# Information Theory

In 1948, Claude Shannon published a paper colled 'A mathematical Theory of communication'. This Papera herialded a transformation in our underestanding of information. Before shannon's paper, information had been viewed as a kind Of poorry defined miasmic fluid. But offer shannon's papers, it became apparrent that information is a well defined and, above all measurable quantity.

A basic idea in information theory is that information can be treated very much like a physical quantity such as energy on mass."

~ Cloude Shannon. 1085

Information theory defines definite, unneachable. limits on precisely tow much inforcmation can be communicated between and two components of any system, whether the system is mon mode on natural.

Problem:

Symbol and preobability (A paret of my name 'UDDIM'):

Symbol (2)	U		per common en el circi con le recursos con con con con con en	part consist an executive size constitution as which insure in our price in out the constitution as an origin and
Probability P(x)	1 5	2 5	1 5	<u>1</u> 5

Find the information content of each symbol. entrophy of source.

### solution:

We Know.

Information content.  $I(x_i) = log_2(\frac{1}{P(x_i)})$ 

Message 'u': 
$$\frac{1}{I(u)} = \log_2 \frac{1}{P(u)} = \log_2 \frac{1}{\frac{1}{5}} = 2.322 \text{ bits}$$

Message 'D':
$$\overline{I(D)} = \log_2 \frac{1}{P(D)} = 1.322 \text{ bits}$$

Hessage M':
$$\frac{1}{(M)} = \log_2\left(\frac{1}{P(M)}\right) = 2.322 \text{ bits}$$

Again,

We know,
The entropy of the source.  $H(x) = -\sum_{i=1}^{n} P(x_i) (\log_2 P(x_i))$ 

: 
$$H(X) = -\frac{4}{5} P(X_1) \log_2 P(X_1)$$
  
=  $\frac{1}{5} \times 2.0522 + \frac{2}{5} \times 1.0522 + \frac{4}{5} \times 2.0522$ 

$$= \frac{1}{5} \times 2.0322 + \frac{1}{5} \times 1.0322 \times 3$$

$$+ \frac{1}{5} \times 2.0322 - \frac{1}{5} \times 1.0322 \times 3$$

## Shannon-Fano coding

Shannon-Fano coding, nomed after claude Elwood Shannon and Robert Fano, is a technique for constructing a priefix code based on a set of symbols and their probabilities.

The algorithm works and it produces fairly efficient varciable—length encodings; when the two smallers sets produced by a partitioning one in fact of equal probability, the one bit of information used to distinguish them is used most efficiently. Unfortunately, shannon-Fana does not always produce optimal profix codes.

Problem 01: Design Shannon-Fano for the following text 'BORHAM'. Find code efficiency and redundancy.

#### solution:

Number of total symbols, N = 6

Probability of each symbol,

$$P(B) = \frac{1}{6}$$
,  $P(O) = \frac{1}{6}$ ,  $P(P) = \frac{1}{6}$   
 $P(H) = \frac{1}{6}$ ,  $P(A) = \frac{1}{6}$ ,  $P(H) = \frac{1}{6}$ 

Encoding the source symbols using shannon-Fano encoder gives:-

					and the second second
Symbol	Probability	Code			Length (6)
B	1 6	0	0		2
0	1/6	O	1	0	B
R	A/6	0	1		3
H	1/6	1	O	The Barrier of Market of Conference of the Market of Mar	2
A	1/6	1	1	٥	3
N	1/6	1	1	1	3

Code table

The Entropy of the source,

$$H = -\sum_{i=0}^{5} P_i \log_2 P_i = 2.58 \text{ bits [symbo]}$$

The average length length of the binary code is,

Thus. the code efficiency,

Redundancy. = 
$$100 - \eta = 100 - 96.99$$
  
=  $3.0176$ .

# Code tree:

