

Bayesian and classical biomass allometries for open grown valonian oaks $(Q.\ ithaburensis\ subs.\ macrolepis\ L.)$ in a silvopastoral system

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Abstract Allometric models predicting aboveground woody biomass for open grown valonian oak (Q. ithaburensis subs. macrolepis L.) trees growing in a Mediterranean silvopastoral system were built based on Bayesian and classical statistical techniques. The simple power model $M = aD^b$ was used for predicting aboveground woody biomass (M), stem (M_S) and branch $(M_{\rm B})$ biomass through tree diameter (D). An informative Bayesian approach (IB) based on prior information about a and b and increasing variance of predicted values in relation to D was applied on 25 destructively sampled trees for estimating M. Noninformative Bayesian (NB), log-linear regression (LR) and non-linear regression were also built for M, M_S and $M_{\rm B}$. Quite similar M distribution was derived from LR and NB across the D range, totally different from IB predictions which provided biologically sound estimates. Tree height, stem length and crown length did not substantially improve predictions for M, $M_{\rm S}$ and $M_{\rm B}$. Comparisons to oak trees growing in closed stands indicated that open-grown oaks sustain much less stem biomass but maintain larger branch biomass than forest-grown counterparts. Comparisons to published values for open-grown green ash trees supported the hypothesis that open grown broadleaved specimens may sustain similar M values, irrespectively of species, growth conditions and tree size. On the contrary, allocation pattern of organic matter to stem and branches seems to vary by species and/or site conditions. Finally, predictions for b=2.67 derived from a theoretical model was not supported by this dataset.

Keywords Mediterranean agroforestry · Carbon stocks · Regression · Scaling · Greece

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Introduction

Silvopastoral systems are considered to be one of the most prominent agroforestry practice in the Mediterranean landscape and may considered to be both a source or a sink of carbon depending on their function and structure (Montagnini and Nair 2004; Schoeneberger 2009). Additionally, agroforestry systems are reported to provide important opportunities for adaptation and mitigation of climate change (Gitay et al. 2002, p. 37). Murthy et al. (2013) report that carbon

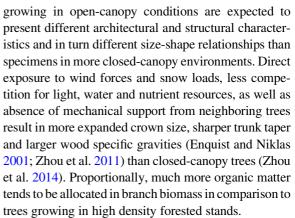


stocks in tree biomass in such a system is generally much higher than a treeless land, but empirical estimates are rather limited (Makungwa et al. 2013; Zhou et al. 2014). One of the main carbon pool in a silvopastoral system is expected to be the aboveground woody biomass (M) of tree species located in a specific area, although several other components may significantly contribute to carbon storage. Biomass estimates for agroforestry systems and therefore allometric equations that relate tree M to the diameter at breast height (D) and/or tree height (H) are rather limited. Specifically for Mediterranean silvopastoral systems, such information is largely missing from the literature.

On the other hand, a vast amount of tree allometries were developed for closed forest stands. Linear regression analysis on logarithmically transformed biomass data and non-linear regression have extensively been used to derive an empirical equation between M and D or H. The aforementioned approaches have been based on the classical statistical theories, but nowadays Bayesian theorem is rapidly emerging in ecological studies and specifically in forest biomass research (Zapata-Cuartas et al. 2012; Tredennick et al. 2013; Zell et al. 2014; Zianis et al. 2016). Bayes rule can be used to obtain probability distributions for the predicted biomass values as well as for the scaling parameters of allometric relationship (Gilks et al. 1995; McCarthy 2007, pp. 119-120; Gelman et al. 2014, p. 355).

The theoretical background on tree allometry originates with the proposition that tree stem is considered to be an ideal geometric object and therefore $M \propto V \propto D^2 H$, where V is stem volume. Biomechanical constraints assume that $H \propto D^{\gamma}$ or $M \propto D^{b=2+\gamma}$ and under fractal geometry 2 < b < 3. An integrated approach based on the fractal distribution of tree branching system was presented by (West et al. 1997; WBE hereafter) and predicted that $M \propto D^{2.67}$ and $M \propto H^4$, applicable for trees growing across the globe. Analyses on a plethora of empirical aboveground biomass allometries indicated that the value of b is statistically different from the theoretical estimate of 2.67 (Muller-Landau et al. 2006; Zianis 2008; Navar 2010 to cite but a few).

Many empirical relationships were reported for trees growing in closed forest stands and plantations but equations for open grown trees are largely missing (Kort and Turnock 1999; Zhou et al. 2014). Trees



The main objective of this study was to report potential deviation of predicted values obtained by classical and Bayesian allometries for aboveground biomass of tree compartments for valonian oak (*Q. ithaburensis* subs. *macrolepis* L.) specimens growing in an open-canopy Mediterranean silvopastoral ecosystem. Secondly, the obtained biomass estimates were compared to published values for open-grown ash trees. Thirdly, the differences in the allometric relationships between open-canopy and closed-canopy trees for *Quercus* genus reported in the literature were analyzed. Finally, theoretical predictions from WBE model were validated against empirical values obtained by the analyzed dataset.

Materials and methods

Study area

The studied forest is located in the western part of central Greece and about 23 km west of Agrinio town. The heterogeneity of the landscape, consisting of agricultural, grazing and forested lands, characterizes the studied silvopastoral system. In the study area, valonia oaks are found on shallow calcareous soils in all aspects within an elevation range from 70 to 400 m above sea level. Mean yearly rainfall amounts to 938.5 mm and mean yearly temperature is 16.8 °C (National Meteorological Service for the period 1956–2012). The forested stands cover an area of more than 4400 ha while partially forested area amounts to 3300 ha. The stands are even-aged and range from 200 to 240 years. Stand density ranges from 50 to 60 trees per hectare.



Biomass measurements

Twenty five valonian oak trees were selected and cut down. Diameter at breast height (1.3 m above ground) was measured before cutting and tree height (H), stem $(S_{\rm L})$ and crown length $(C_{\rm L})$ were recorded after cutting the tree. Branches were separated from the stem after felling. Fresh weights were measured separately for stem and for each of the main branches (up to four for some trees). Two discs were removed from the stem at 0.3 m from the base and the base of crown. The fresh weight of discs was measured in the field and their dry weight was determined (oven dried at 80 °C until a constant weight was reached) in the laboratory. The oven dried biomass over the fresh weight (measured in the field) from each disc was therefore determined and their average value was applied to the stem fresh weight to obtain dry stem biomass (M_S) . For each branch, a disc was removed near its base (about 5 cm from the insertion point for large branches and about 2 cm for small branches) and the oven dried biomass over the fresh weight from each disc was determined. This value was multiplied by the fresh branch weight to derive dry weight for each branch. The summation of branches' dry weight was therefore obtained $(M_{\rm B})$. Total aboveground tree woody biomass (M) was the sum of $M_{\rm S}$ and $M_{\rm B}$.

Classical modeling techniques

Two different frameworks were used to model the allometric relationships in our datasets: the classical regression and the Bayesian analysis. Under the classical framework two different approaches were used (Payandeh 1981; Chiyenda and Kozak 1982), namely the intrinsically linear regression of logarithmically transformed data (LR), which assumes a multiplicative error and thus

$$ln Y = ln a + b ln X$$
(1)

and the intrinsically nonlinear regression (NLR), assuming an additive error term where

$$Y = aX^b (2)$$

A bias is introduced when predictions from LR are back transformed to the ordinal scale and thus a correction factor should be used (Sprugel 1983). In

NLR, a weight function, usually based on a negative power of *X*, is introduced to avoid negative predictions of *Y*. The most appropriate approach (either LR or NLR), was selected using the corrected Akaike information criterion (*A*) proposed by Xiao et al. (2011),

$$A = 2k - 2\ln(L) + 2k(k+1)/(n-k-1)$$
(3)

where k, n and L denote the number of parameters, the sample size and the corresponding likelihood of the model, respectively. The regression with the lowest A value was selected as the most appropriate empirical model.

In the case of Eq. 1, appropriate formulae should be used in order to predict the mean response for diameter *D* at normal scale by the following equation:

$$M = e^{(\ln a + b \ln D + \nu/2)} \tag{4}$$

where $e^{v/2}$ is the correction factor to eliminate the bias from log-transformation, and

$$v = M_{se} (1 + [1, \ln D](\mathbf{X}'\mathbf{X})[1, \ln D]')$$
 (5)

denotes the variance of the predicted value, $M_{\rm se}$ is the mean square error of the linear regression and $\bf X$ is the design matrix of the linear regression. We used the method by Zou et al. (2009) for the estimation of predicted intervals (specifically, Eqs. 3 and 4 from the aforementioned reference for n=1):

Lower limit of
$$M = M \exp \left[-\left(z_{1-a/2}^2 v + (v/2)^2\right)^{1/2} \right]$$
(6)

Upper limit of
$$M = M \exp \left[\left(z_{1-a/2}^2 v + (v/2)^2 \right)^{1/2} \right]$$
(7)

where $z_{1-a/2}$ denotes the respected quantile of the standard normal distribution.

Tree height (H), stem length (S_L) and crown length (C_L) were also used as regressor variables for predicting M, M_S and M_B under the LR, NLR and NB approaches. For the NLR approach (i.e., Eq. 2), the iterative procedures in the free software environment R (R Development Core Team 2011) provided the 95% predicted values of M based on the nls command.



Bayesian modeling techniques

In the Bayesian context, the parameters in statistical models are allowed to follow pre-specified probability distributions, not assumed to be fixed points as suggested by the classical method. Thus, previously empirical information and/or theoretical expectations are easily incorporated in the modeling approach (McCarthy 2007, p. 23).

The first step for building an informative Bayesian model of aboveground woody dry biomass (*M*) was the specification of prior distributions for the allometric parameters. To this end, a large compendium of published *a* and *b* values was used based on several databases for forested stands (Ter-Mikaelian and Korzukhin 1997; Eamus et al. 2000; Zianis and Mencuccini 2003; Jenkins et al. 2004; Zianis et al. 2005; Pilli et al. 2006; Zianis 2008; Navar 2009; Henry et al. 2011; Zapata-Cuartas et al. 2012). Thus,

 $a \sim \text{Log} - \text{Normal distribution } (-2.0, 0.5),$ $b \sim \text{Normal distribution } (2.35, 0.1).$

Furthermore, following Zianis et al. (2016) the variance (v) of the predicted M_i at a specified D_i was modelled as $v_i \propto M_i^c = g(aD_i^b)^c$

and according to Ducey et al. (2009) c=1.5 for trees growing in an Amazonian region. In the absence of further information about its value for open-grown trees, the aforementioned estimate for c was used in our dataset. The variance in logarithmic scale may be determined as $z = \ln(1 + v/M^2)$, as reported in Thomopoulos and Johnson (2003). Based on the aforementioned priors and relationships, the following informative Bayesian (IB) approach was built:

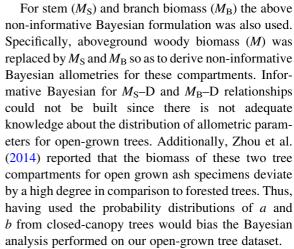
$$M_i \sim \text{Log} - \text{Normal } (\mu_i, z_i),$$

where μ_i is the $\ln(aD^b)$, z_i is the $\ln(1 + v_i/M_i^2)$, v_i is the $g(aD_i^b)^c$, g is the uniform distribution (0.01, 0.05).

For comparison, the following non-informative Bayesian method (NB) was developed based on the most commonly used log-linear regression, with non-informative priors about the parameters:

$$\ln M_i \sim N(\ln a + b \ln D_i, v)$$

 $\ln a$ is the uniform distribution (-4, -1), b is the uniform distribution (1.5, 3.5) and, v is the gamma distribution (0.1, 0.01), while predictions at normal scale were derived as, M_i is the log-normal distribution $(\ln M_i, v)$.



WinBUGS, a free software (Lunn et al. 2000) based on Markov chain Monte Carlo methods (Spiegelhalter et al. 2007), was used in order to generate posterior distributions and in turn to draw estimates for parameters and predictions (via Gibbs sampler). A burn-in period of 2000 steps and 100,000 iterations with a step of 2, were used to obtain 98,000 estimations per variable or parameter. In cases where autocorrelation of MCMC chain was reported, it was eliminated by increasing the number of iterations to 200,000.

Goodness of fit criteria

The mean absolute percentage difference $(P_{\rm D})$ between the predictions and the observed data is reported to be one of the most appropriate criterions for assessing model performance in tree allometric relationships (Parresol 1999; Zianis and Mencuccini 2003; Sileshi 2014) and was therefore used in this study. The absolute difference between observed and predicted values divided by the observed is calculated for each tree and the average value of these deviations is multiplied by 100 to define $P_{\rm D}$, or

$$P_{\rm D} = 1/n \times \Sigma(|1 - P_{\rm i}/O_{\rm i}|) \times 100$$

where P_i and O_i denote predicted and corresponding observed biomass value for the *i*th tree (i = 1 to n = 25).

Values close to 0% indicate accurate predictions while to the best of our knowledge, there is not a published cut-off maximum value for rejecting models. It should be mentioned that for a specific diameter, absolute percentage difference may reach up to 80 or to 37% when the whole dataset is considered



(Ketterings et al. 2001). The lower the $P_{\rm D}$ the better the model, when comparing different models for the same dataset. The coefficient of determination (R^2) was only used as an indicative criterion since Sileshi (2014) reported several caveats related to this statistic.

Results

Stem diameter (D) for the sampled trees ranged from 3.18 to 99.4 cm, covering the size spectrum of the

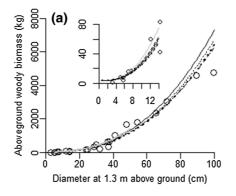
diameter distribution recorded in the forest management plans with 10 < D < 84 cm. Tree height (H) varied from 1.65 to 12.5 m, stem length ($S_{\rm L}$) from 0.6 to 3.9 m, and crown length ($C_{\rm L}$) from 1.40 to 10.12 m. Aboveground woody biomass (M) covered four orders of magnitude from 0.51 to 4753 kg, branch biomass ($M_{\rm B}$) varied from 0.18 to 4123 kg and stem biomass ($M_{\rm S}$) from 0.33 to 884.50 kg. The means and the standard deviations of the aforementioned variables are reported in Table 1. Scatter plots of M, $M_{\rm B}$ and $M_{\rm S}$ against D are presented in Fig. 1a–c, while the plot of

Table 1 Dendrometric characteristic of 25 destructively sampled opengrown oak trees

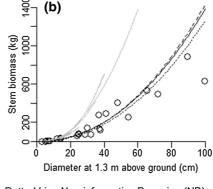
Variable	Mean	Range	SD
Diameter at breast height (D cm)	32.77	3.18-99.4	26.4
Total tree height (H m)	7.54	1.65-12.50	3.72
Stem $(S_L m)$	1.99	0.60-3.90	0.88
Crown length $(C_L m)$	5.76	1.40-10.12	3.02
Aboveground woody biomass (M kg)	905.10	0.51-4753	1392.87
Branch biomass $(M_{\rm B} \text{ kg})$	652.68	0.18-4123	1108.14
Stem biomass $(M_S \text{ kg})$	185.05	0.33-884.50	235.02

Standard deviation (SD) is also reported

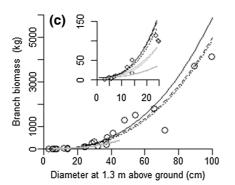
Fig. 1 Allometric relationships based on different regression techniques for a aboveground woody biomass against tree diameter, b stem biomass against tree diameter, c branch biomass against tree diameter and d aboveground woody biomass against tree height. Insets in a and c were provided for clarity. Grey lines depict published empirical allometries for oak specimens growing in closed stands. Raw biomass data collected from the studied area are shown with open circles

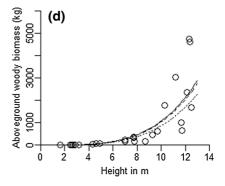


Solid Line:Classical regression (LR)
Bold Dotted Line:Informative Bayesian (IB)
Grey Lines:Published equations



Dotted Line:Non-informative Bayesian (NB) Dash Lines:Non-Linear regression (NLR)







M against H is depicted in Fig. 1d. Using S_L and C_L as the regressor variables did not provide any strong allometric relationships for M, M_S or M_B under the three applied approaches (i.e., LR, NLR and NB).

Predictions of M

Within the classical statistical paradigm and based on the corrected Akaike criterion (Eq. 3), LR is supported against NLR (A equaled to 287.83 and 346.27, respectively), indicating that the analyzed M–D dataset follows a log-normal distribution with multiplicative error structure. As reported in Table 2, LR technique yielded slightly better predictions in M–D allometry, since P_D varied from 37 (LR) to 41% (IB), while size-shape scaling was not statistically

different across the applied methods (the range of b values overlaps among the regression methods). The narrowest 5% credible interval for b was derived from the IB approach and the widest from the NB. Additionally, the inferences from LR and NB techniques were very similar as exemplified by the confidence and credible intervals, respectively, for the scaling parameters a and b. Across the D range, IB and NLR predict quite similar average M values, even though the mean b values for the two techniques differ by more than 0.07. The large relative difference of parameter a between the two approaches compensates for the discrepancy in b, resulting in small differences in M. For D < 24 cm, IB produced larger average M prediction than LR but smaller M values were obtained for bigger trees (e.g., for D = 99.3 cm the

Table 2 Empirical values for the scaling parameters in M-D and M-H allometries under the classical and Bayesian approaches

M–D allometry	a^{A}	SE a	b^{A}	SE b	R^2	$P_{\mathrm{D}} \left(\%\right)^{\mathrm{B}}$
Classical approach						
Log-linear (LR) ^C	-2.5524	0.2793	2.4688	0.0579	0.97	37
	(-3.1302 - 1.9746)		(2.2913 2.6463)			
Nonlinear regression weighted (NLR) ^D	0.1156	0.033	2.3682	0.077	0.97	38
	(0.0611 0.1970)		(2.2207 2.5337)			
Bayesian approach						
Non-informative Bayesian (NB)	-2.558	0.2928	2.47	0.09	0.97	37
	(-3.134 - 1.974)		(2.292 2.648)			
Informative Bayesian (IB)	0.0835	0.0158	2.443	0.0524	0.96	41
	(0.0539 0.1163)		(2.351 2.552)			
M–H allometry	a^{A}	SE a	b^{A}	SE b	R^2	$P_{\mathrm{D}} \left(\%\right)^{\mathrm{B}}$
Classical approach						
Log-linear (LR) ^E	-1.8969	0.3925	3.7756	0.20	0.93	66
	(-2.7089 - 1.0870)		(3.3612 4.1900)			
Nonlinear regression weighted (NLR) ^F	0.1877	0.065	3.7467	0.1970	0.93	65
	(0.077 0.3543)		(3.3357 4.1925)			
Bayesian approach						
Non-informative Bayesian (NB)	-1.66	0.237	3.661	0.1319	0.94	65
	(-1.985 -1.126)		(3.375 3.879)			

Standard error (SE) for a and b, coefficient of determination (R^2) and mean absolute percentage difference (P_D) are also reported

F Weight for the NLR in M-H allometry is H^{-8} . The R^2 for log-linear models are actually pseudo-R and is only an indicative value



A Mean value and credible or confidence intervals in parenthesis

^B $P_{\rm D} = 1/n \times \Sigma(|1 - P_{\rm i}/O_{\rm i}|) \times 100$

^C Correction factor = 1.08

^D Weight for the NLR in M-D allometry is D^{-4}

^E Correction factor = 1.20

relative difference is 32%). In terms of uncertainty, wider prediction intervals were obtained from the IB for D < 15 cm, in relation to the LR and NB, but the reverse trend was derived for $D \ge 15$ cm.

A strong positive correlation $(R^2 = 95\%)$ was obtained when the observed data were regressed against predicted M values derived from LR. The intercept was about 121 and the slope = 0.75 (Table 3). Similar statistics were derived from the NB regression. The corresponding figures for the IB method indicated a lower underestimation in comparison to the previous approaches since the intercept ≈ 114 and the slope equaled to 0.85. Quite similar results were reported for NLR (intercept ≈ 92 and slope = 0.87). In all cases, the variability in predicted M values explained more than 95% of the variability in the raw data, the intercept was not significantly different from zero, the slope was significantly different from one (at 95% level), but the overall underestimation was higher for LR and NB regressions.

Table 3 Linear regression statistics for observed against predicted values derived from log-linear (LR), weighted nonlinear regression (NLR), noninformative Bayesian (NB) and informative Bayesian (IB) for different tree compartments. The coefficient of determination (R^2) , F statistic and the p value are also reported. The confidence intervals at 95% level for the intercept and the slope are presented in the parentheses

24.6 kg for IB, while for LR and NB, M predictions varied from 2.4 to 14.5 kg. For tree diameter equal to 24.8 cm, the three approaches provided different probability distributions for M (Fig. 2b), even though LR and NB presented similar 95% upper limit (ca. 500 kg). For D close to the average value of raw diameters (D = 37.30 cm; Fig. 2c), LR predicted M to vary between 280.5 and 1453.2 kg and for NB the 95% *M* interval varied from 250.5 to 1,421.1 kg. The corresponding prediction interval for IB ranged from 331.40 to 970.90 kg. For the largest recording sampled tree (D = 99.4 cm; Fig. 2d), LR and NB provided practically identical log-normal probability Intercent Slone P value

In Fig. 2, the probability distributions of predicted

M values, derived from the three regression tech-

niques, are illustrated for different diameters. NLR

was dropped from this analysis since it predicted very

narrow normal distribution, implying unsound biolog-

ical outputs. For small diameter (D = 5.73 cm;

Fig. 2a), the 95% interval of M ranged from 1.33 to

Tree compartment	Intercept	Slope	R^2	F	P value
Total aboveground w	oody biomass (M)				
LR	121	0.75	0.95	481	< 0.001
	(-23 to 267)	(0.68-0.83)			
NLR	92	0.87	0.95	557	< 0.001
	(-44 to 229)	(0.79-0.94)			
NB	122	0.75	0.95	481	< 0.001
	(-24 to 268)	(0.68-0.82)			
IB	114	0.85	0.95	500	< 0.001
	(-29 to 258)	(0.77-0.94)			
Stem biomass (M_S)					
LR	43.7	0.62	0.84	127	< 0.001
	(-3 to 93)	(0.50-0.73)			
NLR	45	0.60	0.83	125	< 0.001
	(-1.75 to 92)	(0.48-0.70)			
NB	43	0.62	0.84	127	< 0.001
	(-3 to 90)	(0.50-0.73)			
Branch biomass $(M_{\rm B})$					
LR	67.7	0.73	0.92	270	< 0.001
	(-82 to 210)	(0.64-0.83)			
NLR	50	0.86	0.92	277	< 0.001
	(-99 to 199)	(0.79-0.98)			
NB	63	0.75	0.92	272	< 0.001
	(-87 to 213)	(0.66-0.85)			



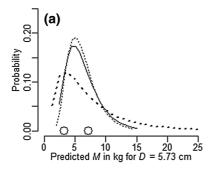
Fig. 2 Probability distributions for predicting aboveground woody biomass (*M*) derived from the three applied regression techniques at

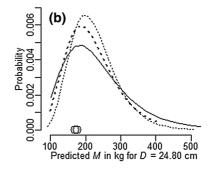
a D = 5.73 cm,

bD = 24.80 cm

c D = 37.30 cm and

d *D* = 99.40 cm. The "superiority" of IB technique is depicted in **d** which is the only one to provide biologically sound upper limit for *M*



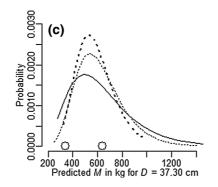


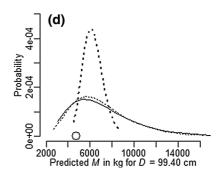
Solid Line: Classical regression (LR)

Dotted Line: Non-informative Bayesian (NB)

Bold Dotted Line:Informative Bayesian (IB)

Open circle:Data for the specific diameter





distributions for M, totally different than the one derived from IB. For LR and NB the 95% uncertainty level ranged from around 3000–17,000 kg (mean = 7179.23 kg) while for IB the range was between 4500 and 8600 kg (mean = 6308.10 kg).

The three applied regressions (LR, NB and NLR) provided quite similar predicted values for M, when H was used as the independent variable (Fig. 1d). The average absolute deviation was ca. 66%, while higher $P_{\rm D}$ values were derived for allometries developed for stem and branch compartments (80 and 70%, respectively). These results indicate that biased estimations may be obtained if allometric equation is solely based on H.

Predictions of $M_{\rm S}$

As expected, LR and NB actually provided identical values for allometric parameters $\ln a$ and b, which were not statistically different from the values obtained from NLR (Table 4). It is clearly illustrated in Fig. 1b that the three applied regression approaches for the studied oaks provided quite similar $M_{\rm S}$ values across

the D spectrum. Even though the Akaike criterion showed that LR technique (A = 234.27) was better than NLR (A = 293.86), P_D indicated that there is no preference of one approach over the other (41.5% for LR and 42% for NLR; Table 4). The linear regression of raw M_S data against predicted values, derived from the three applied regressions (LR, NLR and NB), explained about 84% of the variability (Table 3). For LR, the intercept was ca. 44 and the slope equaled 0.62; for NLR the corresponding parameters were 45 and 0.60, while for NB the intercept was 43 and the slope was around 0.62. In all cases, M_S was underestimated, the intercepts were not significantly different from zero but the slopes were significantly different from one (Table 3). Including S_L , C_L or H did not substantially improved predictions (results not shown).

Predictions of $M_{\rm B}$

The bias in $M_{\rm B}$ –D allometry was around 60% ($P_{\rm D}$ in Table 4) for all the applied methods. Irrespective of the regression technique, $M_{\rm B}$ predictions were similar



Table 4 Empirical values for the scaling parameters in M_S –D and M_B –D allometries under the classical and Bayesian approaches

M _S –D allometry	a^{A}	SE a	$b^{ m A}$	SE b	R^2	$P_{\rm D} \ (\%)^{\rm B}$
Classical approach						
Log-linear (LR) ^C	-2.6007	0.2945	2.1167	0.0904	0.95	41.5
	(-3.2100 to1.9914)		(1.9295 2.3039)			
Nonlinear regression weighted (NLR) ^D	0.0755	0.0208	2.1388	0.0866	0.95	42
	(0.0432 0.1207)		(1.9754 2.3066)			
Bayesian approach						
Non-informative Bayesian (NB)	-2.5990	0.3000	2.1160	0.0944	0.94	42
	(-3.2050 to 1.9880)		(1.9290 2.3030)			
M _B –D allometry	a^*	SE a	<i>b</i> *	SE b	R^2	P _D (%)
Classical approach						
Log-linear (LR) ^E	-3.5154	0.3896	2.6140	0.1197	0.94	61
	(-4.3213 to 2.7093)		(2.36634 2.8617)			
Nonlinear regression weighted (NLR) ^F	0.0454	0.015	2.5198	0.1000	0.94	60
	(0.0211-0.083)		(2.3821 2.7520)			
Bayesian approach						
Non-informative Bayesian (NB)	-3.429	0.3353	2.589	0.105	0.94	60
	(-3.956 to 2.692)		(2.36-2.762)			

Standard error (SE) for a and b, coefficient of determination (R^2) and mean absolute percentage difference (P_D) are also reported

for small trees ($D \le 25$ cm; inset in Fig. 1c), but LR provided the largest values for bigger trees (Fig. 1c). NB and NLR predicted quite similar $M_{\rm B}$ values across the D range. The observed $M_{\rm B}$ data were linearly regressed against predictions derived from the three approaches (Table 3). The value of R^2 was equal to 92, irrespective of the applied method. For LR, the intercept was 68 (-82 to 210) and the slope was 0.73 (0.64–0.83). The corresponding values for NB were 63 (-87 to 213) and 0.75 (0.66-0.85). For NLR, the intercept equaled 50 (-99 to 199) and slope 0.86(0.79-0.98). For the three applied regressions, the confidence intervals for the intercepts included zero but the value of one was not included in the confidence intervals of the slopes. Inserting tree height (H), as a second independent variable did not substantially improve the predictions ($P_D = 55.1\%$) Comparisons to published equations developed for trees growing in American and European oak forest stands, indicates that branch biomass fells below the analyzed opengrown trees, across the *D* range (grey lines in Fig. 1c).

Discussion

The results presented in this article complement tree biomass allometry for open-grown trees. One of the main finding illustrates that both the classical and Bayesian regressions explained much of the variability inherent in aboveground biomass compartments of open grown valonian trees (Fig. 1). However, it should be pointed out that the informative Bayesian model (IB) provided biologically sound predictions while LR and NB approaches failed to derive realistic probability distributions for total above ground woody biomass.

The 'biological' inconsistency of LR and NB is clearly depicted in Fig. 2d, where both techniques



A Mean value and credible or confidence intervals in parenthesis

^B $P_{\rm D} = 1/n \times \Sigma(|1 - P_{\rm i}/O_{\rm i}|) \times 100$

^C Correction factor = 1.09

^D Weight for the NLR in M_S –D allometry is $D^{-4.5}$

^E Correction factor = 1.17

^F Weight for the NLR in $M_{\rm B}$ -D allometry is $D^{-4.5}$. The R^2 for non-linear models are actually pseudo-R and is only an indicative value

predict an upper limit (at 95% level) of M around 16 ton. For a tree with D = 99.40 cm; such a tree is expected to collapse under its own weight. The probability distribution from IB seems to follow a more realistic pattern than LR and NB, as illustrated in Fig. 2a-d. Not enough data were available to empirically support this finding, but bearing in mind that trees sustain similar amount of aboveground organic matter, irrespective of the growing environment (closed stands versus open grown trees in Fig. 1a; Zhou et al. 2014), direct comparisons to published data from trees growing in forest stands can be made. For example, Brown (1997) reported that a tree (tropical species) with D = 97.3 cm attained 4386.60 kg of M (including foliage) while for a specimen with the corresponding D = 99.50 cmvalue 8962.30 kg. The predictions obtained from LR and NB greatly diverge from these observed values, providing unsound uncertainty predictions, but IB approach derived biologically sound M values (for D = 99.40 cm, M ranges from 4523 to 8675 kg; Fig. 2d).

Thus, a coherent analysis for tree biomass allometries should not be based solely on mean predicted values but on their associated uncertainties, as well. Within the classical framework of log-transformed data, linear regressions (LR approach) on different datasets, each one containing several destructively sampled trees, are needed in order to make statistically sound inferences about biomass variability for a specific diameter. However, such an approach is not feasible and rarely (if ever) being applied due to monetary and time restrictions. In Bayesian analysis this restriction is overcome, since biomass variance is modeled in a way that reflects its heteroscedasticity property and derived credible intervals are directly associated with their probability, based on prior information and the collected biomass data (Ellison 2004; McCarthy 2007, pp. 27–29).

Larger bias was reported for open-grown valonian oaks in relation to specimens growing in forested ecosystems. The value of $P_{\rm D}$ ranged between 37 and 41%, depending on the regression approach used for the studied species (Table 2), while $P_{\rm D}$ is usually around 20% for forest trees. A larger degree of variability of M for a specific D is therefore expected for open-grown trees. Similar results were derived for stem and branch biomass, even though R^2 values were quite high (Table 4). As clearly illustrated by Sileshi

(2014), R^2 should be used in conjunction to other goodness-of-fit statistics to test the performance of empirical allometric models and the results in this article support this recommendation.

The obtained large deviations between observed and predicted biomass values are in accordance to the outcomes recently presented by Zhou et al. (2014), who developed aboveground woody biomass equations for coniferous and broadleaved open-grown trees. The value of R^2 , for M-D, M_S-D and M_B-D allometries was equal to 0.97, 0.95 and 0.89, respectively, for green ash trees. Direct comparisons with the predicted values presented in the aforementioned article could not be made, since the lower predicted value for green ash trees with D < 15 cm provides negative biomass estimate, implying bias in their empirical models. However, the raw data by Zhou et al. (2014) for D ca. 15 cm corresponded to M around 80 kg (see Fig. 2a3 in Zhou et al. 2014), which is quite similar to our dataset (for D = 14.33 cm M = 80.71 kg; Fig. 1a). The value of M_S for green ash, at the specific diameter, was about 40 kg (see Fig. 2a1 in Zhou et al. 2014) and close to the valonian oak data (for D = 14.33 cm $M_{\rm S}=31.87$ kg; Fig. 1b), while the $M_{\rm B}$ for green ash ranged from 40 to 100 kg (see Fig. 2a2 in Zhou et al. 2014), including the value of 50.84 kg found in the valonian oak dataset (Fig. 1c).

Green ash and valonian oak trees sustained similar M values for D \approx 28.5 cm (for oak M = 351.99 kg; for ash 320 < M < 420 kg). Stem biomass (M_S) for oaks was smaller (for D = 28.7 cm $M_S = 71.28$ kg; Fig. 1b) in comparison to ash trees (M_S ranged from ca. 220–260 kg; see Fig. 2a1 in Zhou et al. 2014). On the other hand, $M_{\rm B}$ for oaks was larger than ash trees for trees with similar stature. For $D \approx 42$ cm, both species sustained ca. 1000 kg of M. Organic matter was equally allocated to stem and branch compartments for ash trees (around 500 kg) but not for valonian oaks ($M_S \approx 216 \text{ kg}$ and $M_B \approx 714 \text{ kg}$). These results support the line of reasoning presented by Zhou et al. (2014) suggesting that more organic matter is allocated to branch compartment for opengrown trees in relation to stem, than in close-canopy counterparts.

This preliminary comparison between ash and valonian oak trees puts forward the hypothesis that open grown broadleaved specimens may sustain similar total aboveground woody biomass, irrespective of species, growth conditions and tree size. As a



corollary, a 'global' allometric equation for M-D relationship may hold valid for ecosystems including open grown trees. This kind of equation may be developed based on the concept of generalized regressions (Pastor et al. 1984) or on pooled data regression (Zapata-Cuartas et al. 2012). On the contrary, allocation pattern of organic matter to stem and branches seems to vary by species and/or site conditions and therefore 'local' oriented empirical equations should be developed in cases where predictions on $M_{\rm S}$ and $M_{\rm B}$ are needed. To robustly test these hypotheses, extensive biomass datasets originating from different sites and covering several tree species should be analyzed on a statistically sound framework (based on Bayesian modeling).

Comparisons against published equations for trees growing in forested stands illustrated small differences in M. For example, setting D=14 cm the three analyzed techniques yielded a value of M between 52.5 and 60 kg, while the corresponding M prediction from a Q. conferta stand in Greece derived a value of 71 kg (grey line in the inset at Fig. 1a). A value of 60 kg, for the same D, was reported for several oak trees growing in UK. For D=50 cm, the British oak trees sustain 1383 kg of M (grey line in Fig. 1a), while across the three approaches M ranged between 1181 and 1316 kg. The published equations are reported in Zianis et al. (2005).

Comparisons to published equations built for stem and branch compartments for oak trees growing in closed European and American stands presented similar patterns as the ones provided by Zhou et al. (2014) for ash trees. For example, predictions of M_S for several oak species growing in the northern American forests (Ter-Mikaelian and Korzukhin 1997), diverge upwards (grey lines in Fig. 1b) in relation to the trees harvested from the studied ecosystem. Specifically, at D = 40 cm predictions for M_S ranged between 581 and 707 kg for American oaks, while the corresponding figure for the opengrown trees was around 200 kg. The ratio of stem biomass from closed-grown trees over open-grown specimens increases linearly from small (D = 5 cm; ratio ≈ 1.44) to average stature trees (D = 35 cm; ratio \approx 3) and remains constant for larger trees.

Thus, oak trees growing in closed canopies sustain much larger stem biomass than open-grown counterparts (Fig. 1b), but maintain smaller branch biomass (Fig. 1c) across the diameter range. Extensive tree crowns and sharper trunk morphology for open-grown specimens may explain these trends. These findings infer that forest-derived equations should not be applied for estimating stem and branch biomass for open canopy trees. Aboveground woody biomass seems not to be differentiated between open-grown and forest-grown oak trees (relative difference less than 10% as illustrated in Fig. 1a), but the relative difference for open-canopy and closed-canopy ash trees attained a value of 18% (Zhou et al. 2014). Whether forest-derived equations could be used potentially for predicting total aboveground woody biomass for open-grown trees is not clearly demonstrated from the analyses on these two broadleaved species (valonian oak and green ash) and further research is needed.

Surpassingly, tree height did not significantly contribute in capturing much of the variability in woody biomass, either as a sole independent variable (Fig. 1d) or in combination to stem diameter. Additionally given the multicollinearity caveat (Zianis and Radoglou 2006) originating from the strong relationship between H and D, interpretation of predictions when both variables are used should be anticipated with skepticism. Neither stem length nor crown length provided accurate biomass predictions for different tree compartments.

The credible (Bayesian approaches) or confidence (classical approaches) intervals for the scaling exponent in M-D allometry did not include the value of 2.67, predicted by the WBE theoretical model. This result strongly supports similar outcomes from trees growing in forested stands, where b was statistically different than the theoretical value (Zapata-Cuartas et al. 2012; Sileshi 2014). The WBE model failed to predict the exponent in M-H allometry under the NB regression. The empirical value was equal to 3.661 (Table 2) and statistically different (at 95% level) from the theoretical one which is equal to four. The confidence intervals from LR and NLR include the value of four, but on average the model diverged from the empirical estimates (3.7756 for LR and 3.7467 for NLR). Therefore, analyses on empirical studies imply that a specific numeric value for the allometric exponent may not well represent the flexibility found in tree biomass allometry, which possibly originates from the accumulative effect of biotic and abiotic agents acting upon tree size-shape relations. Rather, a probability distribution may better describe the stochastic nature of the allometric equation in open-grown trees.



Conclusions

The IB and NB equations developed may be used to predict aboveground woody biomass for open-grown valonian oaks based on the diameter distributions of sampling plots compiled in the forest management plans of the studied ecosystem. Assuming that uncertainty is equally or even more important than merely predicting average values, it is recommended that future allometric models should report associated probability distribution for predicted tree biomass estimates. Informative Bayesian regression is considered to be more appropriate than classical statistical approaches (such as log-linear or non linear regressions) or non-informative Bayesian technique for deriving the variance of the predictive distribution. Large errors in predicting the biomass of stem and branch compartments are expected from the implementation of the derived models based on D, but not substantial improvement was obtained by inserting tree linear dimensions in the regressions (such as tree height, stem and/or crown length). Given that more biomass data for open-grown trees would become available, informative Bayesian regressions may provide better predictions for stem and branch compartments. Finally, the theoretical WBE model which assumes a specific value for the exponent in M-D allometry (i.e., b = 2.67) was not supported by our findings.

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