

# Analysis of Specific Events on the Deformation Curves under MgO Nano-/Microindentation

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**Abstract:** Specific features on the  $P$ - $h$  curves known as pop-in and pop-out events, were studied using the depth-sensing nano-/microindentation of the (001) plane of MgO single crystals. The sharp (*with* pop-in) and gradual (*without* pop-in) mechanisms of elastic-to-plastic transition were revealed and the conditions of their appearance were analyzed. Three types of pop-in jumps were identified, and the correlation of each of them with the shape of dislocation rosettes around the imprints was established. It was shown that pop-in jumps are caused by different mechanisms of plastic deformation and pop-out jumps are the result of a sharp stress relaxation by cracks generation during the load removal stage.

**Keywords:** MgO single crystal, nanoindentation, deformation speed, strain rate, pop-in effect, pop-out effect, dislocation structure.

## Introduction

The pop-in effect is one of the interesting phenomena revealed under the depth-sensing indentation of crystalline materials representing a step-wise jump, registered on the loading part of nanoindentation curve, caused by instantaneous penetration of the indenter into the material. The pop-in event takes place in a material when the stresses underneath the indenter reach the values corresponding to the theoretical strength of the material and denotes the transition from pure elastic to elastic-plastic deformation.

The pop-in effects were investigated on a range of crystalline materials from superhard ceramics ( $\text{Al}_2\text{O}_3$ ,  $\text{SiC}$ ) to soft metals ( $\text{Cu}$ ,  $\text{Al}$ ) and were attributed to the dislocations nucleation in defect free zones of material [1-18]. It was shown that the pop-in occurrence is more probable for smaller tip radii of the indenter and lower initial density of dislocations in the stressed zone [4]. The pop-in events were successfully obtained by sharp Berkovich and cube-corner indenters with the tip radii of the order of 100-200 nm [5], as well as by 9.5  $\mu\text{m}$  spherical indenter using a special technique for surface preparation [6]. In some works the pop-in was syudied by comparing the theoretical estimates of molecular dynamics (MD) simulation of nanoindentation with the experimental data of the  $P$ - $h$  or  $H$ - $h$  curves shape [14,18,19]. Thus, based on the Gao-Nix model [20] about the geometrically necessary dislocations (GNDs), Durst and colleagues [14] modeled the indentation process and obtained good agreement with the experimental load-displacement data on a number of metals: Cu, Ni, Al, W. They identified three stages of the deformation process: (i) the elastic stage, (ii) the stage that begins immediately after the

pop-in effect, in which the GNDs dominate, and (iii) further the plastic deformation is controlled by GND and statistically stored dislocations (SSDs). Bradby *et al* found a linear dependence between the pop-in load, the extention of pop-in jump and the hardness for a range of semiconductors (GaN, GaAs, InP and ZnO) [7].

Some crystals demonstrate several pop-in jumps [13,14,23]. For example, under bulk Al indentation, Ohmura *et al* [13] observed (along with a clear first pop-in jump at a load of 0.05 mN) many smaller pop-in effects with further loading of the sample to 0.25 mN, but the reasons for their occurrence were not discussed. The staircase yielding representing also the a sequence of pop-in events has been detected on Al under indentation with 200  $\mu$ N load [14] and was explained within the framework of the concept of GNDs and SSDs. In our earlier work the peculiarities of the deformation of LiF single crystals under nanoindentation in the large interval of loads  $P = (2 \div 900)$  mN were investigated [23]. A comparison of the  $P$ - $h$  curves with the shape of dislocation rosettes appearing around the imprints demonstrated a clear correlation between the appearance of the first pop-in effect, as well as additional pop-in steps, with the growth of load and sequential development of various dislocation processes. Taking into account that the LiF crystal has a relatively low hardness ( $H = 1.2$  GPa), ionic type of bonding and high dislocation velocity at the room temperature ( $v_{LiF} = 10^{-5} \div 10^0$  cm/s), it was of interest to consider if such a correlation will occur under the indentation of the MgO crystal having higher hardness ( $H = 8.0$  GPa), ion-covalent type of bond and much lower dislocation velocity ( $v_{MgO} = 10^{-6} \div 10^{-2}$  cm/s).

It is known that the

## Experimental

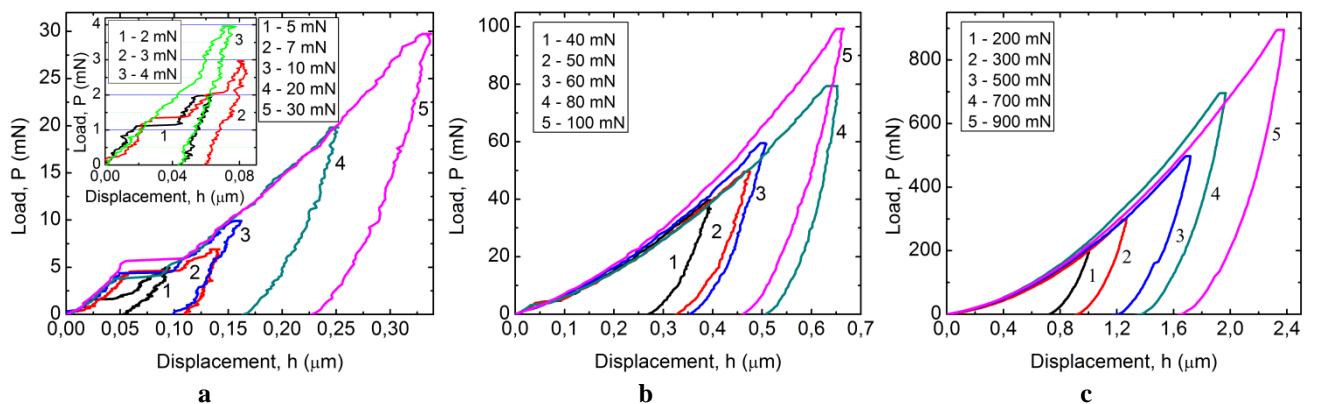
The (001) face of a freshly cleaved MgO single crystal, (10x10x2) mm in size (with no further processing), was subjected to the depth-sensing hardness measurements at the room temperature using the Nanotester-PMT3-NI-02 equipped with a Berkovich indenter.

In order to follow the evolution of the development of the indentation process with the increase in loading, the tests were carried out at 18 values of the peak load in the range  $P_{max} = (2 \div 900)$  mN, according to the following pattern: a load stage of 20 s, holding at a peak load for 5 s, and unloading for 20 s; 5 indentations were made for each load value. Using the  $P$ - $h$  dependence, the values of Young's modulus and hardness were determined for each imprint in accordance with the Oliver-Pharr method [25,26]. It was found that the Young's modulus value for MgO was  $\approx 250$  GPa. According to the obtained results there was constructed a  $P$ - $h$  diagram that governs the loading/unloading process and the hardness  $H$  according to the applied load. The processes of the plastic deformation of the investigated material were evaluated on the basis of the analysis of the indentation curves and dislocation rosettes around the imprints.

The research of the microstructure of the deformed regions around the imprints was carried out using light microscopy (LM) with the help of XJL-101 and Amplival reflection microscopes and a MII-4 interference microscope. The atomic force microscopy (AFM, Nanostation II) was used to study the relief and microstructure of the deformed zone of the imprints at low loads  $P_{max} = (7 \div 40)$  mN. The dislocation rosettes around the indentations were detected with the selective chemical etching in a solution with the following composition: 5p NH<sub>4</sub>Cl + 1p H<sub>2</sub>O + 1p H<sub>2</sub>SO<sub>4</sub>.

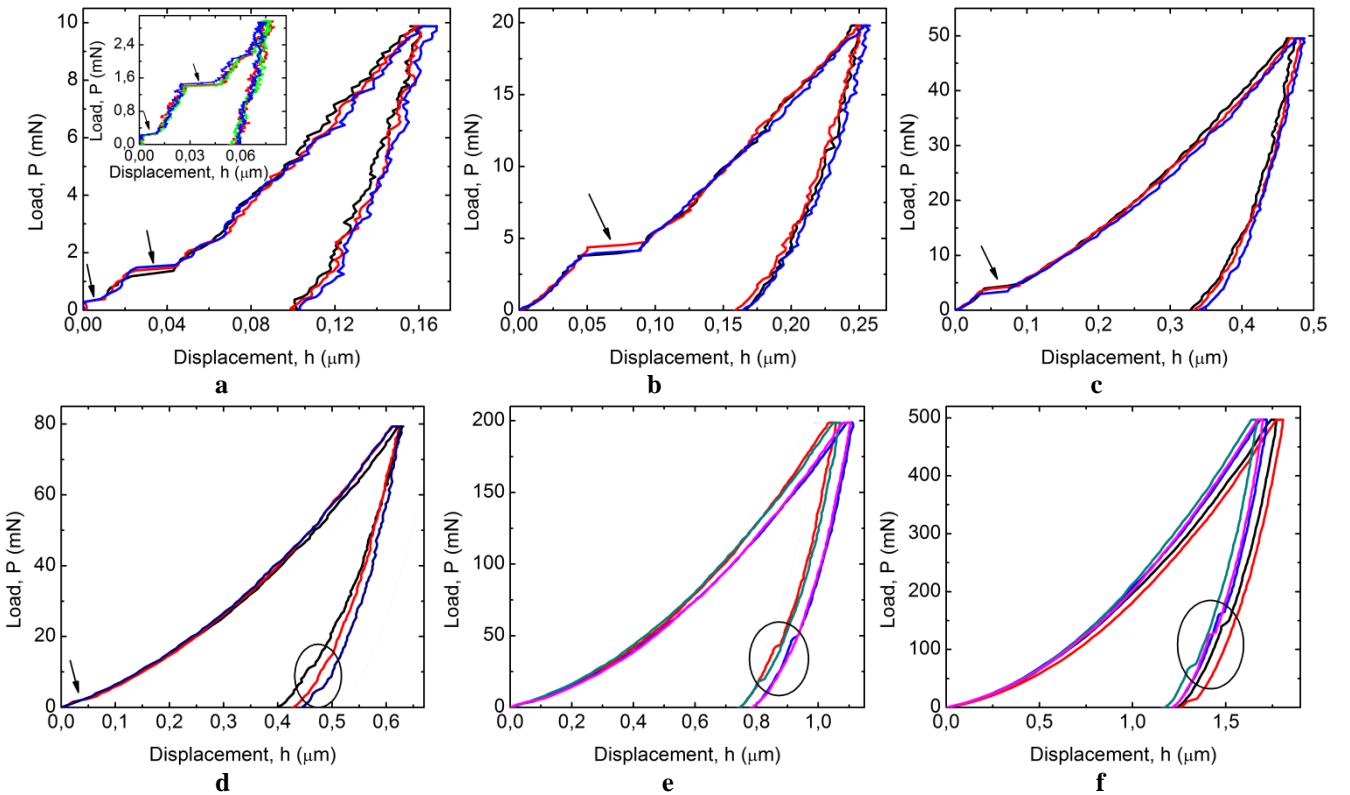
## Results and discussion

The representative  $P$ - $h$  curves for each of the used 18 loads are presented in Fig. 1. The occurrence of three pop-in jumps at the initial stages of loading is clearly visible being most pronounced for low peak loads ( $P_{max} = (2 \div 40)$  mN). Usually, the pop-in effect at the initial stages of indenter penetration in crystalline materials is associated with homogenous dislocation nucleation and the transition from elastic to plastic deformation [21,27]. As a result, a sudden drop of stresses and a simultaneous sharp increase of the penetration depth take place, exhibited as a pop-in jump on the  $P$ - $h$  curves.



**Fig. 1** Loading-unloading diagrams  $P(h)$  obtained at different peak loads,  $P_{max}=2 \div 900$  mN

With a further increase in the load, slight oscillations or "stepped appearance" are observed on the deformation curves both at the stage of loading and at the stage of unloading (serration effect). Presumably, this effect is due to the elastic-plastic recovery (relaxation) of the material that takes place throughout the whole process of indentation [28-36]. The serration of the curves decreases at high loads and the  $P(h)$  dependences become more homogeneous. Let us analyze in more detail the  $P$ - $h$  diagrams presented in Fig. 2 for 7 loads ( $P_{max} = 3, 10, 20, 50, 80, 200$ , and 500 mN), selected from



**Fig. 2** Loading-unloading diagrams  $P(h)$  obtained at different peak loads,  $P_{max}=3$  (in the insert), 10, 20, 50, 80, 200, and 900 mN. The arrows indicate the “pop-in” phenomena at the loading stage, and the circles indicate the “pop-out” effects at the unloading one

all the 18 studied ones, to find out the nature of the above mentioned evolution of the indentation process.

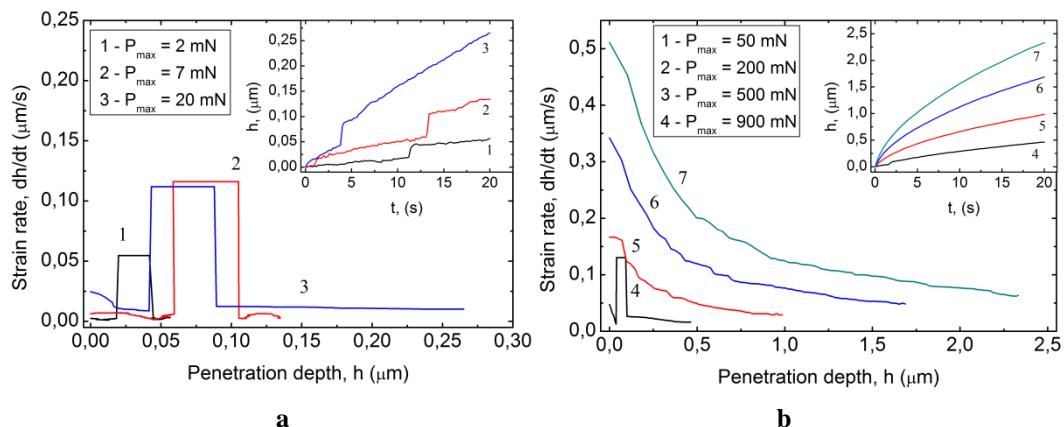
The following features can be identified from the analysis of the loading-unloading curves. Two pop-in effects are clearly distinguished in the  $P-h$  diagrams in the range of the load values  $P_{max} = (3 \div 10)$  mN. The first pop-in jump starts from a load of  $P_i \approx (0.2 \div 0.3)$  mN, with the depth of the indenter penetration about  $h_i \approx 10$  nm (Fig. 2a, the insert). The second pop-in jump occurs in the load interval of  $P_i \approx (1.4 \div 1.7)$  mN, for which the penetration depth is  $h_i \approx (25 \div 30)$  nm (Fig. 2a). The first two pop-in discontinuities decrease in size and almost disappear as the value of  $P_{max}$  increases in the interval  $(20 \div 100)$  mN. They are replaced by the third jump at  $P_i \approx 5$  mN, corresponding to the depth of indentation  $h_i \approx (50 \div 60)$  nm (Fig. 2b-f). At greater loads,  $P_{max} = (200 \div 900)$  mN, the pop-in steps are hardly visible and finally disappear in general on the  $P(h)$  diagrams. The pop-out jumps appear on the  $P(h)$  curves at the unloading stage at  $P_{max} = (80 \div 900)$  mN, may be associated with the formation of cracks around the indentations during the removal of the indenter [37,38].

In our experiments, for all peak loads we used the same indentation time scheme  $(t_1-t_2-t_3) = (20-5-20)$  s, where  $t_1$  is loading time,  $t_2$  is holding time under  $P_{max}$  and  $t_3$  is unloading time. This fact leads to a sharp increase of the loading rate ( $v_p = P_{max}/t_1$ ) with the increase of peak load (Table 1). As follows from the table, an enhancement in  $P_{max}$  from 2 mN to 900 mN increases  $v_p$  by a factor of 450, i.e., by 2.5

orders of magnitude. This in turn leads to the increase of the indenter displacement rate, and hence, to the increase of the rate of the deformation of material. Fig. 3 demonstrates the changes of the deformation rate ( $dh/dt$ ) with penetration depth during loading for indentations made with different loads and loading rates according to Table 1. The increase of peak load and, respectively loading rate (in our particular case) leads to a strong increase of the deformation rate, especially at the beginning of indenter penetration (Fig. 3a, b). For higher loads and loading rates the deformation rate decreases considerably with the increase of penetration depth (Fig. 3b), but higher deformation rate for higher loading rate is anyway maintained for any penetration depth. The surges on the  $dh/dt(h)$  curves 1–4 appear due to a sharp increase of the strain rate during the pop-ins.

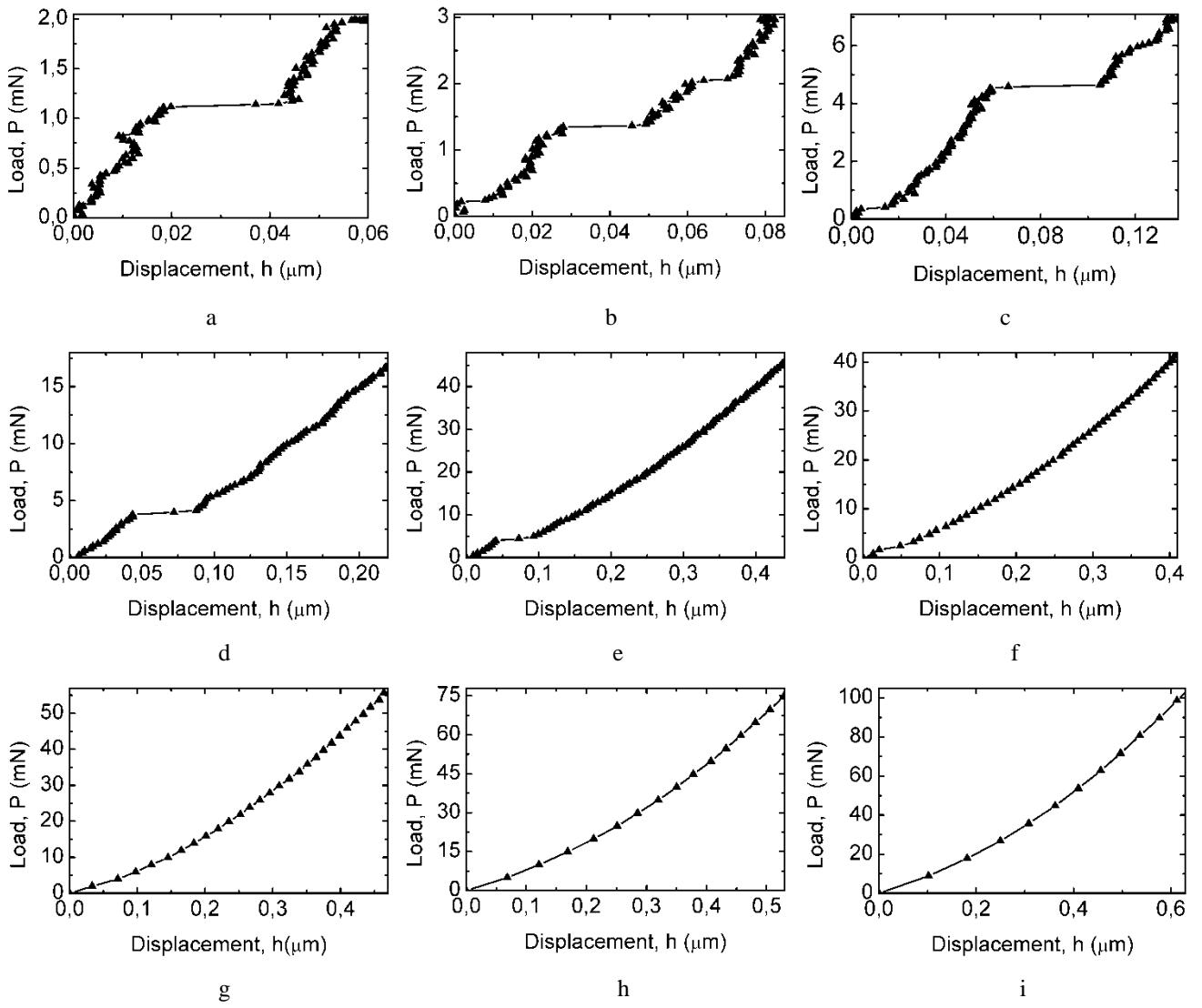
**Table 1** The change of the loading-unloading rate ( $v_p$ ) with the increase of  $P_{max}$  using the same indentation time regime (20-5-20) s

$P_{max}$ , mN	2	3	4	5	7	10	20	30	40	50	60	80	100	200	300	500	700	900
$v_p$ , mN/s	0.1	0.15	0.2	0.25	0.35	0.5	1.0	1.5	2.0	2.5	3.0	4.0	5.0	10.0	15.0	25.0	35.0	45.0



**Fig. 3** The change of strain rate during loading with the increase of peak load  $P_{max}$  and loading rate  $v_p$ , according to Table 1

At the same time the use of an identical indentation time scheme for all peak loads induces some specificity in the registration of indentation process. The initial portions of the  $P-h$  curves for 9 values of  $P_{max}$  are shown in Fig. 4. It can be seen that the number of points recorded by the instrument is considerably different when passing from low values of  $P_{max}$  to high ones.

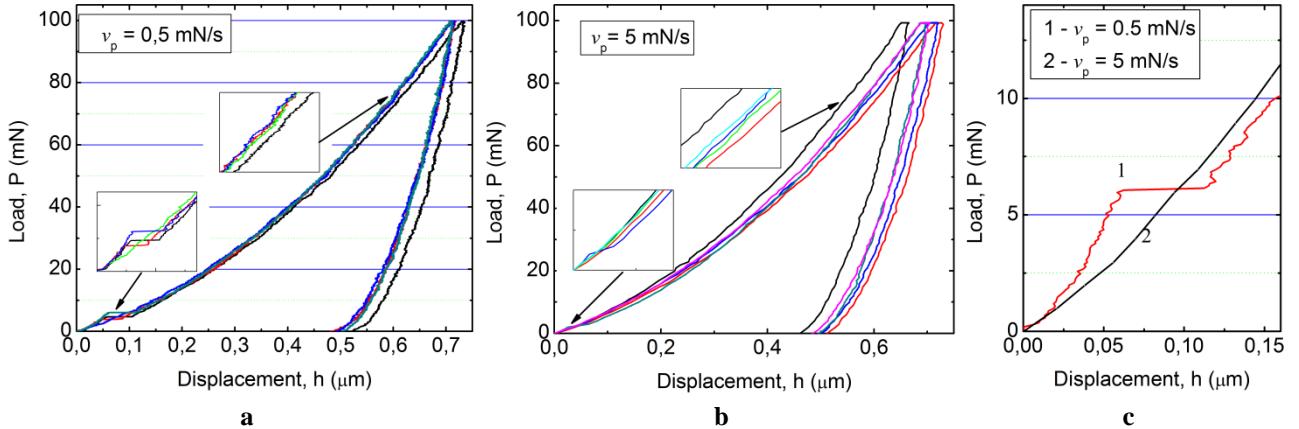


**Fig. 4** The shape of the  $P$ - $h$  diagrams at the initial loading stage for various  $P_{max}$ , mN: a – 2; b – 3; c – 7; d – 20; e – 50; f – 80; g – 200; h – 500; i – 900

The averaged time resolution of the instrument is 0.2 s, hence for the same loading-unloading time,  $t_1 = t_3 = 20$  s, the spatial resolution changes from  $\Delta h \approx 0.75 \text{ nm}$  for 20 mN indentations with maximum depth ( $h_{max}$ ) of  $\sim 75 \text{ nm}$ , to  $\Delta h \approx 24 \text{ nm}$  for 900 mN indentations with  $h_{max}$  of  $\sim 2400 \text{ nm}$ . As a result, one can assume that it is less possible to “capture” subtler effects on the  $P$ - $h$  diagrams, such as pop-in jumps and serration, when the values of  $\Delta h$  become close to the depth of pop-in jumps  $\Delta h_{p-i} \approx (20-50) \text{ nm}$ .

To verify the influence of the above mentioned technical feature we carried out 100 mN indentation using another time regime (200-5-200) s to obtain higher spatial resolution and compare the obtained  $P$ - $h$  curves with those obtained for (20-5-20) s regime and the same 100 mN load (Fig. 5). As one can see,  $h_{max}$  is  $\sim 700 \text{ nm}$  for both regimes and hence  $\Delta h \approx 0.7 \text{ nm}$  for (200-5-200) s regime (Fig. 5a), whereas  $\Delta h \approx 7 \text{ nm}$  for (20-5-20) s one (Fig. 5b). The value  $\Delta h$  of even 7 nm is several times lower than that of the mean depth of pop-in jump  $\Delta h_{p-i} = 47 \text{ nm}$ , well distinguished on the  $P$ - $h$  curves for (200-5-200) s regime (Fig. 5a), that means that from technical point of view both regimes can equally visualize the pop-in effects. But really, the (200-5-200) s regime exhibits well pronounced pop-ins in four of five cases (Fig.

5a), whereas the regime (20-5-20) s displays a pop-in in only one of five case and even this one has a less sharp, gradual aspect (Fig. 5b). This denotes another reason for such a behavior, most probably the different loading rate – 0.5 mN/s demonstrating a higher probability of pop-in formation versus 5 mN/s with lower probability of pop-in formation.



**Fig. 5** The  $P(h)$  diagrams obtained at different loading-unloading rate  $v$ , mN/s: a – 0.5; b – 5. The inserts show the sections of the curves with a larger magnification (marked by arrows). c – the initial parts of the representative curves from a and b

As mentioned above, the pop-in effect is caused by homogenous dislocation nucleation associated with the transition from elastic to plastic deformation. This process begins when the shear stresses beneath the indenter attain critical values necessary for the dislocation nucleation and sliding. From the classical Hertzian analysis and the Tresca criterion the maximum shear stresses  $\tau_{max}$  beneath a spherical indenter can be expressed as a function of the mean contact pressure  $p_m$  [21, 39,]:

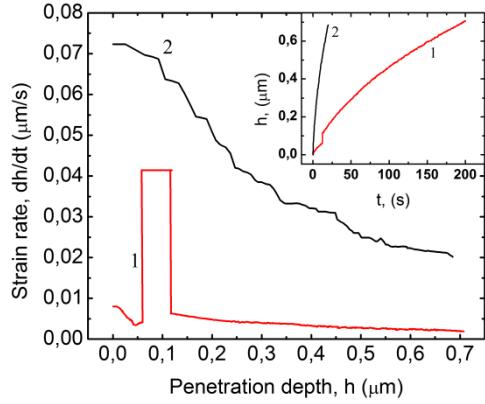
$$\tau_{max} = 0.465p_m \quad (1).$$

The mean contact pressure created by the indenter presents the instantaneous hardness during the deformation that follows directly from the definition of the hardness:

$$p_m = P/A \quad (2),$$

where  $P$  is load and  $A$  is the contact area.

For Berkovich indenter, as well as for spherical one,  $\tau_{max}$  is also directly proportional to  $p_m$ . Therefore, according to equations (1) and (2), for the indentations made with the same  $P_{max} = 100 \text{ mN}$ , as in the case discussed above, the created  $\tau_{max}$  should also have the same value, hence the different behavior of the elastic-to-plastic transition is influenced by different loading rate and the induced strain rate. Similar to Fig. 3, Fig 6 shows that higher loading rate induces higher strain rate of the material.



**Fig. 6** The change of strain rate during loading for 100 mN indentations made at loading rate of 5 mN/s (curve 1) and 0.5 mN/s (curve 2). Inserted are the respective  $h(t)$  dependences

The equation introduced by E. Orowan [40] describes the relation between the macroscopic plastic strain rate of the material  $\dot{h} = dh/dt$  and the mean velocity of dislocations  $\bar{v}$ :

$$\dot{h} = \rho_d b \bar{v} \quad (3),$$

where  $\rho_d$  is the density of moving dislocations and  $b$  is the Burgers vector.

It is known that dislocation velocity is a function of  $\tau$  and temperature of deformation ( $T$ ), but as follows from equation (23) the dislocation velocity also depends on the macroscopic strain rate induced by loading rate. To accommodate to higher loading rate and strain rate at other equal conditions ( $\tau$ ,  $\rho_m$ ,  $T$ ), the velocity of dislocation movement must increase. According to the known formula, dislocations of higher velocities have higher kinetic energy [41]:

$$E_d = \frac{E_0}{\sqrt{1 - \frac{v^2}{c^2}}} \quad (4),$$

where  $E_0$  is the energy of stationary dislocation,  $v$  is the velocity of dislocation and  $c$  is the velocity of sound in material.

The motion of dislocations in crystals requires to overcome various kinds of potential barriers related to both the periodic structure of the crystal (the Peierls barriers) and the lattice defects [42,43]. „Fast” dislocations of higher energies generated at higher strain rate overcome easier these barriers, as opposed to „slow” dislocations generated at lower strain rate, which need higher internal stresses to overcome the barriers. It is clearly seen on Fig. 5c that the curve for 0.5 mN/s demonstrates an increase of  $P$  just before the pop-in, as distinct from curve for 5 mN/s that does not contain any pop-in. As the internal stresses depend on the mean contact pressure at the indenter-material interface (Formula 1), it is reasonable to compare the contact pressures instead of  $P$  for these two cases.

Basing on the Oliver-Pharr method [25], Novikov et al [44] proposed a technique, which allows determining the contact pressure  $p_m$  during indentation process at any penetration depth from  $P(h)$  dependences, assuming that  $h_s$  is directly proportional to the square root of the load  $P$ :

$$\frac{h_{s(i)}}{h_{s(\max)}} = \left( \frac{P_i}{P_{\max}} \right)^{\frac{1}{2}} \quad (5),$$

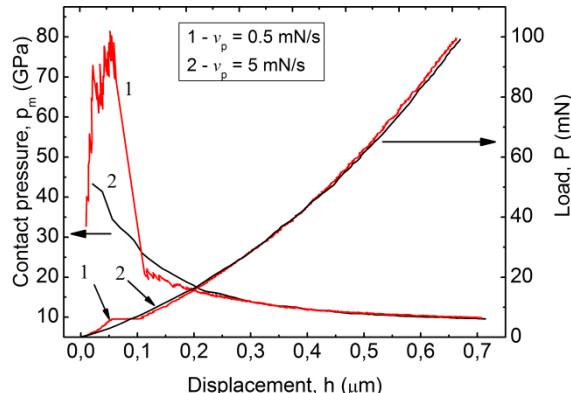
where  $h_{s(i)}$ ,  $h_{c(i)} = h - h_{s(i)}$  and  $P_i$  are, respectively, the elastic bending of the sample surface, the contact depth and load in point „ $i$ ” of the  $P(h)$  curve. Knowing  $h_{s(i)}$ ,  $h_{c(i)}$  in any point of the  $P(h)$  curve can be determined, which allows the estimation of  $p_{c(i)}$  at any penetration depth:

$$p_{c(i)} = \frac{P_i}{A(h_{c(i)})} \quad (6),$$

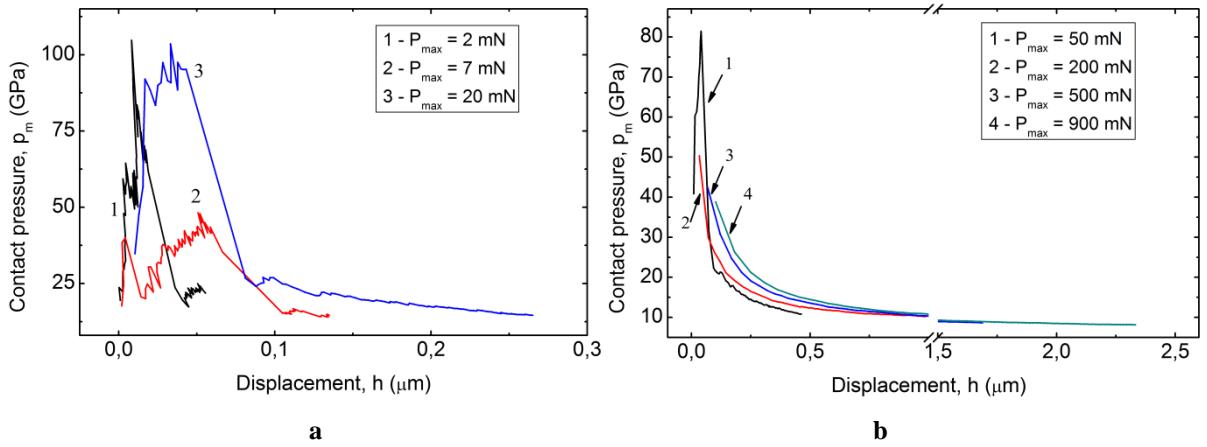
where  $A(h_{c(i)})$  is the projected area at the contact depth  $h_{c(i)}$ .

Using this technique, the  $p_m(h)$  dependences during loading for two cases mentioned above were obtained (Fig. 7). For the indentation with pop-in made at lower loading rate (0.5 mN/s) and strain rate, the contact pressure  $p_m$  demonstrates a sharp increase before the the pop-in as a result of the internal stresses increase, necessary to move „slow” dislocations. Whereas for higher loading rate (5 mN/s), the  $p_m(h)$  curve demonstrates much lower values of  $p_m$  at the beginning of indenter penetration, which decrease gradually, as „fast” dislocations have initially higher kinetic energy and begin to slide at lower stresses. The same evolution of  $p_m(h)$  curves that has the same reason, is observed with the increase of  $P_{\max}$  and strain rate: the  $p_m(h)$  curves corresponding to the indentation process of relatively low strain rates and therefore containing pop-ins, exhibit a considerable increase of  $p_m$  before the pop-in (Fig. 8).

This results demonstrates that higer loading and strain rates cause the generation of dislocations of higher velocity and kinetic energy able to overcome the barriers under lower shear stresses and in this case the transition from elastic to plastic deformation is gradual. For lower loading and strain rates the transition mechanism is different: the dislocations of initially lower velocity and energy need an increase of stresses (confirmed by the calculation of  $p_m$ ) till the critical ones to gain sufficient energy, after which a bulk burst of dislocations takes place causing a pop-in jump and, respectively, a sharp transition from elastic to plastic deformation.



**Fig. 7** Contact pressure versus penetration depth  $p_m(h)$  dependences during loading for 100 mN indentations made at different loading rates: 0.5 and 5 mN/s, and respective  $P(h)$  curves

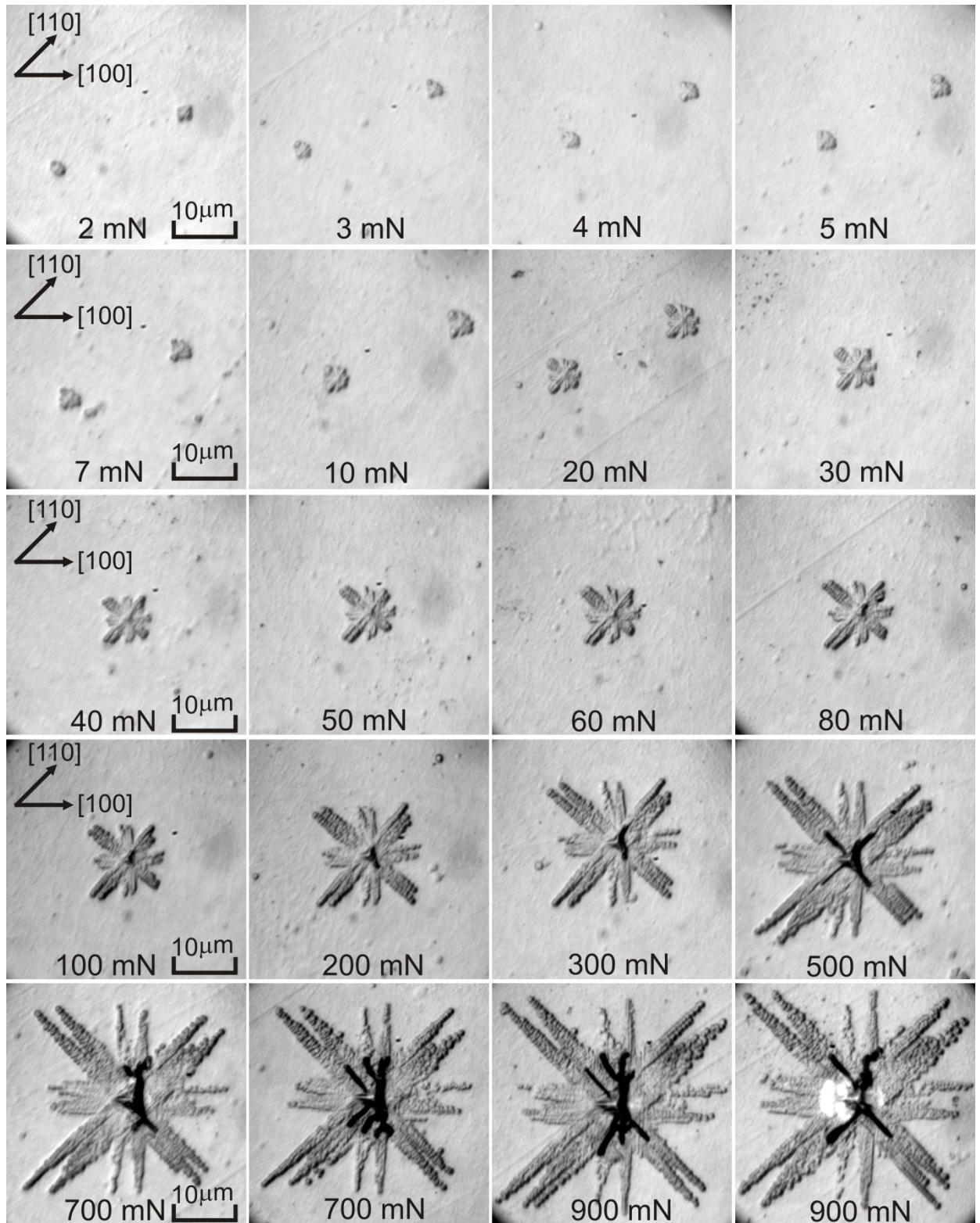


**Fig. 8** Contact pressure versus penetration depth dependences during loading for indentations made with different loads  $P_{max}$ , mN: a – 2, 7, 20; b – 50, 200, 500, 900

One more interesting result confirmed these considerations. One can see from Fig. 3 and 6, that the surges on the  $dh/dt(h)$  curves, caused by sharp increase of the strain rate during pop-ins, disappear with the increase of loading rate, just when the strain rates at the beginning of indenter penetration become higher than the strain rates during pop-ins. This means that just the velocity of dislocations, i.e. their kinetic energy has a determinant role in the elastic-to-plastic transition mechanism. The necessary kinetic energy for dislocation motion is induced by both macroscopic strain rate and stresses, external and internal.

The above presented results allow asserting that the attenuation and disappearance of the pop-ins on the  $P-h$  curves with the increase of peak load (Fig. 4) is not related to the smearing of the effect due to the increased spatial resolution, but it is connected with the increase of loading and strain rate and the change of the elastic-to-plastic transition mechanism from sharp to gradual one.

A comparison of the patterns of dislocation rosettes around the imprints (Fig. 9) with the shape of the  $P-h$  curves shown in Fig. 1, 2 revealed new regularities that allow us to establish a certain hierarchy in the realization of deformation mechanisms in a wide range of loads under nanomicroindentation. As was shown above in Fig. 1, pop-in jumps were recorded on the  $P-h$  curves starting with the smallest load ( $P_{max} = 2$  mN). Two small dislocation rosettes of approximately circular shape are visible for this load in Fig. 9. However, as follows from Fig. 1a, the first jump is formed at a load of  $P_i \approx (0.2 \div 0.3)$  mN. The appearance of the first pop-in jump is due to the initial nucleation of dislocations in the process of nanoindentation.

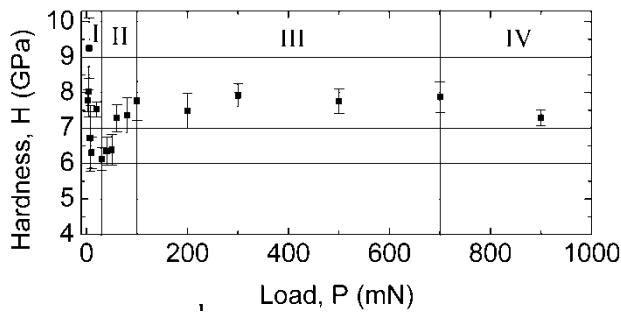


**Fig. 9** Evolution of the dislocation rosettes near the imprints obtained as a result of dynamic nanomicroindentation by various loads in the interval  $P_{max} = (2 \div 900)$  mN

Therefore, it can be assumed that before the first jump, the elastic strain in the crystal predominates over the plastic deformation. With increasing the load value, the internal stresses in the zone under indenter reach critical values, that leads to plastic deformation with the appearance of initial dislocation loops under the imprints. The second pop-in jump occurs at  $P_i \approx (1.4 \div 1.7)$  mN and is due to the

development of dislocation structure formed after the first pop-in jump (compare Fig.1a, the insert, with Fig. 9 ( $P_{max}=2\div4$  mN)).

With the growth in the load in the range  $P_{max}=(5\div50)$  mN, the dislocation structures continue to develop, the edge and screw dislocation arms become more pronounced, and as a result, another pop-in jump appears at the  $P-h$  curves for  $P_i\approx(4.5\div5.0)$  mN (Fig. 1a, b; 2 a-d). The formation of pop-in jumps is also reflected in the course of the hardness curve  $H(P)$ , Fig. 10. Due to the facilitated translational slip of dislocations around the imprint, the hardness of MgO crystals decreases in the interval ( $P_i = (2\div50)$  mN) (stage I on the curve  $H(P)$ ). In the scientific literature this stage is called ISE (Indentation Size Effect) [8,14, 20].



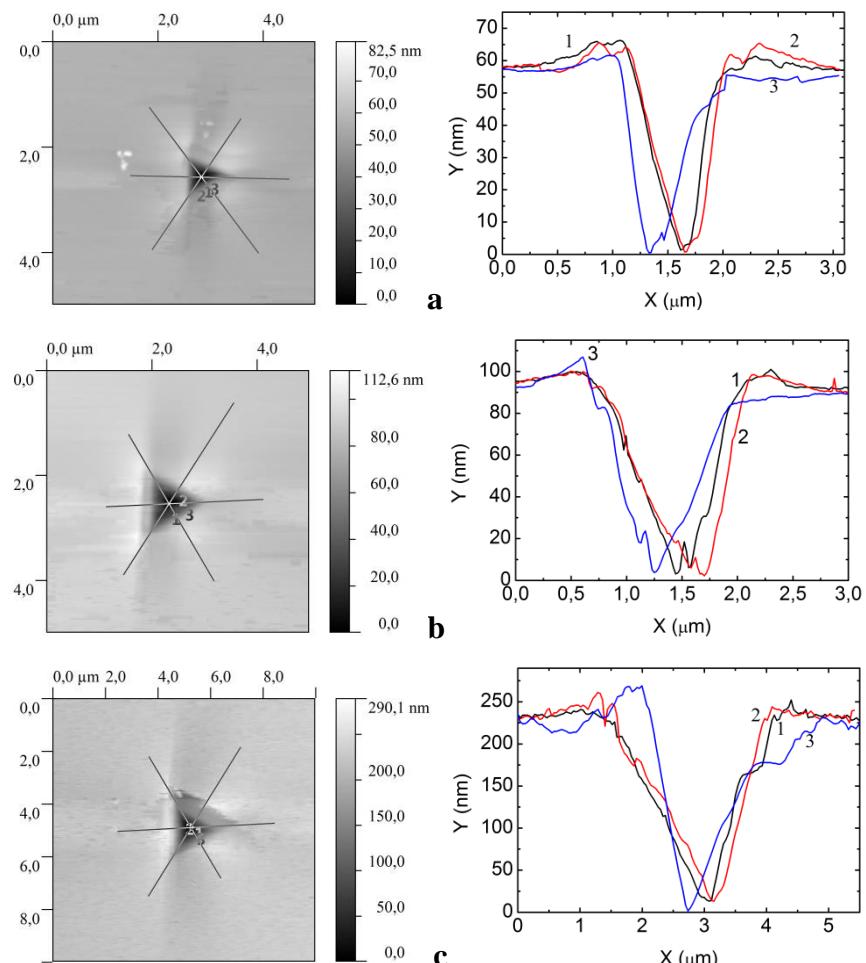
**Fig. 10** The  $H(P)$  hardness-load dependence

As the load increases, (50÷100) mN, and correspondingly, the depth of the imprints grows, the dislocation structures become more complex (Fig. 9, 50÷100 mN). This increases the resistance of the material to the indenter penetration (the section of the curve  $P(h)$ , loading step) and leads to an increase in  $H$  (stage II on the curve  $H(P)$ ). With further increase in the load ( $P_{max} = (200\div700)$  mN), the hardness curve shows a saturation (stage III on the curve  $H(P)$ ). In this interval, the dislocation rosettes actively develop, extend and expand due to the creation of multirow arms (Fig. 9, 200÷900 mN).

At this stage, the multiplication of dislocations takes place, the rosettes are formed from the dislocations located in all the active slip planes of the  $\{110\}_{45}$  ((110)<sub>45</sub>,  $(\bar{1}\bar{1}0)_{45}$ ,  $(\bar{1}10)_{45}$ ,  $(1\bar{1}0)_{45}$ ,  $(101)_{45}$ ,  $(\bar{1}0\bar{1})_{45}$ ,  $(\bar{1}01)_{45}$ ,  $(10\bar{1})_{45}$ ) and  $\{110\}_{90}$  ((110)<sub>90</sub>,  $(\bar{1}\bar{1}0)_{90}$ ,  $(\bar{1}10)_{90}$ ,  $(1\bar{1}0)_{90}$ ) type. All these slip planes intersect mutually and, respectively, dislocation loops located in these planes are also mutually intersected. This leads to the creation of very complex dislocation rosettes in which sedentary dislocations, dislocation walls and disclinations are formed. For this reason, the most complex dislocation-disclination reactions take place in the indentation zone, leading to the translation-rotation processes, fragmentation of the structure, the nanocracks creation and so on [45-48]. In the area under imprints the superhigh internal stresses are created, which are discharged due to the crack formation during the unloading stage.

The cracks are clearly visible in the center of the dislocation rosettes near the imprints at  $P_{max} = (80 \div 900)$  mN (Fig. 9). This process is recorded on the unloading part of  $P$ - $h$  curves as pop-out jumps, that is, these cracks are of a relaxation nature. Along with this, the cracks may appear as well during loading for the loads  $P_{max} > 700$  mN. It leads to a decrease in hardness and the appearance of a softening portion on the  $H(P)$  curve (step IV in Fig. 10).

The data presented above demonstrate the result of relaxation of the MgO single crystal during dynamic indentation by the formation of cracks and elastic-plastic reconstruction of the deformed zone. To confirm this statement, the images of imprints and the micro-relief near them are shown in Fig. 11 for loads  $P_{max} = (7 \div 40)$  mN. The images taken in the atomic force microscope indicate the displacement of the material to the surface with the formation of nanoscale hills of the material near the imprints (pile-up effect), mainly due to the slip of dislocations along the  $\{110\}_{45}$  planes [45-49].



**Fig. 11** AFM images of imprints and the micro-relief near them.  $P_{max}$ , mN: a – 7; b – 10; c – 40

The study of the imprint microstructure using the atomic force microscopy (AFM) showed that the relief of the material in the pile-up zone is not uniform, but it forms a wavy surface with oval bends, which becomes smoother by moving away from the sides of the imprints. It is known [50], that under the action of concentrated load the stresses in a given point of a solid can be described by the equation:

$$\sigma_r = (A \cos \theta) / r \quad (7),$$

where  $\theta$  and  $r$  are the polar coordinates of the given point with respect to the loading point, and  $A$  is a constant. According to equation 7, the stresses around the imprint decrease inverse proportionally to the distance from the applied load  $r$ . Therefore the displacement of material decreases gradually when moving away from the imprint that leads to the decrease of the height of the pile-ups and the diminution of the oval bends. Also it was observed that the surface of the imprints is not absolutely smooth. The irregularities in the form of small steps and facets are clearly seen on the cross section of the imprint surface (Fig. 11) and can be attributed to the development of the translation-rotation deformation. These facts together with several other results (reorientation bands, asterism of Laue spots, fragmentation) [45, 46, 48, 51-53] allowed us to conclude that the displacement of the material during indentation takes place through the dislocation-disclination deformation mechanism leading to rotational effects and intensive movement of material.

## Conclusion

The instrumented nanomicroindentation of the (001) face of MgO single crystals under different loading rate and peak loads revealed different elastic-to-plastic transition: with pop-ins formation - a sharp mechanism, and without pop-ins formation – a gradual one. This difference was explained by different strain rate and kinetic energy of dislocations, the increase of which leads to the transition from the sharp to the gradual mechanism.

For the first time, three types of pop-in jumps were identified, as well as a serration effect, and the relationship between their appearance and the type of dislocation rosettes around the imprints was established. It is shown that the formation of pop-in jumps is due to various mechanisms of plastic deformation:

- 'pop-in'-1 – homogeneous nucleation of sliding dislocation loops near the imprint at the initial stages of indentation;
- 'pop-in'-2 – the development of dislocation structures around the imprints, the formation of edge and screw dislocation beams arms;
- 'pop-in'-3 – further development of the dislocation structures due to the deformation across all the active slip planes of the {110}<sub>45</sub> and {110}<sub>90</sub> type by the multiplication of dislocations.

With further growth of the load, the new deformation structures are formed under the imprints (sedentary dislocations, dislocation walls, disclinations, cracks, etc.). As a result, the translation-rotation mechanism of the deformation takes place on this stage of indentation. During the load removal, the relaxation processes cause the appearance of the pop-out jumps.

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