

$$P(A|B) = \frac{P(AB)}{P(B)}, P(A) = \sum_{k=1}^n P(A|B_k)P(B_k), P(B_i|A) = \frac{P(A|B_i)P(B_i)}{\sum_{k=1}^n P(A|B_k)P(B_k)}$$

$$f_X(x) = P(X = x), E(H(X)) = \sum_x H(x)f_X(x), \\ Var(X) = E((X - E(X))^2) = EX^2 - (EX)^2$$

$$P(|X - \mu| \geq c\sigma) \leq 1/c^2 \\ \hat{E}X = \frac{X_1+X_2+\dots+X_n}{n}, \hat{V}X = \frac{X_1^2+X_2^2+\dots+X_n^2}{n-1} - \frac{(X_1+X_2+\dots+X_n)^2}{n(n-1)}$$

$$G_X(z) = E(z^X), G'_X(1) = EX, G''_X(1) + G'_X(1) - (G'_X(1))^2 = VX$$

$$f_{XY}(x,y) = P(X = x, Y = y), f_X(x) = \sum_y f_{XY}(x,y), f_Y(y) = \sum_x f_{XY}(x,y) \\ E(H(X,Y)) = \sum_x \sum_y H(x,y)f_{XY}(x,y)$$

$$Cov(X,Y) = E((X - \mu_x)(Y - \mu_y)) = E(XY) - E(X)E(Y), \rho_{XY} = \frac{Cov(X,Y)}{\sqrt{VarX}\sqrt{VarY}} \\ f_{X|Y}(x) = f_{X|Y=y}(x) = \frac{f_{XY}(x,y)}{f_Y(y)}$$

$$U_n: f_X(x) = \frac{1}{n}, G_X(e^t) = \frac{\sum_{k=1}^n e^{tx_k}}{n}, EX = \frac{\sum_{k=1}^n x_k}{n}, VX = \frac{\sum_{k=1}^n x_k^2}{n} - \left(\frac{\sum_{k=1}^n x_k}{n} \right)^2$$

$$Be(p): f_X(x) = p^x(1-p)^{1-x}, G_X(e^t) = q + pe^t, EX = p, VX = p(1-p)$$

$$Ge(p): f_X(x) = (1-p)^{x-1}p, G_X(e^t) = \frac{pe^t}{1-qe^t}, EX = \frac{1}{p}, VX = \frac{q}{p^2}$$

$$Bi(n,p): f_X(x) = \binom{n}{x}p^x(1-p)^{n-x}, G_X(e^t) = (q + pe^t)^n, EX = np, VX = npq$$

$$NegBi(r,p): f_X(x) = \binom{x-1}{r-1}p^r(1-p)^{x-r}, G_X(e^t) = \frac{(pe^t)^r}{(1-qe^t)^r}, EX = \frac{r}{p}, VX = \frac{rq}{p^2}$$

$$HG(N,r,n): f_X(x) = \frac{\binom{r}{x}\binom{N-r}{n-x}}{\binom{N}{n}}, G_X(e^t) = , EX = n\frac{r}{N}, VX = n\frac{r}{N}\frac{N-r}{N}\frac{N-n}{N-1}$$

$$Po(k): f_X(x) = \frac{e^{-k}k^x}{x!}, G_X(e^t) = e^{k(e^t-1)}, EX = k, VX = k$$