory, use the following commands (assuming residue 2).

```
relax> dx.map('m4', ['S2', 'te', 'Rex'], res_num=2, file='test', dir=None)
relax> dx.map(run='m4', params=['S2', 'te', 'Rex'], res_num=2, inc=100, file='test',
dir=None)
```

## Regular expression

The python function ‘match’, which uses regular expression, is used to determine which data type to set values to, therefore various data\_type strings can be used to select the same data type. Patterns used for matching for specific data types are listed below.

This is a short description of python regular expression, for more information see the regular expression syntax section of the Python Library Reference. Some of the regular expression syntax used in this function is:

‘[]’ – A sequence or set of characters to match to a single character. For example, ‘[Ss]2’ will match both ‘S2’ and ‘s2’.

‘^’ – Match the start of the string.

‘\$’ – Match the end of the string. For example, ‘^[Ss]2\$’ will match ‘s2’ but not ‘S2f’ or ‘s2s’.

‘.’ – Match any character.

‘x\*’ – Match the character ‘x’ any number of times, for example ‘x’ will match, as will ‘xxxxx’

‘.\*’ – Match any sequence of characters of any length.

Importantly, do not supply a string for the data type containing regular expression. The regular expression is implemented so that various strings can be supplied which all match the same data type.

**Diffusion tensor parameter string matching patterns**

Data type	Object name	Patterns
Global correlation time - $\tau_m$	‘tm’	‘tm’
Isotropic component of the diffusion tensor - $\mathfrak{D}_{iso}$	‘Diso’	‘[Dd]iso’
Anisotropic component of the diffusion tensor - $\mathfrak{D}_a$	‘Da’	‘[Dd]a’
Rhombic component of the diffusion tensor - $\mathfrak{D}_r$	‘Dr’	‘[Dd]r\$’
Eigenvalue associated with the x-axis of the diffusion diffusion tensor - $\mathfrak{D}_x$	‘Dx’	‘[Dd]x’
Eigenvalue associated with the y-axis of the diffusion diffusion tensor - $\mathfrak{D}_y$	‘Dy’	‘[Dd]y’
Eigenvalue associated with the z-axis of the diffusion diffusion tensor - $\mathfrak{D}_z$	‘Dz’	‘[Dd]z’
Diffusion coefficient parallel to the major axis of the spheroid diffusion tensor - $\mathfrak{D}_{  }$	‘Dpar’	‘[Dd]par’
Diffusion coefficient perpendicular to the major axis of the spheroid diffusion tensor - $\mathfrak{D}_{\perp}$	‘Dper’	‘[Dd]per’
Ratio of the parallel and perpendicular components of the spheroid diffusion tensor - $\mathfrak{D}_{ratio}$	‘Dratio’	‘[Dd]ratio’
The first Euler angle of the ellipsoid diffusion tensor - $\alpha$	‘alpha’	‘^a\$’ or ‘alpha’
The second Euler angle of the ellipsoid diffusion tensor - $\beta$	‘beta’	‘^b\$’ or ‘beta’
The third Euler angle of the ellipsoid diffusion tensor - $\gamma$	‘gamma’	‘^g\$’ or ‘gamma’
The polar angle defining the major axis of the spheroid diffusion tensor - $\theta$	‘theta’	‘theta’
The azimuthal angle defining the major axis of the spheroid diffusion tensor - $\phi$	‘phi’	‘phi’

**Model-free data type string matching patterns**

Data type	Object name	Patterns
Local $\tau_m$	'tm'	'^tm\$'
Order parameter $S^2$	's2'	'^[Ss]2\$'
Order parameter $S_f^2$	's2f'	'^[Ss]2f\$'
Order parameter $S_s^2$	's2s'	'^[Ss]2s\$'
Correlation time $\tau_e$	'te'	'^te\$'
Correlation time $\tau_f$	'tf'	'^tf\$'
Correlation time $\tau_s$	'ts'	'^ts\$'
Chemical exchange	'rex'	'^[Rr]ex\$' or '[Cc]emical[ -_][Ee]xchange'
Bond length	'r'	'^r\$' or '[Bb]ond[ -_][Ll]ength'
CSA	'csa'	'^[Cc][Ss][Aa]\$'

### 3.2.12 eliminate

#### Synopsis

Function for model elimination.

#### Defaults

**eliminate**(self, run=None, function=None, args=None)

#### Keyword arguments

**run**: The name of the run(s). By supplying a single string, array of strings, or None, a single run, multiple runs, or all runs will be selected respectively.

**function**: A user supplied function for model elimination.

**args**: A tuple of arguments for model elimination.

#### Description

This function is used for model validation to eliminate or reject models prior to model selection. Model validation is a part of mathematical modelling whereby models are either accepted or rejected.

Empirical rules are used for model rejection and are listed below. However these can be overridden by supplying a function. The function should accept five arguments, a string defining a certain parameter, the value of the parameter, the run name, the minimisation instance (ie the residue index if the model is residue specific), and the function arguments. If the model is rejected, the function should return 1, otherwise it should return 0. The function will be executed multiple times, once for each parameter of the model.

The ‘**args**’ keyword argument should be a tuple, a list enclosed in round brackets, and will be passed to the user supplied function or the inbuilt function. For a description of the arguments accepted by the inbuilt functions, see below.

Once a model is rejected, the select flag corresponding to that model will be set to 0 so that model selection, or any other function, will then skip the model.

#### Local $\tau_m$ model elimination rule

The local  $\tau_m$ , in some cases, may exceed the value expected for a global correlation time. Generally the  $\tau_m$  value will be stuck at the upper limit defined for the parameter. These models are eliminated using the rule:

$$\tau_m \geq c$$

The default value of  $c$  is 50 ns, although this can be overridden by supplying the value (in seconds) as the first element of the `args` tuple.

### Internal correlation times $\{\tau_e, \tau_f, \tau_s\}$ model elimination rules

These parameters may experience the same problem as the local  $\tau_m$  in that the model fails and the parameter value is stuck at the upper limit. These parameters are constrained using the formula  $(\tau_e, \tau_f, \tau_s \leq 2\tau_m)$ . These failed models are eliminated using the rule:

$$\tau_e, \tau_f, \tau_s \geq c \cdot \tau_m$$

The default value of  $c$  is 1.5. Because of round-off errors and the constraint algorithm, setting  $c$  to 2 will result in no models being eliminated as the minimised parameters will always be less than  $2\tau_m$ . The value can be changed by supplying the value as the second element of the tuple.

### Arguments

The `'args'` argument must be a tuple of length 2, the elements of which must be numbers. For example, to eliminate models which have a local  $\tau_m$  value greater than 25 ns and models with internal correlation times greater than 1.5 times  $\tau_m$ , set `'args'` to `(25 * 1e-9, 1.5)`.

### 3.2.13 fix

#### Synopsis

Function for either fixing or allowing parameter values to change.

#### Defaults

**fix**(self, run=None, element=None, fixed=1)

#### Keyword Arguments

**run**: The name of the run.

**element**: Which element to fix.

**fixed**: A flag specifying if the parameters should be fixed or allowed to change.

#### Description

The keyword argument ‘**element**’ can be any of the following:

‘**diff**’ - the diffusion tensor parameters. This will allow all diffusion tensor parameters to be toggled.

an integer - if an integer number is given, then all parameters for the residue corresponding to that number will be toggled.

‘**all\_res**’ - using this keyword, all parameters from all residues will be toggled.

‘**all**’ - all parameter will be toggled. This is equivalent to combining both ‘**diff**’ and ‘**all\_res**’.

The flag ‘**fixed**’, if set to 1, will fix parameters, while a value of 0 will allow parameters to vary.

Only parameters corresponding to the given run will be affected.



### 3.2.14 `grace.view`

#### Synopsis

Function for running Grace.

#### Defaults

**`grace.view`**(self, file=None, dir='grace', grace\_exe='xmgrace')

#### Keyword Arguments

file: The name of the file.

dir: The directory name.

grace\_exe: The Grace executable file.

#### Description

This function can be used to execute Grace to view the specified file the Grace '`.agr`' file and the execute Grace. If the directory name is set to None, the file will be assumed to be in the current working directory.

#### Examples

To view the file '`s2.agr`' in the directory '`grace`', type:

```
relax> grace.view(file='s2.agr')
```

```
relax> grace.view(file='s2.agr', dir='grace')
```

### 3.2.15 `grace.write`

#### Synopsis

Function for creating a grace ‘.agr’ file.

#### Defaults

```
grace.write(self, run=None, x_data_type='res', y_data_type=None, res_num=None,
res_name=None, plot_data='value', file=None, dir='grace', force=0)
```

#### Keyword Arguments

`run`: The name of the run.

`x_data_type`: The data type for the X-axis (no regular expression is allowed).

`y_data_type`: The data type for the Y-axis (no regular expression is allowed).

`res_num`: The residue number (regular expression is allowed).

`res_name`: The residue name (regular expression is allowed).

`plot_data`: The data to use for the plot.

`file`: The name of the file.

`dir`: The directory name.

`force`: A flag which, if set to 1, will cause the file to be overwritten.

#### Description

This function is designed to be as flexible as possible so that any combination of data can be plotted. The output is in the format of a Grace plot (also known as ACE/gr, Xmgr, and xmgrace) which only supports two dimensional plots. Three types of keyword arguments can be used to create various types of plot. These include the X-axis and Y-axis data types, the residue number and name selection arguments, and an argument for selecting what to actually plot.

The X-axis and Y-axis data type arguments should be plain strings, regular expression is not allowed. If the X-axis data type argument is not given, the plot will default to having the residue number along the x-axis. The two axes of the Grace plot can be absolutely any of the data types listed in the tables below. The only limitation, currently anyway, is that the data must belong to the same run.

The residue number and name arguments can be used to limit the residues used in the plot. The default is that all residues will be used, however, these arguments can be used to select a subset of all residues, or a single residue for plots of Monte Carlo simulations,

etc. Regular expression is allowed for both the residue number and name, and the number can either be an integer or a string.

The property which is actually plotted can be controlled by the ‘`plot_data`’ argument. It can be one of the following:

‘`value`’ – Plot values (with errors if they exist).

‘`error`’ – Plot errors.

‘`sims`’ – Plot the simulation values.

### Examples

To write the NOE values for all residues from the run ‘`noe`’ to the Grace file ‘`noe.agr`’, type:

```
relax> grace.write('noe', 'res', 'noe', file='noe.agr')
relax> grace.write('noe', y_data_type='noe', file='noe.agr')
relax> grace.write('noe', x_data_type='res', y_data_type='noe', file='noe.agr')
relax> grace.write(run='noe', y_data_type='noe', file='noe.agr', force=1)
```

To create a Grace file of ‘`S2`’ vs. ‘`te`’ for all residues, type:

```
relax> grace.write('m2', 'S2', 'te', file='s2.te.agr')
relax> grace.write('m2', x_data_type='S2', y_data_type='te', file='s2.te.agr')
relax> grace.write(run='m2', x_data_type='S2', y_data_type='te', file='s2.te.agr', force=1)
```

To create a Grace file of the Monte Carlo simulation values of ‘`Rex`’ vs. ‘`te`’ for residue 123, type:

```
relax> grace.write('m4', 'Rex', 'te', res_num=123, plot_data='sims', file='s2.te.agr')
relax> grace.write(run='m4', x_data_type='Rex', y_data_type='te', res_num=123,
plot_data='sims', file='s2.te.agr')
```

### Regular expression

The python function ‘`match`’, which uses regular expression, is used to determine which data type to set values to, therefore various `data_type` strings can be used to select the same data type. Patterns used for matching for specific data types are listed below.

This is a short description of python regular expression, for more information see the regular expression syntax section of the Python Library Reference. Some of the regular expression syntax used in this function is:

‘`[]`’ – A sequence or set of characters to match to a single character. For example, ‘`[Ss]2`’ will match both ‘`S2`’ and ‘`s2`’.

‘`^`’ – Match the start of the string.

‘\$’ – Match the end of the string. For example, ‘`^[Ss]2$`’ will match ‘s2’ but not ‘S2f’ or ‘s2s’.

‘.’ – Match any character.

‘x\*’ – Match the character ‘x’ any number of times, for example ‘x’ will match, as will ‘xxxxx’

‘.\*’ – Match any sequence of characters of any length.

Importantly, do not supply a string for the data type containing regular expression. The regular expression is implemented so that various strings can be supplied which all match the same data type.

### Minimisation statistic data type string matching patterns

Data type	Object name	Patterns
Chi-squared statistic	‘chi2’	‘ <code>^[Cc]hi2\$</code> ’ or ‘ <code>^[Cc]hi[-_ ] [Ss]quare</code> ’
Iteration count	‘iter’	‘ <code>^[Ii]ter</code> ’
Function call count	‘f_count’	‘ <code>^[Ff].*[-_] [Cc]ount</code> ’
Gradient call count	‘g_count’	‘ <code>^[Gg].*[-_] [Cc]ount</code> ’
Hessian call count	‘h_count’	‘ <code>^[Hh].*[-_] [Cc]ount</code> ’

**Model-free data type string matching patterns**

Data type	Object name	Patterns
Local $\tau_m$	'tm'	'^tm\$'
Order parameter $S^2$	's2'	'^[Ss]2\$'
Order parameter $S_f^2$	's2f'	'^[Ss]2f\$'
Order parameter $S_s^2$	's2s'	'^[Ss]2s\$'
Correlation time $\tau_e$	'te'	'^te\$'
Correlation time $\tau_f$	'tf'	'^tf\$'
Correlation time $\tau_s$	'ts'	'^ts\$'
Chemical exchange	'rex'	'^[Rr]ex\$' or '[Cc]emical[ -_] [Ee]xchange'
Bond length	'r'	'^r\$' or '[Bb]ond[ -_] [Ll]ength'
CSA	'csa'	'^[Cc] [Ss] [Aa]\$'

**Reduced spectral density mapping data type string matching patterns**

Data type	Object name	Patterns
$J(0)$	'j0'	'^[Jj]0\$' or '[Jj](0)'
$J(\omega_X)$	'jwx'	'^[Jj]w[Xx]\$' or '[Jj](w[Xx])'
$J(\omega_H)$	'jwh'	'^[Jj]w[Hh]\$' or '[Jj](w[Hh])'
Bond length	'r'	'^r\$' or '[Bb]ond[ -_] [Ll]ength'
CSA	'csa'	'^[Cc] [Ss] [Aa]\$'

**NOE calculation data type string matching patterns**

Data type	Object name	Patterns
Reference intensity	'ref'	'^[Rr]ef\$' or '[Rr]ef[ -_] [Ii]nt'
Saturated intensity	'sat'	'^[Ss]at\$' or '[Ss]at[ -_] [Ii]nt'
NOE	'noe'	'^[Nn] [Oo] [Ee]\$'

### 3.2.16 `grid_search`

#### Synopsis

The grid search function.

#### Defaults

**`grid_search`**(self, run=None, lower=None, upper=None, inc=21, constraints=1, print\_flag=1)

#### Keyword Arguments

**run:** The name of the run to apply the grid search to.

**lower:** An array of the lower bound parameter values for the grid search. The length of the array should be equal to the number of parameters in the model.

**upper:** An array of the upper bound parameter values for the grid search. The length of the array should be equal to the number of parameters in the model.

**inc:** The number of increments to search over. If a single integer is given then the number of increments will be equal in all dimensions. Different numbers of increments in each direction can be set if '**inc**' is set to an array of integers of length equal to the number of parameters.

**constraints:** A flag specifying whether the parameters should be constrained. The default is to turn constraints on (**constraints**=1).

**print\_flag:** The amount of information to print to screen. Zero corresponds to minimal output while higher values increase the amount of output. The default value is 1.

### 3.2.17 `init_data`

#### Synopsis

Function for reinitialising `self.relax.data`

#### Defaults

**`init_data`**(`self`)

### 3.2.18 `intro_off`

#### Synopsis

Function for turning the function introductions off.

#### Defaults

**`intro_off`**(self)



### 3.2.19 `intro_on`

#### Synopsis

Function for turning the function introductions on.

#### Defaults

**`intro_on`**(self)

### 3.2.20 `jw_mapping.set_frq`

#### Synopsis

Function for selecting which relaxation data to use in the  $J(\omega)$  mapping.

#### Defaults

**`jw_mapping.set_frq`**(self, run=None, frq=None)

#### Keyword Arguments

run: The name of the run.

frq: The spectrometer frequency in Hz.

#### Description

This function will select the relaxation data to use in the reduced spectral density mapping corresponding to the given frequency.

#### Examples

```
relax> jw_mapping.set_frq('jw', 600.0 * 1e6)
relax> jw_mapping.set_frq(run='jw', frq=600.0 * 1e6)
```

### 3.2.21 minimise

#### Synopsis

Minimisation function.

#### Defaults

**minimise**(self, \*args, \*\*keywords)

#### Arguments

The arguments, which should all be strings, specify the minimiser as well as its options. A minimum of one argument is required. As this calls the function ‘**generic\_minimise**’ the full list of allowed arguments is shown below in the reproduced ‘**generic\_minimise**’ docstring. Ignore all sections except those labelled as minimisation algorithms and minimisation options. Also do not select the Method of Multipliers constraint algorithm as this is used in combination with the given minimisation algorithm if the keyword argument ‘**constraints**’ is set to 1. The grid search algorithm should also not be selected as this is accessed using the ‘**grid**’ function instead. The first argument passed will be set to the minimisation algorithm while all other arguments will be set to the minimisation options.

Keyword arguments differ from normal arguments having the form ‘**keyword = value**’. All arguments must precede keyword arguments in python. For more information see the examples section below or the python tutorial.

#### Keyword Arguments

**run**: The name of the run.

**func\_tol**: The function tolerance. This is used to terminate minimisation once the function value between iterations is less than the tolerance. The default value is 1e-25.

**grad\_tol**: The gradient tolerance. Minimisation is terminated if the current gradient value is less than the tolerance. The default value is None.

**max\_iterations**: The maximum number of iterations. The default value is 1e7.

**constraints**: A flag specifying whether the parameters should be constrained. The default is to turn constraints on (constraints=1).

**scaling**: The diagonal scaling flag. The default that scaling is on (scaling=1).

**print\_flag**: The amount of information to print to screen. Zero corresponds to minimal output while higher values increase the amount of output. The default value is 1.

## Diagonal scaling

Diagonal scaling is the transformation of parameter values such that each value has a similar order of magnitude. Certain minimisation techniques, for example the trust region methods, perform extremely poorly with badly scaled problems. In addition, methods which are insensitive to scaling such as Newton minimisation may still benefit due to the minimisation of round off errors.

In Model-free analysis for example, if  $S^2 = 0.5$ ,  $\tau_e = 200$  ps, and  $R_{ex} = 15$  1/s at 600 MHz, the unscaled parameter vector would be  $[0.5, 2.0\text{e-}10, 1.055\text{e-}18]$ .  $R_{ex}$  is divided by  $(2 * \pi * 600,000,000)**2$  to make it field strength independent. The scaling vector for this model may be something like  $[1.0, 1\text{e-}9, 1/(2 * \pi * 6\text{e}8)**2]$ . By dividing the unscaled parameter vector by the scaling vector the scaled parameter vector is  $[0.5, 0.2, 15.0]$ . To revert to the original unscaled parameter vector, the scaled parameter vector and scaling vector are multiplied.

## Examples

To minimise the model-free run ‘m4’ using Newton minimisation together with the GMW81 Hessian modification algorithm, the More and Thuente line search algorithm, a function tolerance of  $1\text{e-}25$ , no gradient tolerance, a maximum of 10,000,000 iterations, constraints turned on to limit parameter values, and have normal printout, type any combination of:

```
relax> minimise('newton', run='m4')
relax> minimise('Newton', run='m4')
relax> minimise('newton', 'gmw', run='m4')
relax> minimise('newton', 'mt', run='m4')
relax> minimise('newton', 'gmw', 'mt', run='m4')
relax> minimise('newton', 'mt', 'gmw', run='m4')
relax> minimise('newton', run='m4', func_tol=1e-25)
relax> minimise('newton', run='m4', func_tol=1e-25, grad_tol=None)
relax> minimise('newton', run='m4', max_iter=1e7)
relax> minimise('newton', run=name, constraints=1, max_iter=1e7)
relax> minimise('newton', run='m4', print_flag=1)
```

To minimise the model-free run ‘m5’ using constrained Simplex minimisation with a maximum of 5000 iterations, type:

```
relax> minimise('simplex', run='m5', constraints=1, max_iter=5000)
```

## Note

All the text which follows is a reproduction of the docstring of the `generic_minimise` function. Only take note of the minimisation algorithms and minimisation options sections, the other sections are not relevant for this function. The Grid search and Method of

Multipliers algorithms CANNOT be selected as minimisation algorithms for this function.

The section entitled Keyword Arguments is also completely inaccessible therefore please ignore that text.

Generic minimisation function.

This is a generic function which can be used to access all minimisers using the same set of function arguments. These are the function tolerance value for convergence tests, the maximum number of iterations, a flag specifying which data structures should be returned, and a flag specifying the amount of detail to print to screen.

### Keyword Arguments

**func:** The function which returns the value.

**dfunc:** The function which returns the gradient.

**d2func:** The function which returns the Hessian.

**args:** The tuple of arguments to supply to the functions func, dfunc, and d2func.

**x0:** The vector of initial parameter value estimates (as an array).

**min\_algor:** A string specifying which minimisation technique to use.

**min\_options:** A tuple to pass to the minimisation function as the min\_options keyword.

**func\_tol:** The function tolerance value. Once the function value between iterations decreases below this value, minimisation is terminated.

**grad\_tol:** The gradient tolerance value.

**maxiter:** The maximum number of iterations.

**A:** Linear constraint matrix  $m \times n$  ( $A \cdot x \geq b$ ).

**b:** Linear constraint scalar vector ( $A \cdot x \geq b$ ).

**l:** Lower bound constraint vector ( $l \leq x \leq u$ ).

**u:** Upper bound constraint vector ( $l \leq x \leq u$ ).

**c:** User supplied constraint function.

**dc:** User supplied constraint gradient function.

**d2c:** User supplied constraint Hessian function.

**full\_output:** A flag specifying which data structures should be returned.

**print\_flag:** A flag specifying how much information should be printed to standard output during minimisation. 0 means no output, 1 means minimal output, and values above 1 increase the amount of output printed.

## Minimisation output

The following values of the ‘full\_output’ flag will return, in tuple form, the following data

0 – ‘xk’,

1 – ‘(xk, fk, k, f\_count, g\_count, h\_count, warning)’,

where the data names correspond to

‘xk’ – The array of minimised parameter values,

‘fk’ – The minimised function value,

‘k’ – The number of iterations,

‘f\_count’ – The number of function calls,

‘g\_count’ – The number of gradient calls,

‘h\_count’ – The number of Hessian calls,

‘warning’ – The warning string.

## Minimisation algorithms

A minimisation function is selected if the minimisation algorithm argument, which should be a string, matches a certain pattern. Because the python regular expression ‘match’ statement is used, various strings can be supplied to select the same minimisation algorithm. Below is a list of the minimisation algorithms available together with the corresponding patterns.

This is a short description of python regular expression, for more information, see the regular expression syntax section of the Python Library Reference. Some of the regular expression syntax used in this function is:

‘[]’ – A sequence or set of characters to match to a single character. For example, ‘[Nn]ewton’ will match both ‘Newton’ and ‘newton’.

‘^’ – Match the start of the string.

‘\$’ – Match the end of the string. For example, ‘^[Ll][Mm]\$’ will match ‘lm’ and ‘LM’ but will not match if characters are placed either before or after these strings.

To select a minimisation algorithm, set the argument to a string which matches the given pattern.

Parameter initialisation methods:

Minimisation algorithm	Patterns
Grid search	<code>^[Gg]rid</code>

Unconstrained line search methods:

Minimisation algorithm	Patterns
Back-and-forth coordinate descent	<code>^[Cc][Dd]\$</code> or <code>^[Cc]oordinate[_][Dd]escent\$</code>
Steepest descent	<code>^[Ss][Dd]\$</code> or <code>^[Ss]teepest[_][Dd]escent\$</code>
Quasi-Newton BFGS	<code>^[Bb][Ff][Gg][Ss]\$</code>
Newton	<code>^[Nn]ewton\$</code>
Newton-CG	<code>^[Nn]ewton[_][Cc][Gg]\$</code> or <code>^[Nn][Cc][Gg]\$</code>

Unconstrained trust-region methods:

Minimisation algorithm	Patterns
Cauchy point	<code>^[Cc]auchy</code>
Dogleg	<code>^[Dd]ogleg</code>
CG-Steihaug	<code>^[Cc][Gg][_][Ss]teihaug</code> or <code>^[Ss]teihaug</code>
Exact trust region	<code>^[Ee]xact</code>

Unconstrained conjugate gradient methods:

Minimisation algorithm	Patterns
Fletcher-Reeves	<code>^[Ff][Rr]\$</code> or <code>^[Ff]letcher[_][Rr]eeves\$</code>
Polak-Ribière	<code>^[Pp][Rr]\$</code> or <code>^[Pp]olak[_][Rr]ibiere\$</code>
Polak-Ribière +	<code>^[Pp][Rr]\+\$</code> or <code>^[Pp]olak[_][Rr]ibiere\+\$</code>
Hestenes-Stiefel	<code>^[Hh][Ss]\$</code> or <code>^[Hh]estenes[_][Ss]tiefel\$</code>

Miscellaneous unconstrained methods:

Minimisation algorithm	Patterns
Simplex	<code>^[Ss]implex\$</code>
Levenberg-Marquardt	<code>^[Ll][Mm]\$</code> or <code>^[Ll]evenburg-[Mm]arquardt\$</code>

Constrained methods:

Minimisation algorithm	Patterns
Method of Multipliers	<code>^[Mm][Oo][Mm]\$</code> or <code>^[Mm]ethod of [Mm]ultipliers\$</code>

### Minimisation options

The minimisation options can be given in any order.

Line search algorithms. These are used in the line search methods and the conjugate gradient methods. The default is the Backtracking line search.

Line search algorithm	Patterns
Backtracking line search	<code>^[Bb]ack</code>
Nocedal and Wright interpolation based line search	<code>^[Nn][Ww][Ii]</code> or <code>^[Nn]ocedal[ ][Ww]right[ ][Ii]nt</code>
Nocedal and Wright line search for the Wolfe conditions	<code>^[Nn][Ww][Ww]</code> or <code>^[Nn]ocedal[ ][Ww]right[ ][Ww]olfe</code>
More and Thuente line search	<code>^[Mm][Tt]</code> or <code>^[Mm]ore[ ][Tt]huyente\$</code>
No line search	<code>^[Nn]one\$</code>

Hessian modifications. These are used in the Newton, Dogleg, and Exact trust region algorithms.

Hessian modification	Patterns
Unmodified Hessian	<code>[Nn]one</code>
Eigenvalue modification	<code>^[Ee]igen</code>
Cholesky with added multiple of the identity	<code>^[Cc]hol</code>
The Gill, Murray, and Wright modified Cholesky algorithm	<code>^[Gg][Mm][Ww]\$</code>
The Schnabel and Eskow 1999 algorithm	<code>^[Ss][Ee]99</code>

Hessian type, these are used in a few of the trust region methods including the Dogleg and Exact trust region algorithms. In these cases, when the Hessian type is set to Newton, a Hessian modification can also be supplied as above. The default Hessian type is Newton, and the default Hessian modification when Newton is selected is the GMW algorithm.



Hessian type	Patterns
Quasi-Newton BFGS	<code>^[Bb] [Ff] [Gg] [Ss]\$</code>
Newton	<code>^[Nn]ewton\$</code>

For Newton minimisation, the default line search algorithm is the More and Thiente line search, while the default Hessian modification is the GMW algorithm.

### 3.2.22 `model_free.copy`

#### Synopsis

Function for copying model-free data from `run1` to `run2`.

#### Defaults

**`model_free.copy`**(self, run1=None, run2=None, sim=None)

#### Keyword Arguments

`run1`: The name of the run to copy the sequence from.

`run2`: The name of the run to copy the sequence to.

`sim`: The simulation number.

#### Description

This function will copy all model-free data from ‘`run1`’ to ‘`run2`’. Any model-free data in ‘`run2`’ will be overwritten. If the argument ‘`sim`’ is an integer, then only data from that simulation will be copied.

#### Examples

To copy all model-free data from the run ‘`m1`’ to the run ‘`m2`’, type:

```
relax> model_free.copy('m1', 'm2')
```

```
relax> model_free.copy(run1='m1', run2='m2')
```

### 3.2.23 `model_free.create_model`

#### Synopsis

Function to create a model-free model.

#### Defaults

**`model_free.create_model`**(self, run=None, model=None, equation=None, params=None, res\_num=None)

#### Keyword Arguments

**run**: The run to assign the values to.

**model**: The name of the model-free model.

**equation**: The model-free equation.

**params**: The array of parameter names of the model.

**res\_num**: The residue number.

#### Model-free equation

**'mf\_orig'** selects the original model-free equations with parameters  $\{S^2, \tau_e\}$ . **'mf\_ext'** selects the extended model-free equations with parameters  $\{S_f^2, \tau_f, S^2, \tau_s\}$ . **'mf\_ext2'** selects the extended model-free equations with parameters  $\{S_f^2, \tau_f, S_s^2, \tau_s\}$ .

#### Model-free parameters

The following parameters are accepted for the original model-free equation:

**'S2'** – The square of the generalised order parameter.

**'te'** – The effective correlation time.

The following parameters are accepted for the extended model-free equation:

**'S2f'** – The square of the generalised order parameter of the faster motion.

**'tf'** – The effective correlation time of the faster motion.

**'S2'** – The square of the generalised order parameter  $S^2 = S_f^2 * S_s^2$ .

**'ts'** – The effective correlation time of the slower motion.

The following parameters are accepted for the extended 2 model-free equation:

‘S2f’ – The square of the generalised order parameter of the faster motion.

‘tf’ – The effective correlation time of the faster motion.

‘S2s’ – The square of the generalised order parameter of the slower motion.

‘ts’ – The effective correlation time of the slower motion.

The following parameters are accepted for all equations:

‘Rex’ – The chemical exchange relaxation.

‘r’ – The average bond length  $\langle r \rangle$ .

‘CSA’ – The chemical shift anisotropy.

## Residue number

If ‘res\_num’ is supplied as an integer then the model will only be created for that residue, otherwise the model will be created for all residues.

## Examples

The following commands will create the model-free model ‘m1’ which is based on the original model-free equation and contains the single parameter ‘S2’.

```
relax> model_free.create_model('m1', 'm1', 'mf_orig', ['S2'])
```

```
relax> model_free.create_model(run='m1', model='m1', params=['S2'], equation='mf_orig')
```

The following commands will create the model-free model ‘large\_model’ which is based on the extended model-free equation and contains the seven parameters ‘S2f’, ‘tf’, ‘S2’, ‘ts’, ‘Rex’, ‘CSA’, ‘r’.

```
relax> model_free.create_model('test', 'large_model', 'mf_ext', ['S2f', 'tf', 'S2', 'ts', 'Rex', 'CSA', 'r'])
```

```
relax> model_free.create_model(run='test', model='large_model', params=['S2f', 'tf', 'S2', 'ts', 'Rex', 'CSA', 'r'], equation='mf_ext')
```

### 3.2.24 `model_free.delete`

#### Synopsis

Function for deleting all model-free data corresponding to the run.

#### Defaults

**`model_free.delete`**(self, run=None)

#### Keyword Arguments

run: The name of the run.

#### Examples

To delete all model-free data corresponding to the run 'm2', type:

```
relax> model_free.delete('m2')
```

### 3.2.25 `model_free.remove_tm`

#### Synopsis

Function for removing the local  $\tau_m$  parameter from a model.

#### Defaults

**`model_free.remove_tm`**(self, run=None, res\_num=None)

#### Keyword Arguments

**run**: The run to assign the values to.

**res\_num**: The residue number.

#### Description

This function will remove the local  $\tau_m$  parameter from the model-free parameters of the given run. Model-free parameters must already exist within the run yet, if there is no local  $\tau_m$ , nothing will happen.

If no residue number is given, then the function will apply to all residues.

#### Examples

The following commands will remove the parameter ‘tm’ from the run ‘local\_tm’:

```
relax> model_free.remove_tm('local_tm')
```

```
relax> model_free.remove_tm(run='local_tm')
```

**3.2.26 model\_free.select\_model****Synopsis**

Function for the selection of a preset model-free model.

**Defaults**

**model\_free.select\_model**(self, run=None, model=None, res\_num=None)

**Keyword Arguments**

run: The run to assign the values to.

model: The name of the preset model.

**The preset models**

The standard preset model-free models are

‘m0’ – [],

‘m1’ – [ $S^2$ ],

‘m2’ – [ $S^2$ ,  $\tau_e$ ],

‘m3’ – [ $S^2$ ,  $R_{ex}$ ],

‘m4’ – [ $S^2$ ,  $\tau_e$ ,  $R_{ex}$ ],

‘m5’ – [ $S_f^2$ ,  $S^2$ ,  $\tau_s$ ],

‘m6’ – [ $S_f^2$ ,  $\tau_f$ ,  $S^2$ ,  $\tau_s$ ],

‘m7’ – [ $S_f^2$ ,  $S^2$ ,  $\tau_s$ ,  $R_{ex}$ ],

‘m8’ – [ $S_f^2$ ,  $\tau_f$ ,  $S^2$ ,  $\tau_s$ ,  $R_{ex}$ ],

‘m9’ – [ $R_{ex}$ ].

The preset model-free models with optimisation of the CSA value are

‘m10’ – [CSA],

‘m11’ – [CSA,  $S^2$ ],

‘m12’ – [CSA,  $S^2$ ,  $\tau_e$ ],

‘m13’ – [CSA,  $S^2$ ,  $R_{ex}$ ],

$$\begin{aligned}
\text{'m14'} &= [\text{CSA}, S^2, \tau_e, R_{ex}], \\
\text{'m15'} &= [\text{CSA}, S_f^2, S^2, \tau_s], \\
\text{'m16'} &= [\text{CSA}, S_f^2, \tau_f, S^2, \tau_s], \\
\text{'m17'} &= [\text{CSA}, S_f^2, S^2, \tau_s, R_{ex}], \\
\text{'m18'} &= [\text{CSA}, S_f^2, \tau_f, S^2, \tau_s, R_{ex}], \\
\text{'m19'} &= [\text{CSA}, R_{ex}].
\end{aligned}$$

The preset model-free models with optimisation of the bond length are

$$\begin{aligned}
\text{'m20'} &= [r], \\
\text{'m21'} &= [r, S^2], \\
\text{'m22'} &= [r, S^2, \tau_e], \\
\text{'m23'} &= [r, S^2, R_{ex}], \\
\text{'m24'} &= [r, S^2, \tau_e, R_{ex}], \\
\text{'m25'} &= [r, S_f^2, S^2, \tau_s], \\
\text{'m26'} &= [r, S_f^2, \tau_f, S^2, \tau_s], \\
\text{'m27'} &= [r, S_f^2, S^2, \tau_s, R_{ex}], \\
\text{'m28'} &= [r, S_f^2, \tau_f, S^2, \tau_s, R_{ex}], \\
\text{'m29'} &= [r, \text{CSA}, R_{ex}].
\end{aligned}$$

The preset model-free models with both optimisation of the bond length and CSA are

$$\begin{aligned}
\text{'m30'} &= [r, \text{CSA}], \\
\text{'m31'} &= [r, \text{CSA}, S^2], \\
\text{'m32'} &= [r, \text{CSA}, S^2, \tau_e], \\
\text{'m33'} &= [r, \text{CSA}, S^2, R_{ex}], \\
\text{'m34'} &= [r, \text{CSA}, S^2, \tau_e, R_{ex}], \\
\text{'m35'} &= [r, \text{CSA}, S_f^2, S^2, \tau_s], \\
\text{'m36'} &= [r, \text{CSA}, S_f^2, \tau_f, S^2, \tau_s], \\
\text{'m37'} &= [r, \text{CSA}, S_f^2, S^2, \tau_s, R_{ex}], \\
\text{'m38'} &= [r, \text{CSA}, S_f^2, \tau_f, S^2, \tau_s, R_{ex}], \\
\text{'m39'} &= [r, \text{CSA}, R_{ex}].
\end{aligned}$$



Warning: The models in the thirties range fail when using standard  $R_1$ ,  $R_1$ , and NOE relaxation data. This is due to the extreme flexibility of these models where a change in the parameter ‘ $r$ ’ is compensated by a corresponding change in the parameter ‘ $CSA$ ’ and vice versa.

Additional preset model-free models, which are simply extensions of the above models with the addition of a local  $\tau_m$  parameter are:

$$\begin{aligned}
\text{‘tm0’} &= [\tau_m], \\
\text{‘tm1’} &= [\tau_m, S^2], \\
\text{‘tm2’} &= [\tau_m, S^2, \tau_e], \\
\text{‘tm3’} &= [\tau_m, S^2, R_{ex}], \\
\text{‘tm4’} &= [\tau_m, S^2, \tau_e, R_{ex}], \\
\text{‘tm5’} &= [\tau_m, S_f^2, S^2, \tau_s], \\
\text{‘tm6’} &= [\tau_m, S_f^2, \tau_f, S^2, \tau_s], \\
\text{‘tm7’} &= [\tau_m, S_f^2, S^2, \tau_s, R_{ex}], \\
\text{‘tm8’} &= [\tau_m, S_f^2, \tau_f, S^2, \tau_s, R_{ex}], \\
\text{‘tm9’} &= [\tau_m, R_{ex}].
\end{aligned}$$

The preset model-free models with optimisation of the CSA value are

$$\begin{aligned}
\text{‘tm10’} &= [\tau_m, CSA], \\
\text{‘tm11’} &= [\tau_m, CSA, S^2], \\
\text{‘tm12’} &= [\tau_m, CSA, S^2, \tau_e], \\
\text{‘tm13’} &= [\tau_m, CSA, S^2, R_{ex}], \\
\text{‘tm14’} &= [\tau_m, CSA, S^2, \tau_e, R_{ex}], \\
\text{‘tm15’} &= [\tau_m, CSA, S_f^2, S^2, \tau_s], \\
\text{‘tm16’} &= [\tau_m, CSA, S_f^2, \tau_f, S^2, \tau_s], \\
\text{‘tm17’} &= [\tau_m, CSA, S_f^2, S^2, \tau_s, R_{ex}], \\
\text{‘tm18’} &= [\tau_m, CSA, S_f^2, \tau_f, S^2, \tau_s, R_{ex}], \\
\text{‘tm19’} &= [\tau_m, CSA, R_{ex}].
\end{aligned}$$

The preset model-free models with optimisation of the bond length are

$$\text{‘tm20’} = [\tau_m, r],$$

`'tm21'` –  $[\tau_m, r, S^2]$ ,  
`'tm22'` –  $[\tau_m, r, S^2, \tau_e]$ ,  
`'tm23'` –  $[\tau_m, r, S^2, R_{ex}]$ ,  
`'tm24'` –  $[\tau_m, r, S^2, \tau_e, R_{ex}]$ ,  
`'tm25'` –  $[\tau_m, r, S_f^2, S^2, \tau_s]$ ,  
`'tm26'` –  $[\tau_m, r, S_f^2, \tau_f, S^2, \tau_s]$ ,  
`'tm27'` –  $[\tau_m, r, S_f^2, S^2, \tau_s, R_{ex}]$ ,  
`'tm28'` –  $[\tau_m, r, S_f^2, \tau_f, S^2, \tau_s, R_{ex}]$ ,  
`'tm29'` –  $[\tau_m, r, \text{CSA}, R_{ex}]$ .

The preset model-free models with both optimisation of the bond length and CSA are

`'tm30'` –  $[\tau_m, r, \text{CSA}]$ ,  
`'tm31'` –  $[\tau_m, r, \text{CSA}, S^2]$ ,  
`'tm32'` –  $[\tau_m, r, \text{CSA}, S^2, \tau_e]$ ,  
`'tm33'` –  $[\tau_m, r, \text{CSA}, S^2, R_{ex}]$ ,  
`'tm34'` –  $[\tau_m, r, \text{CSA}, S^2, \tau_e, R_{ex}]$ ,  
`'tm35'` –  $[\tau_m, r, \text{CSA}, S_f^2, S^2, \tau_s]$ ,  
`'tm36'` –  $[\tau_m, r, \text{CSA}, S_f^2, \tau_f, S^2, \tau_s]$ ,  
`'tm37'` –  $[\tau_m, r, \text{CSA}, S_f^2, S^2, \tau_s, R_{ex}]$ ,  
`'tm38'` –  $[\tau_m, r, \text{CSA}, S_f^2, \tau_f, S^2, \tau_s, R_{ex}]$ ,  
`'tm39'` –  $[\tau_m, r, \text{CSA}, R_{ex}]$ .

## Residue number

If `'res_num'` is supplied as an integer then the model will only be selected for that residue, otherwise the model will be selected for all residues.

## Examples

To pick model `'m1'` for all selected residues and assign it to the run `'mixed'`, type:

```

relax> model_free.select_model('mixed', 'm1')
relax> model_free.select_model(run='mixed', model='m1')
```

**3.2.27 model\_selection****Synopsis**

Function for model selection.

**Defaults**

**model\_selection**(self, method=None, modsel\_run=None, runs=None)

**Keyword arguments**

**method**: The model selection technique (see below).

**modsel\_run**: The run name to assign to the results of model selection.

**runs**: An array containing the names of all runs to include in model selection.

**Description**

The following model selection methods are supported:

**AIC**: Akaike's Information Criteria.

**AICc**: Small sample size corrected AIC.

**BIC**: Bayesian or Schwarz Information Criteria.

**Bootstrap**: Bootstrap model selection.

**CV**: Single-item-out cross-validation.

**Expect**: The expected overall discrepancy (the true values of the parameters are required).

**Farrow**: Old model-free method by Farrow et al., 1994.

**Palmer**: Old model-free method by Mandel et al., 1995.

**Overall**: The realised overall discrepancy (the true values of the parameters are required).

For the methods 'Bootstrap', 'Expect', and 'Overall', the function 'monte\_carlo' should have previously been run with the type argument set to the appropriate value to modify its behaviour.

If the runs argument is not supplied then all runs currently set or loaded will be used for model selection, although this could cause problems.

### Example

For model-free analysis, if the preset models 1 to 5 are minimised and loaded into the program, the following commands will carry out AIC model selection and assign the results to the run name 'mixed':

```
relax> model_selection('AIC', 'mixed')
```

```
relax> model_selection(method='AIC', modsel_run='mixed')
```

```
relax> model_selection('AIC', 'mixed', ['m1', 'm2', 'm3', 'm4', 'm5'])
```

```
relax> model_selection(method='AIC', modsel_run='mixed', runs=['m1', 'm2', 'm3', 'm4',  
'm5'])
```

**3.2.28 molmol.clear\_history****Synopsis**

Function for clearing the Molmol command history.

**Defaults**

**molmol.clear\_history**(self)

### 3.2.29 `molmol.command`

#### Synopsis

Function for executing a user supplied Molmol command.

#### Defaults

**`molmol.command`**(self, command)

#### Example

```
relax> molmol.command("InitAll yes")
```

### 3.2.30 molmol.view

#### Synopsis

Function for viewing the collection of molecules extracted from the PDB file.

#### Defaults

**molmol.view**(self, run=None)

#### Keyword Arguments

run: The name of the run which the PDB belongs to.

#### Example

```
relax> molmol.view('m1')  
relax> molmol.view(run='pdb')
```

### 3.2.31 monte\_carlo.create\_data

#### Synopsis

Function for creating simulation data.

#### Defaults

**monte\_carlo.create\_data**(self, run=None, method='back\_calc')

#### Keyword Arguments

run: The name of the run.

method: The simulation method.

#### Description

The method argument can either be set to 'back\_calc' or 'direct', the choice of which determines the simulation type. If the values or parameters of a run are calculated rather than minimised, this option will have no effect, hence, 'back\_calc' and 'direct' are identical.

For error analysis, the method argument should be set to 'back\_calc' which will result in proper Monte Carlo simulations. The data used for each simulation is back calculated from the minimised model parameters and is randomised using Gaussian noise where the standard deviation is from the original error set. When the method is set to 'back\_calc', this function should only be called after the model or run is fully minimised.

The simulation type can be changed by setting the method argument to 'direct'. This will result in simulations which cannot be used in error analysis and which are no longer Monte Carlo simulations. However, these simulations are required for certain model selection techniques (see the documentation for the model selection function for details), and can be used for other purposes. Rather than the data being back calculated from the fitted model parameters, the data is generated by taking the original data and randomising using Gaussian noise with the standard deviations set to the original error set.

#### Monte Carlo Simulation Overview

For proper error analysis using Monte Carlo simulations, a sequence of function calls is required for running the various simulation components. The steps necessary for implementing Monte Carlo simulations are:

1. The measured data set together with the corresponding error set should be loaded into relax.



2. Either minimisation is used to optimise the parameters of the chosen model, or a calculation is run.
3. To initialise and turn on Monte Carlo simulations, the number of simulations,  $n$ , needs to be set.
4. The simulation data needs to be created either by back calculation from the fully minimised model parameters from step 2 or by direct calculation when values are calculated rather than minimised. The error set is used to randomise each simulation data set by assuming Gaussian errors. This creates a synthetic data set for each Monte Carlo simulation.
5. Prior to minimisation of the parameters of each simulation, initial parameter estimates are required. These are taken as the optimised model parameters. An alternative is to use a grid search for each simulation to generate initial estimates, however this is extremely computationally expensive. For the case where values are calculated rather than minimised, this step should be skipped (although the results will be unaffected if this is accidentally run).
6. Each simulation requires minimisation or calculation. The same techniques as used in step 2, excluding the grid search when minimising, should be used for the simulations.
7. Failed simulations are removed using the techniques of model elimination.
8. The model parameter errors are calculated from the distribution of simulation parameters.

Monte Carlo simulations can be turned on or off using functions within this class. Once the function for setting up simulations has been called, simulations will be turned on. The effect of having simulations turned on is that the functions used for minimisation (grid search, minimise, etc) or calculation will only affect the simulation parameters and not the model parameters. By subsequently turning simulations off using the appropriate function, the functions used in minimisation will affect the model parameters and not the simulation parameters.

An example, for model-free analysis, which includes only the functions required for implementing the above steps is:

```

relax> grid_search('m1', inc=11) # Step 2.
relax> minimise('newton', run='m1') # Step 2.
relax> monte_carlo.setup('m1', number=500) # Step 3.
relax> monte_carlo.create_data('m1', method='back_calc') # Step 4.
relax> monte_carlo.initial_values('m1') # Step 5.
relax> minimise('newton', run='m1') # Step 6.
relax> eliminate('m1') # Step 7.
relax> monte_carlo.error_analysis('m1') # Step 8.

```

An example for reduced spectral density mapping is:

```

relax> calc('600MHz') # Step 2.
relax> monte_carlo.setup('600MHz', number=500) # Step 3.

```

```
relax> monte_carlo.create_data('600MHz', method='back_calc') # Step 4.  
relax> calc('600MHz') # Step 6.  
relax> monte_carlo.error_analysis('600MHz') # Step 8.
```

### 3.2.32 monte\_carlo.error\_analysis

#### Synopsis

Function for calculating parameter errors from the Monte Carlo simulations.

#### Defaults

**monte\_carlo.error\_analysis**(self, run=None, prune=0.0)

#### Keyword Arguments

**run**: The name of the run.

**prune**: Legacy argument corresponding to ‘trim’ in Art Palmer’s Modelfree program.

#### Description

Parameter errors are calculated as the standard deviation of the distribution of parameter values. This function should never be used if parameter values are obtained by minimisation and the simulation data are generated using the method ‘direct’. The reason is because only true Monte Carlo simulations can give the true parameter errors.

The prune argument is legacy code which corresponds to the ‘trim’ option in Art Palmer’s Modelfree program. To remove failed simulations, the eliminate function should be used prior to this function. Eliminating the simulations specifically identifies and removes the failed simulations whereas the prune argument will only, in a few cases, positively identify failed simulations but only if severe parameter limits have been imposed. Most failed models will pass through the pruning process and hence cause a catastrophic increase in the parameter errors. If the argument must be used, the following must be taken into account. If the values or parameters of a run are calculated rather than minimised, the prune argument must be set to zero. The value of this argument is proportional to the number of simulations removed prior to error calculation. If prune is set to 0.0, all simulations are used for calculating errors, whereas a value of 1.0 excludes all data. In almost all cases prune must be set to zero, any value greater than zero will result in an underestimation of the error values. If a value is supplied, the lower and upper tails of the distribution of chi-squared values will be excluded from the error calculation.

#### Monte Carlo Simulation Overview

For proper error analysis using Monte Carlo simulations, a sequence of function calls is required for running the various simulation components. The steps necessary for implementing Monte Carlo simulations are:

1. The measured data set together with the corresponding error set should be loaded into relax.

2. Either minimisation is used to optimise the parameters of the chosen model, or a calculation is run.
3. To initialise and turn on Monte Carlo simulations, the number of simulations,  $n$ , needs to be set.
4. The simulation data needs to be created either by back calculation from the fully minimised model parameters from step 2 or by direct calculation when values are calculated rather than minimised. The error set is used to randomise each simulation data set by assuming Gaussian errors. This creates a synthetic data set for each Monte Carlo simulation.
5. Prior to minimisation of the parameters of each simulation, initial parameter estimates are required. These are taken as the optimised model parameters. An alternative is to use a grid search for each simulation to generate initial estimates, however this is extremely computationally expensive. For the case where values are calculated rather than minimised, this step should be skipped (although the results will be unaffected if this is accidentally run).
6. Each simulation requires minimisation or calculation. The same techniques as used in step 2, excluding the grid search when minimising, should be used for the simulations.
7. Failed simulations are removed using the techniques of model elimination.
8. The model parameter errors are calculated from the distribution of simulation parameters.

Monte Carlo simulations can be turned on or off using functions within this class. Once the function for setting up simulations has been called, simulations will be turned on. The effect of having simulations turned on is that the functions used for minimisation (grid search, minimise, etc) or calculation will only affect the simulation parameters and not the model parameters. By subsequently turning simulations off using the appropriate function, the functions used in minimisation will affect the model parameters and not the simulation parameters.

An example, for model-free analysis, which includes only the functions required for implementing the above steps is:

```

relax> grid_search('m1', inc=11) # Step 2.
relax> minimise('newton', run='m1') # Step 2.
relax> monte_carlo.setup('m1', number=500) # Step 3.
relax> monte_carlo.create_data('m1', method='back_calc') # Step 4.
relax> monte_carlo.initial_values('m1') # Step 5.
relax> minimise('newton', run='m1') # Step 6.
relax> eliminate('m1') # Step 7.
relax> monte_carlo.error_analysis('m1') # Step 8.
```

An example for reduced spectral density mapping is:

```

relax> calc('600MHz') # Step 2.
relax> monte_carlo.setup('600MHz', number=500) # Step 3.
```

```
relax> monte_carlo.create_data('600MHz', method='back_calc') # Step 4.  
relax> calc('600MHz') # Step 6.  
relax> monte_carlo.error_analysis('600MHz') # Step 8.
```

### 3.2.33 monte\_carlo.initial\_values

#### Synopsis

Function for setting the initial simulation parameter values.

#### Defaults

**monte\_carlo.initial\_values**(self, run=None)

#### Keyword Arguments

run: The name of the run.

#### Description

This function only effects runs where minimisation occurs and can therefore be skipped if the values or parameters of a run are calculated rather than minimised. However, if accidentally run in this case, the results will be unaffected. It should only be called after the model or run is fully minimised. Once called, the functions ‘**grid\_search**’ and ‘**minimise**’ will only effect the simulations and not the model parameters.

The initial values of the parameters for each simulation is set to the minimised parameters of the model. A grid search can be undertaken for each simulation instead, although this is computationally expensive and unnecessary. The minimisation function should be executed for a second time after running this function.

#### Monte Carlo Simulation Overview

For proper error analysis using Monte Carlo simulations, a sequence of function calls is required for running the various simulation components. The steps necessary for implementing Monte Carlo simulations are:

1. The measured data set together with the corresponding error set should be loaded into relax.
2. Either minimisation is used to optimise the parameters of the chosen model, or a calculation is run.
3. To initialise and turn on Monte Carlo simulations, the number of simulations,  $n$ , needs to be set.
4. The simulation data needs to be created either by back calculation from the fully minimised model parameters from step 2 or by direct calculation when values are calculated rather than minimised. The error set is used to randomise each simulation data set by assuming Gaussian errors. This creates a synthetic data set for each Monte Carlo simulation.

5. Prior to minimisation of the parameters of each simulation, initial parameter estimates are required. These are taken as the optimised model parameters. An alternative is to use a grid search for each simulation to generate initial estimates, however this is extremely computationally expensive. For the case where values are calculated rather than minimised, this step should be skipped (although the results will be unaffected if this is accidentally run).

6. Each simulation requires minimisation or calculation. The same techniques as used in step 2, excluding the grid search when minimising, should be used for the simulations.

7. Failed simulations are removed using the techniques of model elimination.

8. The model parameter errors are calculated from the distribution of simulation parameters.

Monte Carlo simulations can be turned on or off using functions within this class. Once the function for setting up simulations has been called, simulations will be turned on. The effect of having simulations turned on is that the functions used for minimisation (grid search, minimise, etc) or calculation will only affect the simulation parameters and not the model parameters. By subsequently turning simulations off using the appropriate function, the functions used in minimisation will affect the model parameters and not the simulation parameters.

An example, for model-free analysis, which includes only the functions required for implementing the above steps is:

```
relax> grid_search('m1', inc=11) # Step 2.
relax> minimise('newton', run='m1') # Step 2.
relax> monte_carlo.setup('m1', number=500) # Step 3.
relax> monte_carlo.create_data('m1', method='back_calc') # Step 4.
relax> monte_carlo.initial_values('m1') # Step 5.
relax> minimise('newton', run='m1') # Step 6.
relax> eliminate('m1') # Step 7.
relax> monte_carlo.error_analysis('m1') # Step 8.
```

An example for reduced spectral density mapping is:

```
relax> calc('600MHz') # Step 2.
relax> monte_carlo.setup('600MHz', number=500) # Step 3.
relax> monte_carlo.create_data('600MHz', method='back_calc') # Step 4.
relax> calc('600MHz') # Step 6.
relax> monte_carlo.error_analysis('600MHz') # Step 8.
```

### 3.2.34 monte\_carlo.off

#### Synopsis

Function for turning simulations off.

#### Defaults

**monte\_carlo.off**(self, run=None)

#### Keyword Arguments

run: The name of the run.

#### Monte Carlo Simulation Overview

For proper error analysis using Monte Carlo simulations, a sequence of function calls is required for running the various simulation components. The steps necessary for implementing Monte Carlo simulations are:

1. The measured data set together with the corresponding error set should be loaded into relax.
2. Either minimisation is used to optimise the parameters of the chosen model, or a calculation is run.
3. To initialise and turn on Monte Carlo simulations, the number of simulations,  $n$ , needs to be set.
4. The simulation data needs to be created either by back calculation from the fully minimised model parameters from step 2 or by direct calculation when values are calculated rather than minimised. The error set is used to randomise each simulation data set by assuming Gaussian errors. This creates a synthetic data set for each Monte Carlo simulation.
5. Prior to minimisation of the parameters of each simulation, initial parameter estimates are required. These are taken as the optimised model parameters. An alternative is to use a grid search for each simulation to generate initial estimates, however this is extremely computationally expensive. For the case where values are calculated rather than minimised, this step should be skipped (although the results will be unaffected if this is accidentally run).
6. Each simulation requires minimisation or calculation. The same techniques as used in step 2, excluding the grid search when minimising, should be used for the simulations.
7. Failed simulations are removed using the techniques of model elimination.
8. The model parameter errors are calculated from the distribution of simulation parameters.



Monte Carlo simulations can be turned on or off using functions within this class. Once the function for setting up simulations has been called, simulations will be turned on. The effect of having simulations turned on is that the functions used for minimisation (grid search, minimise, etc) or calculation will only affect the simulation parameters and not the model parameters. By subsequently turning simulations off using the appropriate function, the functions used in minimisation will affect the model parameters and not the simulation parameters.

An example, for model-free analysis, which includes only the functions required for implementing the above steps is:

```
relax> grid_search('m1', inc=11) # Step 2.  
relax> minimise('newton', run='m1') # Step 2.  
relax> monte_carlo.setup('m1', number=500) # Step 3.  
relax> monte_carlo.create_data('m1', method='back_calc') # Step 4.  
relax> monte_carlo.initial_values('m1') # Step 5.  
relax> minimise('newton', run='m1') # Step 6.  
relax> eliminate('m1') # Step 7.  
relax> monte_carlo.error_analysis('m1') # Step 8.
```

An example for reduced spectral density mapping is:

```
relax> calc('600MHz') # Step 2.  
relax> monte_carlo.setup('600MHz', number=500) # Step 3.  
relax> monte_carlo.create_data('600MHz', method='back_calc') # Step 4.  
relax> calc('600MHz') # Step 6.  
relax> monte_carlo.error_analysis('600MHz') # Step 8.
```

### 3.2.35 monte\_carlo.on

#### Synopsis

Function for turning simulations on.

#### Defaults

**monte\_carlo.on**(self, run=None)

#### Keyword Arguments

run: The name of the run.

#### Monte Carlo Simulation Overview

For proper error analysis using Monte Carlo simulations, a sequence of function calls is required for running the various simulation components. The steps necessary for implementing Monte Carlo simulations are:

1. The measured data set together with the corresponding error set should be loaded into relax.
2. Either minimisation is used to optimise the parameters of the chosen model, or a calculation is run.
3. To initialise and turn on Monte Carlo simulations, the number of simulations,  $n$ , needs to be set.
4. The simulation data needs to be created either by back calculation from the fully minimised model parameters from step 2 or by direct calculation when values are calculated rather than minimised. The error set is used to randomise each simulation data set by assuming Gaussian errors. This creates a synthetic data set for each Monte Carlo simulation.
5. Prior to minimisation of the parameters of each simulation, initial parameter estimates are required. These are taken as the optimised model parameters. An alternative is to use a grid search for each simulation to generate initial estimates, however this is extremely computationally expensive. For the case where values are calculated rather than minimised, this step should be skipped (although the results will be unaffected if this is accidentally run).
6. Each simulation requires minimisation or calculation. The same techniques as used in step 2, excluding the grid search when minimising, should be used for the simulations.
7. Failed simulations are removed using the techniques of model elimination.
8. The model parameter errors are calculated from the distribution of simulation parameters.

Monte Carlo simulations can be turned on or off using functions within this class. Once the function for setting up simulations has been called, simulations will be turned on. The effect of having simulations turned on is that the functions used for minimisation (grid search, minimise, etc) or calculation will only affect the simulation parameters and not the model parameters. By subsequently turning simulations off using the appropriate function, the functions used in minimisation will affect the model parameters and not the simulation parameters.

An example, for model-free analysis, which includes only the functions required for implementing the above steps is:

```
relax> grid_search('m1', inc=11) # Step 2.  
relax> minimise('newton', run='m1') # Step 2.  
relax> monte_carlo.setup('m1', number=500) # Step 3.  
relax> monte_carlo.create_data('m1', method='back_calc') # Step 4.  
relax> monte_carlo.initial_values('m1') # Step 5.  
relax> minimise('newton', run='m1') # Step 6.  
relax> eliminate('m1') # Step 7.  
relax> monte_carlo.error_analysis('m1') # Step 8.
```

An example for reduced spectral density mapping is:

```
relax> calc('600MHz') # Step 2.  
relax> monte_carlo.setup('600MHz', number=500) # Step 3.  
relax> monte_carlo.create_data('600MHz', method='back_calc') # Step 4.  
relax> calc('600MHz') # Step 6.  
relax> monte_carlo.error_analysis('600MHz') # Step 8.
```

### 3.2.36 monte\_carlo.setup

#### Synopsis

Function for setting up Monte Carlo simulations.

#### Defaults

**monte\_carlo.setup**(self, run=None, number=500)

#### Keyword Arguments

run: The name of the run.

number: The number of Monte Carlo simulations.

#### Description

This function must be called prior to any of the other Monte Carlo functions. The effect is that the number of simulations for the given run will be set and that simulations will be turned on.

#### Monte Carlo Simulation Overview

For proper error analysis using Monte Carlo simulations, a sequence of function calls is required for running the various simulation components. The steps necessary for implementing Monte Carlo simulations are:

1. The measured data set together with the corresponding error set should be loaded into relax.
2. Either minimisation is used to optimise the parameters of the chosen model, or a calculation is run.
3. To initialise and turn on Monte Carlo simulations, the number of simulations,  $n$ , needs to be set.
4. The simulation data needs to be created either by back calculation from the fully minimised model parameters from step 2 or by direct calculation when values are calculated rather than minimised. The error set is used to randomise each simulation data set by assuming Gaussian errors. This creates a synthetic data set for each Monte Carlo simulation.
5. Prior to minimisation of the parameters of each simulation, initial parameter estimates are required. These are taken as the optimised model parameters. An alternative is to use a grid search for each simulation to generate initial estimates, however this is extremely computationally expensive. For the case where values are calculated rather

than minimised, this step should be skipped (although the results will be unaffected if this is accidentally run).

6. Each simulation requires minimisation or calculation. The same techniques as used in step 2, excluding the grid search when minimising, should be used for the simulations.

7. Failed simulations are removed using the techniques of model elimination.

8. The model parameter errors are calculated from the distribution of simulation parameters.

Monte Carlo simulations can be turned on or off using functions within this class. Once the function for setting up simulations has been called, simulations will be turned on. The effect of having simulations turned on is that the functions used for minimisation (grid search, minimise, etc) or calculation will only affect the simulation parameters and not the model parameters. By subsequently turning simulations off using the appropriate function, the functions used in minimisation will affect the model parameters and not the simulation parameters.

An example, for model-free analysis, which includes only the functions required for implementing the above steps is:

```
relax> grid_search('m1', inc=11) # Step 2.
relax> minimise('newton', run='m1') # Step 2.
relax> monte_carlo.setup('m1', number=500) # Step 3.
relax> monte_carlo.create_data('m1', method='back_calc') # Step 4.
relax> monte_carlo.initial_values('m1') # Step 5.
relax> minimise('newton', run='m1') # Step 6.
relax> eliminate('m1') # Step 7.
relax> monte_carlo.error_analysis('m1') # Step 8.
```

An example for reduced spectral density mapping is:

```
relax> calc('600MHz') # Step 2.
relax> monte_carlo.setup('600MHz', number=500) # Step 3.
relax> monte_carlo.create_data('600MHz', method='back_calc') # Step 4.
relax> calc('600MHz') # Step 6.
relax> monte_carlo.error_analysis('600MHz') # Step 8.
```

### 3.2.37 noe.error

#### Synopsis

Function for setting the errors in the reference or saturated NOE spectra.

#### Defaults

```
noe.error(self,      run=None,      error=0.0,      spectrum_type=None,      res_num=None,  
res_name=None)
```

#### Keyword Arguments

**run**: The name of the run.

**error**: The error.

**spectrum\_type**: The type of spectrum.

**res\_num**: The residue number.

**res\_name**: The residue name.

#### Description

The **spectrum\_type** argument can have the following values:

**‘ref’** – The NOE reference spectrum.

**‘sat’** – The NOE spectrum with proton saturation turned on.

If the **‘res\_num’** and **‘res\_name’** arguments are left as the defaults of None, then the error value for all residues will be set to the supplied value. Otherwise the residue number can be set to either an integer for selecting a single residue or a python regular expression string for selecting multiple residues. The residue name argument must be a string and can use regular expression as well.

### 3.2.38 noe.read

#### Synopsis

Function for reading peak intensities from a file for NOE calculations.

#### Defaults

**noe.read**(self, run=None, file=None, dir=None, spectrum\_type=None, format='sparky', heteronuc='N', proton='HN', int\_col=None)

#### Keyword Arguments

**run**: The name of the run.

**file**: The name of the file containing the sequence data.

**dir**: The directory where the file is located.

**spectrum\_type**: The type of spectrum.

**format**: The type of file containing peak intensities.

**heteronuc**: The name of the heteronucleus as specified in the peak intensity file.

**proton**: The name of the proton as specified in the peak intensity file.

**int\_col**: The column containing the peak intensity data (for a non-standard formatted file).

#### Description

The peak intensity can either be from peak heights or peak volumes.

The 'spectrum\_type' argument can have the following values:

'ref' – The NOE reference spectrum.

'sat' – The NOE spectrum with proton saturation turned on.

The 'format' argument can currently be set to:

'sparky'

'xeasy'

If the ‘**format**’ argument is set to ‘**sparky**’, the file should be a Sparky peak list saved after typing the command ‘**lt**’. The default is to assume that columns 0, 1, 2, and 3 (1<sup>st</sup>, 2<sup>nd</sup>, 3<sup>rd</sup>, and 4<sup>th</sup>) contain the Sparky assignment, w1, w2, and peak intensity data respectively. The frequency data w1 and w2 are ignored while the peak intensity data can either be the peak height or volume displayed by changing the window options. If the peak intensity data is not within column 3, set the argument ‘**int\_col**’ to the appropriate value (column numbering starts from 0 rather than 1).

If the ‘**format**’ argument is set to ‘**xeasy**’, the file should be the saved XEasy text window output of the list peak entries command, ‘**tw**’ followed by ‘**le**’. As the columns are fixed, the peak intensity column is hardwired to number 10 (the 11<sup>th</sup> column) which contains either the peak height or peak volume data. Because the columns are fixed, the ‘**int\_col**’ argument will be ignored.

The ‘**heteronuc**’ and ‘**proton**’ arguments should be set respectively to the name of the heteronucleus and proton in the file. Only those lines which match these labels will be used.

## Examples

To read the reference and saturated spectra peak heights from the Sparky formatted files ‘**ref.list**’ and ‘**sat.list**’ to the run ‘**noe**’, type:

```
relax> noe.read('noe', file='ref.list', spectrum_type='ref')
relax> noe.read('noe', file='sat.list', spectrum_type='sat')
```

To read the reference and saturated spectra peak heights from the XEasy formatted files ‘**ref.text**’ and ‘**sat.text**’ to the run ‘**noe**’, type:

```
relax> noe.read('noe', file='ref.text', spectrum_type='ref', format='xeasy')
relax> noe.read('noe', file='sat.text', spectrum_type='sat', format='xeasy')
```



### 3.2.39 nuclei

#### Synopsis

Function for setting the gyromagnetic ratio of the heteronucleus.

#### Defaults

**nuclei**(self, heteronuc='N')

#### Keyword arguments

heteronuc: The type of heteronucleus.

#### Description

The heteronuc argument can be set to the following strings:

**N** – Nitrogen, -2.7126e7

**C** – Carbon, 2.2e7

### 3.2.40 palmer.create

#### Synopsis

Function for creating the Modelfree4 input files.

#### Defaults

**palmer.create**(self, run=None, dir=None, force=0, diff\_search='none', sims=0, sim\_type='pred', trim=0, steps=20, constraints=1, nucleus='15N', atom1='N', atom2='H')

#### Keyword Arguments

run: The name of the run.

dir: The directory to place the files. The default is the value of 'run'.

force: A flag which if set to 1 will cause the results file to be overwritten if it already exists.

diff\_search: See the Modelfree4 manual for 'diffusion\_search'.

sims: The number of Monte Carlo simulations.

sim\_type: See the Modelfree4 manual.

trim: See the Modelfree4 manual.

steps: See the Modelfree4 manual.

constraints: A flag specifying whether the parameters should be constrained. The default is to turn constraints on (constraints=1).

nucleus: A three letter string describing the nucleus type, ie 15N, 13C, etc.

atom1: The symbol of the X nucleus in the pdb file.

atom2: The symbol of the H nucleus in the pdb file.

#### Description

The following files are created

```
'dir/mfin',  
'dir/mfdata',  
'dir/mfpar',  
'dir/mfmodel',
```

`'dir/run.sh'.`

The file `'run/run.sh'` contains the single command,

`'modelfree4 -i mfin -d mfddata -p mfpar -m mfmodel -o mfout -e out'`,

which can be used to execute `modelfree4`.

### 3.2.41 palmer.execute

#### Synopsis

Function for executing Modelfree4.

#### Defaults

**palmer.execute**(self, run=None, dir=None, force=0)

#### Keyword Arguments

run: The name of the run.

dir: The directory to place the files. The default is the value of 'run'.

force: A flag which if set to 1 will cause the results file to be overwritten if it already exists.

#### Description

Modelfree 4 will be executed as

```
'modelfree4 -i mfin -d mfddata -p mfpar -m mfmodel -o mfout -e out'
```

If a PDB file is loaded and non-isotropic diffusion is selected, then the file name will be placed on the command line as '-s `pdb_file_name`'.

### 3.2.42 palmer.extract

#### Synopsis

Function for extracting data from the Modelfree4 ‘mfout’ star formatted file.

#### Defaults

**palmer.extract**(self, run=None, dir=None)

#### Keyword Arguments

**run**: The name of the run.

**dir**: The directory where the file ‘mfout’ is found. The default is the value of ‘run’.

### 3.2.43 pdb

#### Synopsis

The pdb loading function.

#### Defaults

**pdb**(self, run=None, file=None, dir=None, model=None, heteronuc='N', proton='H', load\_seq=1)

#### Keyword Arguments

run: The run to assign the structure to.

file: The name of the PDB file.

dir: The directory where the file is located.

model: The PDB model number.

heteronuc: The name of the heteronucleus as specified in the PDB file.

proton: The name of the proton as specified in the PDB file.

load\_seq: A flag specifying whether the sequence should be loaded from the PDB file.

#### Description

To load a specific model from the PDB file, set the model flag to an integer  $i$ . The structure beginning with the line 'MODEL  $i$ ' in the PDB file will be loaded. Otherwise all structures will be loaded starting from the model number 1.

To load the sequence from the PDB file, set the 'load\_seq' flag to 1. If the sequence has previously been loaded, then this flag will be ignored.

Once the PDB structures are loaded, unit XH bond vectors will be calculated. The vectors are calculated using the atomic coordinates of the atoms specified by the arguments heteronuc and proton. If more than one model structure is loaded, the unit XH vectors for each model will be calculated and the final unit XH vector will be taken as the average.

#### Example

To load all structures from the PDB file 'test.pdb' in the directory '~/pdb' for use in the model-free analysis run 'm8' where the heteronucleus in the PDB file is 'N' and the proton is 'H', type:

```
relax> pdb('m8', 'test.pdb', '~/pdb', 1, 'N', 'H')
```

```
relax> pdb(run='m8', file='test.pdb', dir='pdb', model=1, heteronuc='N', proton='H')
```

To load the 10<sup>th</sup> model from the file 'test.pdb', use:

```
relax> pdb('m1', 'test.pdb', model=10)
```

```
relax> pdb(run='m1', file='test.pdb', model=10)
```

### 3.2.44 `relax_data.back_calc`

#### Synopsis

Function for back calculating relaxation data.

#### Defaults

**`relax_data.back_calc`**(self, run=None, ri\_label=None, frq\_label=None, frq=None)

#### Keyword Arguments

run: The name of the run.

ri\_label: The relaxation data type, ie 'R1', 'R2', or 'NOE'.

frq\_label: The field strength label.

frq: The spectrometer frequency in Hz.



### 3.2.45 relax\_data.copy

#### Synopsis

Function for copying relaxation data from run1 to run2.

#### Defaults

**relax\_data.copy**(self, run1=None, run2=None, ri\_label=None, frq\_label=None)

#### Keyword Arguments

run1: The name of the run to copy the sequence from.

run2: The name of the run to copy the sequence to.

ri\_label: The relaxation data type, ie 'R1', 'R2', or 'NOE'.

frq\_label: The field strength label.

#### Description

This function will copy relaxation data from 'run1' to 'run2'. If ri\_label and frq\_label are not given then all relaxation data will be copied, otherwise only a specific data set will be copied.

#### Examples

To copy all relaxation data from run 'm1' to run 'm9', type one of:

```
relax> relax_data.copy('m1', 'm9')
```

```
relax> relax_data.copy(run1='m1', run2='m9')
```

```
relax> relax_data.copy('m1', 'm9', None, None)
```

```
relax> relax_data.copy(run1='m1', run2='m9', ri_label=None, frq_label=None)
```

To copy only the NOE relaxation data with the frq\_label of '800' from 'm3' to 'm6', type one of:

```
relax> relax_data.copy('m3', 'm6', 'NOE', '800')
```

```
relax> relax_data.copy(run1='m3', run2='m6', ri_label='NOE', frq_label='800')
```

### 3.2.46 `relax_data.delete`

#### Synopsis

Function for deleting the relaxation data corresponding to `ri_label` and `frq_label`.

#### Defaults

**`relax_data.delete`**(self, run=None, ri\_label=None, frq\_label=None)

#### Keyword Arguments

`run`: The name of the run.

`ri_label`: The relaxation data type, ie ‘R1’, ‘R2’, or ‘NOE’.

`frq_label`: The field strength label.

#### Examples

To delete the relaxation data corresponding to `ri_label=‘NOE’`, `frq_label=‘600’`, and the run ‘m4’, type:

```
relax> relax_data.delete('m4', 'NOE', '600')
```

### 3.2.47 `relax_data.display`

#### Synopsis

Function for displaying the relaxation data corresponding to `ri_label` and `frq_label`.

#### Defaults

**`relax_data.display`**(self, run=None, ri\_label=None, frq\_label=None)

#### Keyword Arguments

`run`: The name of the run.

`ri_label`: The relaxation data type, ie 'R1', 'R2', or 'NOE'.

`frq_label`: The field strength label.

#### Examples

To display the NOE relaxation data at 600 MHz from the run 'm4', type

```
relax> relax_data.display('m4', 'NOE', '600')
```

### 3.2.48 `relax_data.read`

#### Synopsis

Function for reading  $R_1$ ,  $R_2$ , or NOE relaxation data from a file.

#### Defaults

**`relax_data.read`**(self, run=None, ri\_label=None, frq\_label=None, frq=None, file=None, dir=None, num\_col=0, name\_col=1, data\_col=2, error\_col=3, sep=None)

#### Keyword Arguments

`run`: The name of the run.

`ri_label`: The relaxation data type, ie 'R1', 'R2', or 'NOE'.

`frq_label`: The field strength label.

`frq`: The spectrometer frequency in Hz.

`file`: The name of the file containing the relaxation data.

`dir`: The directory where the file is located.

`num_col`: The residue number column (the default is 0, ie the first column).

`name_col`: The residue name column (the default is 1).

`data_col`: The relaxation data column (the default is 2).

`error_col`: The experimental error column (the default is 3).

`sep`: The column separator (the default is white space).

#### Description

The frequency label argument can be anything as long as data collected at the same field strength have the same label.

#### Examples

The following commands will read the NOE relaxation data collected at 600 MHz out of a file called 'noe.600.out' where the residue numbers, residue names, data, errors are in the first, second, third, and forth columns respectively.

```
relax> relax_data.read('m1', 'NOE', '600', 599.7 * 1e6, 'noe.600.out')
```

```
relax> relax_data.read('m1', ri_label='NOE', frq_label='600', frq=600.0 * 1e6,  
file='noe.600.out')
```

The following commands will read the  $R_1$  data out of the file 'r2.out' where the residue numbers, residue names, data, errors are in the second, third, fifth, and sixth columns respectively. The columns are separated by commas.

```
relax> relax_data.read('m1', 'R2', '800 MHz', 8.0 * 1e8, 'r2.out', 1, 2, 4, 5, ',',')  
  
relax> relax_data.read('m1', ri_label='R2', frq_label='800 MHz', frq=8.0*1e8,  
file='r2.out', num_col=1, name_col=2, data_col=4, error_col=5, sep=',,')
```

The following commands will read the  $R_1$  data out of the file 'r1.out' where the columns are separated by the symbol '%'

```
relax> relax_data.read('m1', 'R1', '300', 300.1 * 1e6, 'r1.out', sep='%')
```

### 3.2.49 `relax_data.write`

#### Synopsis

Function for writing  $R_1$ ,  $R_2$ , or NOE relaxation data to a file.

#### Defaults

**`relax_data.write`**(self, run=None, ri\_label=None, frq\_label=None, file=None, dir=None, force=0)

#### Keyword Arguments

run: The name of the run.

ri\_label: The relaxation data type, ie 'R1', 'R2', or 'NOE'.

frq\_label: The field strength label.

file: The name of the file.

dir: The directory name.

force: A flag which, if set to 1, will cause the file to be overwritten.

#### Description

If no directory name is given, the file will be placed in the current working directory. The 'ri\_label' and 'frq\_label' arguments are required for selecting which relaxation data to write to file.

### 3.2.50 relax\_fit.read

#### Synopsis

Function for reading peak intensities from a file.

#### Defaults

**relax\_fit.read**(self, run=None, file=None, dir=None, relax\_time=0.0, fit\_type='exp', format='sparky', heteronuc='N', proton='HN', int\_col=None)

#### Keyword Arguments

run: The name of the run.

file: The name of the file containing the sequence data.

dir: The directory where the file is located.

relax\_time: The time, in seconds, of the relaxation period.

fit\_type: The type of relaxation curve to fit.

format: The type of file containing peak intensities.

heteronuc: The name of the heteronucleus as specified in the peak intensity file.

proton: The name of the proton as specified in the peak intensity file.

int\_col: The column containing the peak intensity data (for a non-standard formatted file).

#### Description

The peak intensity can either be from peak heights or peak volumes.

The supported relaxation experiments include the default two parameter exponential fit, selected by setting the 'fit\_type' argument to 'exp', and the three parameter inversion recovery experiment in which the peak intensity limit is a non-zero value, selected by setting the argument to 'inv'.

The format argument can currently be set to:

'sparky'

'xeasy'

If the format argument is set to ‘**sparky**’, the file should be a Sparky peak list saved after typing the command ‘**lt**’. The default is to assume that columns 0, 1, 2, and 3 (1<sup>st</sup>, 2<sup>nd</sup>, 3<sup>rd</sup>, and 4<sup>th</sup>) contain the Sparky assignment, w1, w2, and peak intensity data respectively. The frequency data w1 and w2 are ignored while the peak intensity data can either be the peak height or volume displayed by changing the window options. If the peak intensity data is not within column 3, set the argument `int_col` to the appropriate value (column numbering starts from 0 rather than 1).

If the format argument is set to ‘**xeasy**’, the file should be the saved XEasy text window output of the list peak entries command, ‘**tw**’ followed by ‘**le**’. As the columns are fixed, the peak intensity column is hardwired to number 10 (the 11<sup>th</sup> column) which contains either the peak height or peak volume data. Because the columns are fixed, the `int_col` argument will be ignored.

The heteronuc and proton arguments should be set respectively to the name of the heteronucleus and proton in the file. Only those lines which match these labels will be used.



### 3.2.51 results.display

#### Synopsis

Function for displaying the results of the run.

#### Defaults

**results.display**(self, run=None, format='columnar')

#### Keyword Arguments

run: The name of the run.

format: The format of the output.

### 3.2.52 results.read

#### Synopsis

Function for reading results from a file.

#### Defaults

**results.read**(self, run=None, file='results', dir='run', format='columnar')

#### Keyword Arguments

run: The name of the run.

file: The name of the file to read results from.

dir: The directory where the file is located.

#### Description

If no directory name is given, the results file will be searched for in a directory named after the run name. To search for the results file in the current working directory, set dir to None.

This function is able to handle uncompressed, bzip2 compressed files, or gzip compressed files automatically. The full file name including extension can be supplied, however, if the file cannot be found, this function will search for the file name with `‘.bz2’` appended followed by the file name with `‘.gz’` appended.

### 3.2.53 results.write

#### Synopsis

Function for writing results of the run to a file.

#### Defaults

**results.write**(self, run=None, file='results', dir='run', force=0, format='columnar', compress\_type=1)

#### Keyword Arguments

run: The name of the run.

file: The name of the file to output results to. The default is 'results'.

dir: The directory name.

force: A flag which, if set to 1, will cause the results file to be overwritten.

format: The format of the output.

compress\_type: The type of compression to use when creating the file.

#### Description

If no directory name is given, the results file will be placed in a directory named after the run name. To place the results file in the current working directory, set dir to None.

The default behaviour of this function is to compress the file using bzip2 compression. If the extension '.bz2' is not included in the file name, it will be added. The compression can, however, be changed to either no compression or gzip compression. This is controlled by the compress\_type argument which can be set to

- 0 – No compression (no file extension),
- 1 – bzip2 compression ('.bz2' file extension),
- 2 – gzip compression ('.gz' file extension).

The complementary read function will automatically handle the compressed files.

### 3.2.54 run.create

#### Synopsis

Function for setting up a run type.

#### Defaults

**run.create**(self, run=None, run\_type=None)

#### Keyword Arguments

run: The name of the run.

type: The type of run.

#### Description

The run name can be any string however the run type can only be one of the following

‘jw’ – Reduced spectral density mapping,

‘mf’ – Model-free analysis,

‘noe’ – Steady state NOE calculation,

‘relax\_fit’ – Relaxation curve fitting,

‘srls’ – SRLS analysis.

#### Examples

To set up a model-free analysis run with the name ‘m5’, type:

```
relax> run.create('m5', 'mf')
```

### 3.2.55 `run.delete`

#### Synopsis

Function for deleting a run.

#### Defaults

**`run.delete`**(self, run=None)

#### Keyword Arguments

`run`: The name of the run.

#### Description

This function will destroy all data corresponding to the given run.

### 3.2.56 `select.all`

#### Synopsis

Function for selecting all residues.

#### Defaults

**`select.all`**(self, run=None)

#### Keyword Arguments

run: The name of the run(s). By supplying a single string, array of strings, or None, a single run, multiple runs, or all runs will be selected respectively.

#### Examples

To select all residues for all runs type:

```
relax> select.all()
```

To select all residues for the run 'srls\_m1', type:

```
relax> select.all('srls_m1')
```

```
relax> select.all(run='srls_m1')
```

### 3.2.57 `select.read`

#### Synopsis

Function for selecting the residues contained in a file.

#### Defaults

**`select.read`**(self, run=None, file=None, dir=None, change\_all=0)

#### Keyword Arguments

**run**: The name of the run(s). By supplying a single string, array of strings, or None, a single run, multiple runs, or all runs will be selected respectively.

**file**: The name of the file containing the list of residues to select.

**dir**: The directory where the file is located.

**change\_all**: A flag specifying if all other residues should be changed.

#### Description

The file must contain one residue number per line. The number is taken as the first column of the file and all other columns are ignored. Empty lines and lines beginning with a hash are ignored.

The ‘`change_all`’ flag argument default is zero meaning that all residues currently either selected or unselected will remain that way. Setting the argument to 1 will cause all residues not specified in the file to be unselected.

#### Examples

To select all residues in the file ‘`isolated_peaks`’, type:

```
relax> select.read('noe', 'isolated_peaks')
```

```
relax> select.read(run='noe', file='isolated_peaks')
```

### 3.2.58 select.res

#### Synopsis

Function for selecting specific residues.

#### Defaults

**select.res**(self, run=None, num=None, name=None, change\_all=0)

#### Keyword Arguments

**run**: The name of the run(s). By supplying a single string, array of strings, or None, a single run, multiple runs, or all runs will be selected respectively.

**num**: The residue number.

**name**: The residue name.

**change\_all**: A flag specifying if all other residues should be changed.

#### Description

The residue number can be either an integer for selecting a single residue or a python regular expression, in string form, for selecting multiple residues. For details about using regular expression, see the python documentation for the module `'re'`.

The residue name argument must be a string. Regular expression is also allowed.

The `'change_all'` flag argument default is zero meaning that all residues currently either selected or unselected will remain that way. Setting the argument to 1 will cause all residues not specified by `'num'` or `'name'` to become unselected.

#### Examples

To select only glycines and alanines for the run `'m3'`, assuming they have been loaded with the names GLY and ALA, type:

```
relax> select.res(run='m3', name='GLY|ALA', change_all=1)
relax> select.res(run='m3', name='[GA]L[YA]', change_all=1)
```

To select residue 5 CYS in addition to the currently selected residues, type:

```
relax> select.res('m3', 5)
relax> select.res('m3', 5, 'CYS')
relax> select.res('m3', '5')
relax> select.res('m3', '5', 'CYS')
relax> select.res(run='m3', num='5', name='CYS')
```



### 3.2.59 `select.reverse`

#### Synopsis

Function for the reversal of the residue selection.

#### Defaults

`select.reverse(self, run=None)`

#### Keyword Arguments

`run`: The name of the run(s). By supplying a single string, array of strings, or None, a single run, multiple runs, or all runs will be selected respectively.

#### Examples

To unselect all currently selected residues and select those which are unselected type:

```
relax> select.reverse()
```

### 3.2.60 `sequence.add`

#### Synopsis

Function for adding a residue onto the sequence.

#### Defaults

**`sequence.add`**(self, run=None, res\_num=None, res\_name=None, select=1)

#### Keyword Arguments

**run**: The name of the run.

**res\_num**: The residue number.

**res\_name**: The name of the residue.

**select**: A flag specifying if the residue should be selected.

#### Description

Using this function a new sequence can be generated without having to load the sequence from a file. However if the sequence already exists, the new residue will be added to the end. The same residue number cannot be used more than once.

#### Examples

The following sequence of commands will generate the sequence 1 ALA, 2 GLY, 3 LYS and assign it to the run 'm3':

```
relax> run = 'm3'
relax> sequence.add(run, 1, 'ALA')
relax> sequence.add(run, 2, 'GLY')
relax> sequence.add(run, 3, 'LYS')
```

### 3.2.61 `sequence.copy`

#### Synopsis

Function for copying the sequence from `run1` to `run2`.

#### Defaults

**`sequence.copy`**(self, run1=None, run2=None)

#### Keyword Arguments

`run1`: The name of the run to copy the sequence from.

`run2`: The name of the run to copy the sequence to.

#### Description

This function will copy the sequence from '`run1`' to '`run2`'. '`run1`' must contain sequence information, while '`run2`' must have no sequence loaded.

#### Examples

To copy the sequence from the run '`m1`' to the run '`m2`', type:

```
relax> sequence.copy('m1', 'm2')
```

```
relax> sequence.copy(run1='m1', run2='m2')
```

### 3.2.62 `sequence.delete`

#### Synopsis

Function for deleting the sequence.

#### Defaults

**`sequence.delete`**(self, run=None)

#### Keyword Arguments

run: The name of the run.

#### Description

This function has the same effect as using the ‘**`delete`**’ function to delete all residue specific data.

### 3.2.63 `sequence.display`

#### Synopsis

Function for displaying the sequence.

#### Defaults

**`sequence.display`**(self, run=None)

#### Keyword Arguments

run: The name of the run.

### 3.2.64 `sequence.read`

#### Synopsis

Function for reading sequence data.

#### Defaults

**`sequence.read`**(self, run=None, file=None, dir=None, num\_col=0, name\_col=1, sep=None)

#### Keyword Arguments

run: The name of the run.

file: The name of the file containing the sequence data.

dir: The directory where the file is located.

num\_col: The residue number column (the default is 0, ie the first column).

name\_col: The residue name column (the default is 1).

sep: The column separator (the default is white space).

#### Description

If no directory is given, the file will be assumed to be in the current working directory.

#### Examples

The following commands will read the sequence data out of a file called '`seq`' where the residue numbers and names are in the first and second columns respectively and assign it to the run '`m1`'.

```
relax> sequence.read('m1', 'seq')
```

```
relax> sequence.read('m1', 'seq', num_col=0, name_col=1)
```

```
relax> sequence.read(run='m1', file='seq', num_col=0, name_col=1, sep=None)
```

The following commands will read the sequence out of the file '`noe.out`' which also contains the NOE values.

```
relax> sequence.read('m1', 'noe.out')
```

```
relax> sequence.read('m1', 'noe.out', num_col=0, name_col=1)
```

```
relax> sequence.read(run='m1', file='noe.out', num_col=0, name_col=1)
```

The following commands will read the sequence out of the file '`noe.600.out`' where the residue numbers are in the second column, the names are in the sixth column and the columns are separated by commas and assign it to the run '`m5`'.

```
relax> sequence.read('m5', 'noe.600.out', num_col=1, name_col=5, sep=',')  
relax> sequence.read(run='m5', file='noe.600.out', num_col=1, name_col=5, sep=',')
```

### 3.2.65 `sequence.sort`

#### Synopsis

Function for numerically sorting the sequence by residue number.

#### Defaults

**`sequence.sort`**(self, run=None)

#### Keyword Arguments

run: The name of the run.



### 3.2.66 `sequence.write`

#### Synopsis

Function for writing the sequence to a file.

#### Defaults

**`sequence.write`**(self, run=None, file=None, dir=None, force=0)

#### Keyword Arguments

**run**: The name of the run.

**file**: The name of the file.

**dir**: The directory name.

**force**: A flag which, if set to 1, will cause the file to be overwritten.

#### Description

If no directory name is given, the file will be placed in the current working directory.

### 3.2.67 `state.load`

#### Synopsis

Function for loading a saved program state.

#### Defaults

**`state.load`**(self, file=None, dir=None)

#### Keyword Arguments

file: The file name, which must be a string, of a saved program state.

dir: Directory which the file is found in.

#### Description

This function is able to handle uncompressed, bzip2 compressed files, or gzip compressed files automatically. The full file name including extension can be supplied, however, if the file cannot be found, this function will search for the file name with `‘.bz2’` appended followed by the file name with `‘.gz’` appended.

#### Examples

The following commands will load the state saved in the file `‘save’`.

```
relax> state.load(‘save’)
```

```
relax> state.load(file=‘save’)
```

The following commands will load the state saved in the bzip2 compressed file `‘save.bz2’`.

```
relax> state.load(‘save’)
```

```
relax> state.load(file=‘save’)
```

```
relax> state.load(‘save.bz2’)
```

```
relax> state.load(file=‘save.bz2’)
```

### 3.2.68 state.save

#### Synopsis

Function for saving the program state.

#### Defaults

**state.save**(self, file=None, dir=None, force=0, compress\_type=1)

#### Keyword Arguments

**file**: The file name, which must be a string, to save the current program state in.

**dir**: The directory to place the file in.

**force**: A flag which if set to 1 will cause the file to be overwritten.

#### Description

The default behaviour of this function is to compress the file using bzip2 compression. If the extension `‘.bz2’` is not included in the file name, it will be added. The compression can, however, be changed to either no compression or gzip compression. This is controlled by the `compress_type` argument which can be set to

**0** – No compression (no file extension).

**1** – bzip2 compression (`‘.bz2’` file extension).

**2** – gzip compression (`‘.gz’` file extension).

#### Examples

The following commands will save the current program state into the file `‘save’`:

```
relax> state.save('save', compress_type=0)
relax> state.save(file='save', compress_type=0)
```

The following commands will save the current program state into the bzip2 compressed file `‘save.bz2’`:

```
relax> state.save('save')
relax> state.save(file='save')
relax> state.save('save.bz2')
relax> state.save(file='save.bz2')
```

If the file ‘**save**’ already exists, the following commands will save the current program state by overwriting the file.

```
relax> state.save('save', 1)
```

```
relax> state.save(file='save', force=1)
```

### 3.2.69 system

#### Synopsis

Function which executes the user supplied shell command.

#### Defaults

**system**(command)

### 3.2.70 `thread.read`

#### Synopsis

Function for reading a file containing entries for each computer to run calculations on.

#### Defaults

**thread.read**(self, file='hosts', dir='~/relax')

#### Keyword Arguments

file: The name of the file containing the host entries.

dir: The directory where the hosts file is located.

#### Description

Certain functions within relax are coded to handle threading. This is achieved by running multiple instances of relax on different processes or computers for each thread. The default behaviour is that the parent instance of relax will execute all the code, however if a hosts file is read or a hosts entry manually entered, then the threaded code will run on the specified hosts. This function is for reading a hosts file which should contain an entry for each computer on which to run calculations.

For remote computers, a SSH connection will be attempted. Public key authentication must be enabled to run calculations on remote machines so that thread can be created without asking for a password. Details on how to do this are given below.

The format of the hosts file is as follows. Default values are specified by placing the character '-' in the corresponding column. Columns can be separated by any whitespace character, and all columns must contain an entry. Any lines beginning with a hash will be ignored.

Column 1: The host name or IP address of the computer on which to run a thread.

Column 2: The login name of the user on the remote machine. The default is to use the same name as the current user.

Column 3: The full program path. The default is to run 'relax'. This only works if relax can be found in the environmental variable \$PATH, as alias are not recognised.

Column 4: The working directory where thread specific files are stored. The default is '~/relax' where the tilde '~' symbol represents the user's home directory on the remote machine.

Column 5: The priority value for running the program. The default is 15. The remote instances of relax will be niced to this value.

Column 6: The number of CPU or CPU cores on the machine. The default is 1. A thread is started for each CPU.

An example is:

# Host	User name	Program path	Working directory	Priority	CPUs
localhost	-	-	-	0	2
192.168.0.10	dauvergne	/usr/local/bin/relax	-	-	-
192.168.0.11	edward	-	-	-	-

In this case, two threads will be run on the parent computer which would be either a dual CPU system or a dual core ‘Hyper threaded’ Pentium processor. These threads will have the highest level user priority of 0. The other two machines will have single threads running with a low priority of 15.

Once threading is enabled, to allow calculations to run on the parent machine a ‘localhost’ entry should be included.

If the keyword argument ‘dir’ is set to None, the hosts file will be assumed to be in the current working directory.

## SSH Public Key Authentication

To enable SSH Public Key Authentication for the use of ssh, sftp, and scp without having to type a password, use the following steps. This is essential for running a thread on a remote machine.

If the files ‘id\_rsa’ and ‘id\_rsa.pub’ do not exist in the directory ‘~/.ssh’, type:

```
$ ssh-keygen -t rsa
```

Press enter three times when asked for input. This will generate the two identification files. Then, to copy the public key into the ‘authorized\_keys’ file on the remote machine, type:

```
$ ssh zucchini "echo $(cat ~/.ssh/id_rsa.pub) >> ~/.ssh/authorized_keys"
```

Make sure you replace ‘zucchini’ with the name or IP address of the remote machine. To use DSA rather than RSA authentication, replace ‘rsa’ with ‘dsa’ in the above commands. Normally the sshd keyword StrictModes, which is found in the file ‘/etc/ssh/sshd\_config’, is set to ‘yes’ or, if unspecified, defaults to ‘yes’. In this case, public key authentication may fail as the permissions of the remote file ‘~/.ssh/authorized\_keys’ may be too permissive. The file should only be read/write for the user, ie 600. To remotely change the permissions, type:

```
$ ssh zucchini "chmod 600 ~/.ssh/authorized_keys"
```

One last keyword may need to be changed in the file ‘/etc/ssh/sshd\_config’. If the keyword PubkeyAuthentication is set to ‘no’, change this to ‘yes’. The default is yes, so if the keyword is missing or is commented out, nothing needs to be done.

Public key authentication should now work. To test, type:

```
$ ssh zucchini
```

This should securely login into the remote machine without asking for a password. If a password prompt appears, check all the permissions on the directory ‘`~/.ssh`’ and all files within or set the `sshd_config` keyword `StrictModes` to ‘`no`’.

```
$ ssh zucchini "chmod 700 ~/.ssh/"
```

```
$ ssh zucchini "chmod 600 ~/.ssh/*"
```

```
$ ssh zucchini "chmod 644 ~/.ssh/*.pub"
```

Finally, if all else fails, make sure the three lines

```
RSAAuthentication yes
PubkeyAuthentication yes
AuthorizedKeysFile      .ssh/authorized_keys
```

of the file ‘`sshd_config`’ found within the directory ‘`/etc/ssh/`’ are uncommented and not set to ‘`no`’ or the ‘`AuthorizedKeysFile`’ set to another file name.



### 3.2.71 `unselect.all`

#### Synopsis

Function for unselecting all residues.

#### Defaults

**`unselect.all`**(self, run=None)

#### Keyword Arguments

**run**: The name of the run(s). By supplying a single string, array of strings, or None, a single run, multiple runs, or all runs will be selected respectively.

#### Examples

To unselect all residues type:

```
relax> unselect.all()
```

To unselect all residues for the run 'srls\_m1', type:

```
relax> select.all('srls_m1')
```

```
relax> select.all(run='srls_m1')
```

### 3.2.72 `unselect.read`

#### Synopsis

Function for unselecting the residues contained in a file.

#### Defaults

**`unselect.read`**(self, run=None, file=None, dir=None, change\_all=0)

#### Keyword Arguments

**run**: The name of the run(s). By supplying a single string, array of strings, or None, a single run, multiple runs, or all runs will be selected respectively.

**file**: The name of the file containing the list of residues to unselect.

**dir**: The directory where the file is located.

**change\_all**: A flag specifying if all other residues should be changed.

#### Description

The file must contain one residue number per line. The number is taken as the first column of the file and all other columns are ignored. Empty lines and lines beginning with a hash are ignored.

The ‘**change\_all**’ flag argument default is zero meaning that all residues currently either selected or unselected will remain that way. Setting the argument to 1 will cause all residues not specified in the file to be selected.

#### Examples

To unselect all overlapped residues in the file ‘**unresolved**’, type:

```
relax> unselect.read('noe', 'unresolved')
```

```
relax> unselect.read(run='noe', file='unresolved')
```

### 3.2.73 `unselect.res`

#### Synopsis

Function for unselecting specific residues.

#### Defaults

**`unselect.res`**(self, run=None, num=None, name=None, change\_all=0)

#### Keyword Arguments

**run**: The name of the run(s). By supplying a single string, array of strings, or None, a single run, multiple runs, or all runs will be selected respectively.

**num**: The residue number.

**name**: The residue name.

**change\_all**: A flag specifying if all other residues should be changed.

#### Description

The residue number can be either an integer for unselecting a single residue or a python regular expression, in string form, for unselecting multiple residues. For details about using regular expression, see the python documentation for the module `'re'`.

The residue name argument must be a string. Regular expression is also allowed.

The `'change_all'` flag argument default is zero meaning that all residues currently either selected or unselected will remain that way. Setting the argument to 1 will cause all residues not specified by `'num'` or `'name'` to become selected.

#### Examples

To unselect all glycines for the run `'m5'`, type:

```
relax> unselect.res(run='m5', name='GLY|ALA')
relax> unselect.res(run='m5', name='[GA]L[YA]')
```

To unselect residue 12 MET type:

```
relax> unselect.res('m5', 12)
relax> unselect.res('m5', 12, 'MET')
relax> unselect.res('m5', '12')
relax> unselect.res('m5', '12', 'MET')
relax> unselect.res(run='m5', num='12', name='MET')
```

### 3.2.74 `unselect.reverse`

#### Synopsis

Function for the reversal of the residue selection.

#### Defaults

**`unselect.reverse`**(self, run=None)

#### Keyword Arguments

**run**: The name of the run(s). By supplying a single string, array of strings, or None, a single run, multiple runs, or all runs will be selected respectively.

#### Examples

To unselect all currently selected residues and select those which are unselected type:

```
relax> unselect.reverse()
```

### 3.2.75 `value.copy`

#### Synopsis

Function for copying residue specific data values from run1 to run2.

#### Defaults

**value.copy**(self, run1=None, run2=None, data\_type=None)

#### Keyword Arguments

run1: The name of the run to copy from.

run2: The name of the run to copy to.

data\_type: The data type.

#### Description

Only one data type may be selected, therefore the data type argument should be a string.

If this function is used to change values of previously minimised runs, then the minimisation statistics (chi-squared value, iteration count, function count, gradient count, and Hessian count) will be reset to None.

#### Examples

To copy the CSA values from the run 'm1' to 'm2', type:

```
relax> value.copy('m1', 'm2', 'CSA')
```

#### Regular expression

The python function '`match`', which uses regular expression, is used to determine which data type to set values to, therefore various `data_type` strings can be used to select the same data type. Patterns used for matching for specific data types are listed below.

This is a short description of python regular expression, for more information see the regular expression syntax section of the Python Library Reference. Some of the regular expression syntax used in this function is:

'`[]`' – A sequence or set of characters to match to a single character. For example, '`[Ss]2`' will match both '`S2`' and '`s2`'.

'`^`' – Match the start of the string.

- ‘\$’ – Match the end of the string. For example, ‘`^[Ss]2$`’ will match ‘s2’ but not ‘S2f’ or ‘s2s’.
- ‘.’ – Match any character.
- ‘x\*’ – Match the character ‘x’ any number of times, for example ‘x’ will match, as will ‘xxxxx’
- ‘.\*’ – Match any sequence of characters of any length.

Importantly, do not supply a string for the data type containing regular expression. The regular expression is implemented so that various strings can be supplied which all match the same data type.

### Model-free data type string matching patterns

Data type	Object name	Patterns
Local $\tau_m$	‘tm’	‘ <code>^tm\$</code> ’
Order parameter $S^2$	‘s2’	‘ <code>^[Ss]2\$</code> ’
Order parameter $S_f^2$	‘s2f’	‘ <code>^[Ss]2f\$</code> ’
Order parameter $S_s^2$	‘s2s’	‘ <code>^[Ss]2s\$</code> ’
Correlation time $\tau_e$	‘te’	‘ <code>^te\$</code> ’
Correlation time $\tau_f$	‘tf’	‘ <code>^tf\$</code> ’
Correlation time $\tau_s$	‘ts’	‘ <code>^ts\$</code> ’
Chemical exchange	‘rex’	‘ <code>^[Rr]ex\$</code> ’ or ‘ <code>[Cc]emical[ -][Ee]xchange</code> ’
Bond length	‘r’	‘ <code>^r\$</code> ’ or ‘ <code>[Bb]ond[ -][Ll]ength</code> ’
CSA	‘csa’	‘ <code>^[Cc][Ss][Aa]\$</code> ’

### Model-free set details

Setting a parameter value may have no effect depending on which model-free model is chosen, for example if  $S_f^2$  values and  $S_s^2$  values are set but the run corresponds to model-free model ‘m4’ then, because these data values are not parameters of the model, they will have no effect.

Note that the  $R_{ex}$  values are scaled quadratically with field strength and should be supplied as a field strength independent value. Use the following formula to get the correct value:

$$\text{value} = R_{ex} / (2.0 * \pi * \text{frequency}) ** 2$$

where:

$R_{ex}$  is the chemical exchange value for the current frequency.

$\pi$  is in the namespace of relax, ie just type ' $\pi$ '.

frequency is the proton frequency corresponding to the data.

### Reduced spectral density mapping data type string matching patterns

Data type	Object name	Patterns
$J(0)$	'j0'	'^[Jj]0\$' or '[Jj](0)'
$J(\omega_X)$	'jwx'	'^[Jj]w[Xx]\$' or '[Jj](w[Xx])'
$J(\omega_H)$	'jwh'	'^[Jj]w[Hh]\$' or '[Jj](w[Hh])'
Bond length	'r'	'^r\$' or '[Bb]ond[ -_][Ll]ength'
CSA	'csa'	'^[Cc][Ss][Aa]\$'

### Reduced spectral density mapping set details

In reduced spectral density mapping, only two values can be set, the bond length and CSA value. These must be set prior to the calculation of spectral density values.

### 3.2.76 `value.display`

#### Synopsis

Function for displaying residue specific data values.

#### Defaults

**`value.display`**(self, run=None, data\_type=None)

#### Keyword Arguments

run: The name of the run.

data\_type: The data type.

#### Description

Only one data type may be selected, therefore the data type argument should be a string.

#### Examples

To show all CSA values for the run 'm1', type:

```
relax> value.display('m1', 'CSA')
```

#### Regular expression

The python function '`match`', which uses regular expression, is used to determine which data type to set values to, therefore various data\_type strings can be used to select the same data type. Patterns used for matching for specific data types are listed below.

This is a short description of python regular expression, for more information see the regular expression syntax section of the Python Library Reference. Some of the regular expression syntax used in this function is:

'`[]`' – A sequence or set of characters to match to a single character. For example, '`[Ss]2`' will match both '`S2`' and '`s2`'.

'`^`' – Match the start of the string.

'`$`' – Match the end of the string. For example, '`^[Ss]2$`' will match '`s2`' but not '`S2f`' or '`s2s`'.

'`.`' – Match any character.



‘**x\***’ – Match the character ‘x’ any number of times, for example ‘x’ will match, as will ‘xxxxx’

‘**.\***’ – Match any sequence of characters of any length.

Importantly, do not supply a string for the data type containing regular expression. The regular expression is implemented so that various strings can be supplied which all match the same data type.

### Model-free data type string matching patterns

Data type	Object name	Patterns
Local $\tau_m$	‘tm’	‘ <sup>^</sup> tm\$’
Order parameter $S^2$	‘s2’	‘ <sup>^</sup> [Ss]2\$’
Order parameter $S_f^2$	‘s2f’	‘ <sup>^</sup> [Ss]2f\$’
Order parameter $S_s^2$	‘s2s’	‘ <sup>^</sup> [Ss]2s\$’
Correlation time $\tau_e$	‘te’	‘ <sup>^</sup> te\$’
Correlation time $\tau_f$	‘tf’	‘ <sup>^</sup> tf\$’
Correlation time $\tau_s$	‘ts’	‘ <sup>^</sup> ts\$’
Chemical exchange	‘rex’	‘ <sup>^</sup> [Rr]ex\$’ or ‘[Cc]emical[ -_] [Ee]xchange’
Bond length	‘r’	‘ <sup>^</sup> r\$’ or ‘[Bb]ond[ -_] [Ll]ength’
CSA	‘csa’	‘ <sup>^</sup> [Cc] [Ss] [Aa]\$’

### Reduced spectral density mapping data type string matching patterns

Data type	Object name	Patterns
$J(0)$	‘j0’	‘ <sup>^</sup> [Jj]0\$’ or ‘[Jj](0)’
$J(\omega_X)$	‘jwx’	‘ <sup>^</sup> [Jj]w[Xx]\$’ or ‘[Jj](w[Xx])’
$J(\omega_H)$	‘jwh’	‘ <sup>^</sup> [Jj]w[Hh]\$’ or ‘[Jj](w[Hh])’
Bond length	‘r’	‘ <sup>^</sup> r\$’ or ‘[Bb]ond[ -_] [Ll]ength’
CSA	‘csa’	‘ <sup>^</sup> [Cc] [Ss] [Aa]\$’

### 3.2.77 value.read

#### Synopsis

Function for reading residue specific data values from a file.

#### Defaults

**value.read**(self, run=None, data\_type=None, file=None, num\_col=0, name\_col=1, data\_col=2, error\_col=3, sep=None)

#### Keyword Arguments

run: The name of the run.

data\_type: The data type.

frq: The spectrometer frequency in Hz.

file: The name of the file containing the relaxation data.

num\_col: The residue number column (the default is 0, ie the first column).

name\_col: The residue name column (the default is 1).

data\_col: The relaxation data column (the default is 2).

error\_col: The experimental error column (the default is 3).

sep: The column separator (the default is white space).

#### Description

Only one data type may be selected, therefore the data type argument should be a string. If the file only contains values and no errors, set the error column argument to None.

If this function is used to change values of previously minimised runs, then the minimisation statistics (chi-squared value, iteration count, function count, gradient count, and Hessian count) will be reset to None.

#### Examples

To load CSA values for the run 'm1' from the file 'csa\_values' in the directory 'data', type any of the following:

```
relax> value.read('m1', 'CSA', 'data/csa_value')
```

```
relax> value.read('m1', 'CSA', 'data/csa_value', 0, 1, 2, 3, None, 1)
```

```
relax> value.read(run='m1', data_type='CSA', file='data/csa_value', num_col=0, name_col=1, data_col=2, error_col=3, sep=None)
```

## Regular expression

The python function `'match'`, which uses regular expression, is used to determine which data type to set values to, therefore various `data_type` strings can be used to select the same data type. Patterns used for matching for specific data types are listed below.

This is a short description of python regular expression, for more information see the regular expression syntax section of the Python Library Reference. Some of the regular expression syntax used in this function is:

`'[]'` – A sequence or set of characters to match to a single character. For example, `'[Ss]2'` will match both `'S2'` and `'s2'`.

`'^'` – Match the start of the string.

`'$'` – Match the end of the string. For example, `'^[Ss]2$'` will match `'s2'` but not `'S2f'` or `'s2s'`.

`'.'` – Match any character.

`'x*'` – Match the character `'x'` any number of times, for example `'x'` will match, as will `'xxxxx'`

`'.*'` – Match any sequence of characters of any length.

Importantly, do not supply a string for the data type containing regular expression. The regular expression is implemented so that various strings can be supplied which all match the same data type.

**Model-free data type string matching patterns**

Data type	Object name	Patterns
Local $\tau_m$	<code>'tm'</code>	<code>'^tm\$'</code>
Order parameter $S^2$	<code>'s2'</code>	<code>'^[Ss]2\$'</code>
Order parameter $S_f^2$	<code>'s2f'</code>	<code>'^[Ss]2f\$'</code>
Order parameter $S_s^2$	<code>'s2s'</code>	<code>'^[Ss]2s\$'</code>
Correlation time $\tau_e$	<code>'te'</code>	<code>'^te\$'</code>
Correlation time $\tau_f$	<code>'tf'</code>	<code>'^tf\$'</code>
Correlation time $\tau_s$	<code>'ts'</code>	<code>'^ts\$'</code>
Chemical exchange	<code>'rex'</code>	<code>'^[Rr]ex\$'</code> or <code>'[Cc]emical[ -_][Ee]xchange'</code>
Bond length	<code>'r'</code>	<code>'^r\$'</code> or <code>'[Bb]ond[ -_][Ll]ength'</code>
CSA	<code>'csa'</code>	<code>'^[Cc][Ss][Aa]\$'</code>

**Model-free set details**

Setting a parameter value may have no effect depending on which model-free model is chosen, for example if  $S_f^2$  values and  $S_s^2$  values are set but the run corresponds to model-free model 'm4' then, because these data values are not parameters of the model, they will have no effect.

Note that the  $R_{ex}$  values are scaled quadratically with field strength and should be supplied as a field strength independent value. Use the following formula to get the correct value:

$$\text{value} = R_{ex} / (2.0 * \pi * \text{frequency}) ** 2$$

where:

$R_{ex}$  is the chemical exchange value for the current frequency.

$\pi$  is in the namespace of relax, ie just type ' $\pi$ '.

frequency is the proton frequency corresponding to the data.

**Reduced spectral density mapping data type string matching patterns**

Data type	Object name	Patterns
$J(0)$	'j0'	'^[Jj]0\$' or '[Jj](0)'
$J(\omega_X)$	'jwx'	'^[Jj]w[Xx]\$' or '[Jj](w[Xx])'
$J(\omega_H)$	'jwh'	'^[Jj]w[Hh]\$' or '[Jj](w[Hh])'
Bond length	'r'	'^r\$' or '[Bb]ond[ -_][Ll]ength'
CSA	'csa'	'^[Cc][Ss][Aa]\$'

**Reduced spectral density mapping set details**

In reduced spectral density mapping, only two values can be set, the bond length and CSA value. These must be set prior to the calculation of spectral density values.

### 3.2.78 value.set

#### Synopsis

Function for setting residue specific data values.

#### Defaults

**value.set**(self, run=None, value=None, data\_type=None, res\_num=None, res\_name=None)

#### Keyword arguments

**run**: The run to assign the values to.

**value**: The value(s).

**data\_type**: The data type(s).

**res\_num**: The residue number.

**res\_name**: The residue name.

#### Description

If this function is used to change values of previously minimised runs, then the minimisation statistics (chi-squared value, iteration count, function count, gradient count, and Hessian count) will be reset to None.

The value argument can be None, a single value, or an array of values while the data type argument can be None, a string, or array of strings. The choice of which combination determines the behaviour of this function. The following table describes what occurs in each instance. The Value column refers to the ‘value’ argument while the Type column refers to the ‘data\_type’ argument. In these columns, ‘None’ corresponds to None, ‘1’ corresponds to either a single value or single string, and ‘n’ corresponds to either an array of values or an array of strings.

Value	Type	Description
None	None	This case is used to set the model parameters prior to minimisation or calculation. The model parameters are set to the default values.
1	None	Invalid combination.
$n$	None	This case is used to set the model parameters prior to minimisation or calculation. The length of the value array must be equal to the number of model parameters for <i>an</i> individual residue. The parameters will be set to the corresponding number.
None	1	The data type matching the string will be set to the default value.
1	1	The data type matching the string will be set to the supplied number.
$n$	1	Invalid combination.
None	$n$	Each data type matching the strings will be set to the default values.
1	$n$	Each data type matching the strings will be set to the supplied number.
$n$	$n$	Each data type matching the strings will be set to the corresponding number. Both arrays must be of equal length.

Residue number and name argument.

If the ‘`res_num`’ and ‘`res_name`’ arguments are left as the defaults of None, then the function will be applied to all residues. Otherwise the residue number can be set to either an integer for selecting a single residue or a python regular expression string for selecting multiple residues. The residue name argument must be a string and can use regular expression as well.

### Examples

To set the parameter values for the run ‘`test`’ to the default values, for all residues, type:

```
relax> value.set('test')
```

To set the parameter values of residue 10, which is the model-free run ‘`m4`’ and has the parameters  $\{S^2, \tau_e, R_{ex}\}$ , the following can be used.  $R_{ex}$  term is the value for the first given field strength.

```
relax> value.set('m4', [0.97, 2.048*1e-9, 0.149], res_num=10)
```

```
relax> value.set('m4', value=[0.97, 2.048*1e-9, 0.149], res_num=10)
```

To set the CSA value for the model-free run ‘`tm3`’ to the default value, type:

```
relax> value.set('tm3', data_type='csa')
```

To set the CSA value of all residues in the reduced spectral density mapping run ‘`600MHz`’ to -170 ppm, type:

```
relax> value.set('600MHz', -170 * 1e-6, 'csa')
relax> value.set('600MHz', value=-170 * 1e-6, data_type='csa')
```

To set the NH bond length of all residues in the model-free run 'm5' to 1.02 Å, type:

```
relax> value.set('m5', 1.02 * 1e-10, 'bond_length')
relax> value.set('m5', value=1.02 * 1e-10, data_type='r')
```

To set both the bond length and the CSA value for the run 'new' to the default values, type:

```
relax> value.set('new', data_type=['bond length', 'csa'])
```

To set both  $\tau_f$  and  $\tau_s$  in the model-free run 'm6' to 100 ps, type:

```
relax> value.set('m6', 100e-12, ['tf', 'ts'])
relax> value.set('m6', value=100e-12, data_type=['tf', 'ts'])
```

To set the  $S^2$  and  $\tau_e$  parameter values for model-free run 'm4' which has the parameters  $\{S^2, \tau_e, R_{ex}\}$  to 0.56 and 13 ps, type:

```
relax> value.set('m4', [0.56, 13e-12], ['S2', 'te'], 10)
relax> value.set('m4', value=[0.56, 13e-12], data_type=['S2', 'te'], res_num=10)
relax> value.set(run='m4', value=[0.56, 13e-12], data_type=['S2', 'te'], res_num=10)
```

## Regular expression

The python function 'match', which uses regular expression, is used to determine which data type to set values to, therefore various data\_type strings can be used to select the same data type. Patterns used for matching for specific data types are listed below.

This is a short description of python regular expression, for more information see the regular expression syntax section of the Python Library Reference. Some of the regular expression syntax used in this function is:

- '[]' – A sequence or set of characters to match to a single character. For example, '[Ss]2' will match both 'S2' and 's2'.
- '^' – Match the start of the string.
- '\$' – Match the end of the string. For example, '^ [Ss] 2\$' will match 's2' but not 'S2f' or 's2s'.
- '.' – Match any character.
- 'x\*' – Match the character 'x' any number of times, for example 'x' will match, as will 'xxxxx'.
- '.\*' – Match any sequence of characters of any length.

Importantly, do not supply a string for the data type containing regular expression. The regular expression is implemented so that various strings can be supplied which all match the same data type.



**Model-free data type string matching patterns**

Data type	Object name	Patterns
Local $\tau_m$	'tm'	'^tm\$'
Order parameter $S^2$	's2'	'^[Ss]2\$'
Order parameter $S_f^2$	's2f'	'^[Ss]2f\$'
Order parameter $S_s^2$	's2s'	'^[Ss]2s\$'
Correlation time $\tau_e$	'te'	'^te\$'
Correlation time $\tau_f$	'tf'	'^tf\$'
Correlation time $\tau_s$	'ts'	'^ts\$'
Chemical exchange	'rex'	'^[Rr]ex\$' or '[Cc]emical[ -_][Ee]xchange'
Bond length	'r'	'^r\$' or '[Bb]ond[ -_][Ll]ength'
CSA	'csa'	'^[Cc][Ss][Aa]\$'

**Model-free set details**

Setting a parameter value may have no effect depending on which model-free model is chosen, for example if  $S_f^2$  values and  $S_s^2$  values are set but the run corresponds to model-free model 'm4' then, because these data values are not parameters of the model, they will have no effect.

Note that the  $R_{ex}$  values are scaled quadratically with field strength and should be supplied as a field strength independent value. Use the following formula to get the correct value:

$$\text{value} = R_{ex} / (2.0 * \pi * \text{frequency}) ** 2$$

where:

$R_{ex}$  is the chemical exchange value for the current frequency.

$\pi$  is in the namespace of relax, ie just type ' $\pi$ '.

frequency is the proton frequency corresponding to the data.

**Model-free default values**

Data type	Object name	Value
Local $\tau_m$	‘tm’	10 * 1e-9
Order parameters $S^2$ , $S_f^2$ , and $S_s^2$	‘s2’, ‘s2f’, ‘s2s’	0.8
Correlation time $\tau_e$	‘te’	100 * 1e-12
Correlation time $\tau_f$	‘tf’	10 * 1e-12
Correlation time $\tau_s$	‘ts’	1000 * 1e-12
Chemical exchange relaxation	‘rex’	0.0
Bond length	‘r’	1.02 * 1e-10
CSA	‘csa’	-170 * 1e-6

**Reduced spectral density mapping data type string matching patterns**

Data type	Object name	Patterns
$J(0)$	‘j0’	‘^[Jj]0\$’ or ‘[Jj](0)’
$J(\omega_X)$	‘jwx’	‘^[Jj]w[Xx]\$’ or ‘[Jj](w[Xx])’
$J(\omega_H)$	‘jwh’	‘^[Jj]w[Hh]\$’ or ‘[Jj](w[Hh])’
Bond length	‘r’	‘^r\$’ or ‘[Bb]ond[ -_] [Ll]ength’
CSA	‘csa’	‘^[Cc] [Ss] [Aa]\$’

**Reduced spectral density mapping set details**

In reduced spectral density mapping, only two values can be set, the bond length and CSA value. These must be set prior to the calculation of spectral density values.

**Reduced spectral density mapping default values**

Data type	Object name	Value
Bond length	‘r’	1.02 * 1e-10
CSA	‘csa’	-170 * 1e-6

### 3.2.79 value.write

#### Synopsis

Function for writing residue specific data values to a file.

#### Defaults

**value.write**(self, run=None, data\_type=None, file=None, dir=None, force=0)

#### Keyword Arguments

run: The name of the run.

data\_type: The data type.

file: The name of the file.

dir: The directory name.

force: A flag which, if set to 1, will cause the file to be overwritten.

#### Description

If no directory name is given, the file will be placed in the current working directory.

The data type argument should be a string.

#### Examples

To write the CSA values for the run 'm1' to the file 'csa.txt', type:

```
relax> value.write('m1', 'CSA', 'csa.txt')
```

```
relax> value.write(run='m1', data_type='CSA', file='csa.txt')
```

To write the NOE values from the run 'noe' to the file 'noe', type:

```
relax> value.write('noe', 'noe', 'noe.out')
```

```
relax> value.write('noe', data_type='noe', file='noe.out')
```

```
relax> value.write(run='noe', data_type='noe', file='noe.out')
```

```
relax> value.write(run='noe', data_type='noe', file='noe.out', force=1)
```

## Regular expression

The python function `'match'`, which uses regular expression, is used to determine which data type to set values to, therefore various `data_type` strings can be used to select the same data type. Patterns used for matching for specific data types are listed below.

This is a short description of python regular expression, for more information see the regular expression syntax section of the Python Library Reference. Some of the regular expression syntax used in this function is:

`'[]'` – A sequence or set of characters to match to a single character. For example, `'[Ss]2'` will match both `'S2'` and `'s2'`.

`'^'` – Match the start of the string.

`'$'` – Match the end of the string. For example, `'^[Ss]2$'` will match `'s2'` but not `'S2f'` or `'s2s'`.

`'.'` – Match any character.

`'x*'` – Match the character `'x'` any number of times, for example `'x'` will match, as will `'xxxxx'`

`'.*'` – Match any sequence of characters of any length.

Importantly, do not supply a string for the data type containing regular expression. The regular expression is implemented so that various strings can be supplied which all match the same data type.

**Model-free data type string matching patterns**

Data type	Object name	Patterns
Local $\tau_m$	'tm'	'^tm\$'
Order parameter $S^2$	's2'	'^[Ss]2\$'
Order parameter $S_f^2$	's2f'	'^[Ss]2f\$'
Order parameter $S_s^2$	's2s'	'^[Ss]2s\$'
Correlation time $\tau_e$	'te'	'^te\$'
Correlation time $\tau_f$	'tf'	'^tf\$'
Correlation time $\tau_s$	'ts'	'^ts\$'
Chemical exchange	'rex'	'^[Rr]ex\$' or '[Cc]emical[ -_][Ee]xchange'
Bond length	'r'	'^r\$' or '[Bb]ond[ -_][Ll]ength'
CSA	'csa'	'^[Cc][Ss][Aa]\$'

**Reduced spectral density mapping data type string matching patterns**

Data type	Object name	Patterns
$J(0)$	'j0'	'^[Jj]0\$' or '[Jj](0)'
$J(\omega_X)$	'jwx'	'^[Jj]w[Xx]\$' or '[Jj](w[Xx])'
$J(\omega_H)$	'jwh'	'^[Jj]w[Hh]\$' or '[Jj](w[Hh])'
Bond length	'r'	'^r\$' or '[Bb]ond[ -_][Ll]ength'
CSA	'csa'	'^[Cc][Ss][Aa]\$'

**NOE calculation data type string matching patterns**

Data type	Object name	Patterns
Reference intensity	'ref'	'^[Rr]ef\$' or '[Rr]ef[ -_][Ii]nt'
Saturated intensity	'sat'	'^[Ss]at\$' or '[Ss]at[ -_][Ii]nt'
NOE	'noe'	'^[Nn][Oo][Ee]\$'

### 3.2.80 vmd.view

#### Synopsis

Function for viewing the collection of molecules extracted from the PDB file.

#### Defaults

**vmd.view**(self, run=None)

#### Keyword Arguments

run: The name of the run which the PDB belongs to.

#### Example

```
relax> vmd.view('m1')
```

```
relax> vmd.view(run='pdb')
```

## Chapter 4

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